Notes for Lecture 24 (Fall 2022 week 11 part 2): Prolog "cut"

Jana Dunfield

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The code for this lecture is in lec24.pl.

1 Controlling Prolog searching

(Some of this section is duplicated from previous notes. If it seems familiar, it's probably safe to skim it.)

By itself, Prolog code doesn't do anything. For something to happen, we have to run queries.

In Haskell, pattern matching goes from the first clause defining a function to the last. As soon as the patterns match, Haskell starts running the right-hand side of the clause.

When we enter a grery, Prologalso looks for matching clauses from top to bettom. Unlike Haskell, Prolog does not necessarily stop with the first clause. As we have seen, we often have to think about this when we translate Haskell functions to Prolog predicates. A common technique in Haskell is to write a function where the patterns in the last clause are wildcards, so we have to think about which arguing it still josi lew let halfel reacte feel feel ast clause.

Here is an extended version of the cycle Haskell function from an earlier lecture. Instead of only cycling between the three colours Orange/Rose/Violet, this version of the code has three additional constructors in the type for our. White, Grey, Black. The Orange-Rose-Violet cycle still exists, but when cycle is pasted White, Grey, black, it for this Grey, Cley, black, it for this Grey, Cley, black, it for this Grey, Cley, black, it for this Grey, black, it for this Grey, colors and colors are the cycle still exists.

In Haskell, this can be implemented economically by adding a single clause that returns Grey. Haskell reaches this clause only when the argument doesn't match any of Orange/Rose/Violet.

```
data Colour = Orange
            | Rose
             | Violet
             | White
             | Grey
             | Black
cycle :: Colour -> Colour
cycle Orange = Rose
cycle Rose = Violet
cycle Violet = Orange
cycle _
             = Grey
We might try to translate this into Prolog:
cycle(orange, rose).
cycle(rose,
              violet).
```

```
cycle(violet, orange).
cycle(_,
              grey).
```

This behaves the same as the Haskell function for *some* queries, but not all. If all our queries look like

```
?- cycle( some-colour, Result).
```

where some-colour is a specific colour like orange or black, and if we stop at the first solution (by typing a period), we get the same answers we would get in Haskell:

```
?- cycle(rose, Result).
Result = violet .
                           % I typed a .
?- cycle(grey, Result).
Result = grey.
                           % Prolog finished by itself
```

In the first query, cycle(rose, Result), Prolog waited for us to tell it whether to look for more

In the second query sydle (grey), Result) Irolog inithed by itself because day one clause matched (the last one: cycle(_, grey)).

If we type a semicolon instead, we get two results, and the second is not consistent with the Haskell code (cycle Potters. Virptowcoder.com

```
?- cycle(rose, Result).
            Add WeChat powcoder
Result = violet
Result = grey.
```

We have two approaches to solving this problem.

The first approach is to "split" the wildcard into its possible Haskell values. Since the wildcard clause in the Haskell version of cycle comes after the Orange, Rose, and Violet patterns, the Haskell clause will match White, Grey, and Black. That leads to the Prolog code

```
cycle(orange, rose).
cycle(rose,
              violet).
cycle(violet, orange).
cycle(white, grey).
cycle(grey,
              grey).
cycle(black, grey).
```

Now, Prolog will give only one answer—the same one Haskell would have given—for queries like cycle (rose, Result).

This approach has two clear advantages, and one disadvantage. Its advantages are:

- It is more clear than the second approach (cuts, discussed below): it requires writing more Prolog code, but the extra code is ordinary Prolog code that does not do anything strange.
- It is robust: it can handle queries with different modes.

The disadvantage is that it requires writing more code. Here, this approach added only two extra clauses, but for functions with many arguments, or complex arguments, this approach can add a *lot* of extra code.

(A variation on this approach is a single clause with a disjunction of equations:

```
cycle(orange, rose).
cycle(rose, violet).
cycle(violet, orange).
cycle(X, grey) :- X = white; X = grey; X = black.
```

Prolog interprets the semicolon; as disjunction ("or"), so the last clause will be true if the argument X equals white, or equals grey, or equals black.)

The second approach is to put something in our code that will force Prolog to stop looking for another solution.

Before explaining the second approach, I would like to discuss my feelings about Prolog.

1.1 Prolog: both good and bad

Like any language Prolog has party I fike and parts I don't Econo of the things I don't like (how arithmetic is done) could be fixed. Some other things I don't like are more fundamental to logic programming.

The attraction of logic programming, to me, is that it purports to let me write a set of logical rules (which I can eas it traisiste in my matter to the those writed in CISC 204) that I can use to prove things without thinking about how to prove them. That sounds amazing.

Unfortunately (or fortunately?), from learning how to do proofs in 204, we know that proofs are only partly mechanical. Some of the steps we did in a 204 proof didn't require original thought: "we are trying to prove an implication of letts at a DOM cone of the steps did: knowing where, when, and how to use the law of excluded middle (LEM) is something of an art. There is no algorithm that always knows when and how to use LEM. We can program an algorithm that sometimes figures it out, but not always.

Prolog's search algorithm is not magic. It moves through the loaded file's clauses in order, looking for something that matches the query; if it does, and the clause is a rule, it tries to prove the body (premises) of the rule. If something doesn't work, it looks for another clause that matches and tries that.

The promise of logic programming is that I can write the rules and not think about how or when to use them. The inevitable disappointment of logic programming is that what Prolog does by default does not always work.

We can often "fix" this by adding information to the clauses (we are about to see how to do this) that tells Prolog when to stop looking for more solutions. This can be very useful. It will let us more easily translate Haskell functions, for example. But it betrays the promise of logic programming: I have to think about how Prolog will search through the rules.

If I have to think that much about Prolog's search algorithm, I'd probably prefer to use Haskell.

1.2 Cuts

To tell Prolog to stop looking for more solutions, we can use "cuts".

A cut is written "!". Roughly, it says to Prolog: "Forget about unexplored paths."

Here is what we get for cycle. I renamed it to newcycle so we can try both cycle and newcycle without having to comment out one set of clauses. I had to turn the first three facts into rules, because you can only use a cut in a rule. A cut is not really a premise of a rule in any logical sense, but it goes in the same place as a premise would.

Facts don't have premises, so we have to turn facts into rules to use cuts.

```
newcycle(orange, rose) :- !.
newcycle(rose, violet) :- !.
newcycle(violet, orange) :- !.
newcycle(_, grey).
```

Whereas cycle(rose, Result), returned both violet and grey, the query newcycle(rose, Result) only returns violet:

```
?- newcycle(rose, Result).
Result = violet.
```

Why did this happen?

Prolog found the clause rewrite (rose), royie lev) : Lyandsaid, To use this rule, I need to prove all its premises. The only premise I need to prove is !. That's a cut, so it's not really a premise. I have no premises left to prove. And I saw the cut, so I won't look for more solutions."

The Prolog code now faithfully implements the Haskell code.

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1.3 Disappointment

cycle(_,

I now have generalized sadness that I had to tell Prolog how to search. Isn't that its job?

But I have a more specific disappointment nat powcoder

A cool thing about Prolog is that when we implement Haskell functions as predicates, we are often implementing the inverse relation *for free*. Look at cycle (*not* newcycle!): We can run queries that run cycle in reverse.

```
?- cycle(Input, violet).
Input = rose.

This isn't magic; it has some limitations. The response to this query isn't terribly satisfying:
?- cycle(Input, grey).
true.

I can't blame Prolog for this, however: the fact
```

says that, given any input, the result is grey. So when I ask Prolog to find an Input such that cycle(Input, grey) is true, how should it know what I want?

We did this with no extra code. In Haskell, we could try to write a separate function:

grey).

```
inv_cycle Rose = Orange
inv_cycle Violet = Rose
inv_cycle Orange = Violet
```

That wouldn't even work, though, because what do we return for inv_cycle Grey? Grey is returned by cycle White, cycle Grey, and cycle Black. We'd have to return a list of colours, instead of a single colour; then we could return [White, Grey, Black]. But this is already getting complicated.

Exercise 1. The original version of cycle from lec16, which does not include the colours White/Grey/Black, *does* have a straightforward inverse in Haskell. Why?

In Prolog, we just got it for free. What happens with newcycle? Do we still get the inverse relation?

```
?- newcycle(Input, violet).
Input = rose.
?- newcycle(Input, violet).
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true.
```

Seems to work as well as cycle does. Okay, let's try something harder.

With cycle, we can give precies wing both around to cycle and type semi-colon repeatedly to get a lot of information:

```
?- cycle(Input, Result)
Input = orange,
Result = rose

Input = rose,
Result = violet

Input = violet,
Result = orange

Result = grey.
```

I added blank lines between each solution—otherwise, the last one is extra confusing because (as explained above) Prolog has no idea what Input is there, and doesn't print a result for it at all. Does that work with newcycle?

```
?- newcycle(Input, Result).
Input = orange,
Result = rose.
```

No. Prolog stopped immediately, because it saw the cut in the first clause.

1.4 What exactly does it mean to "forget unexplored paths"?

In cycle/newcycle, we added cuts to facts, so we had no choice about where to put the cut. In a rule, does it matter where we put the cut?

Yes. A cut prevents Prolog from backtracking: exploring other ways to try to make a query true. A cut only affects the past: any choices *already made* are "frozen". The cut does *not* directly affect choices to be made in the future.

See the discussion of select_twice in lec24.pl.

1.5 When should you use cuts?

A cut that affects the set of possible solutions to queries is called a *red cut*. A cut that does not affect the set of possible solutions to queries is called a *green cut*. However, even a green cut makes code harder to understand: we have to convince ourselves that the cut is green.

It is often convenient to use cuts when translating Haskell code: if we want to mimic the behaviour of the Haskell code, we never want more than one solution.

But even when translating Haskell code, we don't have to use a cut.

When writing code that is meant to produce many solutions (like group on Assignment 4), cuts should be used with extreme caution. We want group to brektrack whenever necessary, so it can find all the groups in the tree; any use of a cut is lable to stop it from finding all the groups.

1.6 More adventures with cuts
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