

CMPSC/Mathematics 451
MATLAB Program Two
Due 1 April 2020
Spring 2020

You are to write MATLAB (or Octave) functions to implement the composite Trapezoid rule and the composite Simpson's Rule for approximate computation of the integral

$$I = \int_a^b f(x)dx.$$

Both integration methods will have $(n+1)$ evenly space mesh points x_0, x_1, \dots, x_n where

$$x_k = a + kh, \quad h = (b - a)/n.$$

Given n you can generate the mesh points with the two MATLAB statements

`h=(b-a)/n;
x=a:h:b;`

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Your function for the Trapezoid rule should have the first line

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function int=trap(f,a,b,n)

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where f is a function handle for the function to be integrated. I recommend reviewing the MATLAB intrinsic functions **feval** for function evaluation and **sum** for summing the entries of a vector. Your code should be very short and should avoid loops. The output *int* is $T_0(h)$ (but don't use this notation in your code). I suggest treating $n = 1$ as a special case.

As part of your Simpson's rule routine, you will need a function called **update_trap** for updating the trapezoid rule. It has the first line

function new_int=update_trap(f,a,b,n,old_int)

where a, b , and n have the same meaning as for **trap**. If we let $h = (b - a)/n$, then $old_int = T_0(h)$. The output argument $new_int = T_0(h/2)$.

This uses the formula in the notes that produces $T_0(h/2)$ from $T_0(h)$ and the function f evaluated at the midpoints

$$x_{k+1/2} = a + (k + 1/2)h, \quad k = 0:n-1.$$

Again, this code for this function should be short.

The last function implements the composite Simpson's rule using the functions **trap** and **update_trap**. Its first line is

```
function [int,err]=simpson(f,a,b,n).
```

where

$$int = T_1(h) = (4 * T_0(h/2) - T_0(h))/3$$

and err is

$err = (T_1(h) - T_0(h))/15$
 is the error estimate from the notes. You may assume that n is divisible by 2. Thus **simpson** will make one call to **trap** (for $n/2$) to compute $T_0(2h)$ and two calls to **update_trap** to compute $T_0(h)$ and $T_0(h/2)$. This function should also be very short.

Test your code on three functions that I will put in the folder **Program Two Examples** in the MATLAB Assignments Folder on Canvas. They are **pifunc.m**, **logderiv.m**, and **intcderiv.m** and they are all one line functions. For these three functions, use the Trapezoid rule and Simpson's Rule with $n = 32, 64, 128$. Also produce compute $T_0(h) - I$ and $T_1(h) - I$ for the "exact" integrals. For Simpson's Rule, also produce the estimated error.

- **pifunc.m**. Compute the integral over the interval $[0, 1]$. This function is

$$pifunc(x) = 1/(1 + x^2).$$

You should get an approximation of π .

- **logderiv.m**. Compute the integral over the interval $[1, e]$ where $e = \exp(1)$ is the natural logarithm base. This function is

$$logderiv(x) = 1/x.$$

The integral should be approximately 1.

- **erfderiv.m**. Compute the integral over the intervals $[0, 1]$ and $[0, 3]$. This function is

$$\text{erfderiv}(x) = \frac{2}{\sqrt{\pi}} e^{-x^2}.$$

You should get good approximations of **erf**(1) and **erf**(3) from the **erf** function in MATLAB.

Please turn in all three functions, your calling script, and your results. I recommend use of the function **diary** in MATLAB to produce a diary file for your output.

Quiz Four will involve using parts of this project to construct a function for Romberg integration.

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