CIS 471/571 (Fall 2020): Introduction to Artificial Intelligence

Lecture 7: Expectimax, Utilities Add WeChat powcoder

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Source: http://ai.berkeley.edu/home.html

Reminders

- Project 2: Multi-agent Search
 - Deadline: Oct 27th, 2020

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- Homework 2: CSPs and Games com
 - Deadline: Oct 24th, 2020WeChat powcoder

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Today

Expectimax Search Assignment Project Exam Help

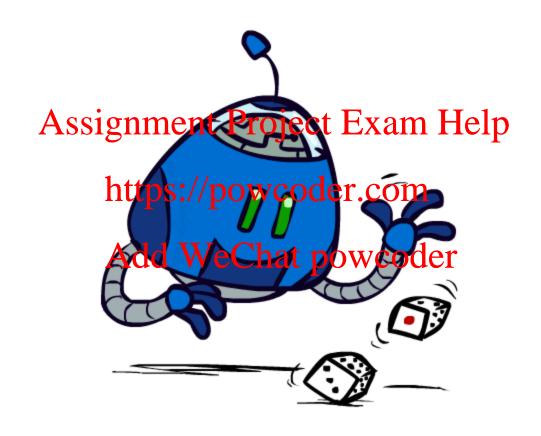
Utilities

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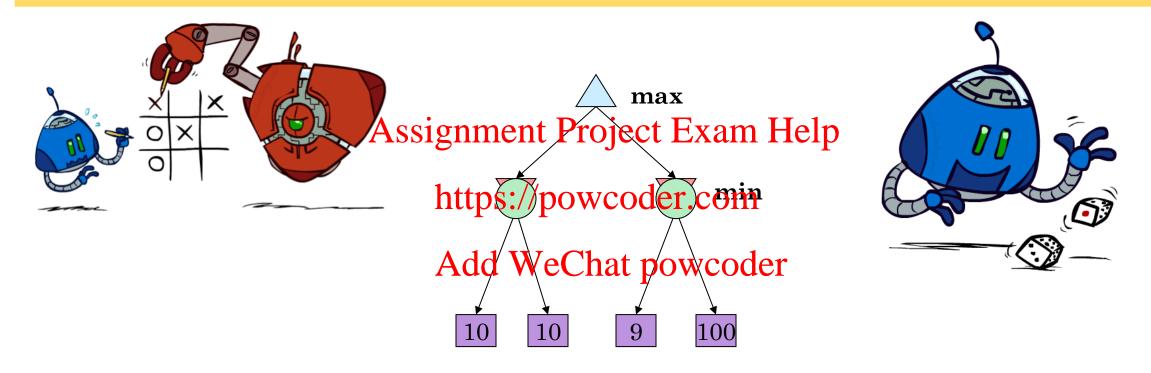
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Uncertain Outcomes



Worst-Case vs. Average Case

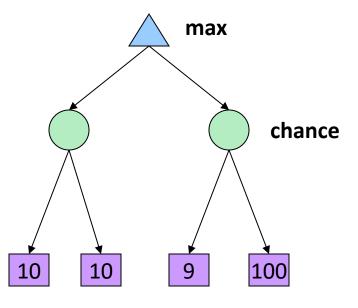


Idea: Uncertain outcomes controlled by chance, not an adversary!



Expectimax Search

- Why wouldn't we know what the result of an action will be?
 - Explicit randomness: rolling dice
 - Unpredictable opponents: the ghosts respond randomly
 - Actions can fail: when moving a robot, wheels might slip
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- Values should now reflect average-case (expectimax) outcomes, not worst-case (mining type type coder.com
- Expectimax search: compute the average score under optimal play
 - Max nodes as in minimax search
 - Chance nodes are like min nodes but the outcome is uncertain
 - Calculate their expected utilities
 - I.e. take weighted average (expectation) of children
- Later, we'll learn how to formalize the underlying uncertain-result problems as Markov Decision Processes



Expectimax Pseudocode

```
def value(state):

if the state is a terminal state: return the state's utility

if the next agent is EXP: return exp-value(state)

if the next agent is EXP: return exp-value(state)

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```

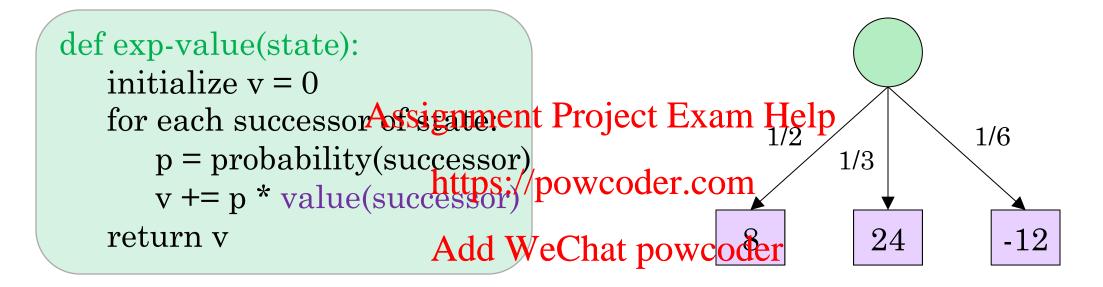
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def max-value(state):
 initialize v = -∞
 for each successor of state:
 v = max(v, value(successor))
 return v

def exp-value(state):
 initialize v = 0
 for each successor of state:
 p = probability(successor)
 v += p * value(successor)

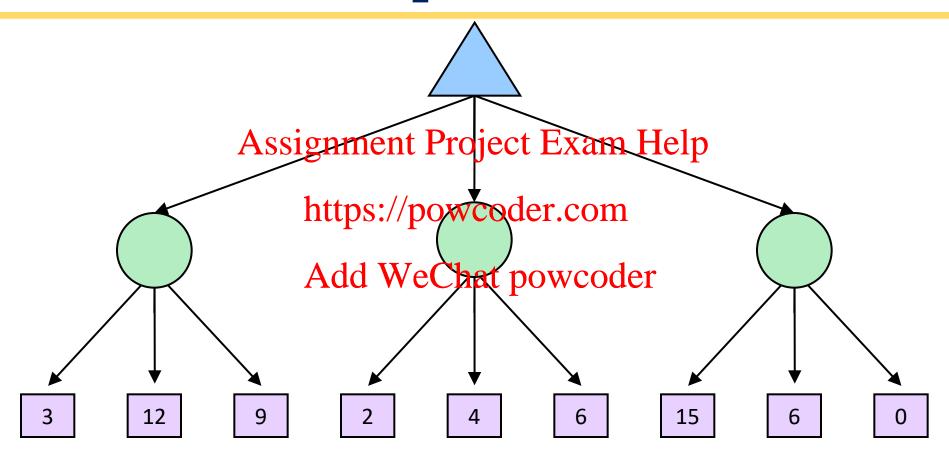
return v

Expectimax Pseudocode

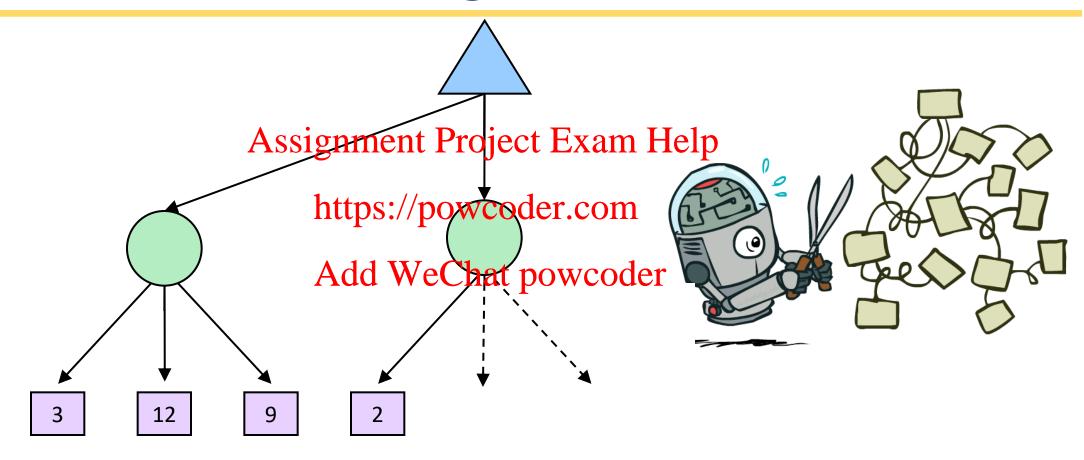


$$v = (1/2) (8) + (1/3) (24) + (1/6) (-12) = 10$$

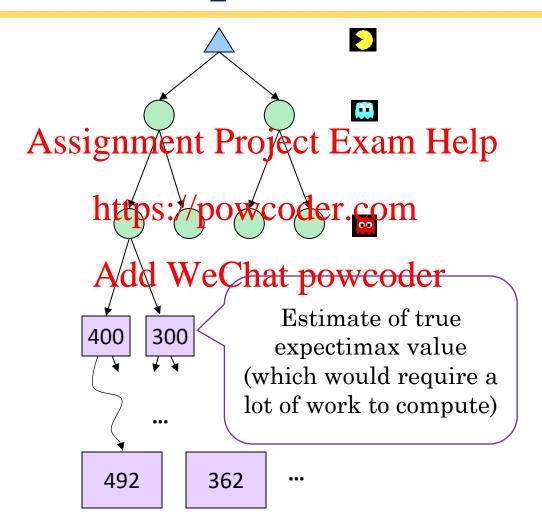
Expectimax Example



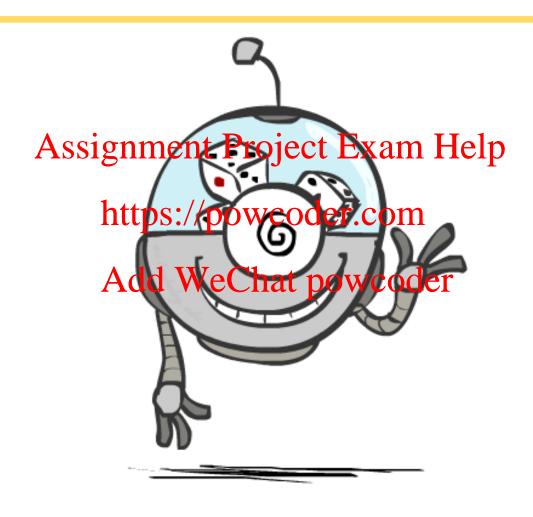
Expectimax Pruning?



Depth-Limited Expectimax



Probabilities

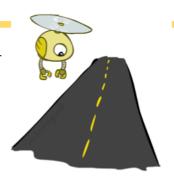


Reminder: Probabilities

- A random variable represents an event whose outcome is unknown
- A probability distribution is an assignment of weights to outcomes
- Example: Traffic on freewayssignment Project Exam Help
 - Random variable: T = whether there's traffic
 - Outcomes: T in {none, light, heavattps://powcoder.com
 - Distribution: P(T=none) = 0.25, P(T=light) = 0.50, P(T=heavy) = 0.25

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- Some laws of probability (more later):
 - Probabilities are always non-negative
 - Probabilities over all possible outcomes sum to one
- As we get more evidence, probabilities may change:
 - P(T=heavy) = 0.25, $P(T=heavy \mid Hour=8am) = 0.60$
 - We'll talk about methods for reasoning and updating probabilities later



0.25



0.50



0.25



Reminder: Expectations

• The expected value of a function of a random variable is the average, weighted by the probability distribution over outcomes Assignment Project Exam Help

• Example: How long to gehttps://powroute?.com

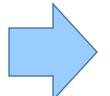
Time:

Probability: 0.25

Add Weeminpowcoder min

0.50

0.25



35









What Probabilities to Use?

• In expectimax search, we have a probabilistic model of how the opponent (or environment) will behave in any state

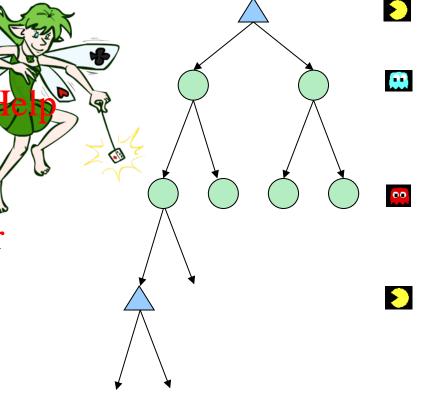
• Model could be a simple uniforing mirror that Paro (redta Exam die)

• Model could be sophisticated and require a great deal computation

• We have a chance node for any autoprove that powcoder control: opponent or environment

• The model might say that adversarial actions are likely!

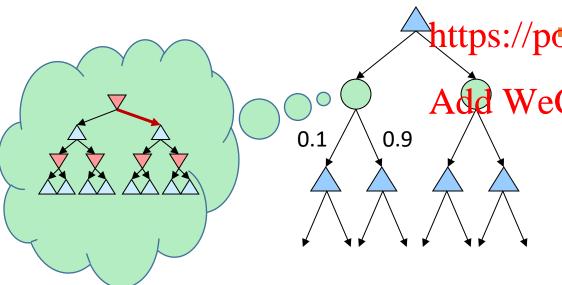
 For now, assume each chance node magically comes along with probabilities that specify the distribution over its outcomes



Having a probabilistic belief about another agent's action does not mean that the agent is flipping any coins!

Quiz: Informed Probabilities

- Let's say you know that your opponent is actually running a depth 2 minimax, using the result 80% of the time, and moving randomly otherwise
- Question: What tree search should projecte Exam Help



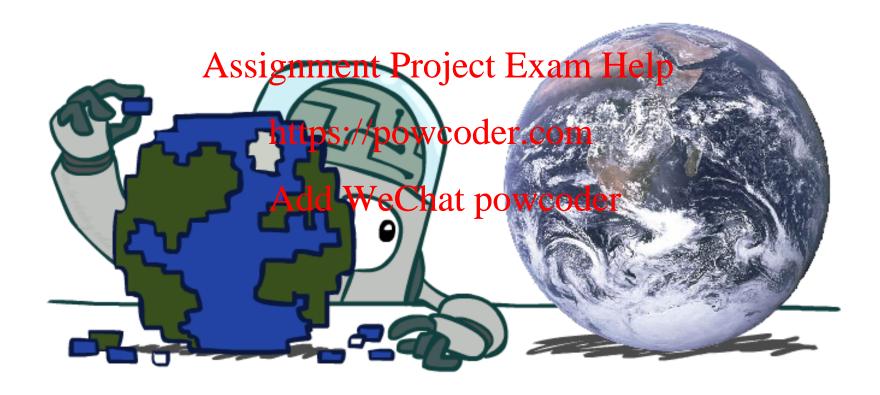
https://poweoderecompectimax!

To figure out EACH chance node's **provedities**, you have to run a simulation of your opponent

- This kind of thing gets very slow very quickly
- Even worse if you have to simulate your opponent simulating you...
- ... except for minimax, which has the nice property that it all collapses into one game tree



Modeling Assumptions



The Dangers of Optimism and Pessimism

Dangerous Optimism

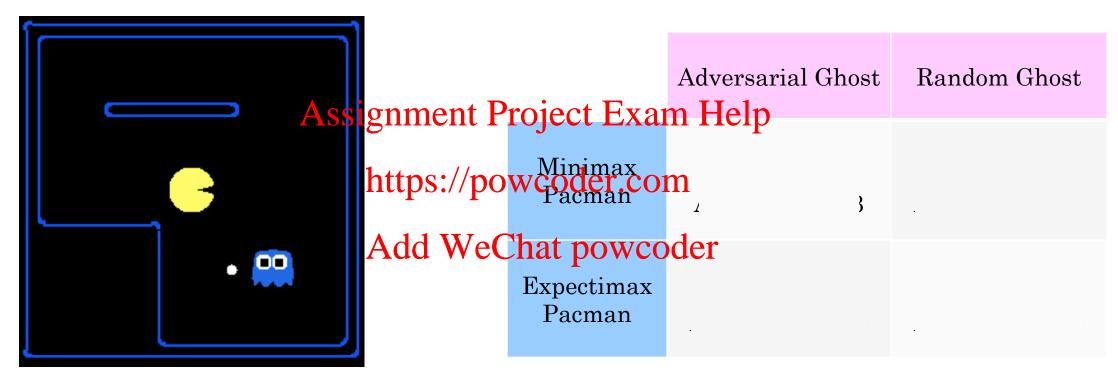
Assuming chance when the world is adversarial

Dangerous Pessimism

Assuming the worst case when it's not likely



Assumptions vs. Reality

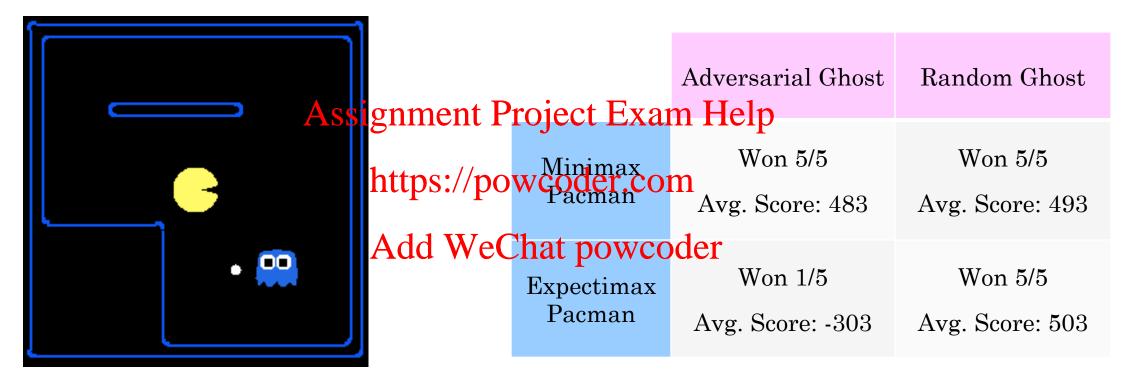


Results from playing 5 games

Pacman used depth 4 search with an eval function that avoids trouble Ghost used depth 2 search with an eval function that seeks Pacman



Assumptions vs. Reality

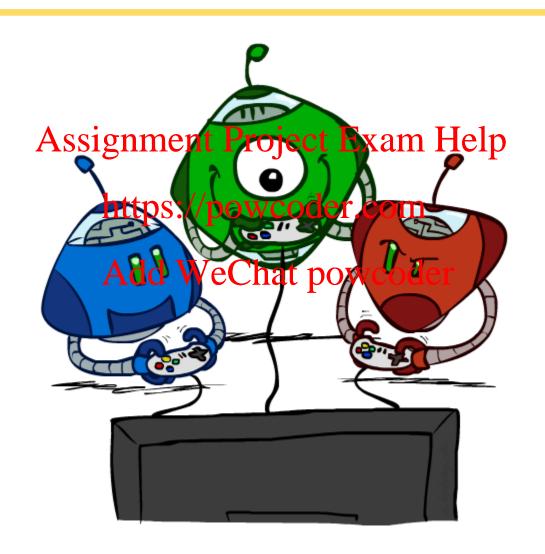


Results from playing 5 games

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Other Game Types



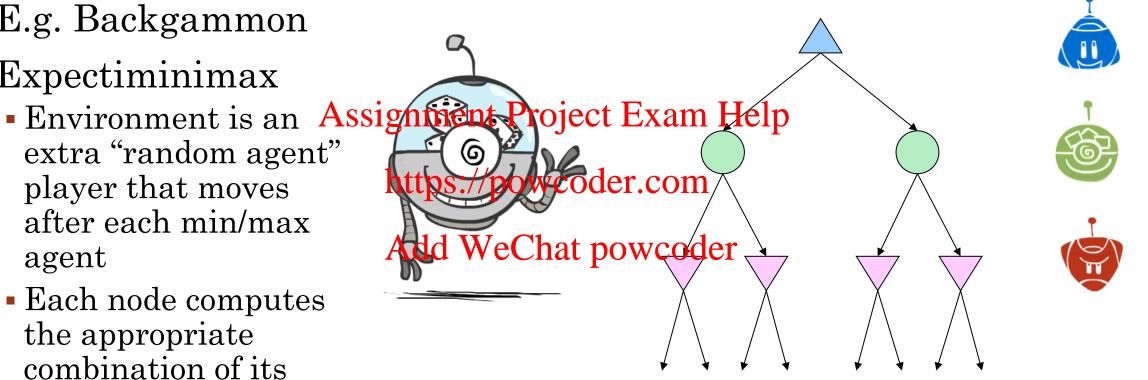
Mixed Layer Types

• E.g. Backgammon

Expectiminimax

extra "random agent" player that moves after each min/max agent

 Each node computes the appropriate combination of its children





Multi-Agent Utilities

• What if the game is not zero-sum, or has multiple players?

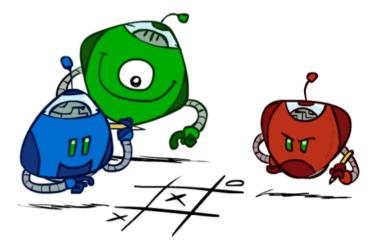


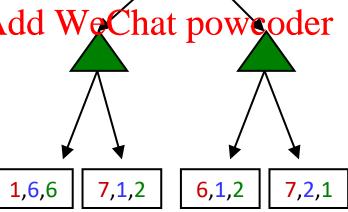
• Terminals have utility tupies ignment Project Exam Help

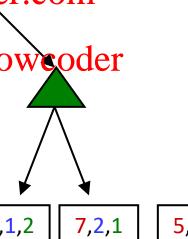
Node values are also utility tuples

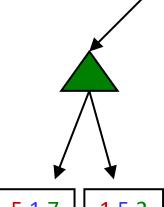
• Each player maximizes its own tons on power ter.com

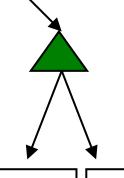
Each player masses
 Can give rise to cooperation and Add We Chat poweder



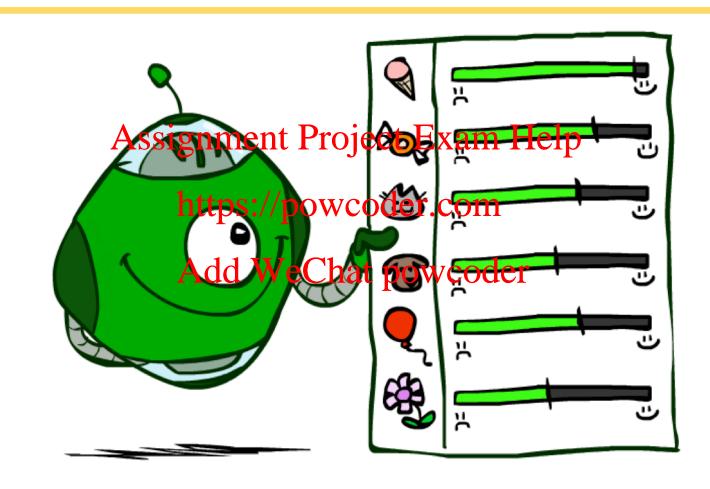








Utilities



Maximum Expected Utility

• Why should we average utilities? Why not minimax?

• Principle of maximum expected utility. Exam Help

• A rational agent should chose the action that maximizes its expected utility, given its knowledge /powcoder.com

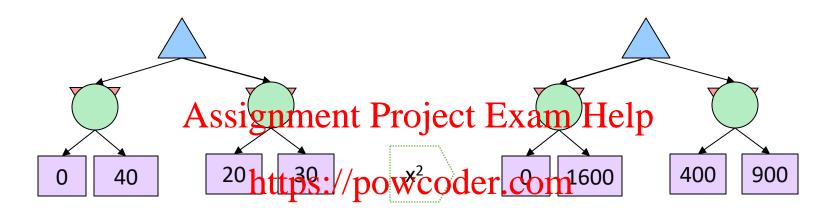
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- Questions:
 - Where do utilities come from?
 - How do we know such utilities even exist?
 - How do we know that averaging even makes sense?
 - What if our behavior (preferences) can't be described by utilities?





What Utilities to Use?



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- For worst-case minimax reasoning, terminal function scale doesn't matter
 - We just want better states to have higher evaluations (get the ordering right)
 - We call this insensitivity to monotonic transformations
- For average-case expectimax reasoning, we need *magnitudes* to be meaningful

Utilities

Utilities are functions from outcomes (states of the world) to real numbers that describe ament Project Exam Help agent's preferences
 https://powcoder.com



- Where do utilities come from WeChat powcoder
 - In a game, may be simple (+1/-1)
 - Utilities summarize the agent's goals
 - Theorem: any "rational" preferences can be summarized as a utility function

Utilities: Uncertain Outcomes



Preferences

 An agent must have preferences among:

• Prizes: *A*, *B*, etc.

- Frizes. A, D, etc.

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Lotteries: situations with uncertain prizes

$$L = [p, A; (1-p)_{https://powcoder.com}]$$

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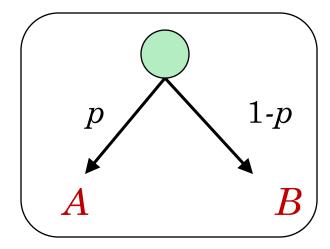
• Preference: $A \succ B$

• Indifference: $A \sim B$



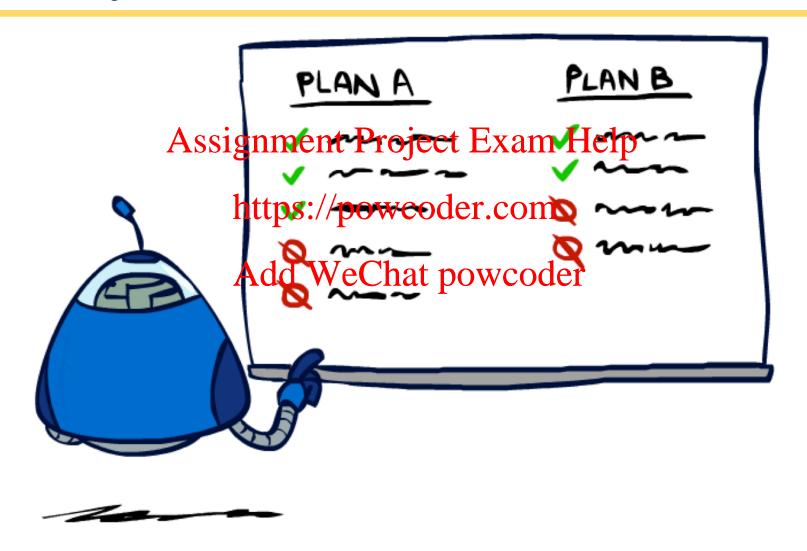
A Prize

A Lottery





Rationality



Rational Preferences

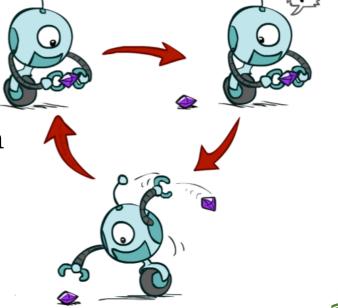
• We want some constraints on preferences before we call them rational, such as:

Axiom of Transitivity: $(A > B) \land (B > C) \Rightarrow (A > C)$

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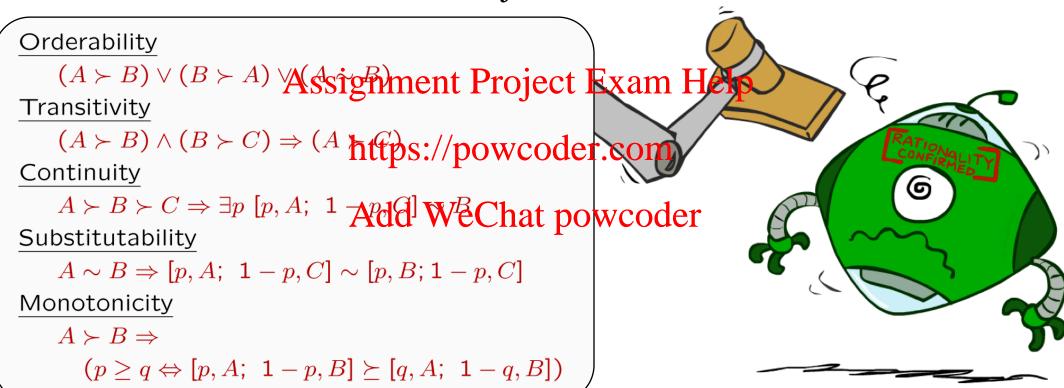
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- For example: an agent with intransitive preferences can be induced to give away all of its money
 - If B > C, then an agent with C would pay (say) 1 cent to get B
 - If A > B, then an agent with B would pay (say) 1 cent to get A
 - If C > A, then an agent with A would pay (say) 1 cent to get C



Rational Preferences

The Axioms of Rationality



Theorem: Rational preferences imply behavior describable as maximization of expected utility

MEU Principle

• Theorem [Ramsey, 1931; von Neumann & Morgenstern, 1944]

• Given any preferences satisfying these constraints, there exists a real-valued

function U such that:

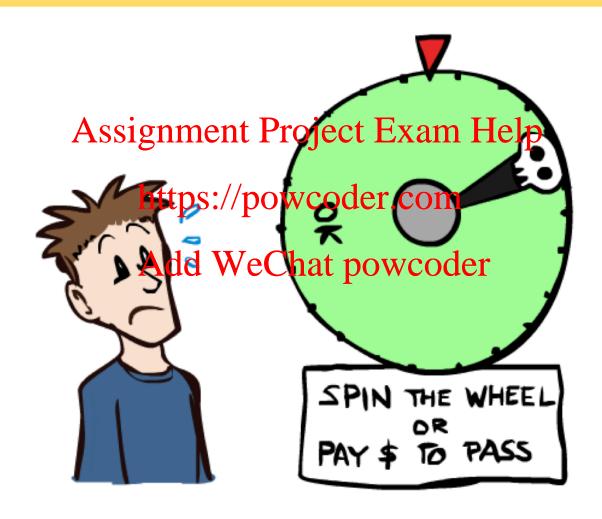
Usuch that:
$$U(A) \geq U(B) \Leftrightarrow A \succeq B$$

$$U([p_1, S_1; \dots; p_n, S_n]) = \sum_i p_i U(S_i)$$
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• I.e. values assigned by U preserve preferences of both prizes and lotteries!

- Maximum expected utility (MEU) principle:
 - Choose the action that maximizes expected utility

Human Utilities



Human Utilities

- Utilities map states to real numbers. Which numbers?
- Standard approach to assessment (elicitation) of human utilities:
 - Compare a prize A to assandardelettprojechetween Help
 - "best possible prize" u₊ with probability p
 - "worst possible catastrophe" https://prowabiliter!com

 - Adjust lottery probability p until indifference: A \sim L_p Resulting p is a utility in [0,4]dd WeChat powcoder





Human Utilities: Example

- •A person is given the choice between 2 scenarios:
 - Guaranteed scenario: the person receives \$50
 - Uncertain scenarios ignorals frigge to the person receive \$100 or not.

 https://powcoder.com
- Which choice would that person make?

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Risk Aversion

- •Risk averse: would accept the guaranteed payment of (less than) \$50 rather than take the gamble

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- •Risk neutral: indifferent powcoder of the bet and the guaranteed \$50 payment eChat powcoder

•Risk seeking: would accept the bet even when the guaranteed payment is more than \$50

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Prospect Theory: Utility Function

Risk aversion: convexity

Risk averse regarding gain

• Risk seeking regarding signment Project Exam Help

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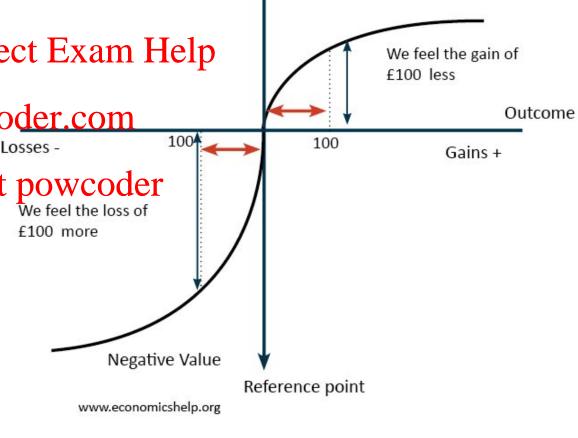
Loss aversion

Losses are felt more strong than WeChat powcoder we feel the loss of

Endowment effect

We values things we own more highly

 Reference point: differentiate gains and loss



Positive Value

Source: https://www.economicshelp.org/blog/glossary/prospect-theory/