

ISM Assignment - 1

①

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Q. 1

Sort the Data

26, 27, 28, 29, 29, 30, 31, 32, 33, 34, 35

1) Mean = $\frac{\text{sum of all values}}{\text{number of values}} = \frac{334}{11} = \underline{\underline{30.36^{\circ}\text{C}}} \text{ (approx.)}$

2) Median - with 11 values, median will be 6th value.

i.e. median = 30°C

3) Range = Max value - min. value
 $= 35 - 26$

Range = 9

4) Variance:
using population variance = $\sigma^2 = \frac{\sum (x - \bar{x})^2}{n}$

Total squared deviations = 84.55

Sr. No.	values	distance	squared distance
1	26	-4.36	19.04
2	27	-3.36	11.31
3	28	-2.36	5.59
4	29	-1.36	1.86
5	29	-1.36	1.86
6	30	-0.36	0.13
7	31	0.64	0.40
8	32	1.64	2.68
9	33	2.64	6.95
10	34	3.64	13.22
11	35	4.64	21.50

Population Variance:

$\sigma^2 = \frac{\text{sum. of squared distance/ deviations}}{n}$

$$\sigma^2 = \frac{84.55}{11} = 7.69$$

⑤ Q_1

lower half : 26, 27, 28, 29, 29

$$Q_1 = 28$$

upper half : 31, 32, 33, 34, 35

$$Q_3 = 33$$

⑥ Skewness:

As mean (30.36) > median (30)

data has positive skew (right skewed slightly)⑦ IQR outlier Detection

$$IQR = Q_3 - Q_1 = 33 - 28 = 5$$

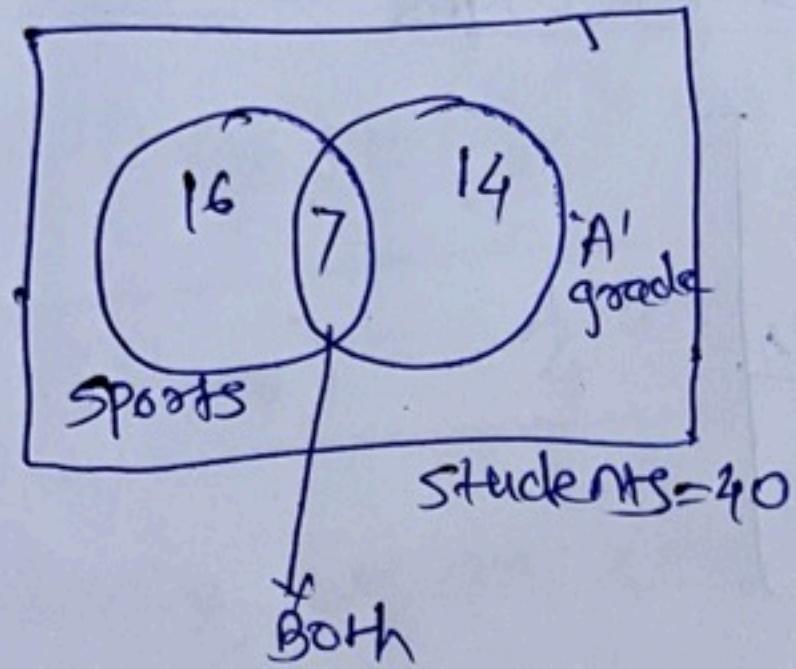
$$1) \text{Lower fence} = Q_1 - 1.5(IQR) = 28 - 1.5(5) = 28 - 7.5 \\ = \underline{\underline{20.5}}$$

$$2) \text{Upper fence} = Q_3 + 1.5(IQR) = 33 + 1.5(5) = 33 + 7.5 \\ = \underline{\underline{40.5}}$$

As there is no data outside 20.5 - 40.5,

so NO outliers by IQR method

Q.2. Using ven diagram



given ↴

$$\text{Sports} = 7 \text{ (boys)} + 9 \text{ (girls)} = 16 \text{ (S)}$$

$$'A' \text{ grade} = 6 \text{ (boys)} + 8 \text{ (girls)} = 14 \text{ (A)}$$

$$\text{Both (S and A)} = 3 \text{ (boys)} + 4 \text{ (girls)} = 7$$

Find out = $P(S \cup A)$

$$P(S \cup A) = P(S) + P(A) - P(S \cap A)$$

$$= \frac{16}{40} + \frac{14}{40} - \frac{7}{40}$$

$$P(S \cup A) = \frac{23}{40} = 0.575$$

So probability of a student is either involved in sports or scored an 'A' grade = 0.575 (57.5%)

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Q3. Using given dataset, create below tables for each feature. with Depression(D)yes & D_{NO}.

Trouble sleeping	D _{yes}	D _{NO}
Yes	2/2	0/2
No	0/2	2/2

low energy	D _{yes}	D _{NO}
Yes	1/2	1/2
No	1/2	1/2

Anxiety	D _{yes}	D _{NO}
Yes	2/2	0/2
No	0/2	2/2

$$P(D_{yes}) = \frac{2}{4} = 0.5 \quad P(D_{NO}) = \frac{2}{4} = 0.5$$

A new person has,

$x_1 \Rightarrow$ Trouble sleeping = Yes

$x_2 \Rightarrow$ Lower energy = No

$x_3 \Rightarrow$ Anxiety = Yes

As per Naive Bayes classifier, compute below scores,

$$P(D_{yes} | x_1, x_2, x_3) = \frac{P(x_1 | D_{yes}) \cdot P(x_2 | D_{yes}) \cdot P(x_3 | D_{yes}) \cdot P(D_{yes})}{P(x_1, x_2, x_3)}$$

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Now, $P(X_1/D_{\text{Yes}}) = \frac{1}{2}$, $P(X_2/D_{\text{Yes}}) = \frac{1}{2}$ & $P(X_3/D_{\text{Yes}}) = \frac{1}{2}$

$$P(D_{\text{Yes}}) = \left(\frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \right) \times \frac{2}{4}$$

$$P(D_{\text{Yes}}) = \frac{1}{4} = 0.25$$

similarly, we can compute $P(D_{\text{No}})$ score as below.

$$P(D_{\text{No}}/(X_1 \cap X_2 \cap X_3)) = \frac{P(X_1/D_{\text{No}}) \cdot P(X_2/D_{\text{No}}) \cdot P(X_3/D_{\text{No}})}{P(X_1 \cap X_2 \cap X_3)} \cdot P(D_{\text{No}}),$$

here, $P(X_1/D_{\text{No}}) = \frac{1}{2}$, $P(X_2/D_{\text{No}}) = \frac{1}{2}$ & $P(X_3/D_{\text{No}}) = \frac{1}{2}$

$$\text{so, } P(D_{\text{No}}) = \left(\frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \right) \times \frac{2}{4} = 0$$

As, $P(D_{\text{Yes}}) > P(D_{\text{No}})$, we can say that a new person Has Depression

Prediction \Rightarrow Person has Depression

Q.4.

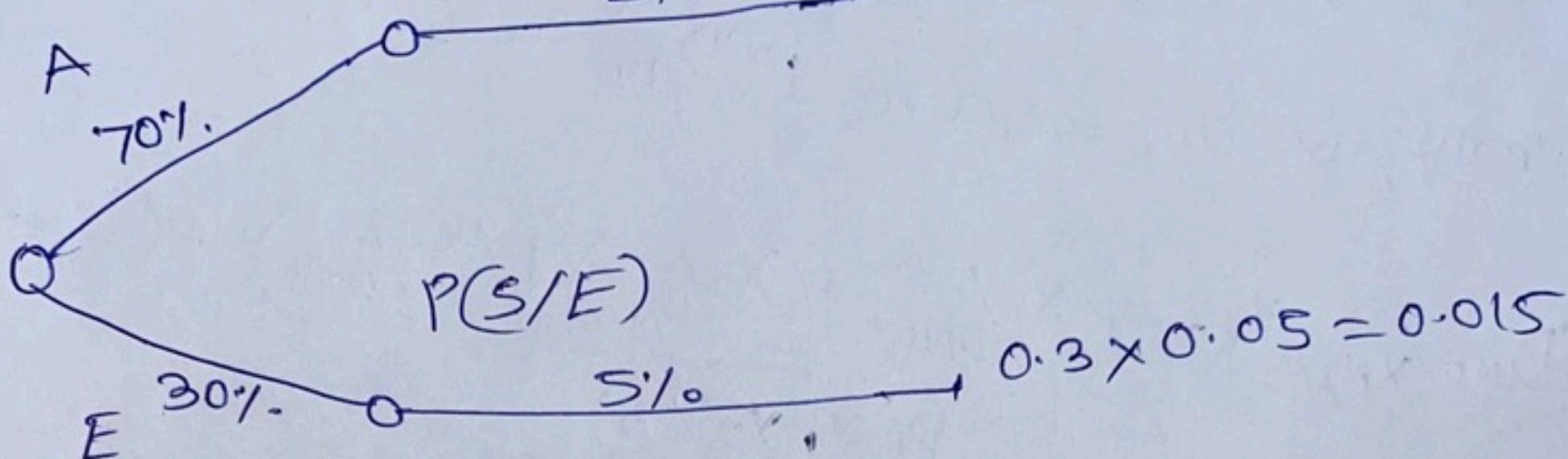
Let,

A = students in Arts

E = students in Engineering

S = students scored above 95%

Given that, $P(S/A) = 2\%$ $\rightarrow 0.02$



we have to find, $P(A/S)$

NOW, $P(S) = P(S/A) \cdot P(A) + P(S/E) \cdot P(E)$ \rightarrow Total probability

$$= 0.014 + 0.015$$

$$P(S) = 0.029$$

As per Baye's theorem,

$$P(A/S) = \frac{P(S/A) \cdot P(A)}{P(S)}$$

$$P(A/S) = \frac{0.014}{0.029} = 0.4828$$

so, there is 48.28% chance that student is from Arts.