# Notes for Lecture 8 (Fall 2022 week 4): 'data' types

Jana Dunfield

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### 1 Continuing discussion of recursive functions

See lec8.py.

### 2 'data' types

Haskell code for this lecture is in lec8.hs.

Type synonyms give names for existing types. To create something new, somewhat similarly to declaring a class in an object-oriented language, we use the 'data' keyword:

## Assignment Project Exam Help

3. defining new data types ("data ...")

```
Time to start de https://powcoder.com
```

```
This says: Building is a data type

The values of this type are:

Goodwin (Valte Might BardshMino) Vicini) der

-}
```

(This example feels strange; I haven't been inside a campus building in a while.) Each of the things after the = is a *data constructor*, often called just a *constructor*. At a high level, the 'data' declaration says:

- this is what a Building is:
  - Goodwin is a Building
  - WalterLight is a Building
  - BeamishMunroe is a Building
  - Dupuis is a Building
- also, please print the constructor names when you need to ("deriving Show")

(Having to write "deriving Show" gets pretty annoying. It might annoy me even more than it annoys you.)

In an object-oriented language, we might define Building by declaring an abstract class Building and deriving the four classes Goodwin, WalterLight, ... as subclasses of Building. There are many differences between using a class and using a Haskell 'data' type; one important difference is that when we use 'data', we are defining the entire type at once. We have to list *all* the possible constructors. In most object-oriented languages, we can keep defining new subclasses (possibly scattered throughout various source files).

We have actually seen a 'data' type already:

(You can do other things with "deriving" than tell Haskell to print the constructor names, but I don't want to get into that right now.)

If we type a constructor name into GHCi, it returns it:

# \*Lec7> GASsignment Project Exam Help

```
That doesn't seem very interesting, This is a little more interesting:

has_elevator :: Building -> Bool

has_elevator Goodwin True Chat powcoder
has_elevator Walter Gut = Vale Chat powcoder
has_elevator BeamishMunroe = True
has_elevator Dupuis = True
```

This function tells us whether a given building has an elevator.

#### **Remark 1.** Building history digression:

According to the stories I've heard, Walter Light does not have an elevator because every floor is connected to every floor of Goodwin, which does have an elevator. Goodwin was supposed to have two elevators, and in fact has two elevator shafts. The second elevator was supposed to be installed when Walter Light was completed, but they ran out of money building Walter Light, so we have one elevator for two buildings.

When it's safe for you to be in Goodwin Hall again—whenever that is—look for evidence of the second elevator shaft on the second floor of Goodwin.

How does the function work? It might be surprising that Haskell is okay with this function: it seems to define itself four times, sort of like a function that uses guards—but has\_elevator doesn't use guards.

Actually, has\_elevator uses pattern matching, but instead of only "lining up" the components of tuples, Haskell is comparing the argument to the pattern. Here's what Haskell does when we step has\_elevator WalterLight. (See the next page, to keep it all on one page.)

```
has_elevator WalterLight
=> ????
 Line up the FIRST CLAUSE, has_elevator Goodwin = ...
 with the expression:
  has_elevator Goodwin
  has_elevator WalterLight
 Does WalterLight match the pattern Goodwin?
 Equivalently: Is there any way to make
   WalterLight equal to Goodwin?
 Answer: no.
 Move on to the SECOND CLAUSE, has_elevator WalterLight = ...
 Line up with the expression:
                                     oject Exam Help
  has_elevator WalterLight
                               -- second clause
  has_elevator WalterLight
                               -- expression
 Is there any way https://powcoder.com
   WalterLight equal to WalterLight?
                                   hat powcoder
 Yes, sure, they're identical
 The pattern WalterLight matched the argument WalterLight,
 so we step to the right-hand side of
   has_elevator WalterLight = False
  has_elevator WalterLight
=> False
```

Pattern matching also works with "more than one argument". Even though my\_and is technically a function of one argument that returns a function of type Bool -> Bool, Haskell lets us write my\_and as if it had two arguments. And Haskell lets us pattern-match on both at the same time.

```
my_and :: Bool -> Bool -> Bool
my_and True True = True
my_and True False = False
my_and False True = False
my_and False False = False
```

Similar to has\_elevator, Haskell tries to match arguments against patterns. Unlike has\_elevator, Haskell matches two things at once. For example, if we step

```
my_and False True
we will first line up
my_and True True = True
my_and False True
```

which doesn't match (the first argument False is definitely not equal to the pattern True). Since it doesn't match, we move on to the second clause.

```
my_and True False = False
my_and False True
```

Again, it doesn't match (neither argument matches!), so we move on to the third clause, which matches:

```
my_and False True = False
my_and False True
```

As my example steppings have suggested, Halkelf always does puttern matching in order. We can take advantage of this to define 'and' more concisely:

```
another_and :: Belt prod / polwcoder.com
another_and True True Frue
another_and _ = False
```

Anything matches the wildcard puttern, spif we apply anythor and to arguments that are not both True, we will match the patterns in the second clause and return False.

The function something in lec7.hs does something like this, but is more complicated:

```
something :: (Building, Building) -> Bool
something (Dupuis, WalterLight) = False
something (Dupuis, _) = True
something (_, WalterLight) = True
something (_, _) = False
```

Experiment in GHCi with something applied to various pairs of Buildings, and see if you follow how Haskell is deciding which clause matches.

The code ends with an exercise:

```
-- adjacent
-- True iff buildings are _directly_ adjacent.
-- For example, Goodwin and WalterLight are adjacent,
-- but WalterLight and BeamishMunroe are not because
-- you have to go through Goodwin.
--
-- "Building map": || and === show direct connections
```

```
-- Dupuis
-- ||
-- BeamishMunroe===Goodwin===WalterLight
--
-- (I think there's a secret locked one-way door from Dupuis to Goodwin.
-- It doesn't count.)
adjacent :: Building -> Building -> Bool
adjacent b1 b2 = undefined

It's a little annoying to write because adjacency is a symmetric relation, so
adjacent Goodwin WalterLight = True
```

isn't enough to model the connection; we also want to return True for adjacent WalterLight Goodwin.

### 3 lec8.hs

### Some more Austrialismment Project Exam Help

### 4 Trees

The Building type front type sis philarw cool crucations can do more than that.

Recall that Goodwin, WalterLight, etc. are data constructors, often called just constructors. Each constructor of the Building Work to k he arguments Goodwin is Building, with no other information needed.

In this section, we define a type Tree that is not like an enum type:

This says: a Tree is either

- Empty, or
- Branch 1 k r where 1 is a Tree, k is an Integer, and r is a Tree.

(The line "deriving Show" tells Haskell to allow itself to print Trees.)

The meaning I intend (which Haskell doesn't know, it only knows what's in the Tree declaration) is that

- Empty represents a leaf (containing no information), and
- Branch 1 k r represents a *branch* whose left child is the tree 1, containing an integer key k, and whose right child is the tree r.

By itself, the word Branch is a constructor but not a tree: we need to know the children of the branch, and the integer key being stored.

Branch Empty 9 Empty is a tree, because we have given three *arguments* to Branch. In fact, the type Haskell gives to Branch is the type of a function:

```
Branch :: Tree -> Integer -> Tree -> Tree

first second third result

argument argument argument
```

As we have seen, igskell will not print functions, so if you are Branch, you will get the type above.

As with built-in functions and functions we define, we can partially apply a constructor:

```
*Lec9> :type Branch Empty://powcoder.com

Branch Empty :: Integer -> Tree -> Tree

*Lec9> :type Branch Empty 3

Branch Empty 3 :: Areight We Chat powcoder

*Lec9> let empty_3 = Branch Empty 3

*Lec9> empty_3 Empty

Branch Empty 3 Empty

*Lec9>
```

The function empty\_3 is "waiting" for its last argument, the right child.

Remark 2. You can declare something (empty\_3) within GHCi by writing let before the declaration. Entering code longer than one line is annoying, but for one-line expressions I sometimes find it easier to do within GHCi, rather than doing it in a file and loading the file.

The rest of this section is in lec8.hs.