CIS 471/571 (Fall 2020): Introduction Artificial Intelligence

Lecture 18: HMINs Particle Filters

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Source: http://ai.berkeley.edu/home.html

Announcement

- •Class on Thursday, Dec 03rd
 - Exam review

Assignment Project Exam Help

- End-of-course Surveytps://powcoder.com
 - Open until 06:00 PM and Frie Dec 04th powcoder

Thanh H. Nguyen 11/30/20

Today

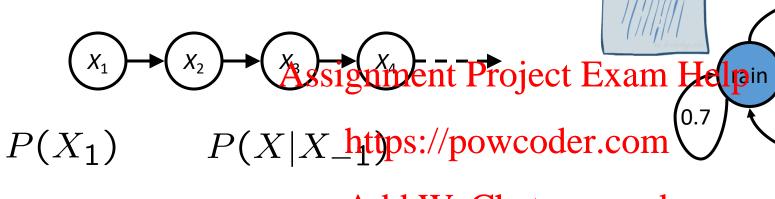
- •HMMs
 - Particle filters

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- Applications: https://powcoder.com
 - Robot localization / mapping Add WeChat powcoder

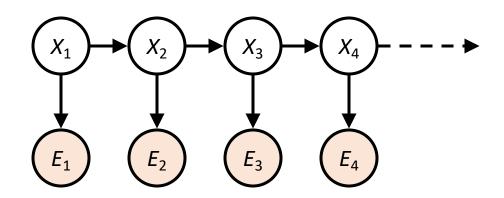
Recap: Reasoning Over Time

Markov models



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Hidden Markov models





0.3

0.3

X	E	Р
rain	umbrella	0.9
rain	no umbrella	0.1
sun	umbrella	0.2
sun	no umbrella	8.0



Filtering / Monitoring

- Filtering, or monitoring, is the task of tracking the distribution $B_t(X) = P_t(X_t \mid e_1, ..., e_t)$ (the belief state) over time Assignment Project Exam Help
- We start with $B_1(X)$ in the start with B_1

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• As time passes, or we get observations, we update B(X)

The Forward Algorithm

We are given evidence at each time and want to know

$$B_t(X) = P(X_t|e_{1:t})$$

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- Induction: assuming we have current belief $B_t(X) = P(X_t|e_{1:t})$ Intermediate belief update: $B_{t+1}(X) = P(X_{t+1}|e_{1:t})$

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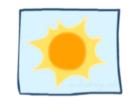
$$P(X_{t+1}|e_{1:(t+1)}) \leftarrow P(X_{t+1}|e_{1:t}) \leftarrow P(X_t|e_{1:t})$$

Observation update

Passage of time update

Example: Weather HMM





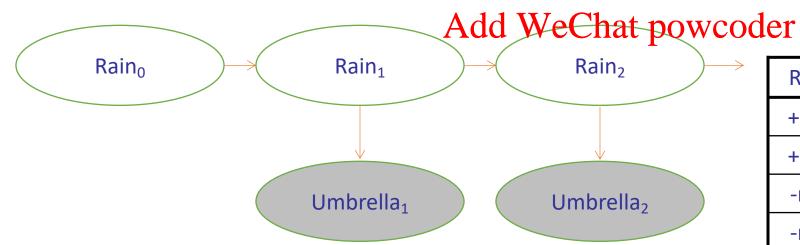


B(+r) = 0.5

$$B(-r) = 0.5$$

$$B(+r) = 0.818$$
 $B(+r)$

$$B(+r) = 0.818$$
 $B(+r) = 0.883$ $B(-r) = 0.182$ https://spowcoder.com

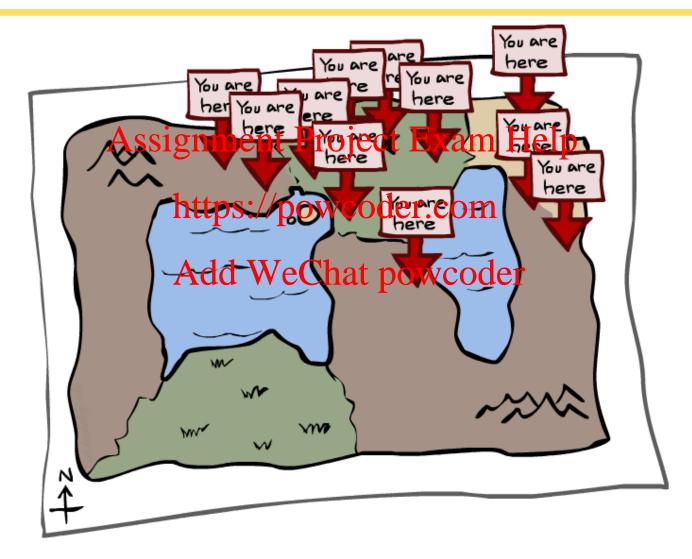


R _t	R _{t+1}	$P(R_{t+1} R_t)$
+r	+r	0.7
+r	-r	0.3
-r	+r	0.3
-r	-r	0.7

R _t	U _t	$P(U_t R_t)$
+r	+u	0.9
+r	-u	0.1
-r	+u	0.2
-r	-u	0.8



Particle Filtering



Particle Filtering

- Filtering: approximate solution
- Sometimes |X| is too big to use exact inference
 - |X| may be too big the style in the two parts of the tw
 - E.g. X is continuous
- Solution: approximate interence powcoder.com
 - Track samples of X, not all values
 Samples are called particles

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 - Time per step is linear in the number of samples
 - But: number needed may be large
 - In memory: list of particles, not states
- This is how robot localization works in practice
- Particle is just new name for sample

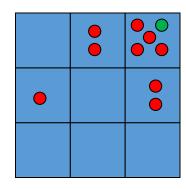
0.0	0.1	0.0
0.0	0.0	0.2
0.0	0.2	0.5



•	

Representation: Particles

- Our representation of P(X) is now a list of N particles (samples)
 - Generally, $N \ll |X|$
 - Storing map from X to counts would defeat the point Assignment Project Exam Help



- P(x) approximated by number of particles with value x
 - So, many x may have P(x) = 0 Add WeChat powcoder
 - More particles, more accuracy
- For now, all particles have a weight of 1

Particles:
(3,3)
(2,3)
(3,3)
(3,2)
(3,3)
(3,2)
(1,2)
(3,3)
(3,3)
(2,3)

Particle Filtering: Elapse Time

 Each particle is moved by sampling its next position from the transition model

 $x' = \text{sample}(PAxsignment Project Exam } H_{asp}^{(3,1)}p$

(1,2)

(2,3)

Particles:

(3,3) (2,3) (3,3)

This is like prior sampling _https://powcoder.com (3,3) (3,3)

frequencies reflect the transition probabilities

Here, most samples move clockwise, but some

move in another direction or stay in place

If enough samples, close to exact values before

This captures the passage of time

and after (consistent)

Particles: (3,2)

(2,3)

(3,2)

(3.3)

(2,2)

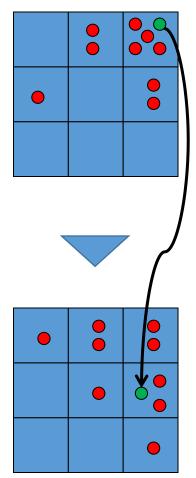
(3,2)

(2,3)

(3,2)

(2,2)





Particle Filtering: Observe

Slightly trickier:

- Don't sample observation, fix it
- Similar to likelihood weightigg, ment Project Exam² Help samples based on the evidence (2,3)

https://powcoder.com⁽³⁾₂₎

$$w(x) = P(e|x)$$

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$$B(X) \propto P(e|X)B'(X)$$

■ As before, the probabilities don't sum to one, since all have been downweighted (in fact they now sum to (N times) an approximation of P(e))

Particles:

Particles:

(3,2) (2,3) (3,2)

(3,1)

(3,2) w=.9

(2,3) w=.2

(3,2) w=.9

(3,1) w=.4

(3,3) w=.4

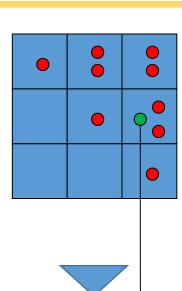
(3,2) w=.9

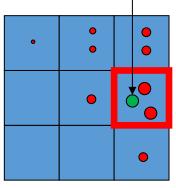
(1,3) w=.1

(2,3) w=.2

(3,2) w=.9

(2,2) w=.4







Particle Filtering: Resample

Rather than tracking weighted samples, we resample
 Particles: (3,2) w=.9 (2,3) w=.2

- N times, we choose from our weighted

- N times, we choose from our weighted

- Sample distribution (i.e. draw with replacement)

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- (3,2) w=.9

- (1,3) w=.1

- (2,3) w=.2

- (2,2) w=.4

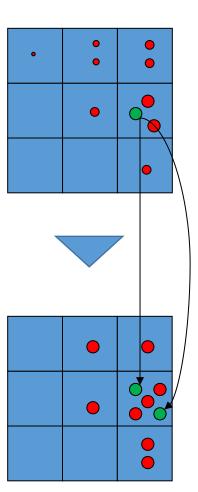
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 This is equivalent to renormalizing the distribution

 Now the update is complete for this time step, continue with the next one (New) Particles:
(3,2)
(2,2)
(3,2)
(2,3)
(3,3)
(3,2)
(1,3)
(2,3)
(3,2)

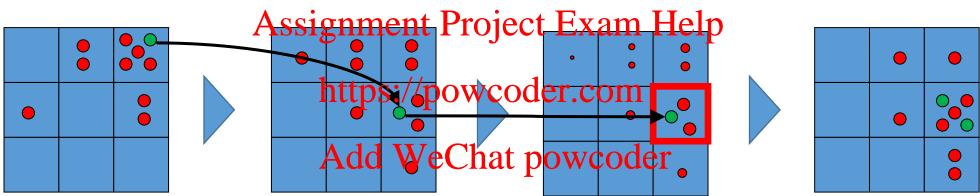
(3,2)

(3,2) w=.9 (3,1) w=.4



Recap: Particle Filtering

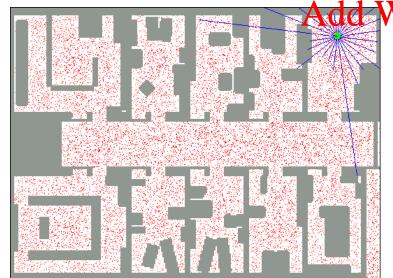
Particles: track samples of states rather than an explicit distribution
 Blapse
 Weight
 Resample



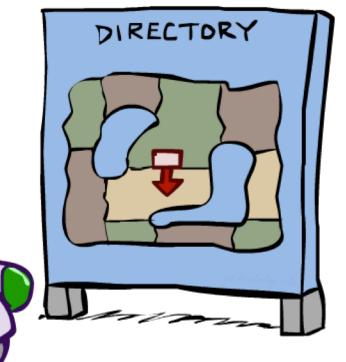
· · · · · · · · · · · · · · · · · · ·			
Particles:	Particles:	Particles:	(New) Particles:
(3,3)	(3,2)	(3,2) w=.9	(3,2)
(2,3)	(2,3)	(2,3) w=.2	(2,2)
(3,3)	(3,2)	(3,2) w=.9	(3,2)
(3,2)	(3,1)	(3,1) w=.4	(2,3)
(3,3)	(3,3)	(3,3) w=.4	(3,3)
(3,2)	(3,2)	(3,2) w=.9	(3,2)
(1,2)	(1,3)	(1,3) w=.1	(1,3)
(3,3)	(2,3)	(2,3) w=.2	(2,3)
(3,3)	(3,2)	(3,2) w=.9	(3,2)
(2,3)	(2,2)	(2,2) w=.4	(3,2)

Robot Localization

- In robot localization:
 - We know the map, but not the robot's position
 - Observations may be vectors of range finder readings
 - State space and reading Assignment Brojectu Exam Help (works basically like a very fine grid) and so we cannot store B(X) https://powcoder.com
 • Particle filtering is a main technique cannot store B(X)







Particle Filter Localization (Sonar)



Dynamic Bayes Nets

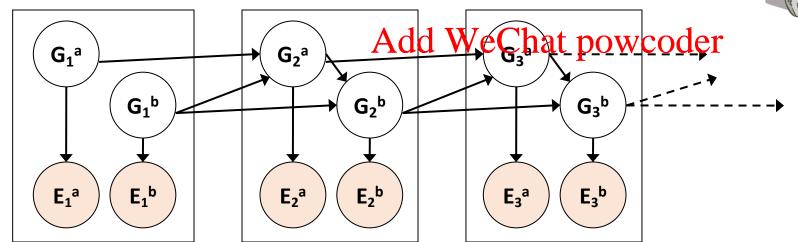


Dynamic Bayes Nets (DBNs)

• We want to track multiple variables over time, using multiple sources of evidence

• Idea: Repeat a fixed Bayes net structure at each time Help

• Variables from time t can condition on those from t-1t=1 t=2https://powcoder.com

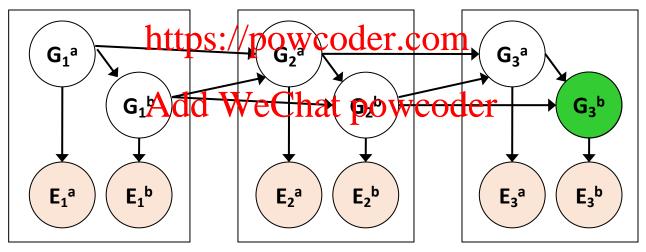


Dynamic Bayes nets are a generalization of HMMs



Exact Inference in DBNs

- Variable elimination applies to dynamic Bayes nets
- Procedure: "unroll" the network for T time steps, then eliminate variables until $P(X_T | e_{1:T})$ is computed Assignment Project Exam Help = 3



• Online belief updates: Eliminate all variables from the previous time step; store factors for current time only

DBN Particle Filters

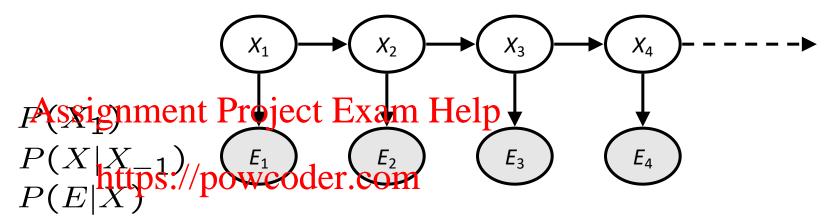
- A particle is a complete sample for a time step
- Initialize: Generate prior samples for the t=1 Bayes net
 Example particle: G₁^a A (Signment) poject Exam Help
- Elapse time: Sample a successor for each particle
 - Example successor: $G_2^a = (2.3)G_2^b = (6.3)$ powcoder
- Observe: Weight each *entire* sample by the likelihood of the evidence conditioned on the sample
 - Likelihood: $P(\mathbf{E_1}^a \mid \mathbf{G_1}^a) * P(\mathbf{E_1}^b \mid \mathbf{G_1}^b)$
- **Resample:** Select prior samples (tuples of values) in proportion to their likelihood

Most Likely Explanation



HMMs: MLE Queries

- HMMs defined by
 - States X
 - Observations E
 - Initial distribution:
 - Transitions:
 - Emissions:



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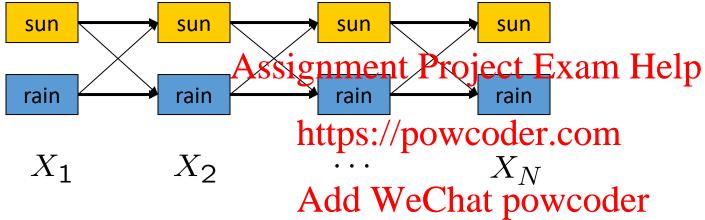
• New query: most likely explanation:

$$\underset{x_{1:t}}{\operatorname{arg\,max}} P(x_{1:t}|e_{1:t})$$

• New method: the Viterbi algorithm

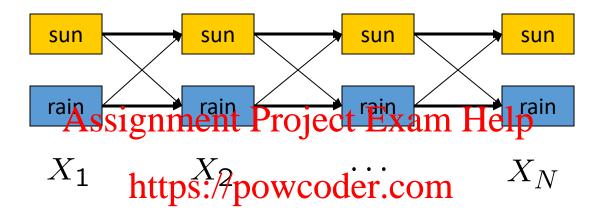
State Trellis

State trellis: graph of states and transitions over time



- Each arc represents some transition $x_{t-1} \to x_t$
- Each arc has weight $P(x_t|x_{t-1})P(e_t|x_t)$
- Each path is a sequence of states
- The product of weights on a path is that sequence's probability along with the evidence
- Forward algorithm computes sums of paths, Viterbi computes best paths

Forward / Viterbi Algorithms



Forward Algorithm (Sum) Chat powerder bi Algorithm (Max)

$$f_t[x_t] = P(x_t, e_{1:t})$$

$$m_t[x_t] = \max_{x_{1:t-1}} P(x_{1:t-1}, x_t, e_{1:t})$$

$$= P(e_t|x_t) \sum_{x_{t-1}} P(x_t|x_{t-1}) f_{t-1}[x_{t-1}]$$

$$= P(e_t|x_t) \max_{x_{t-1}} P(x_t|x_{t-1}) m_{t-1}[x_{t-1}]$$