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Assignment Project Exam Help

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Nature-Inspired Learning Algorithms (7CCSMBIM)



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- Stigmergy and Artificial Pheromone https://powcoder.com
- Simple Ant Colony Optimisation (SACO)
- Ant Sys And We Chat powcoder
- 6 Examples
- Ant Colony System (ACS)

Learning Objectives



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To know the kind of problems that can be solved by Ant Colony

Assignment Project Exam Help To know how Ant Colony Optimisation algorithms work and their

- To know how Ant Colony Optimisation algorithms work and their limitations.
- To appy An poorly Oppicarity a control response problems.

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Swarm Intelligence

As "Swarm intelligence is the property of a system whereby the collective of behaviours of (unsophisticated) age as interacting locally with their environment cause coherent functional global patterns to emerge."

• "Swalm Intelligence provides a basis with which it is possible to explore collective (or distributed) problem solving without centralised control or the provision of a global model."

Example: Add WeChat powcoder

- A group of fishes swim in the same direction.
- Ants work together to find food and haul back to the nest.



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Characteristics of Social Colonies

As Flexible: The colony can repond to internal uper Turbations and Help external challenges.

- Robust: Tasks are completed even if some individuals fail.
- Decentus Bis Sire of Books Company C
- Self-organised: Paths to solutions are emergent rather than predefined.



Self-organisation

A set of dynamical mechanisms whereby structures appear at the vel of a system from interactions of its lower-level compo

- Four basic ingredients:
 - Positive feedback (amplification): To show the right of direction to the o roje optimal solution into reinforce those portions bigood solutions that contribute to the quality of these solutions.
 - Negative feedback: to introduce a time scale into the algorithm through pheron one evaporation, to prevent premature convergence (stagnation), for counter-balance and stabilisation
 - Amplification of fluctuation: Randomness or errors, e.g., lost ant foragers can find new food sources. An element moves more randomly to search for a solution and then amplified by a positive feedback loop.
 - Multiple interactions: Direct or indirect communication (e.g., modification of the environment).



Ants

As Significant or earth to P100 milion years Exam Help Estimated total population: 10¹⁶ individuals.

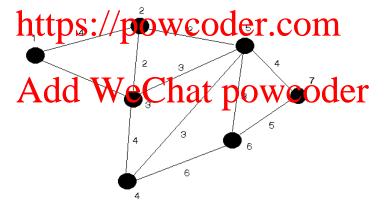
- Social insects live in colonies of 30 to millions of individuals.
- Collective being source of the contraction of nests, etc.
- stimula did se Whe Chat powcoder
- Individual performs simple and basic action based on information of local information.
- Simple actions appear to have a large random component.



Ant Optimisation Algorithm

A \$ 5 Find the shortest pain between their lest and food source, without any

visible, central, active coordination mechanisms.



Notation



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- x^k(t): the solution of ant k, which is a set of nodes visited by ant k.
- $\tilde{x}(t)$: the current best path (the best solution among $x^k(t)$) at generation/iteration t, which is a set of nodes visited by the best ant.

$\hat{x}(t)$: the global best path found from the first iteration of the algorithm $x_i(t)$ the best so this in (1, g, right) shart states (the idealign etc.) X an Help

- p: evaporation rate.
- n_{k} : number of ants.
- os://powcoder.com
- $\tau_{ii}(t)$: pheromone concentration associated with edge (i,j) at generation/iteration t.
- $\Delta \tau_{ii}^k(t)$: the change of pheromone concentration associated with edge (i,j) at generation/iteration t.
- $\Delta \tau_{i:}^{e}(t)$: the change of pheromone concentration associated with edge (i,j) visited by the elite ants at generation/iteration t.
- $f(\tilde{x}(t))$: the quality of the solution of the $\tilde{x}(t)$ (the best ant).
- $f(x^+(t))$: the cost(s) of the best solution(s) for $x^+(t)$ (the iteration-best or global best ant(s)).
- $L^{k}(t)$: length of the path (from the source to the destination) constructed by ant k.
- $d_{ii}(t)$: cos between edge (i,j). When t is dropped, d_{ij} is independent of generation/iteration t.
- $p_{ii}^k(t)$: transition probability of selecting the next node $j \in \mathcal{N}_i^k(t)$ by ant k and node i.
- $\mathcal{N}_{i}^{k}(t)$: the set of feasible nodes connected to node i, with respect to ant k.
- Q > 0: a non-zero positive constant.

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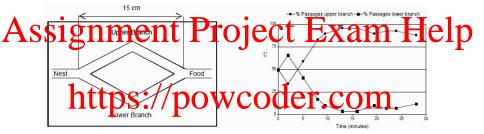
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The Binary Bridge Experiments



A simple and elegant experiment to study of foraging behaviour of ants.



- Ants deposit chemical pheromone while walking.
- Ants have larger profability to follow put th with night rether more viril WCOCET Probability of the next ant to choose path A:

$$P_A(t+1) = \frac{(c + n_A(t))^{\alpha}}{(c + n_A(t))^{\alpha} + (c + n_B(t))^{\alpha}} = 1 - P_B(t+1)$$

 $n_A(t)$ and $n_B(t)$: Number of ants on paths A and B, respectively.

c: degree of attraction of an unexplored branch.

 α : the bias to using pheromone deposits in the decision process



Artificial Ant Decision Process

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https: $|c| = \frac{(c+n_A(t))^{\alpha}}{(c+n_A(t))^{\alpha} + (c+n_B)^{\alpha}}$ if $r \leq P_A$ then; $|c| = \frac{(c+n_A(t))^{\alpha}}{(c+n_A(t))^{\alpha} + (c+n_B)^{\alpha}}$ end
end

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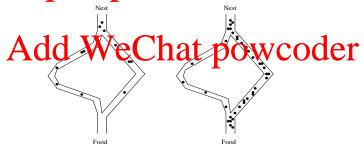
The Binary Bridge Experiments



Shortest path selection by forager ants

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• The pheromone on the shortest path is reinforced sooner (positive feed at the state of the shortest path is reinforced sooner (positive feed at the shortest path i



The Binary Bridge Experiments



Shortest path selection by forager ants

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Stigmergy and Artificial Pheromone



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Stigmergy is a class of mechanisms that mediate animal-to-animal interactions.

Assignment Project Fxam Help environment.

- Some signs observed by individual trigger a specific response or action, mitigal sinforce problems (and poster in the second of others).
- Two forms of stigmergy: sematectonic and sign-based.
 - Samategonic stipple communication on characteristics of the environment.
 - Sign-based stigmergy: communication via a signalling mechanism,
 e.g., implemented via chemical compounds deposited by ants.

Stigmergy and Artificial Pheromone



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• Artificial stigmergy: "indirect communication mediated by numeric

As modifications of environmental states which are invocally accessible lp by the communicating agent". (Dorigo and Di Caro)

• Artificial pheromone plays the role of stigmergic variable, which encapsulate the information used by artificial arts to communicate indirectly.

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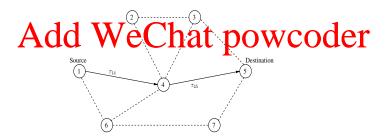
Simple Ant Colony Optimisation (SACO) https://powcoder.com



• (i,j): An edge from node i to node j.

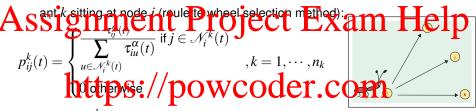
As 5 in Physippen Project with Edge in Help

- $\tau_{ii}(0)$ is assigned a small random value. Why?
- $L^k(t)$ I the battle from the source of the destination constructed by ant k.





ullet Transition probability of selecting the next node $j\in \mathscr{N}_i^k(t)$ by the



where $\mathcal{N}_i^k(t)$ is the set of feasible nodes connected to node i, with respect to the ant $k \neq 0$ is a constant.

- respect to the ant $k:\alpha>0$ is a constant.

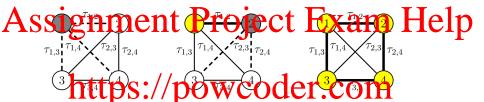
 If \mathcal{N}_{t} the previous sorth late i is included in the constant of the constant i is included in the constant i in the constant i is included in the constant i in the constant i is included in the constant i in the constant i is included in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i in the constant i is included in the constant i in the constant i in the constant i in the constant i is included in the constant i is the constant i in the constant i in
 - This may cause loops.
 - Loops are removed when the destination has been reached.

Example: Found path with a loop: 1–4–2–3–4–5

Path after removing a loop: 1-4-5



Example



$$\begin{array}{|c|c|c|c|c|} \hline \text{Node 1: } \mathcal{N}_1^k(t) = \{2,3,4\} & \text{Node 2: } \mathcal{N}_2^k(t) = \{3,4\} & \text{Node 4: } \mathcal{N}_4^k(t) = \{3\} \\ \hline p_{1,2}^k(t) = \overbrace{\tau_{1,3}^\alpha(t) + \tau_{1,3}^\alpha(t) + \tau_{1,4}^\alpha(t)}^{\tau_{1,3}^\alpha(t)} & \overbrace{\tau_{2,3}^\alpha(t) + \tau_{2,4}^\alpha(t)}^{\tau_{2,3}^\alpha(t)} & \overbrace{\tau_{2,3}^\alpha(t) + \tau_{2,4}^\alpha(t)}^{\tau_{2,3}^\alpha(t)} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,3}^\alpha(t) + \tau_{1,4}^\alpha(t)}^{\tau_{1,4}^\alpha(t)} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,3}^\alpha(t) + \tau_{1,4}^\alpha(t)}^{\tau_{1,4}^\alpha(t)}} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,3}^\alpha(t) + \tau_{1,4}^\alpha(t)}^{\tau_{1,4}^\alpha(t)}} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,3}^\alpha(t) + \tau_{1,4}^\alpha(t)}^{\tau_{1,4}^\alpha(t)}} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,3}^\alpha(t) + \tau_{1,4}^\alpha(t)}}^{\tau_{1,4}^\alpha(t)} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,3}^\alpha(t) + \tau_{1,4}^\alpha(t)}}^{\tau_{1,4}^\alpha(t)}} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,3}^\alpha(t) + \tau_{1,4}^\alpha(t)}}^{\tau_{1,4}^\alpha(t)} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,3}^\alpha(t) + \tau_{1,4}^\alpha(t)}}^{\tau_{1,4}^\alpha(t)}} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,4}^\alpha(t)}^{\tau_{1,4}^\alpha(t)}} & \overbrace{\tau_{1,2}^\alpha(t) + \tau_{1,4}^\alpha(t)}}^{\tau_{1,4}^\alpha(t)}} & \overbrace{\tau_{1,$$

Note: $\tau_{i,j}(t) = \tau_{j,i}(t)$



Example: Transition probability Table (as in the Binary Genetic Algorithm)

Æ	Not Sode D	That is 10 $ ho$ baptity p_{ij} (if	Octomulate I Transition Propago it	Help
	2	$rac{ au_{1,2}^{lpha}(t)}{ au_{1,2}^{lpha}(t) + au_{1,3}^{lpha}(t) + au_{1,4}^{lpha}(t)}$	$\frac{\tau_{1,2}^{\alpha}(t)}{\tau_{1,2}^{\alpha}(t) + \tau_{1,3}^{\alpha}(t) + \tau_{1,4}^{\alpha}(t)}$	_
	3	$\frac{\tau_{1,3}^{\alpha}(t)}{\tau_{1,2}^{\alpha}(t) + \tau_{1,3}^{\alpha}(t) + \tau_{1,4}^{\alpha}(t)}$	$\frac{\tau_{1,2}^{\alpha}(t) + \tau_{1,3}^{\alpha}(t)}{\tau_{1,2}^{\alpha}(t) + \tau_{1,3}^{\alpha}(t) + \tau_{1,4}^{\alpha}(t)}$	
	4		vc @der cem	

Assume that $\alpha = 1$, $\tau_{1,2} = 0.5$, $\tau_{1,3} = 0.3$ and $\tau_{1,4} = 0.2$.

Next node j	Transition Probability p_1^k :(t) Accur	nulated Transition Probability
2		nowcoder
3	$\frac{0.3}{0.5 + 0.3 + 0.2} = 0.3$	9.5 + 0.3 = 0.8
4	$\frac{0.3}{0.5 + 0.3 + 0.2} = 0.2$	0.5 + 0.3 + 0.2 = 1

Generate a random number, say, r=0.6. Node 3 is chosen as 0.6 is lying in between 0.5 and 0.8.



Evaporation of Pheromone Intensity (negative feedback)

Assignment of explore more. Assignment of explore more.

- To prevent premature convergence.
- For each edge (i,j), object mone intensity is reduced according to $\begin{array}{c} \text{TUPS.} / \text{POWCOGEN.COM} \\ \tau_{ii}(t) \leftarrow (1-\rho)\tau_{ii}(t) \end{array}$

where A and) (Who even the even or atting the responsibilities of the even of t



Update of Pheromone Intensity (positive feedback)

As After all ants have constructed their paths from the source to the Help destination, and air loops are removed, the pheromone intensity on

edge (i,j) is adjusted:

https://powconten.com

where



 $x^k(t)$ is the solution of ant k,

 $f(x^k(t))$ is the quality of the solution,

Q > 0 is a constant,

 n_k is the number of ants.



Example: Source node: 1; Target node: 5 ($d_{ij} = d_{ji}$, $\tau_{ij} = \tau_{ji}$ and $n_k = 2$)



- Ant 1: x (n) Etps://powcoder.com
- $f(x^1(t)) = d_{14} + d_{34} + d_{35}$

 $f(x^2(t)) = d_{14} + d_{42} + d_{23} + d_{35}$





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Example: Source node: 1; Target node: 5 ($d_{ij} = d_{ji}$, $\tau_{ij} = \tau_{ji}$ and $n_k = 2$)



- . Ant 1: https://powcoder.com
- $f(x^1(t)) = d_{14} + d_{34} + d_{35}$

 $f(x^2(t)) = d_{14} + d_{42} + d_{23} + d_{35}$

Pheromone update:

- Pheromagain: Weornate powcoder
- Update according to Ants' solutions



```
Simple Ant Colony Optimisation Algorithm
Initialise \tau_{ii}(0) to small random values; Let t = 0;
 Place n_{\nu} ents on the origin node;
                                                                                                       nent Project Exam Help
                              While destination has not been reached do.
                                              Select next node based on translation probability p_{ii}^{k}(t);
                                             Add (i,j) to path x^k(t);
                           Removal to the post of the pos
            end
            for each edge (i, j) of the graph do
                             Reduce the pheromone, \tau_{ii}(t) \leftarrow (1 - \rho)\tau_{ii}(t);
            end
                           Update that powcoder
            end
          t \leftarrow t + 1;
```

Table 2: Pseudo Code of Simple Ant Colony Optimisation Algorithm.





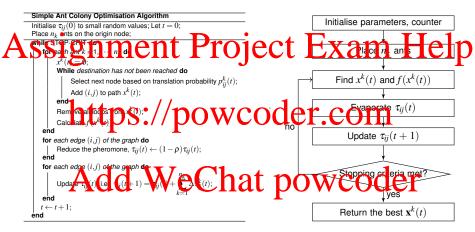


Table 2: Pseudo Code of Simple Ant Colony Optimisation Algorithm.

Figure 1: Flowchart of Simple Ant Colony Optimisation Algorithm.



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Stopping Criteria:

Assignment iterapisches been excelled an Help an acceptable solution has been found.

all (or most) ants follow the same path.

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Ant System (AS)



Ant System was developed based on SACO.

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- Includes **heuristic information** to transition probability $p_{ij}^k(t)$.
- Includes (attabulist to the set of feasible nodes of the set of feasible nodes).

 May include only the immediate neighbours of node i.
 - Market death and a set of Shall and I have a street
 - May include all nodes not yet visited by ant k to prevent loops.
- Different undate stricted for pheromone intensity coder
- Elitism is implemented.



Transition Probability (two methods):

Assignment Project Exam Help $p_{ij}^{k}(t) = \begin{cases} \sum_{u \in \mathcal{N}_{i}^{k}(t)} \tau_{iu}^{\alpha}(t) \eta_{iu}^{\beta}(t) & , k = 1, \cdots, n_{k} \\ \text{https://powcoder.com} \end{cases}$

- $\tau_{ij}(t)$: pheromone intensity/concentration.
- $\eta_{ij}(t)$: a priori effectiveness of the move from i to j (i.e. the attractiveness, or desirability) of the move $\alpha>0$, $\beta>0$: predefined constants.
- $\eta_{ij}(t) = \frac{1}{d_{ii}(t)}$ improves the attractiveness of the edge (i,j).
 - $d_{ij}(t)$: cost between edge (i,j).



Transition Probability (two methods):



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Pheromone evaporation:

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Update of pheromone intensity/concentration:

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Update of pheromone intensity/concentration:

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- Ant-cycle AS: $\Delta \tau_{ij}^k(t) = \sqrt{\frac{\varrho}{f(x^k(t))}}$ if edge (i,j) occurs in path $x^k(t)$
- Ant-density AS: $\Delta \tau_{ij}^k(t) = \begin{cases} \mathcal{Q} \text{ if edge } (i,j) \text{ occurs in path } x^k(t) \\ \text{Perwise at powcoder} \end{cases}$ Ant-quantity AS: $\Delta \tau_{ij}^k(t) = \begin{cases} \frac{\mathcal{Q}}{d_{ij}(t)} \text{ if edge } (i,j) \text{ occurs in path } x^k(t) \\ 0 \text{ otherwise} \end{cases}$
- - $d_{ii}(t)$: cost between edge (i,j).



Elitist Strategy:

$$Assign the transfer fix (solution) a Conjugate fix (solution) and the fixed transfer fix (solution) and the fixed transfer fixed transfer$$

- n_e : number of elite ants.
- ·http://www.powcoder.com

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Ant System (AS)



Elitist Strategy:

 $\begin{array}{l} \bullet \quad \tau_{ij}(t+1) = \tau_{ij}(t) + \sum_{i=1}^{n_k} \Delta \tau_{ii}^k(t) + n_e \Delta \tau_{ij}^e(t) \\ \textbf{Assignment}(solution) \\ \textbf{Exam Help} \end{array}$ $\bullet \ f(\tilde{x}(t)) = \min_{k=1,\dots,n_k} f(x^k(t)).$

n_e: number of elite ants.

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- Ant 1: $x^1(t) = \tilde{x}(t) = \{1,4,3,5\}$ (Assume this is the shortest path)
- $f(x^1(t)) = f(\tilde{x}(t)) = d_{14} + d_{34} + d_{35}$

• Ant 2:
$$x^2(t) = \{1, 4, 2, 3, 5\}$$

 $f(x^2(t)) = d_{14} + d_{42} + d_{23} + d_{35}$

Ant System (AS)



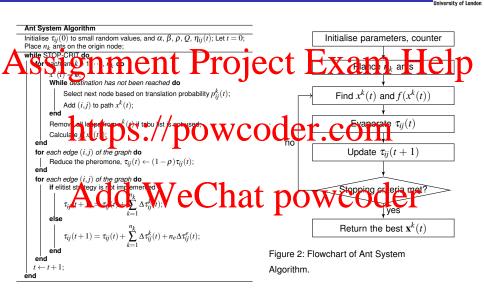


Table 3: Pseudo Code of Ant System Algorithm.

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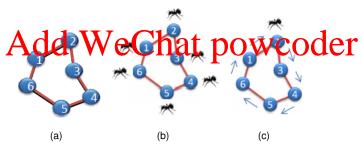
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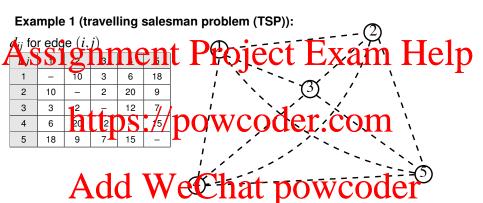
Example 1 (travelling salesman problem (TSP)): Given a set of *n* cities,

TSP requires a salesman to find the shortest route to return to the starting its sold entire entire entire exam Help

- Place ants at different nodes.
- Find the path for each ant.
- Go to step 2 urtill stopping creeia have be satisfied.











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2	10	-	2	20	9
3	3	12	LĪ.	12	7/
4	6	20	2	DS	1 5/

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 $au_{ij}(t)$ for edge (i,j)

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ı (j		<u> </u>	4 P 4	7		-
1	_	0.3	1.2	0.8	0.1	x
2	0.3	-	1.5	0.1	0.7	١.
3	1.2	1.5	-	0.9	0.5	x
4	0.8	0.1	0.9	-	0.2	x
5	0.1	0.7	0.5	0.2	-	x

$$x^{2}(t) = \{1\}$$

 $x^{2}(t) = \{2\}$

$$x^3(t) = \{3\}$$

$$x^4(t) = \{4\}$$

$$x^5(t) = \{5\}$$







ment Project Exam Help $_{ij}$ for edge (i,j)

2	10	_	2	20	9	!
3	3	12	LĪ.	12	7/	
4	6	20	2	08	/ 5/	powco
						, ,

 $\tau_{ij}(t)$ for edge (i,j)

$\iota \setminus j$	- 1	4	(P(4	/ \	P
1	_	0.3	1.2	0.8	0.1	x
2	0.3	-	1.5	0.1	0.7	
3	1.2	1.5	_	0.9	0.5	x
4	0.8	0.1	0.9	-	0.2	x
5	0.1	0.7	0.5	0.2	-	x

٦	Talland	40.0111.000.7	1 = = =
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4	$x^{1}(t) = \{1, 3\}$	r	
╛	$r^2(t) = \{2, 1\}$		

$$x^{3}(t) = \{3,4\}$$

 $x^{4}(t) = \{4,2\}$

$$x^5(t) = \{5,4\}$$

$$x^{3}(t) = \{5,4\}$$







1	-	10	3	6	18
2	10	-	2	20	9
3	3	12	Ī.	12	7/
4	6	20	2) S	1 5

Example 1 (travelling salesman problem (TSP)):

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 $\tau_{ij}(t)$ for edge (i,j)

l\J	1	2		4	ΛI (Р
1	-	0.3	1.2	0.8	0.1	x
2	0.3	-	1.5	0.1	0.7	
3	1.2	1.5	_	0.9	0.5	x
4	0.8	0.1	0.9	-	0.2	x
5	0.1	0.7	0.5	0.2	-	x

_ 9	21.			```	`\
7	Rani	f no	***	vd a	(C) <mark>₹</mark>
	$(t) = \{1, 3, 2\}$	i po	WCC	JUCI	L
$\frac{1}{7}$	$(t) = \{1, 3, 2\}$	} —			

$$x^{2}(t) = \{2, 1, 3\}$$

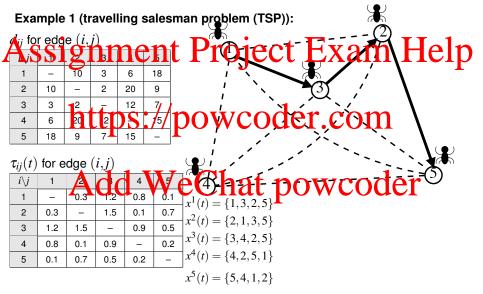
 $x^{3}(t) = \{3, 4, 2\}$

$$x^4(t) = \{4, 2, 5\}$$

$$x^5(t) = \{5, 4, 1\}$$

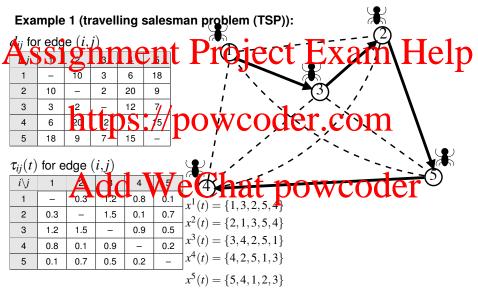






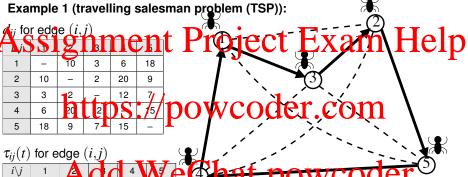








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- 0		\rightarrow			
1	_	0.3	1.2	0.8	0.1
2	0.3	-	1.5	0.1	0.7
3	1.2	1.5	-	0.9	0.5
4	0.8	0.1	0.9	_	0.2
5	0.1	0.7	0.5	0.2	-

$(x^*(t) = \{1, 3, 2, 3, 4, 1\}, f(x^*(t)) = a_{13} + a_{32} + a_{25} + a_{54} + a_{41} = 33$
$x^{2}(t) = \{2, 1, 3, 5, 4, 2\}, f(x^{2}(t)) = d_{21} + d_{13} + d_{35} + d_{54} + d_{42} = 55$
$x^2(t) = \{2,1,3,5,4,2\}, f(x^2(t)) = d_{21} + d_{13} + d_{35} + d_{54} + d_{42} = 55$ $x^3(t) = \{3,4,2,5,1,3\}, f(x^3(t)) = d_{34} + d_{42} + d_{25} + d_{51} + d_{13} = 62$ $x^4(t) = \{4,2,5,1,3,4\}, f(x^4(t)) = d_{42} + d_{25} + d_{51} + d_{13} + d_{34} = 62$
$x^{4}(t) = \{4, 2, 5, 1, 3, 4\}, f(x^{4}(t)) = d_{42} + d_{25} + d_{51} + d_{13} + d_{34} = 62$

 $x^{5}(t) = \{5, 4, 1, 2, 3, 5\}, f(x^{5}(t)) = d_{54} + d_{41} + d_{12} + d_{23} + d_{35} = 40$



Example 1 (travelling salesman problem (TSP)):

• Evaporation of Pheromone Intensity (negative feedback)

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• e.g., $\rho = 0.2$, $\tau_{54}(t) = (1 - 0.2)\tau_{54}(t) = 0.8 \times 0.2 = 0.16$

Update of Phetopane Intensity (positive feedback) $\begin{array}{c} \text{Oder } f_{ij}(t+1) = \tau_{ij}(t) + \sum_{k=1}^{n_k} \Delta \tau_{ij}^k(t), \quad \Delta \tau_{ij}^k(t) = \begin{cases} \frac{Q}{f(x^k(t))} & \text{if edge } (i,j) \text{ occurs in path } x^k(t) \\ 0 & \text{otherwise} \end{cases}$

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- SACO: e.g., edge (5,4), $n_k=5$ (only ants 1, 2, 5 passed through), Q=1, $\tau_{54}(t+1)=0.16+\frac{1}{35}+\frac{1}{55}+\frac{1}{40}=0.2318$
- AS: e.g., edge (5,4), Ant-quantity AS, elitism is implemented, Q=1, $n_e=1$, $\tau_{54}(t+1)=0.16+\frac{1}{15}+\frac{1}{15}+\frac{1}{15}+1\times\frac{1}{35}=0.3886$

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Ant Colony System was developed based on AS.

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- Candidate lists are used to favour specific nodes.
- Different pheromone Jupidate rule, $\tau_{ii}(t)$ oder. com
 - Local update rule: pheromone evaporation.

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Transition Probability: The k-th ant moving from node i to node j is

Assignment Project Exam Help $\int_{J \text{ otherwise}} \prod_{u \in \mathcal{N}_{i}^{k}(t)} \Pr_{u \in \mathcal{N}_{i}^{k}(t)} \Pr_$ according to

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- $r_0 \in [0,1]$: user-specified parameter; used to balance exploration and exploitation.
- $\mathcal{N}_i^k(t)$: a set of valid nodes to be visited by the k-th ant sitting at node i.
 $J \in \mathcal{N}_i^k(t)$ is a node random value cteral coording to that node to the point \mathbf{v} if $J \in \mathcal{N}_i^k(t)$ if $J \in \mathcal{N}_i^k(t)$ $p_{iJ}^k(t) = \begin{cases} \frac{\tau_{iJ}(t)\eta_{iJ}^\beta(t)}{\sum\limits_{u \in \mathcal{N}_i^k(t)} \tau_{iu}(t)\eta_{iu}^\beta(t)} & \text{if } J \in \mathcal{N}_i^k(t) \\ 0 & \text{otherwise} \end{cases}$
- $r \le r_0$: the algorithm exploits by favouring the best edge.
- r > r₀: the algorithm explores.



Example:

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Example:

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- A set of valid nodes for ant 4: $\mathcal{N}_1^4(t) = \{2,3,7\}$
- $\bullet \ \, \text{For ar} \\ \mathbf{h} \\ \mathbf{ttp} \\ \mathbf{h} \\ \mathbf{m} \\ \mathbf{pow} \\ \mathbf{pow} \\ \mathbf{coder} \\ \mathbf{ttp} \\ \mathbf{h} \\ \mathbf{ttp} \\ \mathbf{pow} \\ \mathbf{coder} \\ \mathbf{ttp} \\ \mathbf{tt$
 - Assume $r_0 = 0.2$, r = 0.1.
 - $\label{eq:theorem} \begin{array}{l} \bullet \ \, \text{Assume} \, \, \eta_{1,2}^{\beta}(t) = \eta_{1,3}^{\beta}(t) = \eta_{1,7}^{\beta}(t); \, \tau_{1,2}(t) = 0.22, \, \tau_{1,3}(t) = 0.33, \, \tau_{1,7}(t) = 0.44, \\ \text{with policial choice.} \ \, \text{VeChat powcoder.} \end{array}$



Example:

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- A set of valid nodes for ant 4: $\mathcal{N}_1^4(t) = \{2,3,7\}$
- For ar \mathbf{h} ttp \mathbf{h} arg \mathbf{m} arg \mathbf{m} \mathbf{h} \mathbf{h}
 - Assume $r_0 = 0.2$, r = 0.1.
 - Assume $\eta_{1,2}^{\beta}(t) = \eta_{1,3}^{\beta}(t) = \eta_{1,7}^{\beta}(t); \tau_{1,2}(t) = 0.22, \tau_{1,3}(t) = 0.33, \tau_{1,7}(t) = 0.44,$

- - Probability of choosing nodes 2, 3, 7 for ant 4 (sitting at node 1 currently) are $p_{12}^4(t)$, $p_{13}^4(t)$ and $p_{17}^4(t)$, respectively.
 - Probability is 0 for choosing nodes other than nodes 2, 3, 7.



Local and Global Update Rules:

As sois update rule: Phoron Pre-conceptrations Te updated for Help

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Local and Global Update Rules:

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- $\rho_L \in (0,1)$ (0 and 1 are not inclusive): a user-specified parameter.
- · A dad matter that powcoder

Why 0 and 1 are not allowed in ρ_L ?

Why τ_0 is not allowed to be 0?



Local and Global Update Rules:

Global update rule: Reinforcement of pheromone concentrations is

Assignment Project Exam Help $\tau_{ii}(t+1) = (1-\rho_G)\tau_{ii}(t) + \rho_G\Delta\tau_{ii}(t)$

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Local and Global Update Rules:

• Global update rule: Reinforcement of pheromone concentrations is

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$\underset{0 \text{ otherwise}}{\underbrace{https://powcoder.com}}$

- $\in (0,1)$ (0 and 1 are not inclusive, why?): a user-specified VeChat powcoder
- $x^+(t)$: the best solution(s) giving the shortest path(s).
 - iteration-best strategy: $x^+(t)$ represents the best path found during the current generation/iteration t, denoted as $\tilde{x}(t)$.
 - global-best strategy: $x^+(t)$ represents the best path found from the first iteration to the current generation/iteration t of the algorithm, denoted as $\hat{x}(t)$.
- $f(x^+(t))$ denotes the cost(s) of the best solution(s).



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```
Ant Colony System Algorithm
Initialise \tau_{ij}(0) to small random values, and \beta, \rho_L, \rho_G, \tau_0 to \eta_{ij}(t); Let t=0;
Place \eta_A arts in the printing of the initial position of the color of the colo
  Ant Colony System Algorithm
                                    While destination has not been reached do.
                                                    Select next node based on equation (1);
                                                    Add (i, j) to path x^k(t);
                                                                                                                                                               by lift is/n psowcoder.com
                end
                for each edge (i, j) of the graph do
                                  Apply local update rule: \tau_{ii}(t) \leftarrow (1 - \rho_L)\tau_{ii}(t) + \rho_L\tau_0;
                end
                                                                                                                                                                                        Vechat powcoder
                Update the global best solution \hat{i}(t) and its
                end
              t \leftarrow t + 1;
```

Table 4: Pseudo Code of Ant Colony System Algorithm.



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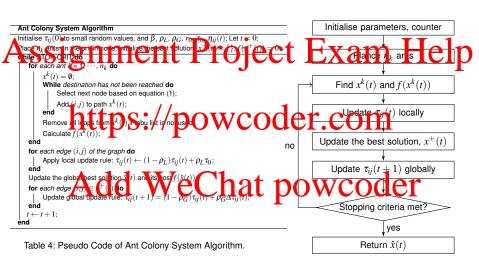


Figure 3: Flowchart of Ant Colony System Algorithm.