

15-213 Introduction to Computer Systems
Final Exam
May 10, 2007

Name: Model Solution
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Recitation Section: _____

- This is an open-book exam.
- Notes and calculators are permitted, but not computers.
- Write your answer legibly in the space provided.
- You have 180 minutes for this exam.

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	Problem	Max	Score
Floating Point	1	20	20
Assembly Language	2	20	20
Optimization	3	20	20
Cache Memory	4	20	20
Signals	5	20	20
Garbage Collection	6	20	20
Threads	7	20	20
Synchronization	8	20	20
	Total	150+10	160

1. Floating Point (20 points)

In this problem we consider properties of floating point operations. For each property state whether it is true or false. If false, give a counterexample as a (possibly negative) power of 2 within the range of precision for the variables. We assume that the variables on an x86_64 architecture are declared as follows

```
float x, y, z;
double d, e;
```

and initialized to some unknown value **different from NaN, $+\infty$, and $-\infty$** . We have given the first answer as an example.

$(x + y) + z == x + (y + z)$	false	$x = 1, y = 2^{127}, z = -2^{127}$
If $x > 0$ then $x / 2 > 0$	false	$x = 2^{-149}$
$(x + y) * z == x * z + y * z$	false	$x = 2^{127}, y = -2^{127}, z = 2^{127}$
If $x \geq y$ and $z \leq 0$ then $x * z \leq y * z$	true	
If $x > y$ then $(\text{double})x > (\text{double})y$	true	
If $d > e$ then $(\text{float})d > (\text{float})e$	false	$d = 2^{129}, e = 2^{128}$
$x + d < x$	false	$x = 2^{127}$

2. Assembly Language (20 points)

In this problem we consider an illustrative program for multiplication of two unsigned int's, returning an unsigned long int holding the product.

```
unsigned long mult (unsigned i, unsigned k) {
    unsigned long p = 0;
    unsigned long q = k;
    while (i != 0) {
        if (i & 1)
            p = p + q;
        q = q << 1;
        i = i >> 1;
    }
    return p;
}
```

The following is the resulting machine code when compiled on an x86_64 machine with gcc -O2, omitting two instructions.

```
mult:
    xorl    %ecx, %ecx
    mov     %esi, %edx
    testl   %edi, %edi
    jmp     .L8

.L10:
    leaq    4(%rdx, %rdx), %rax
    testb   $1, %dil

    _____ # missing conditional move
    addq    %rdx, %rdx
    shrl    %edi

.L8:
    jne     .L10

    _____ # missing move
    ret
```

1. (5 pts) For each register, give the value it holds during the iteration, expressed in terms of the C program.

Register	C expression
%rcx	p
%rdx	q
%rax	p+q
%edi	i
%dil	(char) i

2. (5 pts) Fill in the missing two instructions in the code.

```
cmovne %rax, %rcx and movq %rcx, %rax
```

3. (4 pts) Rewrite the loop to use a conditional jump instead of a conditional move.

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See one solution below; there are many others.

```
testb $1, %dil  
jne .L9  
movq %rax, %rcx  
.L9  
addq %rdx, %rdx
```

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4. (3 pts) Explain briefly why the compiler preferred to use a conditional move instruction.

Because the branch misprediction penalty would make the loop slower, especially since the outcome of test will be difficult to accurately predict.

5. (3 pts) Assume we declared and initialized

```
int i,k;  
long m;
```

and called

```
m = (long)mult((unsigned)i, (unsigned)k);
```

using the above definition of `mult`. Will `m` hold the correct value of the signed product of `i` and `k`? Circle the correct answer.

yes no **no**

Briefly explain your answer.

For example, when multiplying 1 times -1 , the negative 1 will actually be interpreted as $2^{32} - 1$ and the result will also be $2^{32} - 1$ instead of -1 . However, the answer will be correct modulo 2^{32} because on two's-complement representations, signed and unsigned addition and multiplication are identical: they operate in the ring of integers modulo 2^w for the word size w ($= 32$, in this case).

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3. Optimization (20 points)

Consider the following code for calculating the dot product of two vectors of double precision floating point numbers.

```
double dot_prod(double A[], double B[], int n) {
    int i;
    double r = 0;
    for (i = 0; i < n; i++)
        r = r + A[i] * B[i];
    return r;
}
```

Assume that multiplication has a latency of 12 cycles and addition a latency of 7 cycles and load 4 cycles. Also assume that there are an unlimited number of functional units. [Hint: Under this assumption, theoretically optimal performance is dominated by the critical data dependency path.]

1. (5 points) What is the theoretically optimal CPE for this loop?

7 CPE, since the addition constitutes the critical path.

2. (10 points) Show the code for the loop unrolled by 2. You may apply associativity and commutativity of multiplication and addition, assuming that rounding errors are insignificant.

```
double dot_prod2(double A[], double B[], int n) {
    int i;
    double r = 0;
    for (i = 0; i < n-1; i+=2)
        r = r + (A[i] * B[i] + A[i+1] * B[i+1]);

    for (; i < n; i++)
        r = r + A[i] * B[i];

    return r;
}
```

3. (5 points) What is the theoretically optimal CPE for this loop?

$7/2 = 3.5$ CPE, since the critical path is still addition, but now two elements will be added in each iteration.

4. Cache Memory (20 points)

In this problem we explore the operation of a basic TLB as a cache. Assume the following

- Virtual addresses are 32 bits.
- The virtual page number (VPN) is 24 bits.
- The physical page number (PPN) is 32 bits.
- The TLB is 2-way set associative containing a total of 512 lines.

1. (6 points) Please fill in the following blanks by giving a bit range, such as “0–15”.

- The VPO of a virtual address consists of bits 0–7 of the VA.
- The VPN of a virtual address consists of bits 8–31 of the VA.
- The PPO of a physical address consists of bits 0–7 of the PA.
- The PPN of a physical address consists of bits 8–39 of the PA.
- The TLB index (TLBI) consists of bits 0–7 of the VPN.
- The TLB tag (TLBT) consists of bits 8–23 of the VPN.

We show a part of the TLB relevant to the next two questions.

Index	Valid?	Tag	Entry
3D	1	0x083F	0x0913ABDE
3E	0	0xF3E9	0x0913ABDE
	1	0x083F	0xAB18ED24
3F	1	0x409A	0x0913ABDE
	1	0x083F	0xAB18ED24
40	0	0x083E	0x0913ABDE
	1	0x3E40	0xAB18ED24

2. (7 points) Assume the virtual address is $0x083F3E9A$. Fill in the following table in hexadecimal notation. Write **U** for any value that is unknown, that is, not determined from the parameters and the table above.

Parameter	Value
VPN	0x083F3E
VPO	0x9A
TLBI	0x3E
TLBT	0x083F
Cache Hit? (Y/N/U)	Y
PPN	0xAB18ED24
PA	0xAB18ED249A

3. (7 points) Assume the virtual address is $0x083E409B$. Fill in the following table in hexadecimal notation. Write **U** for any value that is unknown, that is, not determined from the parameters and the table above.

Parameter	Value
VPN	0x083E40
VPO	0x9B
TLBI	0x40
TLBT	0x083E
Cache Hit? (Y/N/U)	N
PPN	U
PA	U

5. Signals (20 points)

Consider the following program.

```
int counter = 0;

void handler (int sig) {
    counter++;
}

int main() {
    signal(SIGUSR1, handler);
    signal(SIGUSR2, handler);
    int parent = getpid();
    int child = fork();

    if (child == 0) {

        /* insert code here */
        exit(0);
    }

    sleep(1);
    waitpid(child, NULL, 0);
    printf("Received %d USR{1,2} signals\n", counter);
    return 0;
}
```

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For each of the following four versions of the above code, list the possible outputs of this program, assuming that all function and system calls succeed and exit without error. You may also assume no externally issued signals are sent to either process.

1. (5 pts)

```
kill(parent, SIGUSR1);
kill(parent, SIGUSR1);
```

1,2: If the second SIGUSR1 is sent before the first one is received it will be dropped.

2. (5 pts)

```
kill(parent, SIGUSR1);  
kill(parent, SIGUSR1);  
kill(parent, SIGUSR1);
```

1,2,3: The second and third SIGUSR1 may be sent before the first one is received.

3. (5 pts)

```
kill(parent, SIGUSR1);  
kill(parent, SIGUSR2);
```

1,2: Because of a race condition when SIGUSR2 is received while SIGUSR1 is handled, one increment may be dropped.

4. (5 pts)

```
kill(parent, SIGUSR1);  
kill(parent, SIGUSR2);  
kill(parent, SIGUSR1);  
kill(parent, SIGUSR2);
```

1,2,3,4: Two consecutive occurrences as in the answer to the previous question can lead to answers 1+1, 1+2, 2+1 or 2+2. And the race condition from the previous question can lead to the answer 1 if the first three signals are sent before any are received.

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6. Garbage Collection (20 points)

In this problem we consider a tiny list processing machine in which each memory word consists of two bytes: the first byte is a pointer to the tail of the list and the second byte is a data element. The end of a list is marked by a pointer of 0x00. We assume that the data element is never a pointer.

We start with the memory state on the left, where the range 0x10–0x1F is the from-space and the range 0x20–0x2F is the to-space. All addresses and values in the diagram are in hexadecimal.

Write in the state of memory after a copying collector is called with root pointers 0x10 and 0x12, in this order. You may leave cells that remain unchanged blank.

Please be sure to use the proper breadth-first traversal algorithm covered in lecture.

Before GC			After GC					
Addr	Ptr	Data	Addr	Ptr	Data	Addr	Ptr	Data
10	14	A2	10	20		20	24	A2
12	1A	1F	12	22		22	16	1F
14	1E	02	14	24		24	28	02
16	1E	20	16	26		26	2A	BC
18	00	33	18	2A		28	20	8F
1A	18	BC	1A	26		2A	00	33
1C	12	DE	1C	2C		2C		
1E	10	8F	1E	28		2E		

After garbage collection, free space starts at address 2C

7. Threads (20 points)

Consider three concurrently executing threads in the same process using two semaphores s_1 and s_2 . Assume s_1 has been initialized to 1, while s_2 has been initialized to 0.

What are the possible values of the global variable x , initialized to 0, after all three threads have terminated?

```
/* thread A */
P(&s2);
P(&s1);
x = x*2;
V(&s1);
```

```
/* thread B */
P(&s1);
x = x*x;
V(&s1);
```

```
/* thread C */
P(&s1);
x = x+3;
V(&s2);
V(&s1);
```

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The possible sequences are B,C,A ($x = 6$) or C,A,B ($x = 36$) or C,B,A ($x = 18$).

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8. Synchronization (20 points)

We explore the so-called *barbershop problem*. A barbershop consists of a n waiting chairs and the barber chair. If there are no customers, the barber waits. If a customer enters, and all the waiting chairs are occupied, then the customer leaves the shop. If the barber is busy, but waiting chairs are available, then the customer sits in one of the free chairs.

Here is the skeleton of the code, without synchronization.

```
extern int N;    /* initialized elsewhere to value > 0 */
int customers = 0;

void* customer() {

    if (customers > N) {

        return NULL;
    }

    customers += 1;

    getHairCut();

    customers -= 1;

    return NULL;
}

void* barber() {
    while(1) {

        cutHair();

    }
}
```

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For the solution, we use three binary semaphores:

- `mutex` to control access to the global variable `customers`.
- `customer` to signal a customer is in the shop.
- `barber` to signal the barber is busy.

1. (5 points) Indicate the initial values for the three semaphores.

- `mutex`
- `customer`
- `barber`

2. (15 points) Complete the code above filling in as many copies of the following commands as you need, but no other code.

```
P(&mutex);  
V(&mutex);  
P(&customer);  
V(&customer);  
P(&barber);  
V(&barber);
```

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Solution: There are a number of solutions; below is one. Be careful to release the mutex before leaving. For this solution, initial values are `mutex = 1` (variable `customers` may be accessed), `customer = 0` (no customers) and `barber = 0` (barber is not busy).

```
void* customer() {  
  
    P(&mutex);  
    if (customers > N) {  
        V(&mutex);  
        return NULL;  
    }  
    customers += 1;  
    V(&mutex);  
  
    V(&customer);  
    P(&barber);  
    getHairCut();  
  
    P(&mutex);  
    customers -= 1;  
    V(&mutex);  
  
    return NULL;  
}  
  
void* barber() {  
    while(1) {  
        P(&customer);  
        V(&barber);  
        cutHair();  
    }  
}
```

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