# CS306: Introduction to IT Security Assignment Project Exam Help

https://powcoder.com Lecture 7: Public-key Cryptography

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### Assignment Project Exam Help

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7.0 Announcements
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#### CS306: Announcements

- HW2 did not come too much in view of next week's midterm exam
- Road ahead
  - no lecture on Asto bemanant were jeste Ewill run bled ponday schedule)
  - regular lecture on October 20
  - midterm exam on outpes://powcoder.com
    - online exam, quiz format
       accommodations to be provided as needed

    - covers all materials discussed so far: lectures 1-7, labs 1-7, HW1
    - Lab 7 will offer a general revision on most important topics
    - exact list of topics to be provided tomorrow

### CS306: Tentative Syllabus

Week	Date	Topics	Reading	Assignment
1	Sep 1	Introduction  Drodoot Example	Lecture 1	-
2	ASSIGII Sep 8	ment Project Exam	Lecture 2	Lab 1
3	Sep 15 ht	ps://powcoder.com	Lecture 3	Lab 2, HW 1
4	<b>Sep 22</b>	Ciphers in practice I	Lecture 4	Lab 3, HW 1
5	Sep 29 <b>A</b> (	dd Wechatepowcod	<b>er</b> ecture 5	Lab 4
6	Oct 6	MACs & hashing	Lecture 6	Lab 5
<u>-</u>	Oct 13	No class (Monday schedule)		Lab 6
7	Oct 20	Public-key cryptography	Lecture 7	Lab 7, HW2

### CS306: Tentative Syllabus

### (continued)

Week	Date	Topics	Reading	Assignment
8	Oct 27 Assign	ment Project Exam	All materials	
9	Nov 3	Network/Web security	•	
10	Nov 10 htt	ps:df/po/wooderucon	1	
11	Nov 17	Cloud security	1	
12	Nov 24	dd WeChat powcoc	ier	
13	Dec 1	Economics		
14	Dec 8	Legal & ethical issues		
15	Dec 10 (or later)	Final (closed "books")	All materials covered*	

### Two weeks ago

- Message authentication
  - MACs
  - Replay attack Assignment Project Exam Help
  - Constructionshttps://powcoder.com
- Cryptographic hashing
  - Hash functions Add WeChat powcoder
  - Constructions
- Demo
  - Hash functions in practice

### Today

- Revision on message authentication & cryptographic hashing
  - Practical applications
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       authenticated encryption, hash functions security strength, HMAC
- Public-key (PK) crypt bettposy/powcoder.com
  - Motivation, PK Infrastructure, PK encryption, digital signatures Add WeChat powcoder
  - Discrete log problem, DH key agreement, hybrid encryption
- Demo
  - The length-extension attack...

### Assignment Project Exam Help

https://powcoderic-public-key encryption
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#### Recall: Principles of modern cryptography

(A) security definitions, (B) precise assumptions, (C) formal proofs

For symmetric-key message encryption/authentication

adversary Assignment Project Exam Help
 types of attacks
 trusted set-up
 secret key is distributed securely
 secret key remains secret
 trust basis
 underlying primitives are secure

acc

- PRG, PRF, hashing, ...
  - e.g., block ciphers, AES, SHA-2, etc.

### On "secret key is distributed securely"

Alice & Bob (or 2 individuals) must securely obtain a shared secret key

- "securely obtain"
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   need of a secure channel
- "shared secret key" <a href="https://powcoden.goging problem">https://powcoden.goging problem</a> to manage
  - too many keys Add WeChat powcoder



Public-key cryptography to the rescue...

### On "secret key is distributed securely"

Alice & Bob (or 2 individuals) must securely obtain a shared secret key

- "securely obtain"
   (A) strong assumption to accept
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   requires secure channel for key distribution (chicken & egg situation)

  - seems impossible for two parties having apprier trust relationship
  - not easily justifiable to hold a priori
- "shared secret key" Add WeChat powcoder (B) challenging problem to manage
  - requires too many keys, namely O(n²) keys for n parties to communicate
  - imposes too much risk to protect all such secret keys
  - entails additional complexities in dynamic settings (e.g., user revocation)

### Alternative approaches?

Need to securely distribute, protect & manage many **session-based** secret keys

- (A) for secure distribution, just "make another assumption..."
  - employ "designate by nemental and ject Exam Help
  - physically protected channel (e.g., meet in a "sound-proof" room)
     employ "trusted" party
  - - entities authorized to distribute keys (psychologistribution centers (KDCs))
- (B) for secure management, just 'live with it!"



Public-key cryptography to the rescue...

## Public-key (or asymmetric) cryptography

disclaimer on names private = secret

Goal: devise a cryptosystem where key setup is "more" manageable

Main idea: user-specific keys (that come in pairs)

- user U generates Augus keyn the Inthe Notice to Exam Help
  - ◆ U<sub>pk</sub> is public it can safely be known by everyone (even by the adversary)
  - ◆ U<sub>sk</sub> is private https://powecoder.com (even from other users)

#### Usage

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- employ public key U<sub>pk</sub> for certain "public" tasks (performed by other users)
- employ private key U<sub>sk</sub> for certain "sensitive" tasks (performed by user U)

#### Assumption

public-key infrastructure (PKI): public keys become securely available to users

#### From symmetric to asymmetric encryption

secret-key encryption

- main limitation
  - session-spectics size nmentice Projectote Exam Help c→decrypt→m Bob

public-key encryption <a href="https://powcoder.com">https://powcoder.com</a>

- main flexibility
  - user-specific keys



messages encrypted by receiver's PK can (only) be decrypted by receiver's SK

#### From symmetric to asymmetric message authentication

secret-key message authentication (or MAC) main limitation session-speckickiesnment-Project Exam public-key message authantication powcoder.com (or digital signatures) main flexibility user-specific keys "sensitive" task

(only) messages signed by sender's SK can be verified by sender's PK

#### Thus: Principles of modern cryptography

(A) security definitions, (B) precise assumptions, (C) formal proofs For asymmetric-key message encryption/authentication

- Assignment Project Exam H adversary Bobsk types of attacks trusted set-up  $c \rightarrow decrypt \rightarrow m$ PKI is needed Add WeChat powcoder secret keys remain secrét Alice<sub>PK</sub> re trust basis underlying primitives are secure acc
  - typically, algebraic computationally-hard problems
    - e.g., discrete log, factoring, etc.

#### General comparison

#### Symmetric crypto

- key management
- key management

   less scalable & risksignment Project Regulation Regulatio Regulation Regulation Regulation Regulation Regulation Regulati
- assumptions
  - secret & authentic confittpisation owcoder confitty (PKI)
  - secure storage
- primitives
  - generic assumptions
  - more efficiently in practice

#### **Asymmetric crypto**

- assumptions
  - secure storage
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  - math assumptions
  - less efficiently in practice (2-3 o.o.m.)

#### Public-key infrastructure (PKI)

A mechanism for securely managing, in a dynamic multi-user setting, (to be used by some public-key cryptosystem) user-specific public-key pairs

- dynamic, multi-Assignment Project Exam Help
  - the system is open to anyone; users can join & leave
- user-specific public-keyhttps://powcoder.com
- each user U in the system is assigned a <u>unique</u> key pair (U<sub>pk</sub>, U<sub>sk</sub>)
   secure management (e.g., at the first text to purple keysoder
  - public keys are authenticated: <u>current</u> U<sub>pk</sub> of user U is <u>publicly</u> known to everyone

#### Very challenging to realize

currently using digital certificates; ongoing research towards a better approach...

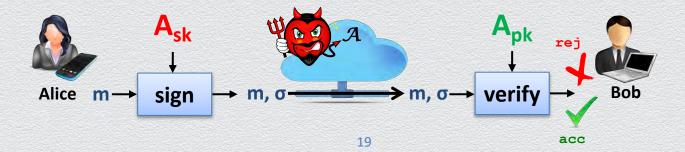
#### Overall: Public-key encryption & signatures

#### Assume a trusted set-up

public keys are securely available (PKI) & secret keys remain secret

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### Secret-key vs. public-key encryption

	Secret Key (Symmetric)	Public Key (Asymmetric)	
Number of keys	1 Assignment Project Ev	2 am Heln	
Key size (bits)	56-112 (DES), 128-256 (AES)	Unlimited; typically no less than 256; 1000 to 2000 currently considered desirable for most uses	
Protection of key	Must be kept see of .// powcouch.c	one key must be kept secret; the other can be freely exposed	
Best uses	Cryptographic workhorse. Sorrecy and integrity of data, bon viole data posw to blocks of data, messages and files	Key exchange, authentication,	
Key distribution	Must be out-of-band	Public key can be used to distribute other keys	
Speed	Fast	Slow, typically by a factor of up to 10,000 times slower than symmetric algorithms	

#### Public-key cryptography: Early history

#### Proposed by Diffie & Hellman

- documented in "New Directions in Cryptography" (1976)
- solution concepts of public-key encryption schemes & registral signatures
- key-distribution systems
  - Diffie-Hellman keyterge ment of the protection of the protect
    - "reduces" symmetric crypto to asymmetric crypto

Public-key encryption was del lev tenthiad appropriate proposed by James Ellis

- classified paper (1970)
- published by the British Governmental Communications Headquarters (1997)
- concept of digital signature is still originally due to Diffie & Hellman

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7.2 Public-key certificates
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#### How to set up a PKI?

- How are public keys stored? How to obtain a user's public key?
- How does Bob know or 'trust' that A<sub>RK</sub> is Alice's public key?
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   How A<sub>PK</sub> (a bit-string) is securely bound to an entity (user/identity)?

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public key: Bpk

secret key: B<sub>sk</sub>

#### Achieving a PKI...

How can we maintain the invariant that at all times

- any given user U is assigned a unique public-private key pair; and
- any other user kan ignument project Exam Help
  - secret keys can be lost, stolen or they should be revoked <a href="https://powcoder.com">https://powcoder.com</a>

entails binding users/identities to public keys

#### Recall

- PK cryptosystems come with a weelghrith now wick is de le User the leger the leger to le leger to leger to
  - on input a security-strength parameter, it outputs a random valid key pair for U
- public keys can be made publicly available
  - e.g., sent by email, published on web page, added into a public directory, etc.

#### Distribution of public keys

#### **Public announcement**

users distribute public keys to recipients or broadcast to community at large

#### Publicly available Airsignment Project Exam Help

• can obtain greater security by registering keys with a public directory

Both approaches have problems and pre-Winerable to forgeries

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#### Do you trust your public key?

- Impostor claims to be a true party
  - true party has a public and private key
  - impostor also Assignment Project Exam Help
- Impostor sends impostor's own public key to the verifier
  - says, "This is the true party weblickey" powcoder
  - this is the critical step in the deception

#### Certificates: Trustable identities & public keys

#### Certificate

- a public key & an identity bound together
- in a document signed by a certificate authority Exam Help

#### Certificate authority (Ch)ttps://powcoder.com

- an authority that users trust to securely bind identity to public keys
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   CA verifies identities before generating certificates for these identities

  - secure binding via digital signatures
    - ◆ ASSUMPTION: The authority's PK CA<sub>PK</sub> is authentic

#### Public-key certificates in practice

Current (imperfect) practice for achieving trustable identities & public keys

- everybody trusts a Certificate Authority (CA)
  - everybody knows picaramosost that of the total the total responding secret key CAsk
- a certificate binds identities to public keys in a CA-signed statement
  - e.g., Alice obtains a significate of the scale ment Alice's public key is 1032xD"
- users query CA for public keys of intended recipients or signers

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   e.g., when Bob wants to send an encrypted message to Alice
  - - he first obtains & verifies a certificate of Alice's public key
  - e.g., when Alice wants to verify the latest software update by Company
    - she first obtains & verifies a certificate of Company's public key

#### Example

a certificate is a public key and an identity bound together and signed by a certificate authority (CA)

Document containing the public key and identity for Mario Rossi

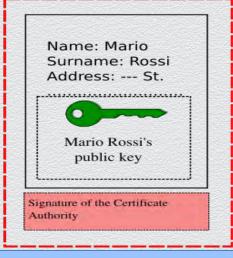
Name: Mario
Surname: Rossi
Surname: Rossi
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Mario Rossi's public key

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a certificate authority is an **authority** that users **trust** to accurately verify identities before generating certificates that bind those identities to keys

#### Mario Rossi's Certificate



document signed by CA



#### Certificate hierarchy

Single CA certifying every public key is impractical Instead, use trusted signericinate Projectics xam Help

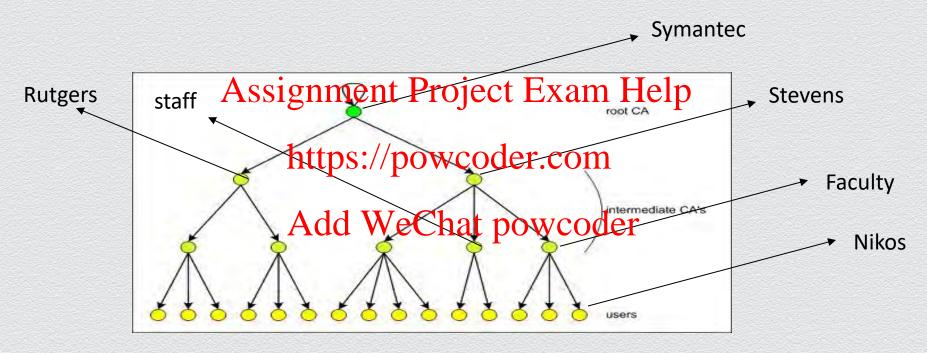
- root CA signs certificates for intermediate CAs,
   they sign certificates for lower-level CAs, etc.
  - certificate "chain of Audd WeChat powcoder
    - sig<sub>Symantec</sub>("Stevens", PK<sub>Stevens</sub>)
    - sig<sub>UMD</sub>("faculty", PK<sub>faculty</sub>)
    - sig<sub>faculty</sub>("Nikos", PK<sub>Nikos</sub>)

### Example 1: Certificate signing & hierarchy

#### To create Diana's certificate: To create Delwyn's certificate: Diana creates and delivers to Edward: Delwyn creates and delivers to Diana: Name: Diana Name: Delwyn Position: Division Manager Position: Dept Manager Public key: 17EF83CA ... Public key: 3AB3882C .. Edward adds: Name: Diana hash value Name: Delwyn hash value Position: Division Manager 128C4 Position: Dept Manager 48CFA Public kev: 17EF83GA Public key: 3AB3882C ... Edward signs with his private key: Diana signs with her private key: hash value Name: Diana Name: Delwvn hash value Position: Division Manager Position: Dept Manager 48CFA Public key: 17EF83C Which is Diana's certificate. And appends her certificate: Name: Delwyn hash value Position: Dept Manager 48CFA Public key: 3AB3882C ... Name: Diana hash value 128C4 Position: Division Manager Public key: 17EF83CA ...

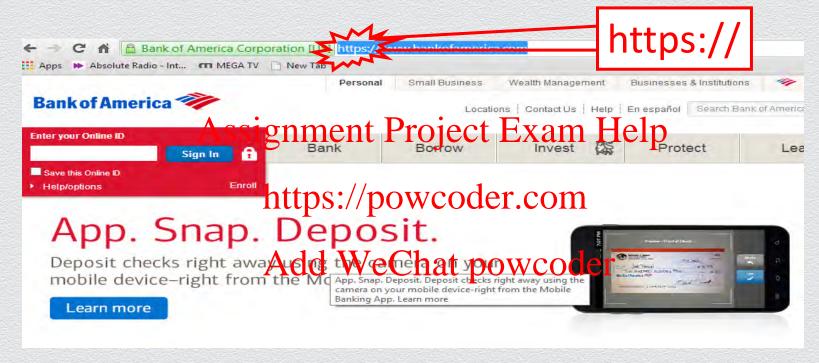
Which is Delwyn's certificate.

### Example 2



What bad things can happen if the root CA system is compromised?

#### Secure communication over the Internet



What cryptographic keys are used to protect communication?

#### X.509 certificates

Defines framework for authentication services

- defines that public keys stored as certificates in a public directory
- certificates are issued and signed by a CA Exam Help

Used by numerous applications//Sowcoder.com

Example: see certificates accepted by your browser Add WeChat powcoder

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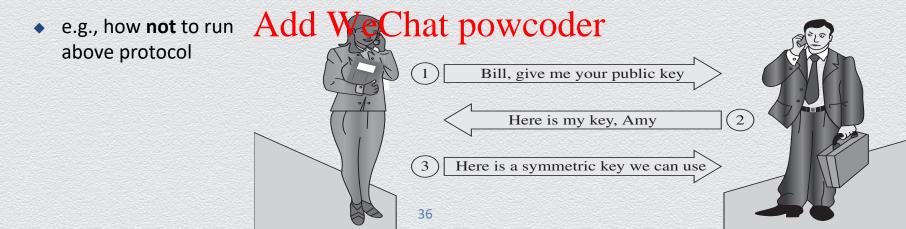
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7.3 Hybrid encryption
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### Secret-key cryptography is "reduced" to public-key

PK encryption can be used "on-the-fly" to securely distribute session keys

Main idea: Leverage PK encryption to securely distribute session keys

- sender generates a fresh session-specific secret key k and learns receiver's public key R<sub>pk</sub>
- session key k is sent to receiver encrypted under key R https://powcoder.com
- session key k is employed to run symmetric-key crypto



#### Hybrid encryption

"Reduces" secret-key crypto to public-key crypto

better performance than block-based public-key CPA-encryption

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main idea

apply PK encryption of plants of

### Hybrid encryption using the KEM/DEM approach

"Reduces" secret-key crypto to public-key crypto



- CPA-secure if KEM is CPA-secure and Enc' EAV-secure
- CCA-secure if KEM and Enc' are CCA-secure

### Assignment Project Exam Help

https://powcoder.com Discrete Log problem & its
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#### The discrete logarithm problem

#### Setting

- if p be an odd prime, then  $G = (Z_p^*, \cdot)$  is a cyclic group of order p 1
  - ◆ Z<sub>p</sub>\* = {1, 2, 3, A. ssiggemeent Projection Exxam Help
    - for i = 0, 1, 2, ..., p-2, the process  $g^i \mod p$  produces all elements in  $Z_p^*$
  - for any x in the group, we have that g mod p = x, for some integer k
  - k is called the discrete logarithm (or log) of x (mod p) er

#### Example

- $(Z_{17}^*, \cdot)$  is a cyclic group G with order 16, 3 is the generator of G and  $3^{16} = 1 \mod 17$
- let k = 4,  $3^4 = 13 \mod 17$  (which is easy to compute)
- the inverse problem: if  $3^k = 13 \mod 17$ , what is k? what about large p?

#### Computational assumption

#### Discrete-log setting

- cyclic G =  $(Z_p^*, \cdot)$  of order p 1 generated by g, prime p of length t (|p|=t) Assignment Project Exam Help Problem
- given G, g, p and x in Z\*, compute the discrete log k of x (mod p)
   tttps://powcoder.com
   we know that x = g<sup>k</sup> mod p for some unique k in {0, 1, ..., p-2}... but

#### Discrete log assumption Add WeChat powcoder

- for groups of specific structure, solving the discrete log problem is infeasible
- any efficient algorithm finds discrete logs negligibly often (prob =  $2^{-t/2}$ )

#### Brute force attack

cleverly enumerate and check O(2<sup>t/2</sup>) solutions

#### ElGamal encryption

Assumes discrete-log setting (cyclic G =  $(Z_p^*, \cdot)$  = <g>, prime p, message space  $Z_p$ ) Gen

- secret key: random number x & Z\* Project Ex an grand p, along w/ G, g, p Enc
- pick a fresh <u>random</u>  $r = \frac{7}{100} \cdot \frac{7}{100} \cdot$

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where  $c_1^x = g^{xr}$ •  $Dec_{SK}(c_1,c_2) = c_2 (1/c_1^x) \mod p$ 

Security is based on Computational Diffie-Hellman (CDH) assumption

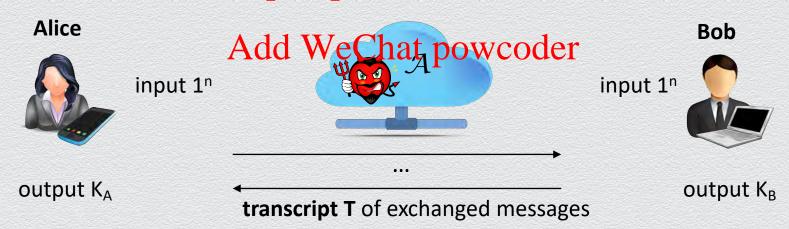
given (g, g<sup>a</sup>,g<sup>b</sup>) it is hard to compute g<sup>ab</sup>

A signature scheme can be also derived based on above discussion

### Application: Key-agreement (KA) scheme

Alice and Bob want to securely establish a shared key for secure chatting over an insecure line

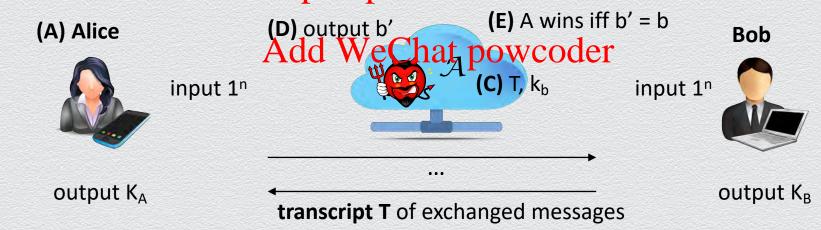
- instead of meeting in person in a secret place, they want to use the insecure line...
- \* KA scheme: they rupackeiven and the contributed p shared key K
- correctness: K<sub>A</sub> = K<sub>B</sub>
- security: no PPT adversary httpisen/pawwww.datshortom a trully random one



### Key agreement: Game-based security definition

- scheme  $\Pi(1^n)$  runs to generate  $K = K_A = K_B$  and transcript T; random bit b is chosen
- adversary  $\mathcal{A}$  is given T and  $k_b$ ; if b = 1, then  $k_b = K$ , else  $k_b$  is random (both n-bit long)
- A outputs bit b' a Adswirg in ment Project Exam Help
- ◆ then: П is secure if no PPT A wins non-negligibly often https://powcoder.com

(B) b is randomly chosen

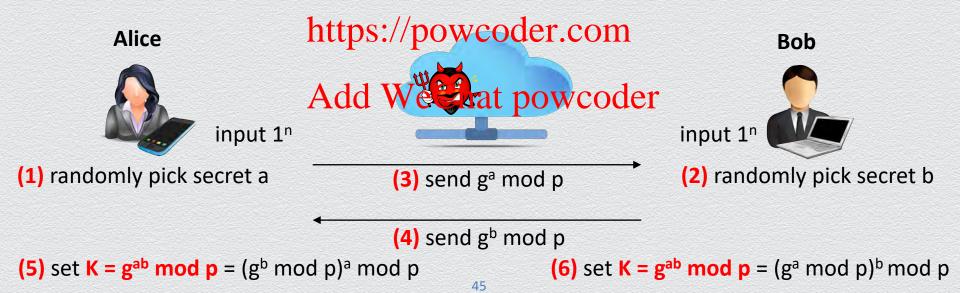


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### The Diffie-Hellman key-agreement protocol

Alice and Bob want to securely establish a shared key for secure chatting over an insecure line

- DH KA scheme Π
  - discrete log settings igniphie where reject plantament in telp



#### Security

- discrete log assumption is necessary but not sufficient
- decisional DH assumption
  - given g, g<sup>a</sup> and g<sup>a</sup>, g<sup>a</sup> is computationally indistinguishable from uniform

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#### Authenticated Diffie-Hellman

