

Assignment Project Exam Help

Relational Model and Algebra

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Relations are sets of typed tuples

Relations

Relations take the form $R(A, B, \dots)$ where

- R is the name of the relation
- A, B, \dots is the set of attributes of the relation
 - Often write the set without commas: $A, B, \dots \equiv AB\dots$, and can refer to a set of attributes as A
 - The number of attributes n is the **arity** of the relation
Can call $R(A_1, \dots, A_n)$ an n -ary relation
 - $Domain(A)$ is the set of values (type) that the attribute can have
 - Will use $Atts(R)$ to find A, B, \dots
- The **extent** of $R(A, B, \dots)$ is the set of tuples:

$$\{\langle v_1^A, v_1^B, \dots \rangle, \langle v_2^A, v_2^B, \dots \rangle, \langle v_3^A, v_3^B, \dots \rangle, \dots\}$$
 - $\forall x. v_x^A \in Domain(A)$
 - No duplicate tuples
 - Not ordered
 - All tuples have the same arity

Relation=Table

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R		
A	B	...
v_1^A	v_1^B	...
v_2^A	v_2^B	...
v_3^A	v_3^B	...
\vdots	\vdots	\vdots

Set Semantics

- Order of columns not significant
- Order of rows not significant
- No duplicate rows

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- Attribute=Column
- Tuple=Row

Quiz 1: Equivalent Relations

Which is the odd one out?

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branch		
sortcode	bname	cash
56	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

branch		
bname	sortcode	cash
'Wimbledon'	56	94340.45
'Goodge St'	34	8900.67
'Strand'	67	34005.00

branch		
sortcode	bname	cash
34	'Goodge St'	8900.67
56	'Wimbledon'	94340.45
67	'Strand'	34005.00

branch		
sortcode	bname	cash
56	'Wimbledon'	94340.45
56	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

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Handling 'missing' attribute values

Suppose we want to have a relation `account(no,type,cname,rate,sortcode)`, but not all accounts have a rate.

Solution 1: Separate relations

account				
no	type	cname	rate	sortcode
100	'current'	'McBrien, P.'		67
101	'deposit'	'McBrien, P.'		67
103	'current'	'Boyd, M.'		34
107	'current'	'Poulovassilis, A.'		56
119	'deposit'	'Poulovassilis, A.'		56
125	'current'	'Bailey, J.'		56

account_rate	
no	rate
101	5.25
119	5.50

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Solution 2: NULL values

account				
no	type	cname	rate	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	67
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

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Relational Keys

Key

A **key** of a relation $R(AB\dots)$ is a subset of the attributes for which the values in any extent are unique across all tuples

- Every relation has at least one key, which is the entire set of attributes
- A key is **violated** by there being two tuples in the extent which have the same values for the attributes of the key
- If A is a key, then so must AB be a key
- A **minimal key** is a set of attributes $AB\dots$ for which no subset of the attributes is also a key
- The **primary key** is one of the keys of the relation: serves as the default key when no key explicitly stated

Quiz 2: Violation of Relational Keys

movement			
mid	no	amount	tdate
1000	100	2300.00	5/1/1999
1001	101	4000.00	5/1/1999
1002	100	-223.45	5/1/1999
1004	107	-100.00	11/1/1999
1005	103	145.50	12/1/1999
1006	100	10.23	15/1/1999
1007	107	345.56	15/1/1999
1008	101	1230.00	15/1/1999
1009	119	5600.00	18/1/1999

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Which key is violated?

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A

movement(mid)

B

movement(no,amount)

C

movement(no,tdate)

D

movement(amount,tdate)

Quiz 3: Correct Keys for Relations

movement			
mid	no	amount	tdate
1000	100	2300.00	5/1/1999
1001	101	4000.00	5/1/1999
1002	100	-223.45	5/1/1999
1004	107	-100.00	11/1/1999
1005	103	145.50	12/1/1999
1006	100	10.23	15/1/1999
1007	107	345.56	15/1/1999
1008	101	1230.00	15/1/1999
1009	119	5600.00	18/1/1999

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Which key makes most sense in a bank UoD?

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A

movement(amount)

B

movement(no,amount)

C

movement(no,tdate)

D

movement(amount,tdate)

Relational Foreign Keys

Foreign Key

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A **foreign key** $R(X) \xRightarrow{fk} S(Y)$ of a relation $R(AB\dots)$ is a subset $X \subseteq AB\dots$ of the attributes for which the values in the extent of R also appear as values of attributes \vec{Y} in the extent of S , and \vec{Y} is a key of S .

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$\text{account}(\text{sortcode}) \xRightarrow{fk} \text{branch}(\text{sortcode})$

account				
no	type	cname	rate	sortcode
100	'current'	'McBrien, S.'	NULL	47
101	'deposit'	'McBrien, P.'	5.25	17
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

key branch(sortcode)

branch		
sortcode	name	cash
36	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

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Quiz 4: Foreign Key Violation

$$\text{account}(\text{sortcode}) \xRightarrow{fk} \text{branch}(\text{sortcode})$$

account				
no	type	cname	rate	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	67
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

key_branch(sortcode)		
sortcode	bname	cash
56	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

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Which update violates the foreign key?

A

insert into account
(126,'business','McBrien, P.',1.00,67)

insert into branch
(78,'Ealing',1000.00)

C

delete from branch
(67,'Strand',34005.00)

D

delete from account
(103,'current','Boyd, M.',NULL,34)

Example Relational Schema

branch			
sortcode	branch	cash	
56	'Wimbledon'	94340.45	
34	'Goodge St'	8900.67	
67	'Strand'	34005.00	

movement			
mid	no	amount	tdate
1000	100	2300.00	5/1/1999
1001	101	4000.00	5/1/1999
1002	100	-223.45	8/1/1999
1004	107	-100.00	11/1/1999
1005	103	145.50	12/1/1999
1006	100	11.23	15/1/1999
1007	107	345.56	15/1/1999
1008	101	1230.00	15/1/1999
1009	119	5600.00	18/1/1999

account			
no	type	balance	sortcode
100	'current'	McBrien, P.	NULL
101	'deposit'	'McBrien, P.'	5.25
103	'current'	'Boyd, M.'	NULL
107	'current'	'Poulovassilis, A.'	NULL
119	'deposit'	'Poulovassilis, A.'	5.50
125	'current'	'Bailey, J.'	NULL

key branch(sortcode)

key branch(bname)

key movement(no)

key account(no)

movement(no) \xRightarrow{fk} account(no)account(sortcode) \xRightarrow{fk} branch(sortcode)

Relational Algebra: A Query Language for the Relational Model

Primitive operators of the Relational Algebra

Symbol	Name	Type
π	Project	Unary
σ	Select	Unary
\times	Cartesian Product	Binary
\cup	Union	Binary
$-$	Difference	Binary

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- All operators take relations as input
- All operators produce one relation as their output
- Other (useful) operators may be defined in terms of the five primitive operators

Relational Algebra: Project π

account				
<u>no</u>	type	cname	rate	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	56
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

Project Operator

$\pi_{no, type} account$	
<u>no</u>	type
100	'current'
101	'deposit'
103	'current'
107	'current'
119	'deposit'
125	'current'

$\pi_{sortcode} account$	
sortcode	
67	
34	
56	

Relational Algebra: Select σ

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Account				
no	type	cname	rate	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	67
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

Select Operator

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Account				
no	type	cname	rate	sortcode
101	'deposit'	'McBrien, P.'	5.25	67
119	'deposit'	'Poulovassilis, A.'	5.50	56

Relational Algebra: Product \times

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<u>sortcode</u>	branch	cash
56	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

<u>no</u>	type	cname	rate	sortcode
101	'deposit'	'McBrien, P.'	5.25	67
119	'deposit'	'Poulovassilis, A.'	5.50	56

Product Operator

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branch \times $\sigma_{\text{rate} > 0}$ account							
<u>sortcode</u>	bname	cash	<u>no</u>	type	cname	rate	sortcode
56	'Wimbledon'	94340.45	101	'deposit'	'McBrien, P.'	5.25	67
56	'Wimbledon'	94340.45	119	'deposit'	'Poulovassilis, A.'	5.50	56
34	'Goodge St'	8900.67	101	'deposit'	'McBrien, P.'	5.25	67
34	'Goodge St'	8900.67	119	'deposit'	'Poulovassilis, A.'	5.50	56
67	'Strand'	34005.00	101	'deposit'	'McBrien, P.'	5.25	67
67	'Strand'	34005.00	119	'deposit'	'Poulovassilis, A.'	5.50	56

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Quiz 5: RA Queries

branch		
sortcode	bname	cash
56	'Wimbleton'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

account				
no	type	cname	rate	sortcode
100	'current'	'McBrien, P.'	NULL	57
101	'deposit'	'McBrien, P.'	5.2	57
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

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Which RA query lists the name of branches that have deposit accounts?

A

 $\pi_{\text{sortcode}} \sigma_{\text{type}='deposit'} (\text{account})$

B

 $\pi_{\text{bname}} \sigma_{\text{account.sortcode}=\text{branch.sortcode} \wedge \text{type}='deposit'} (\text{account} \times \text{branch})$

C

 $\pi_{\text{bname}} (\text{branch} \times \sigma_{\text{type}='deposit'} \text{account})$

D

 $\pi_{\text{bname}} \sigma_{\text{type}='deposit'} (\text{account} \times \text{branch})$

SPJ Queries

Select Project Join (SPJ) queries

If a product of tables is formed, where a selection is then done that compares the attributes of those tables, we say that a **join** has been performed.

Normally not all columns of the product are returned, and therefore a project is also required.

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Branches with current accounts

$\pi_{\text{bname, no}} \sigma_{\text{branch.sortcode}=\text{account.sortcode} \wedge \text{account.type}='current'} (\text{branch} \times \text{account})$

bname	no
'Goodge St'	103
'Wimbledon'	107
'Wimbledon'	125
'Strand'	100

Relational Algebra: Union \cup

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$\pi_{\text{sortcode as id}} \text{account}$	$\pi_{\text{no as id}} \text{account}$
id	id
67	100
34	101
56	103
	107
	119
	125

Union Operator

$\pi_{\text{sortcode as id}} \text{account} \cup \pi_{\text{no as id}} \text{account}$
id
67
34
56
100
101
103
107
119
125

- relations must be **union compatible**

Relational Algebra: Difference —

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$\pi_{no} account$	$\pi_{no} movement$
100	100
101	101
103	103
107	107
119	119
125	

Difference Operator

$\pi_{no} account - \pi_{no} movement$

125

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- relations must be **union compatible**

Rules for Combining Operators

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Since all operators produce a relation as output, *any* operator may produce one of the inputs to any other operator.

well formed F.A. query

- the output of the nested operator must contain the attributes required by an outer π or σ
- the two inputs to a \Join must contain the same number of attributes

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Quiz 6: Well formed queries

account				
no	type	sname	rate	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	67
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulouvassilis, A.'	NULL	56
119	'deposit'	'Poulouvassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

movement			
mid	no	amount	tdate
1000	100	2300.00	5/1/1999
1001	101	4000.00	5/1/1999
1002	100	-223.45	8/1/1999
1004	107	-100.00	11/1/1999
1005	103	145.50	12/1/1999
1006	100	10.23	15/1/1999
1007	107	345.56	15/1/1999
1008	101	1230.00	15/1/1999
1009	119	5600.00	18/1/1999

Which RA query is well formed?

A

$\sigma_{\text{type}='current'} \pi_{\text{no}} \text{ account}$

B

$\pi_{\text{no}} \text{ account} - \pi_{\text{no}, \text{mid}} \text{ movement}$

C

$\pi_{\text{no}} \sigma_{\text{type}='current'} \text{ account}$

D

$\pi_{\text{no}} \pi_{\text{type}} \text{ account}$

Worksheet: Primitive Relational Algebra Operators

sortcode	branch	cash
56	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

mid	no	amount	tdate
1000	100	2300.00	5/1/1999
1001	101	4000.00	5/1/1999
1002	100	-223.45	8/1/1999
1004	107	-100.00	11/1/1999
1005	103	145.50	12/1/1999
1006	100	11.23	15/1/1999
1007	107	345.56	15/1/1999
1008	101	1230.00	15/1/1999
1009	119	5600.00	18/1/1999

no	type	name	rate	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	67
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

key branch(sortcode)

key branch(bname)

key movement(no, mid)

key account(no)

 $\text{movement}(\text{no}) \xRightarrow{fk} \text{account}(\text{no})$ $\text{account}(\text{sortcode}) \xRightarrow{fk} \text{branch}(\text{sortcode})$

Derived Relational Algebra: Natural Join \bowtie

Natural Join

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Natural Join

$\text{branch} \bowtie \text{account} \equiv \text{branch} \text{ sortcode} = \text{account sortcode} \text{ branch} \bowtie \text{account}$

branch \bowtie account						
sortcode	bname	cash	no	type	cname	rate
34	'Goedge St'	8900.67	103	'current'	'Boyd, M.'	NULL
56	'Wimbledon'	94340.45	107	'current'	'Poullovassilis, A.'	NULL
56	'Wimbledon'	94340.45	119	'deposit'	'Poullovassilis, A.'	5.50
56	'Wimbledon'	94340.45	125	'current'	'Bailey, J.'	NULL
67	'Strand'	34005.00	100	'current'	'McBrien, P.'	NULL
67	'Strand'	34005.00	101	'deposit'	'McBrien, P.'	5.25

Quiz 7: Natural Join

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What is the result of $\pi_{no}(\text{account} \bowtie \text{movement})$?

A

$\pi_{no}(\text{account} \bowtie \text{movement})$
no
100
101
103
107
119
125

B

$\pi_{no}(\text{account} \bowtie \text{movement})$
no
100
101
103
107
119
125

C

$\pi_{no}(\text{account} \bowtie \text{movement})$
no
125

D

$\pi_{no}(\text{account} \bowtie \text{movement})$
no

Derived Relational Algebra: Semi Join \ltimes

Semi Join

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$$R \ltimes S = R \bowtie \pi_{Attr(R) \cap Attr(S)}(S)$$

Semi Join

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$account \ltimes movement = account \bowtie \pi_{no, rate, sortcode}(movement)$

account \ltimes movement				
<u>no</u>	type	cname	rate	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	67
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56

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Derived Relational Algebra: Joins

Natural Join

$$R \bowtie S = \sigma_{R.A_1=S.A_1 \wedge \dots \wedge R.A_m=S.A_m}(R \times S)$$

Equi Join

$$R \bowtie^B S = \sigma_{R.A=B.A}(R \times S)$$

Semi Join

$$R \ltimes S = R \bowtie (\pi_{Attr(R)}(R) \cap Attr(S)(S))$$

Theta Join

$$R \bowtie^\theta S = \sigma_\theta R \times S$$

Quiz 8: Understanding join operators

branch	branch	branch
sortcode	lname	cash
56	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

account				
no	type	cname	rate	sortcode
100	'current'	'McBrien, P.'	NULL	57
101	'deposit'	'McBrien, P.'	5.25	57
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

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Which RA query produces the most tuples?

A

branch ⋈_{branch.sortcode = account.sortcode} account

B

branch ⋈_{branch.lname = account.cname} account

C

branch ⋈ account

D

branch ⋈_{branch.sortcode = account.sortcode} account

Quiz 9: Foreign Keys and Natural Joins (1)

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Suppose R and S only share attribute A , and there is a foreign key $S(A) \xrightarrow{fk} R(A)$.

If $|R| = 100$ and $|S| = 1,000$, what is $|R \bowtie S|$?

A

100

B

1,000

C

100,000

D

400

Note that $|R|$ returns the number of tuples in the current extent of R

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Quiz 10: Foreign Keys and Natural Joins (2)

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Suppose R and S only share attribute A , and there is a foreign key $R(A) \xrightarrow{fk} S(A)$.

If $|R| = 100$ and $|S| = 1,000$, what is $|R \bowtie S|$?

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A

100

B

1,000

C

100,000

D

900

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Derived Relational Algebra: Intersection \cap

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$$R \cap S = R - (R - S)$$

 $\pi_{\text{noaccount}} \cap \pi_{\text{movement}}$

$\pi_{\text{noaccount}}$
no
100
101
103
107
119
125

 $\pi_{\text{noaccount}} - \pi_{\text{noaccount}}$

no
2

 $\pi_{\text{noaccount}} \cap \pi_{\text{noaccount}}$

$\pi_{\text{noaccount}} \cap \pi_{\text{noaccount}}$
no
100
101
103
107
119

Quiz 11: Intersection

email	
name	address
'McBrien, P.'	p.mcbrien@imperial.ac.uk
'Poulovassilis, A.'	ap@dcsc.bbk.ac.uk
'Pietzuch, P.'	pp@doc.ic.ac.uk

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What is the result of $\pi_{\text{name}} \text{account} \cap \pi_{\text{name}} \text{email}$?

A

cname
'McBrien, P.'
'Boyd, M.'
'Poulovassilis, A.'
'Bailey, J.'
'Pietzuch, P.'

B

cname
'McBrien, P.'
'Boyd, M.'
'Poulovassilis, A.'
'Bailey, J.'

C

cname
'McBrien, P.'
'Poulovassilis, A.'
'Pietzuch, P.'

D

cname
'McBrien, P.'
'Poulovassilis, A.'

Derived Relational Algebra: Division \div

Division

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Division

$$\begin{aligned} \pi_{\text{cname, type}} \text{account} \div \pi_{\text{type}} \text{account} &= \pi_{\text{cname}} \pi_{\text{cname, type}} \text{account} - \\ &\quad \pi_{\text{cname}} ((\pi_{\text{cname}} \pi_{\text{cname, type}} \text{account} \times \pi_{\text{type}} \text{account}) - \pi_{\text{cname, type}} \text{account}) \\ \pi_{\text{cname, type}} \text{account} - \pi_{\text{type}} \text{account} &= \pi_{\text{cname}} \text{account} - \\ &\quad \pi_{\text{cname}} ((\pi_{\text{cname}} \text{account} \times \pi_{\text{type}} \text{account}) - \pi_{\text{cname, type}} \text{account}) \end{aligned}$$

$\pi_{\text{cname, type}} \text{account}$	
cname	type
'McBrien, P.'	'current'
'McBrien, P.'	'deposit'
'Boyd, M.'	'current'
'Poulovassilis, A.'	'current'
'Poulovassilis, A.'	'deposit'
'Bailey, J.'	'current'

$\pi_{\text{type}} \text{account}$
type
'current'
'deposit'

$\pi_{\text{cname, type}} \text{account} \div \pi_{\text{type}} \text{account}$
cname
'McBrien, P.'
'Poulovassilis, A.'

Evaluation of Division

$\pi_{\text{name}} \text{ account}$
cname
'McBrien, P.'
'Boyd, M.'
'Poulovassilis, A.'
'Bailey, J.'

$\pi_{\text{type}} \text{ account}$
type
'current'
'deposit'



name	type
'McBrien, P.'	'current'
'McBrien, P.'	'deposit'
'Boyd, M.'	'current'
'Boyd, M.'	'deposit'
'Poulovassilis, A.'	'current'
'Poulovassilis, A.'	'deposit'
'Bailey, J.'	'current'
'Bailey, J.'	'deposit'

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Evaluation of Division

$$\pi_{\text{name}} \text{ account} \times \pi_{\text{type}} \text{ account}$$

cname	type
'McBrien, P.'	'current'
'McBrien, P.'	'deposit'
'Boyd, M.'	'current'
'Boyd, M.'	'deposit'
'Poulovassilis, A.'	'current'
'Poulovassilis, A.'	'deposit'
'Bailey, J.'	'current'
'Bailey, J.'	'deposit'

$$\pi_{\text{name, type}} \text{ account}$$

cname	type
'McBrien, P.'	'current'
'McBrien, P.'	'deposit'
'Boyd, M.'	'current'
'Boyd, M.'	'deposit'
'Poulovassilis, A.'	'current'
'Poulovassilis, A.'	'deposit'
'Bailey, J.'	'current'
'Bailey, J.'	'deposit'



$$(\pi_{\text{name}} \text{ account} \times \pi_{\text{type}} \text{ account}) \div \pi_{\text{name, type}} \text{ account}$$

cname	type
'Boyd, M.'	'deposit'
'Bailey, J.'	'deposit'

Evaluation of Division

$(\pi_{\text{name account}} \times \pi_{\text{type account}}) - \pi_{\text{name,type account}}$	
cname	type
'Boyd, M.'	'deposit'
'Bailey, J.'	'deposit'



$\pi_{\text{name}}((\pi_{\text{name account}} \times \pi_{\text{type account}}) - \pi_{\text{name,type account}})$	
cname	
'Boyd, M.'	
'Bailey, J.'	

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Evaluation of Division

$\pi_{\text{name}} \text{ account}$
cname
'McBrien, P.'
'Boyd, M.'
'Poulovassilis, A.'
'Bailey, J.'

$\pi_{\text{name}}((\pi_{\text{name}} \text{ account} \times \pi_{\text{type}} \text{ account}) - \pi_{\text{name,type}} \text{ account})$
cname
'Boyd, M.'
'Bailey, J.'



$\pi_{\text{name}} \text{ account} - \pi_{\text{name}}((\pi_{\text{name}} \text{ account} \times \pi_{\text{type}} \text{ account}) - \pi_{\text{name,type}} \text{ account})$
cname
'McBrien, P.'
'Poulovassilis, A.'

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Worksheet: Derived Relational Algebra Operators

sortcode	branch	cash
56	'Wimbledon'	94340.45
34	'Goodge St'	8900.67
67	'Strand'	34005.00

mid	no	amount	tdate
1000	100	2300.00	5/1/1999
1001	101	4000.00	5/1/1999
1002	100	-223.45	8/1/1999
1004	107	-100.00	11/1/1999
1005	103	145.50	12/1/1999
1006	100	11.23	15/1/1999
1007	107	345.56	15/1/1999
1008	101	1230.00	15/1/1999
1009	119	5600.00	18/1/1999

no	type	name	rate	sortcode
100	'current'	'McBrien, P.'	NULL	67
101	'deposit'	'McBrien, P.'	5.25	67
103	'current'	'Boyd, M.'	NULL	34
107	'current'	'Poulovassilis, A.'	NULL	56
119	'deposit'	'Poulovassilis, A.'	5.50	56
125	'current'	'Bailey, J.'	NULL	56

key branch(sortcode)

key branch(bname)

key movement(no, mid)

key account(no)

$\text{movement}(\text{no}) \xRightarrow{fk} \text{account}(\text{no})$

$\text{account}(\text{sortcode}) \xRightarrow{fk} \text{branch}(\text{sortcode})$

Equivalences Involving Project

Project and Project

$$\pi_{\vec{X}} \pi_{\vec{Y}} R \equiv \pi_{\vec{X}} R$$

You can eliminate any inner project (note that to be well formed $\vec{X} \subseteq \vec{Y}$)

Project and Select

$$\pi_{\vec{X}} \sigma_{P(\vec{Y})} R \equiv \sigma_{P(\vec{Y})} \pi_{\vec{X}} R$$

You can move a project of attributes \vec{X} inside a select, provided the select predicate can be answered from those attributes, i.e. $\vec{Y} \subseteq \vec{X}$

Project and Product

$$\pi_{\vec{X}}(R \times S) \equiv \pi_{\vec{X} \cap \text{Attrs}(R)} R \times \pi_{\vec{X} \cap \text{Attrs}(S)} S$$

Project and Union

$$\pi_{\vec{X}}(R \cup S) \equiv \pi_{\vec{X}} R \cup \pi_{\vec{X}} S$$

Project and Difference

$$\pi_{\vec{X}}(R - S) \supseteq \pi_{\vec{X}} R - \pi_{\vec{X}} S$$

Equivalences Involving Select

Select and Project

$$\sigma_{P(\vec{X})} \pi_{\vec{X}} R \equiv \pi_{\vec{X}} \sigma_{P(\vec{X})} R$$

Select and Select

$$\sigma_{P_x(\vec{X})} \sigma_{P_y(\vec{Y})} R \equiv \sigma_{P_x(\vec{X}) \wedge P_y(\vec{Y})} R$$

Select and Product

$$\sigma_{P(\vec{X})} (R \times S) \equiv \sigma_{P(\vec{X})} R \times S \iff \vec{X} \subseteq \text{Atts}(R)$$

You can move a select predicate $P(\vec{X})$ onto one of the relations inside a product provided $\vec{X} \subseteq \text{Atts}(R)$.

Select and Union

$$\sigma_{P(\vec{X})} (R \cup S) \equiv \sigma_{P(\vec{X})} R \cup \sigma_{P(\vec{X})} S$$

Select and Difference

$$\sigma_{P(\vec{X})} (R - S) \equiv \sigma_{P(\vec{X})} R - S$$

Quiz 12: Equivalent RA Expressions (Unary Operators)

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Which RA expression is not equivalent to the other three?

A

 $\pi_{no} \sigma_{type='current'} \text{account}$

B

 $\pi_{no} \sigma_{type='current'} \pi_{no,type,cname} \text{account}$

C

 $\pi_{no} \sigma_{type \neq 'deposit'} \pi_{no,type,cname} \text{account}$

D

 $\pi_{no} \sigma_{type='current'} \sigma_{type \neq 'deposit'} \text{account}$

Quiz 13: Query Evaluation

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Which RA means that the \times operator handles fewer tuples?

A

$\sigma_{\text{account.no}=\text{movement.no}}(\sigma_{\text{sortcode}=67} \text{ account} \times \sigma_{\text{amount}<0} \text{ movement})$

B

$\sigma_{\text{account.no}=\text{movement.no} \wedge \text{sortcode}=67}(\text{account} \times \sigma_{\text{amount}<0} \text{ movement})$

C

$\sigma_{\text{account.no}=\text{movement.no} \wedge \text{amount}<0}(\sigma_{\text{sortcode}=67} \text{ account} \times \text{movement})$

D

$\sigma_{\text{account.no}=\text{movement.no} \wedge \text{sortcode}=67 \wedge \text{amount}<0}(\text{account} \times \text{movement})$

Equivalences Involving Binary Operators

Product and Union

$$R \times (S \cup T) \equiv (R \times S) \cup (R \times T)$$

Product and Difference

$$R \times (S - T) \equiv (R \times S) - (R \times T)$$

Union and Product

$$R \cup (S \times T) \text{ unable to move } \cup \text{ inside } \times$$

Union and Difference

$$R \cup (S - T) \text{ unable to move } \cup \text{ inside } -$$

Difference and Product

$$R - (S \times T) \text{ unable to move } - \text{ inside } \times$$

Difference and Union

$$R - (S \cup T) \equiv (R - S) - T$$

Quiz 14: Equivalent RA Expressions (Binary Operators)

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Which equivalence does not hold?

A

$$(R \times S) \times T \equiv R \times (S \times T)$$

B

$$(R - S) - T \equiv R - (S - T)$$

C

$$(R \cup S) \cup T \equiv R \cup (S \cup T)$$

D

$$(R \cap S) \cap T \equiv R \cap (S \cap T)$$

Worksheet: Equivalences Between RA Expressions

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1 $\pi_{no,type} \sigma_{sortcode=56} \pi_{no,type,sortcode} \sigma_{type='deposit'} \text{account}$

2 $\sigma_{\text{account.no}=\text{movement.no}} (\pi_{no,cname} \text{account} \times \pi_{mid,no} \sigma_{\text{amount}>1000} \text{movement})$

3 $\sigma_{\text{account.no}=\text{movement.no}} (\pi_{no,cname,rate} \text{account} \times$
 $(\sigma_{\text{amount}>1000} \pi_{mid,no} \text{movement} \cup \sigma_{\text{amount}<100} \pi_{mid,no} \text{movement}))$

4 $\pi_{no,cname,tdate} \sigma_{\text{amount}<0} \sigma_{\text{account.no}=\text{movement.no}} \text{account} \times \text{movement}$

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Quiz 15: Monotonic and non-monotonic operators

A monotonic operator has the property that an additional tuple put into any input relation which only cause additional tuples to be generated in the output relation.

A non-monotonic operator has the property that an additional tuple put into an input relation may remove tuples from the output relation

Which RA operator is non-monotonic?

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A

πR

B

$R \times S$

C

$R \cup S$

D

$R - S$

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Incremental Query Evaluation

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Suppose we add rows Δ_R to extent of relation R so it becomes R'

If we represent Δ_R as a relation (with the same attributes as R) then

$$R' = R \cup \Delta_R$$

$$\pi_{\vec{X}} R' \equiv \pi_{\vec{X}} R \cup \pi_{\vec{X}} \Delta_R$$

$$\sigma_{P(\vec{X})} R' \equiv \sigma_{P(\vec{X})} R \cup \sigma_{P(\vec{X})} \Delta_R$$

$$R' \times S \equiv (R \times S) \cup (\Delta_R \times S)$$

$$R' \cup S \equiv (R \cup S) \cup \Delta_R$$

$$R' - S \equiv (R - S) \cup (\Delta_R - S)$$

$$S - R' \equiv (S - R) - \Delta_R$$

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Example: Query result after update to account (1)

- 1 Suppose that we had already evaluated query Q

$\pi_{\text{bname}, \text{no}} \sigma_{\text{branch.sortcode}=\text{account.sortcode} \wedge \text{account.type}='current'}(\text{branch} \times \text{account})$	
bname	no
'Goodge St'	103
'Wimbledon'	107
'Wimbledon'	125
'Strand'	100

- 2 If Δ_{account} is added to account to get account':

$$\begin{aligned} & \pi_{\text{bname}, \text{no}} \sigma_{\text{branch.sortcode}=\text{account.sortcode} \wedge \text{account.type}='current'}(\text{branch} \times \text{account}') \\ & \pi_{\text{bname}, \text{no}} \sigma_{\text{branch.sortcode}=\text{account.sortcode} \wedge \text{account.type}='current'}((\text{branch} \times \text{account}) \cup (\text{branch} \times \Delta_{\text{account}})) \\ & \pi_{\text{bname}, \text{no}} \sigma_{\text{branch.sortcode}=\text{account.sortcode} \wedge \text{account.type}='current'}(\text{branch} \times \text{account}) \cup \\ & \pi_{\text{bname}, \text{no}} \sigma_{\text{branch.sortcode}=\text{account.sortcode} \wedge \text{account.type}='current'}(\text{branch} \times \Delta_{\text{account}}) \end{aligned}$$

- 3 Thus if Δ_{account} is added to account, we only need evaluate

$$\pi_{\text{bname}, \text{no}} \sigma_{\text{branch.sortcode}=\text{account.sortcode} \wedge \text{account.type}='current'}(\text{branch} \times \Delta_{\text{account}})$$

Example: Query result after update to account (2)

4 Suppose we have

Δ_{account}				
126	'business'	'McBrien, P.'	1.00	67
127	'current'	'Pietzuch, P.'	NULL	34

Then

$\pi_{\text{bname}, \text{no}} \sigma_{\text{branch.sortcode} = \text{account.sortcode} \wedge \text{account.type} = \text{'current'}} (\text{branch} \times \Delta_{\text{account}})$				
bname				no
'Goodge St'				127

5 Thus since $Q' = Q \cup \Delta_Q$

$\pi_{\text{bname}, \text{no}} \sigma_{\text{branch.sortcode} = \text{account.sortcode} \wedge \text{account.type} = \text{'current'}} (\text{branch} \times \text{account}')$				
bname				no
'Goodge St'				127
'Wimbledon'				107
'Wimbledon'				125
'Strand'				100
'Goodge St'				127