CISC 6525

Assignment Project Exam Help

Logicowcagents

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Chapter 7

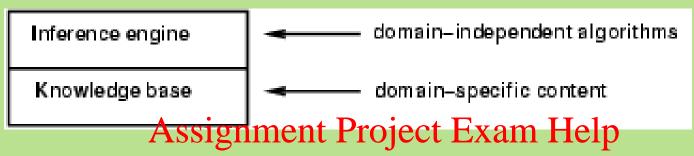
Outline

- Knowledge-based agents
- Wumpus world

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 Logic in general models and entailment
- Propositional https://earycrogiccom
- Equivalence, Addidity Chatipfia bibity r
- Inference rules and theorem proving
 - forward chaining
 - backward chaining
 - resolution

Knowledge bases



- Knowledge base = set of sentences in a formal language
- Declarative approachts building and period on other system):
 - Tell it what it needs to know

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 Then it can Ask itself what to do answers should follow from the KB
- Agents can be viewed at the knowledge level i.e., what they know, regardless of how implemented
- Or at the implementation level
 - i.e., data structures in KB and algorithms that manipulate them

A simple knowledge-based agent

```
function KB-AGENT(percept) returns an action
static: KB, a knowledge base
t, a counter, initially 0, indicating time

Tell(KB, Makespercherent Projecte talm Help
action — Ask(KB, Make-Action-Query(t))

Tell(KB, Make-Action-Sentence(action, t))
t — t + 1
return action

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```

- The agent must be able to:
 - Represent states, actions, etc.
 - Incorporate new percepts
 - Update internal representations of the world
 - Deduce hidden properties of the world
 - Deduce appropriate actions

Wumpus World PEAS description

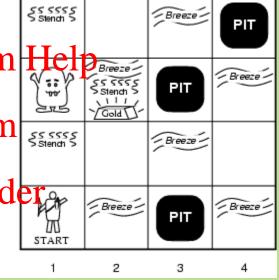
Performance measure

- gold +1000, death -1000
- -1 per step, -10 for using the arrow

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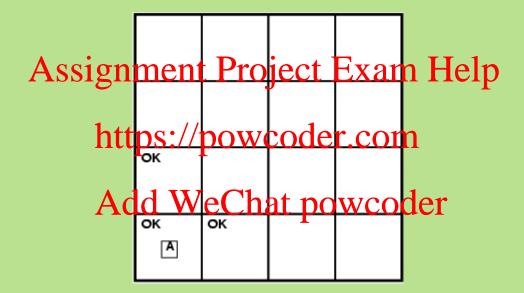
Environment

- Squares adjacent the wyppy of the smelty der.com
- Squares adjacent to pit are breezy
- Glitter iff gold is in the same square nat powco
- Shooting kills wumpus if you are facing it
- Shooting uses up the only arrow
- Grabbing picks up gold if in same square
- Releasing drops the gold in same square
- Sensors: Stench, Breeze, Glitter, Bump, Scream
- Actuators: Left turn, Right turn, Forward, Grab, Release, Shoot



Wumpus world characterization

- Fully Observable No only local perception
- <u>Deterministic</u> Yes outcomes exactly specified Assignment Project Exam Help
 <u>Episodic</u> No sequential at the level of actions
- Static Yes Wormprowande Pagado not move
- Discrete YesAdd WeChat powcoder
- Single-agent? Yes Wumpus is essentially a natural feature

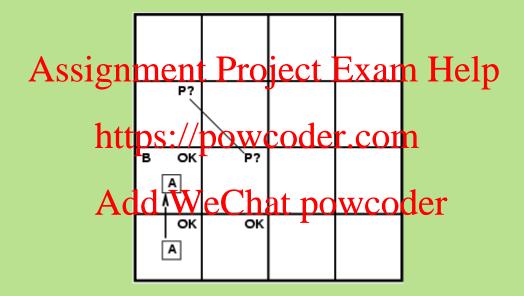


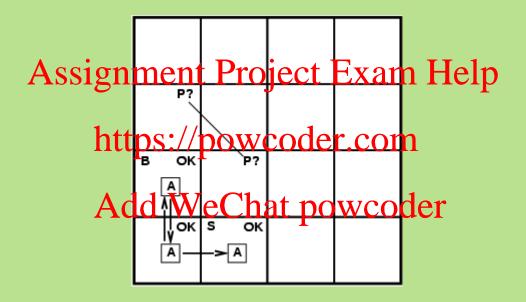
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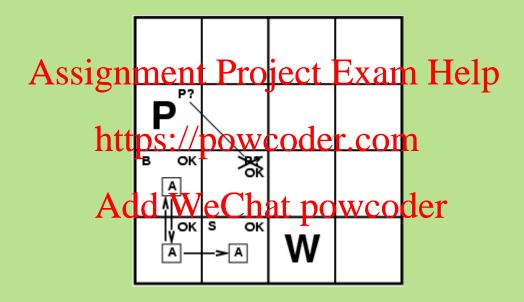
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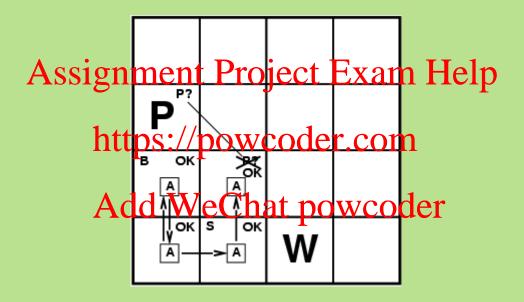
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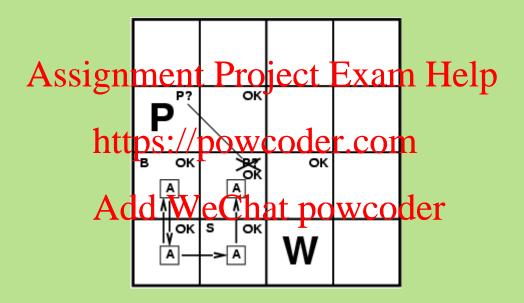
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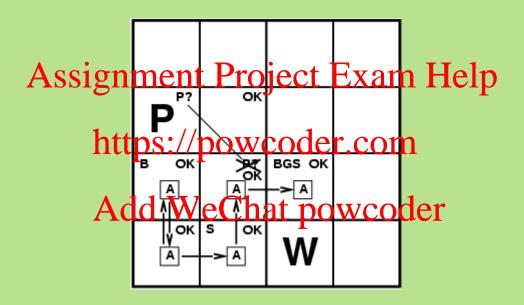












Logic in general

- Logics are formal languages for representing information such that conclusions can be drawn
- Syntax defines the sentences in the language
 Semantics define the "meaning" of sentences;
- - i.e., define truthtfpss/nterve ordew.ordm
- E.g., the language of an thintet powcoder
 - $-x+2 \ge y$ is a sentence; $x2+y > {}$ is not a sentence
 - $-x+2 \ge y$ is true iff the number x+2 is no less than the number y
 - $-x+2 \ge y$ is true in a world where x = 7, y = 1
 - $-x+2 \ge y$ is false in a world where x = 0, y = 6

Entailment

 Entailment means that one thing follows from another:

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 Knowledge base *KB* entails sentence α if and only if a is truletips: alloworlds: whoere KB is true
 - E.g., the KBARAMERGhan every send the Jets won" entails "Either the Giants won or the Jets won"
 - E.g., x+y = 4 entails 4 = x+y
 - Entailment is a relationship between sentences (i.e., syntax) that is based on semantics

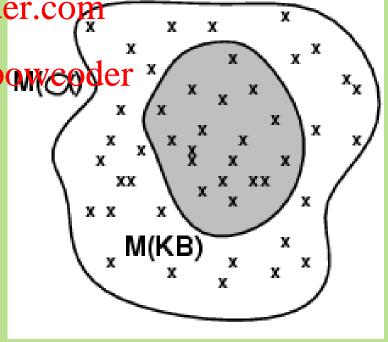
Models

- Logicians typically think in terms of models, which are formally structured worlds with respect to which truth can be evaluated
- We say m is A sysiget interpreted i Existing the lip

• M(α) is the set of all through sport coder.com

Then KB | α iff M(AB) \(\text{MeChat panyeoder} \)

 E.g. KB = Giants won and Reds won α = Giants won

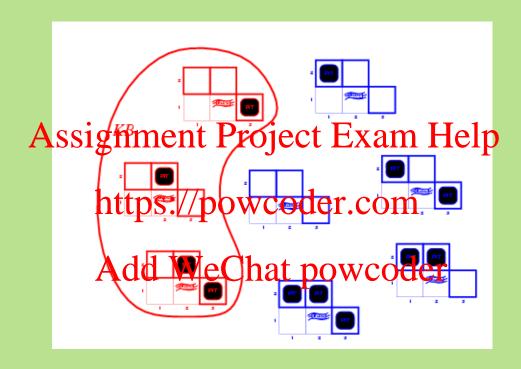


Entailment in the wumpus world

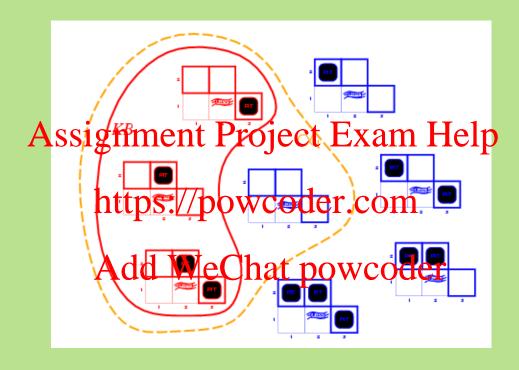
Situation after detecting nothing in [1,1], moving right, bre righ

3 Boolean choices ⇒ 8 possible models

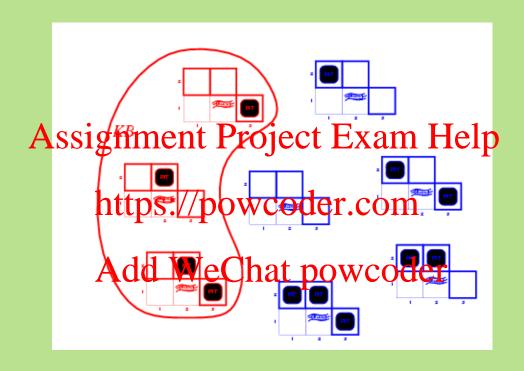




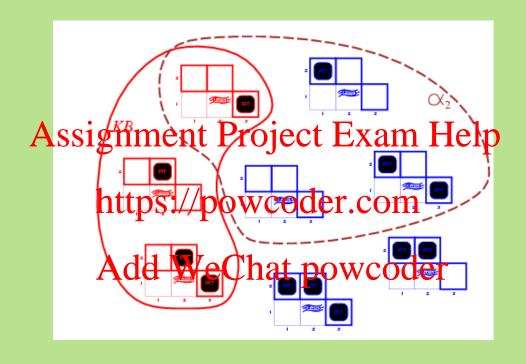
KB = wumpus-world rules + observations



- KB = wumpus-world rules + observations
- $\alpha_1 = "[1,2]$ is safe", $KB \models \alpha_1$, proved by model checking



KB = wumpus-world rules + observations



- KB = wumpus-world rules + observations
- $\alpha_2 = "[2,2]$ is safe", $KB = \alpha_2$

Inference

- $KB \mid_{i} \alpha = \text{sentence } \alpha \text{ can be derived from } KB \text{ by procedure } i$
- Soundness sissemued tif pwhere ver KB | α
- Completeness: https://ppletenewer.kb | α, it is also true that kb | α
 Preview: we will define a logic (first-order logic) which is
- Preview: we will define a logic (first-order logic) which is expressive enough to say almost anything of interest, and for which there exists a sound and complete inference procedure.
- That is, the procedure will answer any question whose answer follows from what is known by the *KB*.

Propositional logic: Syntax

 Propositional logic is the simplest logic – illustrates basic ideas

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- The proposition symbols P₁, P₂ etc are sentences https://powcoder.com

 - If S is a sentence (negation)
 If S₁ and S₂ are sentences, S₁ \(\Lambda \) S₂ is a sentence (conjunction)
 - If S₁ and S₂ are sentences, S₁ v S₂ is a sentence (disjunction)
 - If S_1 and S_2 are sentences, $S_1 \Rightarrow S_2$ is a sentence (implication)
 - If S_1 and S_2 are sentences, $S_1 \Leftrightarrow S_2$ is a sentence (biconditional)

Propositional logic: Semantics

Each model specifies true/false for each proposition symbol

E.g. $P_{1,2}$ $P_{2,2}$ $P_{3,1}$ false true false

With these symbols, specific the Examerated Automatically. Rules for evaluating truth with respect to a model *m*:

¬S is true iff https://spelsecoder.com $S_1 \wedge S_2$ is true iff S_1 is true and S_2 is true $S_1 \vee S_2$ is true iff S_1 is true iff S_2 is true iff S_3 is false or S_4 is true iff S_5 is false or S_5 is true iff S_5 is true and S_5 is false S_5 is true iff S_5 is true and S_5 is true

Simple recursive process evaluates an arbitrary sentence, e.g.,

 $\neg P_{1,2} \land (P_{2,2} \lor P_{3,1}) = true \land (true \lor false) = true \land true = true$

Truth tables for connectives

P	Q	$\neg P$	$P \wedge Q$	$P \lor Q$	$P \Rightarrow Q$	$P \Leftrightarrow Q$
false	false	true	false	false	true	true
	true		false	true	true	false
true	fals e	ទៀវ គឺវិវិជ្ជា	ent Reo	ject _u ex	am Help	false
true	true	false	s://pow	coder.c	om^{true}	true

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Wumpus world sentences

```
Let P_{i,j} be true if there is a pit in [i, j].

Let B_{i,j} be true if there is a breeze in [i, j].

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\neg P_{1,1}

\neg B_{1,1} https://powcoder.com

B_{2,1} Add WeChat powcoder
```

"Pits cause breezes in adjacent squares"

$$B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1})$$

$$B_{2,1} \Leftrightarrow (P_{1,1} \vee P_{2,2} \vee P_{3,1})$$

Truth tables for inference

B	1,1	$B_{2,1}$	$P_{1,1}$	$P_{1,2}$	$P_{2,1}$	$P_{2,2}$	$P_{3,1}$	KB	α_1
fa	lse	false	false	false	false	false	false	false	true
$\int fa$	lse	false	false	false	false	false	true	false	true
	:	: A	ssign	ment	Projec	ct Exa	m He	ln :	:
$\int fa$	lse	true	false	false	false	false	$\mathop{ m m} olimits_{false}$	false	true
fa	lse	true	fallaet	pfg:l/s/p	ofwleo	dferl <i>se</i> c	1true	\underline{true}	\underline{true}
$\int fa$	lse	true					false	\underline{true}	\underline{true}
$\int fa$	lse	true	false	daWæ	Chlat	powc	oder	\underline{true}	\underline{true}
fa	lse	true	false	false	true	false	false	false	true
	:		:	:		:	:		:
tr	ue	true	true	true	true	true	true	false	false

Inference by enumeration

Depth-first enumeration of all models is sound and complete

```
function TT-Entails?(KB, \alpha) returns true or false

symbols \leftarrow a \text{ list of the proposition symbols in } KB \text{ and } \alpha
return TT-Entails.(KB, \alpha, symbols, Colded) \text{ LXam Help}

function TT-Check (ALL) (KB/\alpha) symbols colded returns true or false
if Empty?(symbols) then
if PL-True?(KB, model) then return PL-True?(\alpha, model)
else return false
else do
P \leftarrow \text{First}(symbols); rest \leftarrow \text{Rest}(symbols)
return TT-Check-All(<math>KB, \alpha, rest, Extend(P, true, model) and
TT-Check-All(KB, \alpha, rest, Extend(P, false, model)
```

• For n symbols, time complexity is $O(2^n)$, space complexity is O(n)

Proof methods

- Proof methods divide into (roughly) two kinds:
 - Application of inference rules
 - · Legitimates is unit get heratoje of the weather Heal from old
 - Proof = a sequence of inference rule applications
 http://procedinge.cutes.

 standard search algorithm
 - Typically require transformation of sentences into a normal form
 - Model checking
 - truth table enumeration (always exponential in n)
 - improved backtracking, e.g., Davis--Putnam-Logemann-Loveland (DPLL)
 - heuristic search in model space (sound but incomplete)
 e.g., min-conflicts-like hill-climbing algorithms

Logical equivalence

• Two sentences are logically equivalent} iff true in same models: $\alpha \equiv \beta$ iff $\alpha \models \beta$ and $\beta \models \alpha$

```
(α \Assignment Projecti Exam\Help
          (\alpha \vee \beta) \equiv (\beta \vee \alpha) commutativity of \vee
((\alpha \land \beta) \land \gamma) \equiv h(tops(\beta)pon) coelection of \land
((\alpha \vee \beta) \vee \gamma) \equiv (\alpha \vee (\beta \vee \gamma)) associativity of \vee
           \neg(\neg \alpha) \equiv A\alpha dd Mbe Cheetiproviolier
      (\alpha \Rightarrow \beta) \equiv (\neg \beta \Rightarrow \neg \alpha) contraposition
      (\alpha \Rightarrow \beta) \equiv (\neg \alpha \lor \beta) implication elimination
      (\alpha \Leftrightarrow \beta) \equiv ((\alpha \Rightarrow \beta) \land (\beta \Rightarrow \alpha)) biconditional elimination
       \neg(\alpha \land \beta) \equiv (\neg \alpha \lor \neg \beta) de Morgan
       \neg(\alpha \lor \beta) \equiv (\neg \alpha \land \neg \beta) de Morgan
(\alpha \wedge (\beta \vee \gamma)) \equiv ((\alpha \wedge \beta) \vee (\alpha \wedge \gamma)) distributivity of \wedge over \vee
(\alpha \vee (\beta \wedge \gamma)) \equiv ((\alpha \vee \beta) \wedge (\alpha \vee \gamma)) distributivity of \vee over \wedge
```

Validity and satisfiability

```
A sentence is valid if it is true in all models,
e.g., True, A \lor \neg A, A \Rightarrow A, (A \land (A \Rightarrow B)) \Rightarrow B
```

Validity is connected to inference via the Examine Theorem: $KB \models \alpha$ if and only if $(KB \Rightarrow \alpha)$ is valid

A sentence is satisfiable if it is true in some model e.g., Av B, C

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A sentence is unsatisfiable if it is true in no models e.g., A^¬A

Satisfiability is connected to inference via the following: $KB \models \alpha$ if and only if $(KB \land \neg \alpha)$ is unsatisfiable

Resolution

Conjunctive Normal Form (CNF)

conjunction of disjunctions of literals

clauses

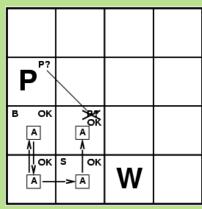
E.g., (A v Assignment Project Exam Help

Resolution inference rule (for CNF):

where I_i and m_i are complementary literals.

E.g.,
$$P_{1,3} \vee P_{2,2}$$
, $\neg P_{2,2}$

 Resolution is sound and complete for propositional logic



Resolution

Soundness of resolution inference rule:

```
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\neg(I_{i} \vee ... \vee I_{i-1} \vee I_{i+1} \vee ... \vee I_{k}) \Rightarrow I_{i}
https://powcoder.com
\neg m_{j} \Rightarrow (m_{1} \vee ... \vee m_{j-1} \vee m_{j+1} \vee ...
\vee m_{n}) \qquad Add WeChat powcoder
\neg(I_{i} \vee ... \vee I_{i-1} \vee I_{i+1} \vee ... \vee I_{k}) \Rightarrow (m_{1} \vee ... \vee m_{j-1} \vee m_{j+1} \vee ... \vee m_{j+1} \vee ... \vee m_{n})
```

Conversion to CNF

$$B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1})\beta$$

- 1. Eliminate \Leftrightarrow replacing $\alpha \Leftrightarrow \beta$ with $(\alpha \Rightarrow \beta) \wedge (\beta \Rightarrow \alpha)$. $(B_{1,1} \Rightarrow (P_{1,2} \lor P_{2,1})) \wedge ((P_{1,2} \lor P_{2,1})) \Rightarrow B_{1,1})$
- 2. Eliminate \Rightarrow , replacing $pow \beta Wer com \beta$. $(\neg B_{1,1} \lor P_{1,2} \lor P_{2,1}) \land (\neg Wer Chat pow coder)$
- 3. Move ¬ inwards using de Morgan's rules and double-negation:

$$(\neg B_{1,1} \lor P_{1,2} \lor P_{2,1}) \land ((\neg P_{1,2} \lor \neg P_{2,1}) \lor B_{1,1})$$

4. Apply distributivity law (∧ over ∨) and flatten:

$$(\neg B_{1,1} \lor P_{1,2} \lor P_{2,1}) \land (\neg P_{1,2} \lor B_{1,1}) \land (\neg P_{2,1} \lor B_{1,1})$$

Resolution algorithm

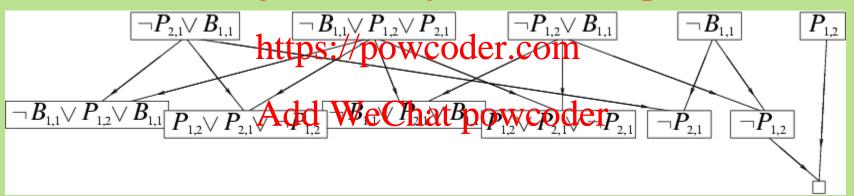
Proof by contradiction, i.e., show KB∧¬α unsatisfiable

```
function PL-Rescription (Rent) Project Least Help clauses \leftarrow the set of clauses in the CNF representation of KB \land \neg \alpha new \leftarrow \{\} https://powcoder.com loop do for each C_i, C_j in clauses do hat powcoder resolvents \leftarrow PL-Resolve(C_i, C_j) owcoder if resolvents contains the empty clause then return true new \leftarrow new \cup resolvents if new \subseteq clauses then return false clauses \leftarrow clauses \cup new
```

Resolution example

•
$$KB = (B_{1,1} \Leftrightarrow (P_{1,2} \vee P_{2,1})) \wedge \neg B_{1,1} \alpha = \neg P_{1,2}$$

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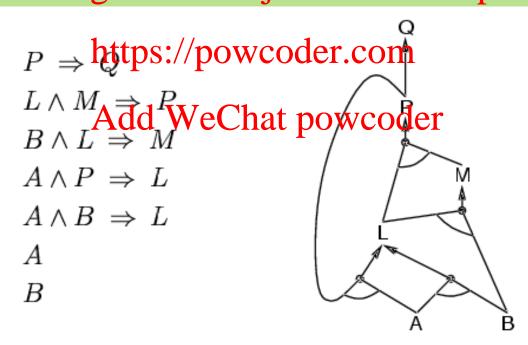
Forward and backward chaining

- Horn Form (restricted)
 KB = conjunction of Horn clauses
 - Horn clause =
 - proposition is proposition of the proposition of
 - (conjunction of symbols) ⇒ symbol
 - E.g., C ∧ (B ⇒https://powebder.com
- Modus Ponens (for Horn Form): complete for Horn KBs

 α₁, ..., α WeChat powcoder α_n ⇒ β
 β
- Can be used with forward chaining or backward chaining.
- These algorithms are very natural and run in linear time

Forward chaining

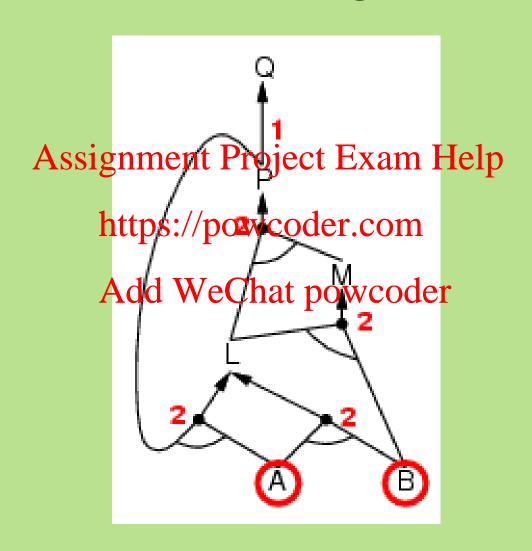
- Idea: fire any rule whose premises are satisfied in the KB,
 - add its conslysion the the the justil Terrain fruit

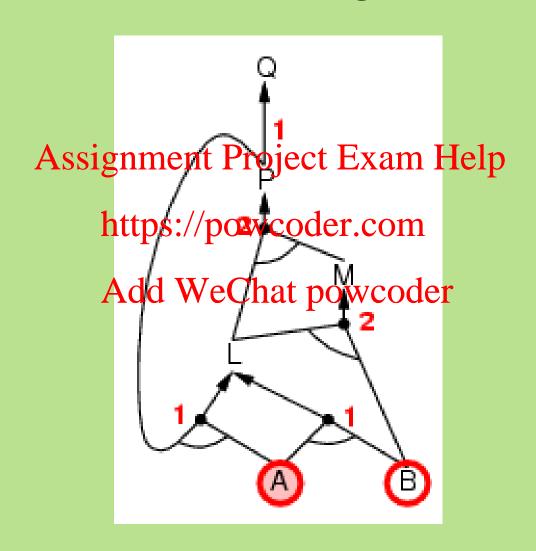


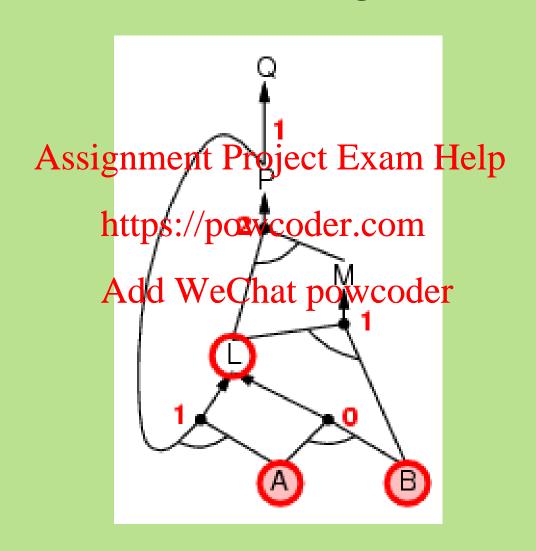
Forward chaining algorithm

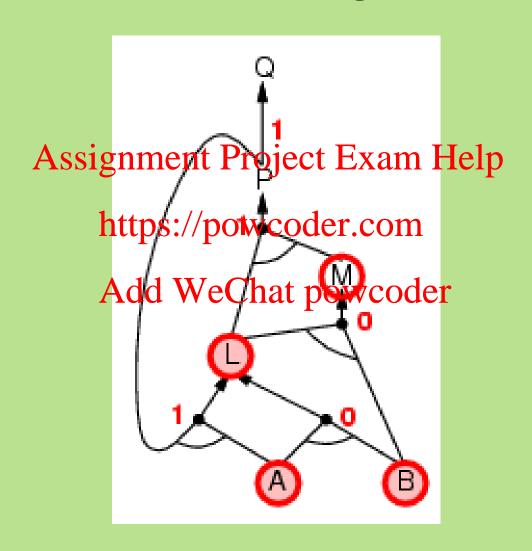
```
function PL-FC-Entails?(KB, q) returns true or false
            local variables: count, a table, indexed by clause, initially the number of premises
                                                                                                              inferred, a table, indexed by symbol, each entry initially false
              while agenda, a list of symbols, initially the symbols known to be true while agenda is not empty do Project Exam Help
                                      p \leftarrow \text{Pop}(agenda)
                                      \frac{\text{unless inferred}}{\text{inferred}[p] \leftarrow true} \text{s://powcoder.com}
                                                             for each Horn clause c in whose premise p appears do decrement decrement decrement decrement <math>decrement decrement decrement <math>decrement decrement decrement decrement <math>decrement decrement decrement decrement <math>decrement decrement decrement decrement <math>decrement decrement decrement decrement decrement <math>decrement decrement d
                                                                                     if count[c] = 0 then do
                                                                                                            if HEAD[c] = q then return true
                                                                                                            Push(Head[c], agenda)
               return false
```

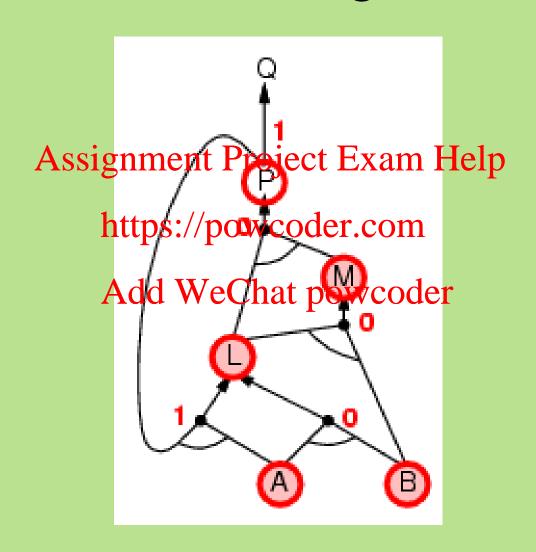
 Forward chaining is sound and complete for Horn KB

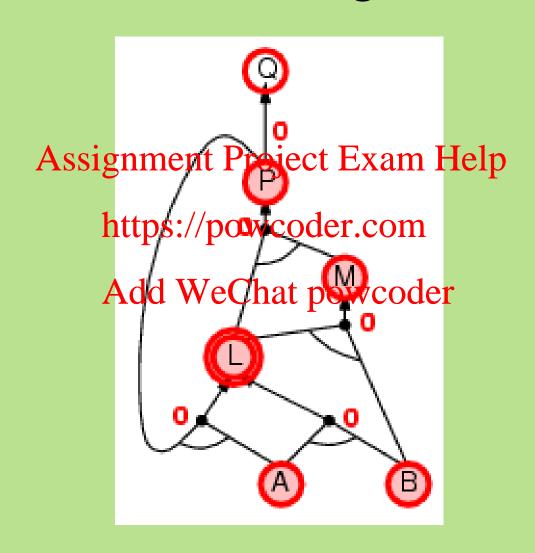


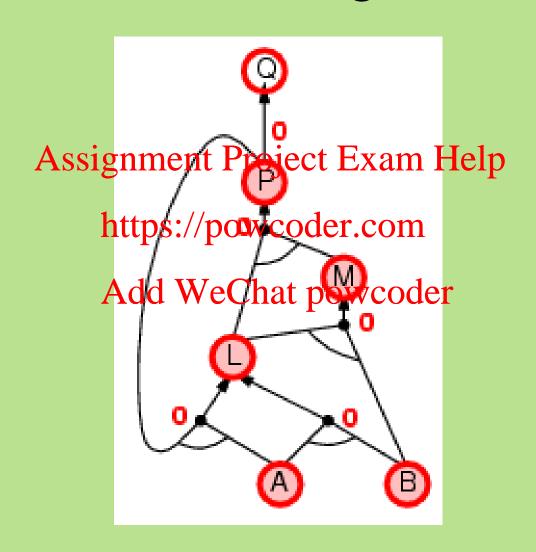


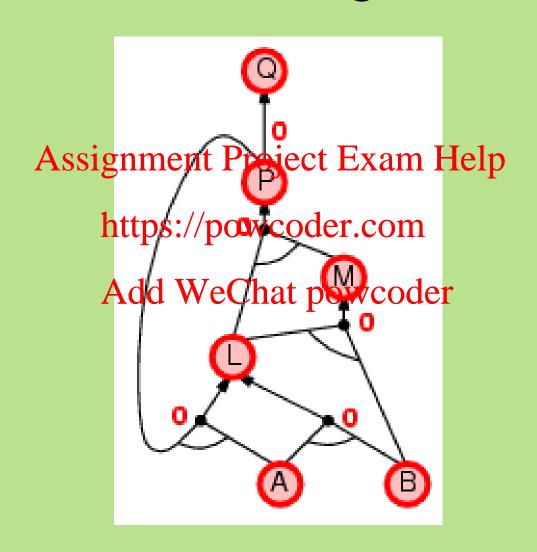












Proof of completeness

- FC derives every atomic sentence that is entailed by KB
 - 1. FC reachismmenta Project Ferend Helw atomic sentences are derived https://powcoder.com
 Consider the final state as a model *m*, assigning
 - true/false tadnWelShat powcoder
 - Every clause in the original *KB* is true in *m* $a_1 \wedge \ldots \wedge a_{k \Rightarrow} b$
 - 4. Hence *m* is a model of *KB*
 - If $KB \models q$, q is true in every model of KB, including m

Backward chaining

```
Idea: work backwards from the query q:

to prove q by BC,

check if A is knowned to Prove by BC all premises of some rule concluding q

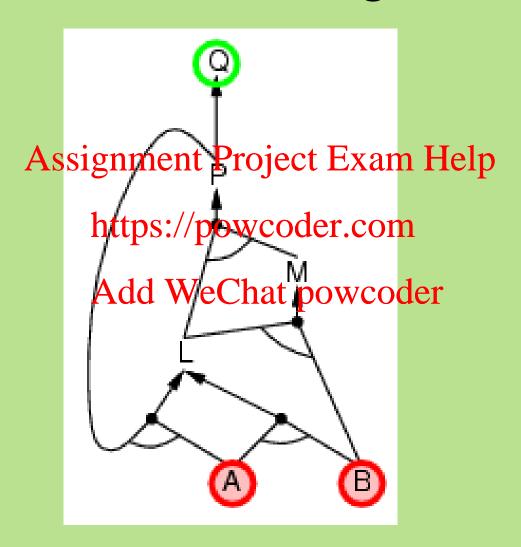
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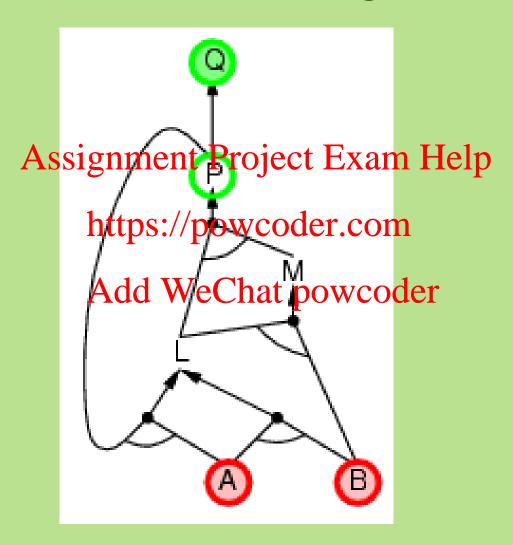
Avoid loops: check if new subgoal is already on the goal stack

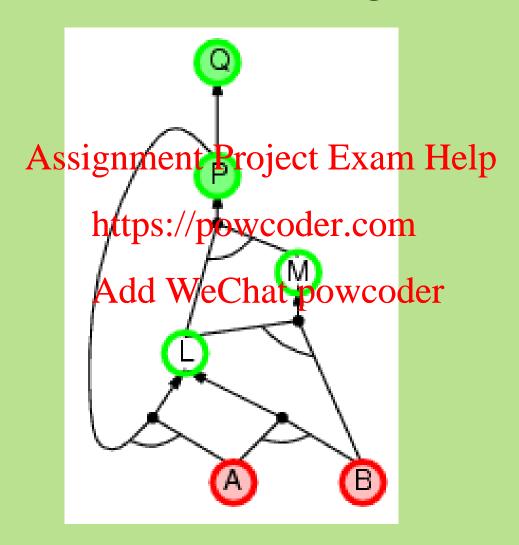
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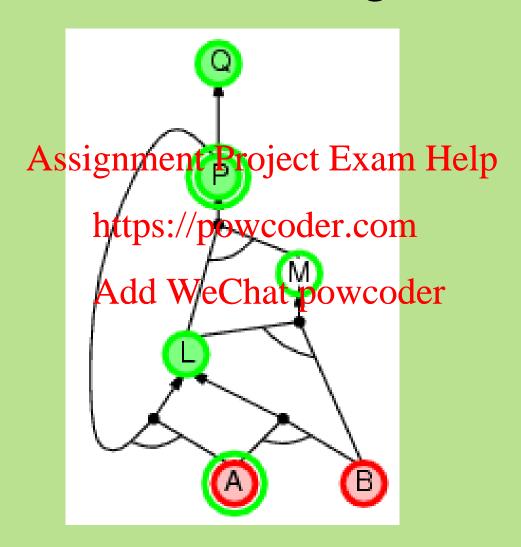
Avoid repeated work: check if new subgoal

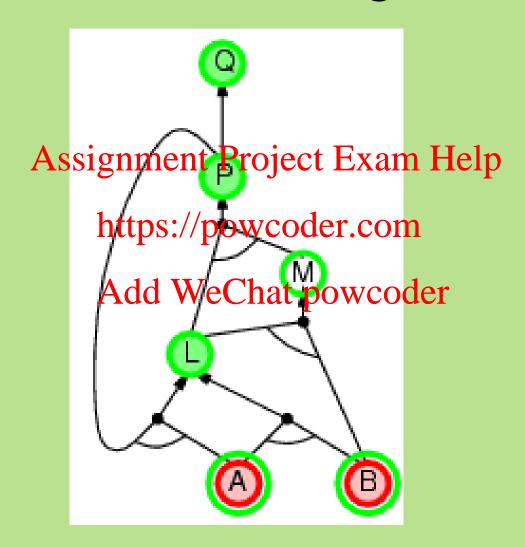
- 1. has already been proved true, or
- 2. has already failed

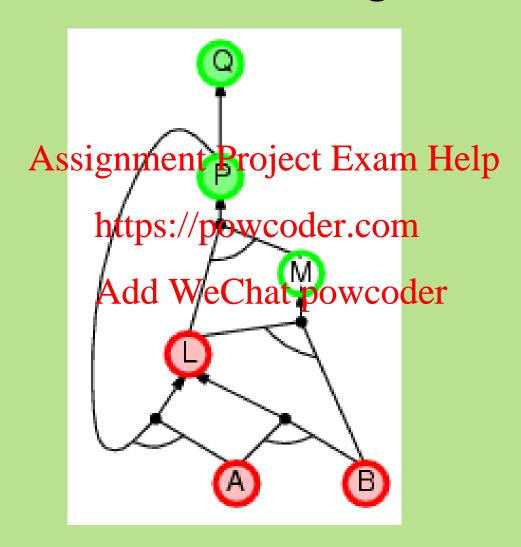


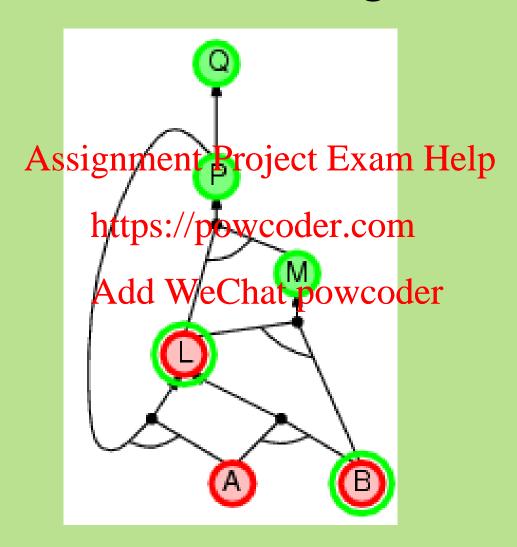


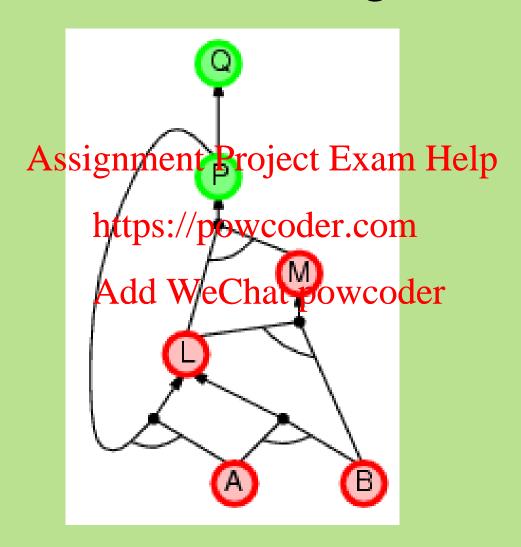


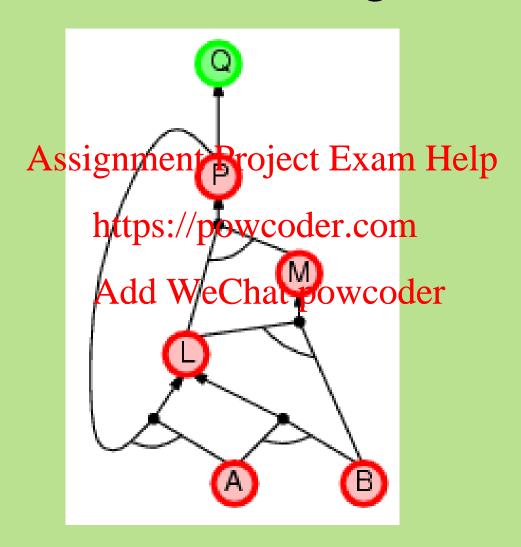


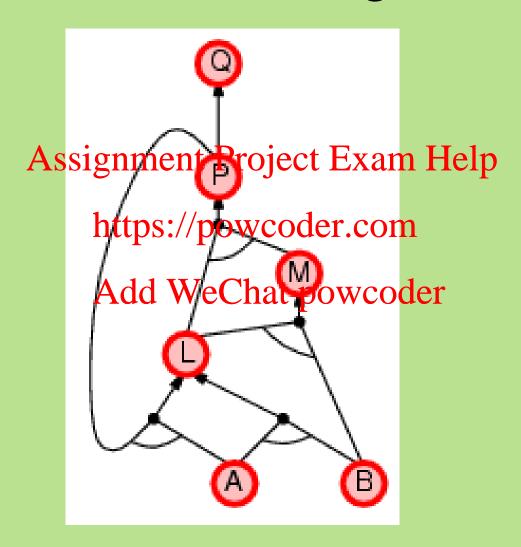












Forward vs. backward chaining

- FC is data-driven, automatic, unconscious processing,
 - e.g., object recognition, routine decisions
- May do lots of work that is lifely the goal
- BC is goal-driven, appropriate for problem-solving,
 - e.g., Where are any keys? How do light a PhD program?
- Complexity of BC can be much less than linear in size of KB

Efficient propositional inference

Two families of efficient algorithms for propositional inference:

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Complete backtracking search algorithms
https://powcoder.com
• DPLL algorithm (Davis, Putnam, Logemann, Loveland)

- Incomplete local delaw la Calgodriphones oder
 - WalkSAT algorithm

The DPLL algorithm

Determine if an input propositional logic sentence (in CNF) is satisfiable.

Improvements over truth table enumeration:

1. Early termination Help

A clause is true if any literal is true.

A sentence is fall the transport of the sentence is fall the transport of the sentence is fall to the

2. Pure symbol heuristic Pure symbol: always appears with the pane Sign for all clauses.

e.g., In the three clauses $(A \lor \neg B)$, $(\neg B \lor \neg C)$, $(C \lor A)$, A and B are pure, C is impure.

Make a pure symbol literal true.

3. Unit clause heuristic

Unit clause: only one literal in the clause

The only literal in a unit clause must be true.

The DPLL algorithm

```
function DPLL-Satisfiable?(s) returns true or false
           inputs: s, a sentence in propositional logic
           clauses \leftarrow the set of clauses in the CNF representation of s
          symbols ← a list of the proposition symbols in sectors Exam Help return DPLL(clauses, symbols, [])
function DPLL(clauhttpsb/spowlcoderscom false
           if every clause in clauses is true in model then return true
           if some clause in clause in clause in clause is fall to what the week of the clause in clause is claused to the clause in clau
           P, value \leftarrow Find-Pure-Symbol (symbols, clauses, model)
           if P is non-null then return DPLL(clauses, symbols-P, [P = value|model])
           P, value \leftarrow \text{Find-Unit-Clause}(clauses, model)
           if P is non-null then return DPLL(clauses, symbols-P, [P = value | model])
           P \leftarrow \text{First}(symbols); rest \leftarrow \text{Rest}(symbols)
           return DPLL(clauses, rest, [P = true | model]) or
                                        DPLL(clauses, rest, [P = false|model])
```

The WalkSAT algorithm

- Incomplete, local search algorithm
- Evaluation function: The min-conflict heuristic of minimizing Algei gumbert of rupeati Effects Plates
- Balance between greediness and randomness https://powcoder.com

Add WeChat powcoder

The WalkSAT algorithm

```
function WalkSat(clauses, p, max-flips) returns a satisfying model or failure inputs: clauses, a set of clauses in propositional logic

p, the probability of choosing to do a "random walk" move 
maxAlipsi number of flips plowed before giving up Help

model — a random assignment of true/false to the symbols in clauses

for i = 1 to max-flipsibs://powcoder.com

if model satisfies clauses then return model

clause — a randomly selected clause from clauses that is false in model

with probability policy has all and powerful selected symbol from clause

else flip whichever symbol in clause maximizes the number of satisfied clauses return failure
```

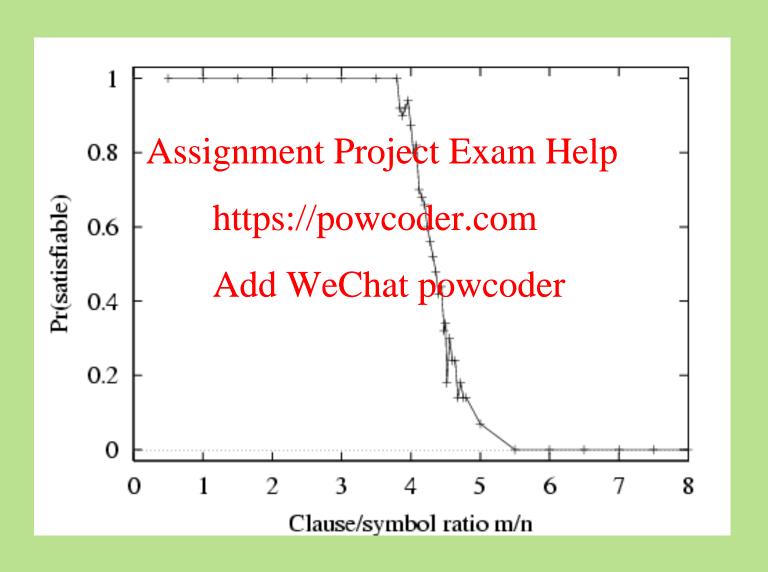
Hard satisfiability problems

Consider random 3-CNF sentences. e.g.,

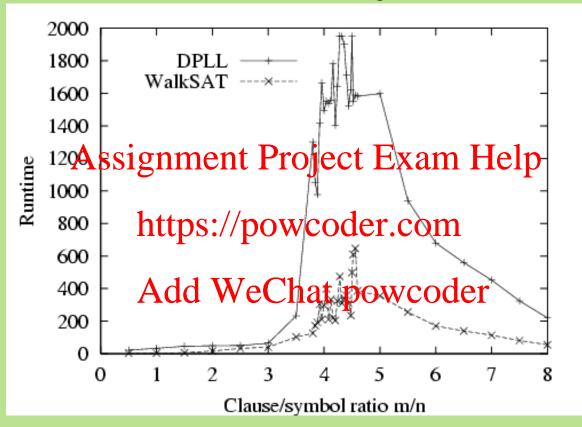
m = number Afficient powcoder n = number of symbols

 Hard problems seem to cluster near m/n = 4.3 (critical point)

Hard satisfiability problems



Hard satisfiability problems



 Median runtime for 100 satisfiable random 3-CNF sentences, n = 50

Inference-based agents in the wumpus world

A wumpus-world agent using propositional logic:

```
\begin{array}{lll}
\neg P_{1,1} & Assignment Project Exam Help \\
B_{x,y} \Leftrightarrow (P_{x,y+1} \lor P_{x,y+1} \lor P_{y,y}) & W_{x,y+1} \lor W_{x,y+1} \lor W_{x+1,y} \lor W_{x-1,y}) \\
W_{1,1} \lor W_{1,2} \lor \dots & W_{1,2} \lor W_{4,4} & WeChat powcoder \\
\neg W_{1,1} \lor \neg W_{1,2} & \neg W_{1,3} & \dots
\end{array}
```

⇒ 64 distinct proposition symbols, 155 sentences

```
function PL-Wumpus-Agent (percept) returns an action
   inputs: percept, a list, [stench, breeze, glitter]
   static: KB, initially containing the "physics" of the wumpus world
           x, y, orientation, the agent's position (init. [1,1]) and orient. (init. right)
            visited, an array indicating which squares have been visited, initially false
           action, the agent's most recent action, initially null
           plan, an action sequence, initially empty
   update x, y, orientation, ment Project, Exam Help
   if stench then Tell(KB, S_{x,y}) else Tell(KB, \neg S_{x,y})
   if breeze then Tell (MATERIAL) POST CORP. (1)
   if glitter then action \leftarrow grab
   else if plan is nonementated that power der
   else if for some fringe square [i,j], A_{SK}(KB, (\neg P_{i,j} \land \neg W_{i,j})) is true or
           for some fringe square [i,j], ASK(KB, (P_{i,j} \vee W_{i,j})) is false then do
        plan \leftarrow A^*-Graph-Search(Route-PB([x,y], orientation, [i,j], visited))
        action \leftarrow Pop(plan)
   else action \leftarrow a randomly chosen move
   return action
```

Expressiveness limitation of propositional logic

- KB contains "physics" sentences for every single square
- For every the game of the forward to the forward
- Rapid proliferation of clauses powcoder

Summary

- Logical agents apply inference to a knowledge base to derive new information and make decisions
- Basic concepts of logic:
 - syntax: formal structure of springest Exam Help
 semantics: truth of sentences wit models

 - entailment: necessary truth of one sentence given another
 - inference: deriving sentences from other sentences
 - soundness: derivations produce only entailed sentences
 - completeness: decidations can patd par valcante ed sentences
- Wumpus world requires the ability to represent partial and negated information, reason by cases, etc.
- Resolution is complete for propositional logic Forward, backward chaining are linear-time, complete for Horn clauses
- Propositional logic lacks expressive power