lecture 4

Combinational logic 2

- ROM

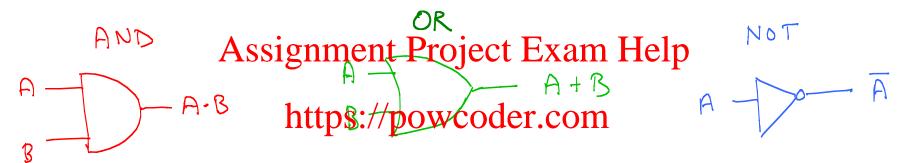
Assignment Project Exam Help

- arithmetic wips with swcoder.com

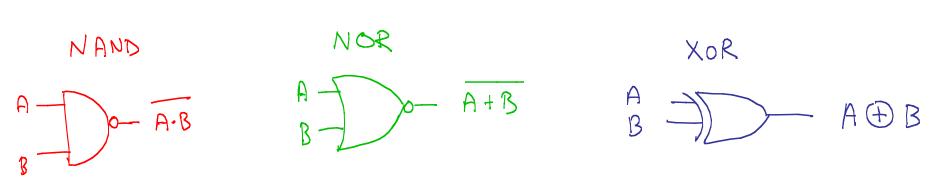
- arithmetic logic unit (ALU)

January 20, 2016

Last lecture: truth tables, logic gates & circuits



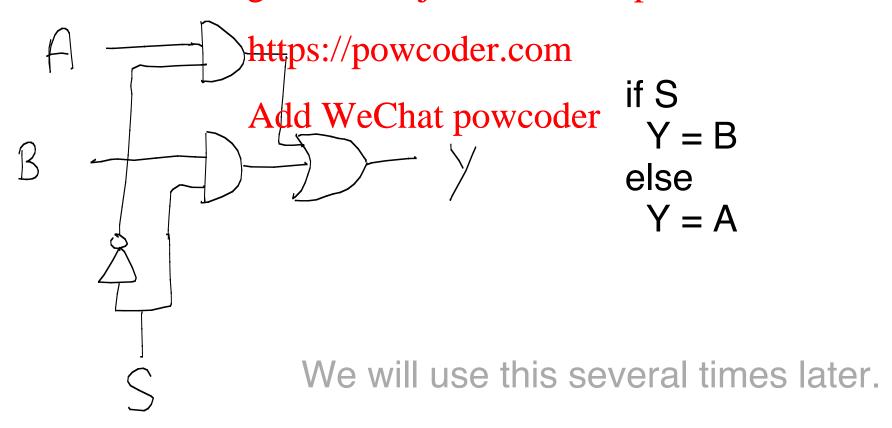
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Recall multiplexor (selector)

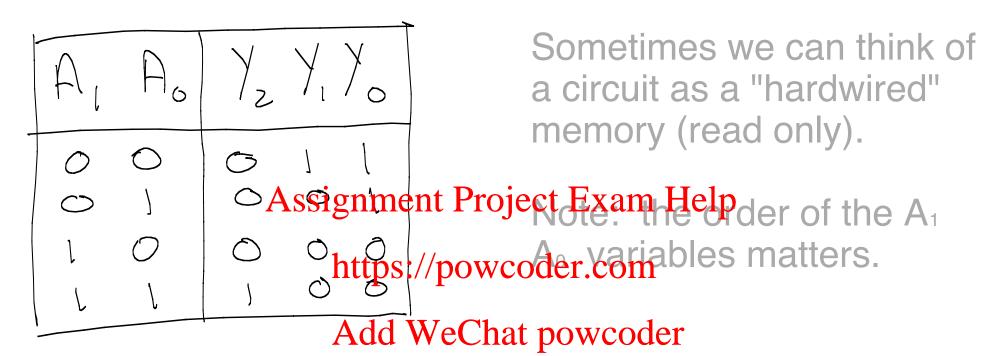
$$Y = \overline{S} \cdot A + S \cdot B$$

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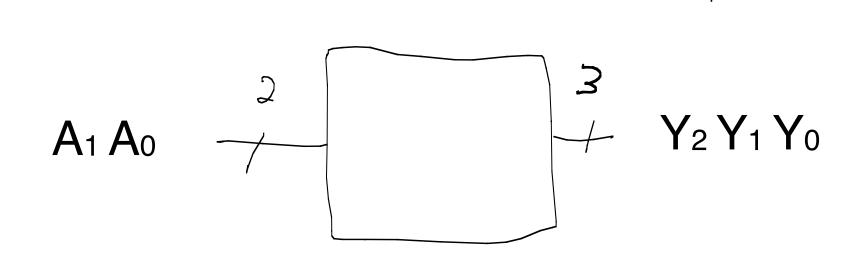


"Read-only Memory"

(leftover topic from last lecture)



address data



Recall: binary arithmetic

Notes:

- Co = 0
- A, B could represent signed or unsigned numbers

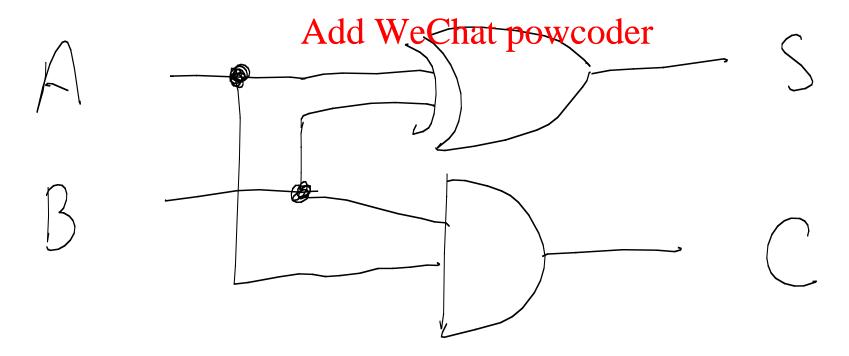
Let's build an "adder" circuit.

Half Adder

 $S = A \oplus B$

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$$C_{n-1} \dots C_{2}C_{1}C_{0}$$

$$A_{n-1} \dots A_{2}A_{1}A_{0}$$

$$B_{n-1} \dots B_{2}B_{1}B_{0}$$

$$S_{n-1} \dots S_{2}S_{1}S_{0}$$

AK	BK	CK
0	\bigcirc	\bigcirc
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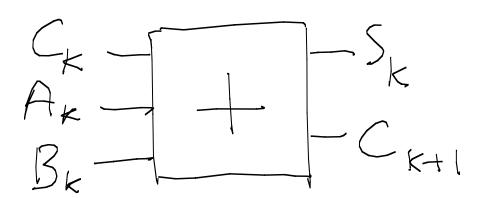
S_k C_{k+1}

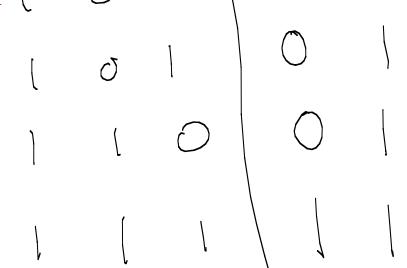
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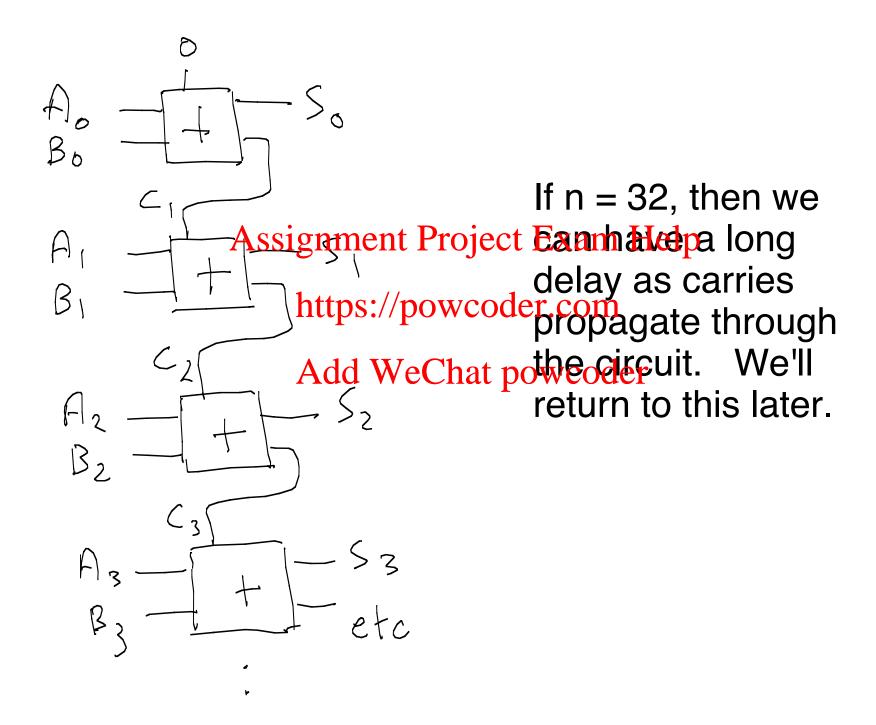
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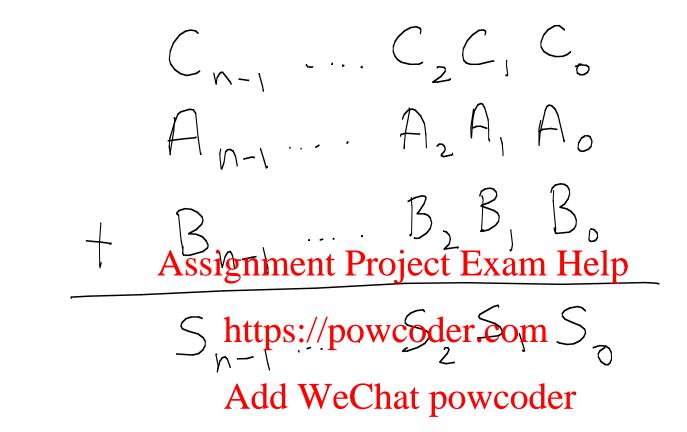
full adder





Ripple Adder





As I mentioned before.... the *interpretation* of the S bit string depends on whether the A and B bit strings are signed or unsigned.

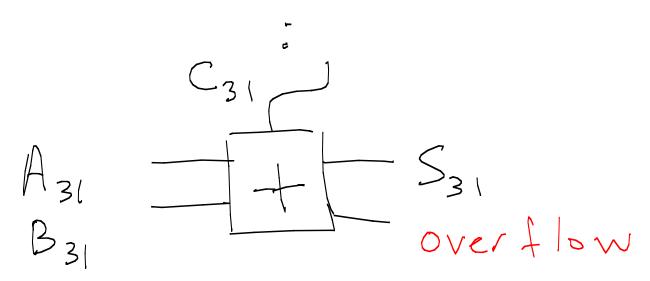
However, the full adder circuit does not depend on whether A and B are signed or unsigned.

Overflow

We still might want to know if we have "overflowed":

- e.g. if the sum of two positive numbers yields a negative
- if the sum of two negative numbers yields a positive Assignment Project Exam Help How can we detect these two cases ? (see Exercises 2) https://powcoder.com

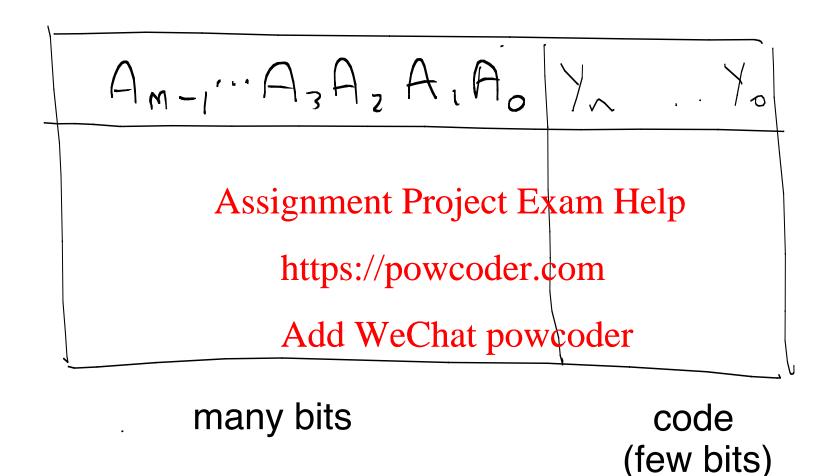
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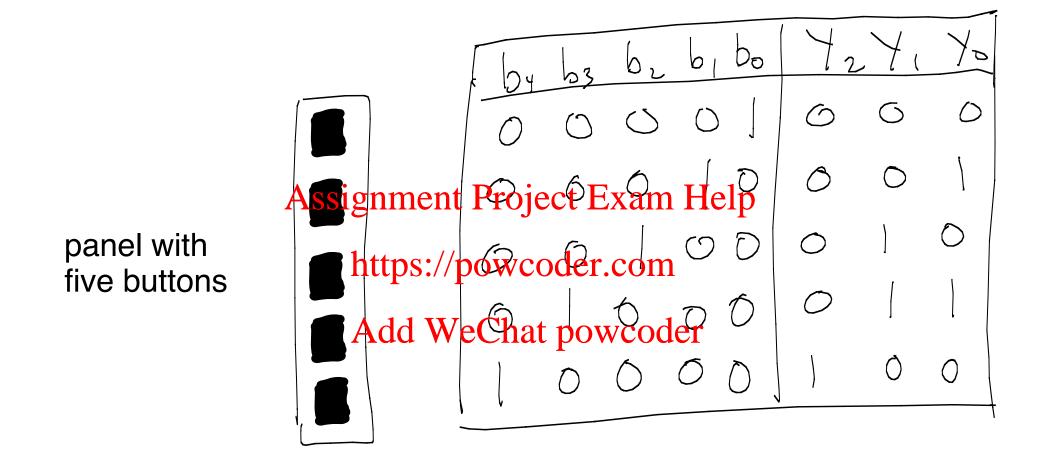
TODO TODAY

- encoder
- decoder
- n-bit multiplexornment Project Exam Help
- fast adder https://powcoder.com
- ALU Add WeChat powcoder

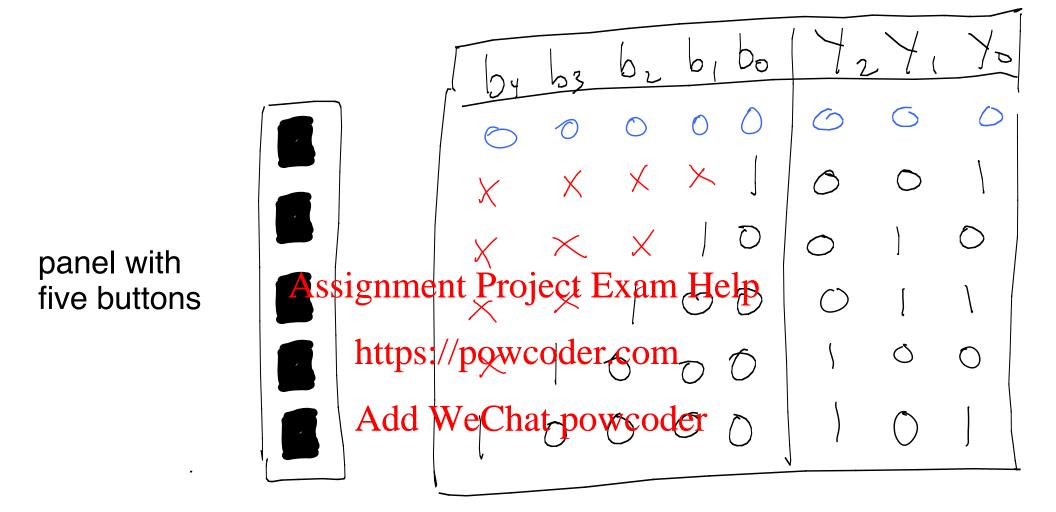
Encoder



Encoder Example 1



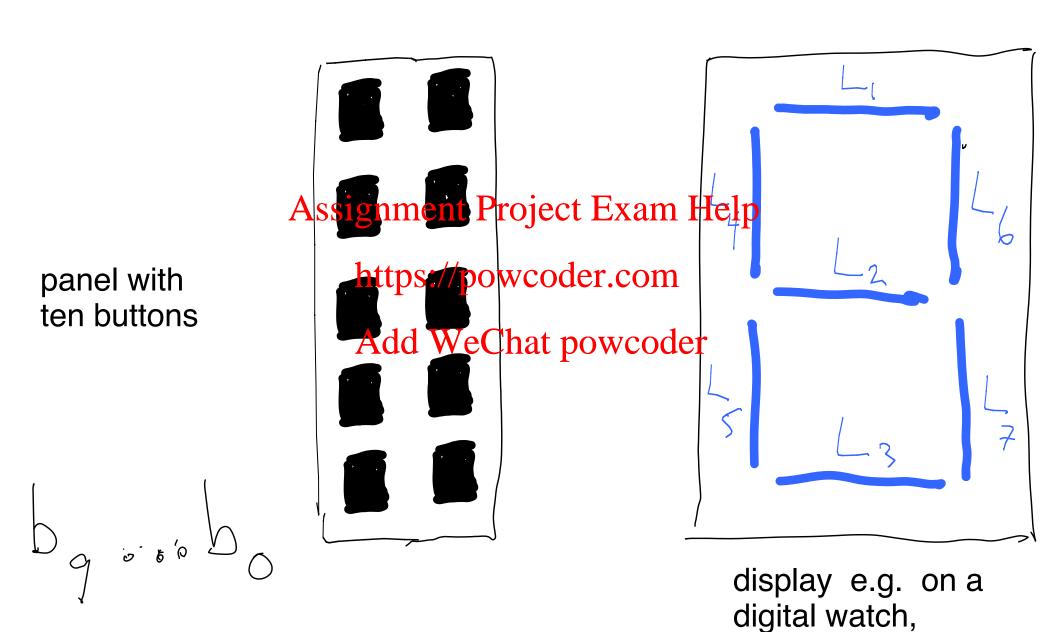
This assumes only one button can be pressed at any time.



This allows two buttons to be pressed at the same time (and encodes the one with the highest index).

lowest

Encoder Example 2



calculator, etc.

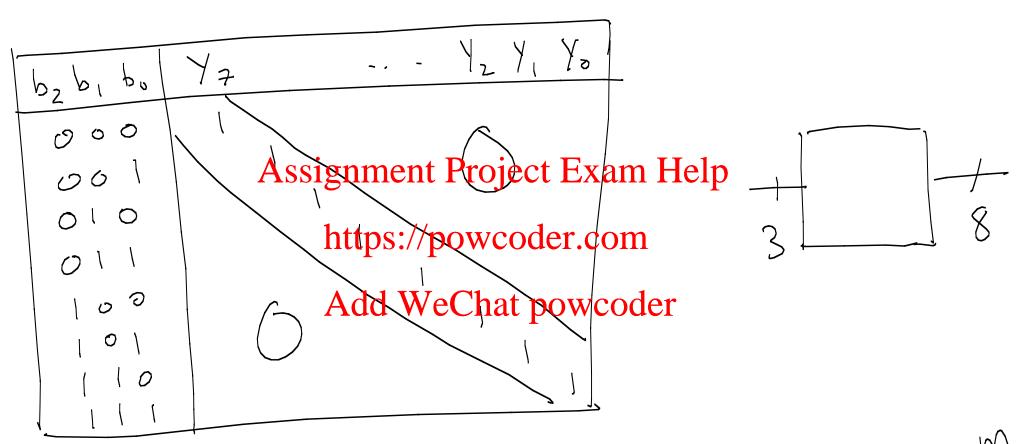
lights buttons Assignment Project Exam Help https://powcoder.com
xercises

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Each light Li is turned on (1) by some set of button presses.

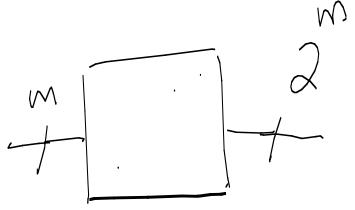
Each button bk turns on (1) some set of lights.

Decoder

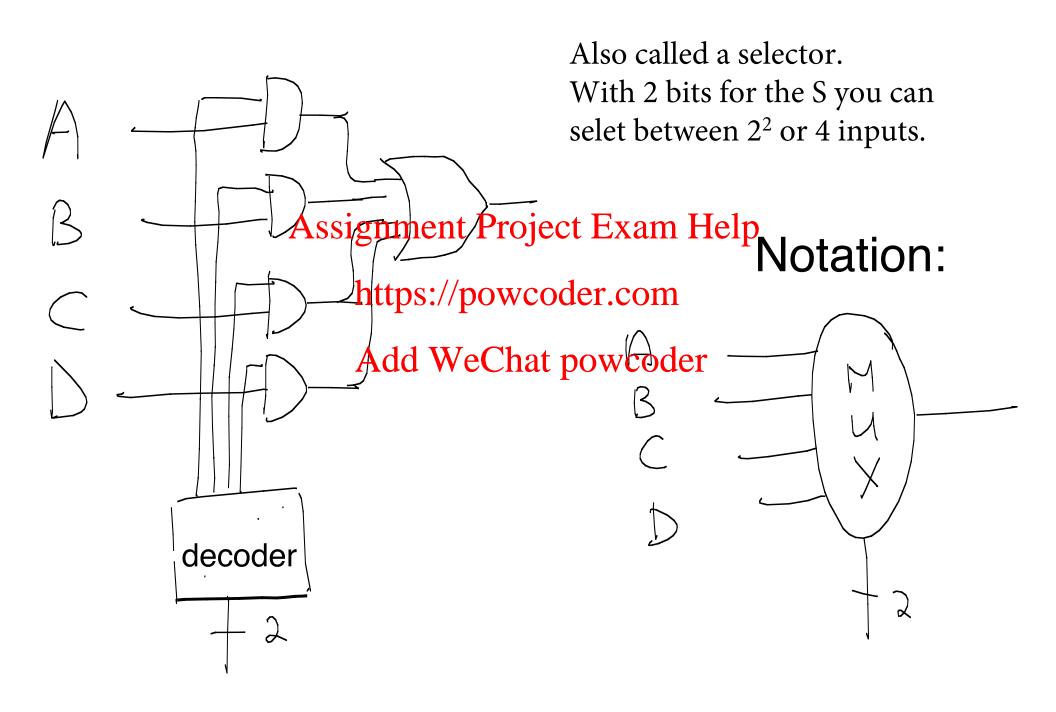


code word (in this

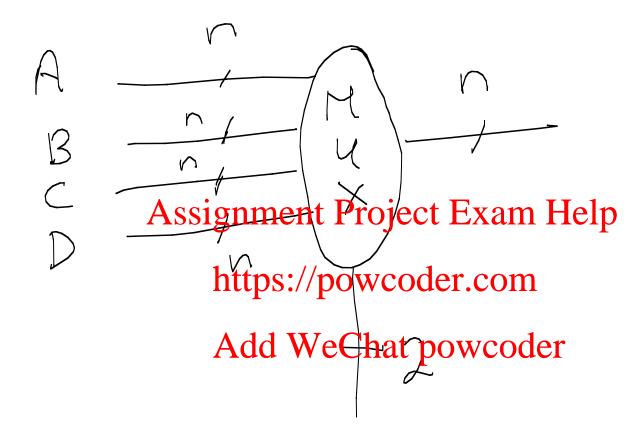
example, it specifies which output is 1)



2-bit multiplexor

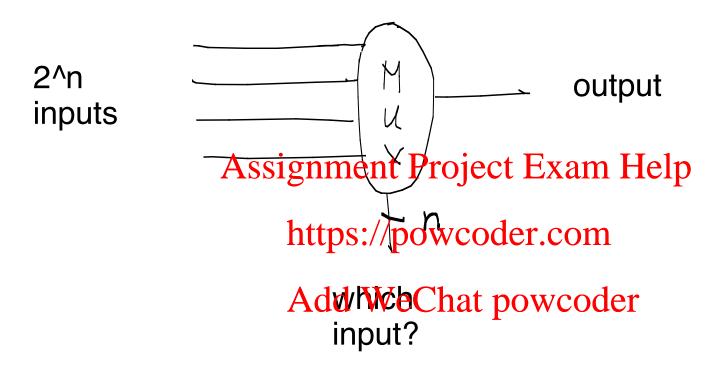


More general example (2-bit multiplexor)



Selects from four n-bit inputs. For each Ai, Bi, Ci, Di, we replicate the circuit on the previous slide, but use the same decoder circuit.

n-bit multiplexor



We will next look at some examples of how multiplexors are used.

Recall the ripple adder.

The main problem is that it is slow.

$$A_0$$
 A_1
 A_1

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https://powcoder.com32 —

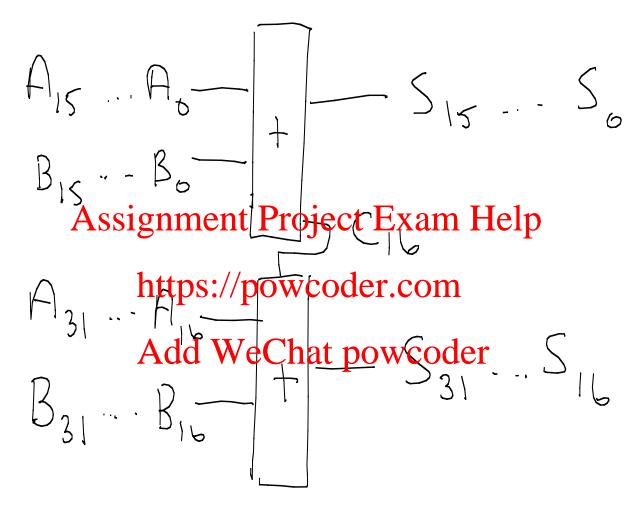
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B

Compared to the service of the service of

$$\begin{array}{c|c}
C_{31} \\
A_{31} \\
B_{31}
\end{array}$$

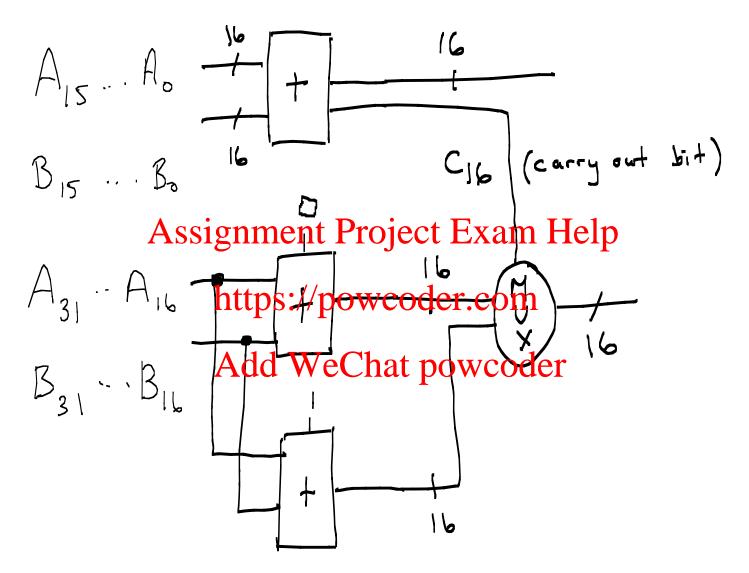
How to speed up the adder?



Instead of one 32 bit adder, think of two 16 bit adders.

We can compute the result of each, in half the time. (However, if C16 = 1, then we have to wait for it to ripple through.)

Fast Adder

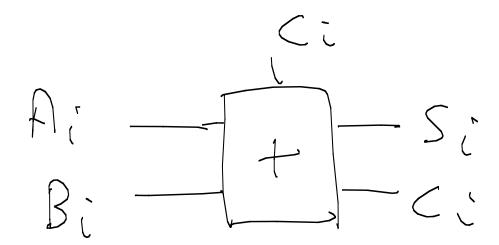


Tradeoffs: we chop the time in half (almost, why?) but it increases the number of gates by more than 50% (why?). Note we can repeat this idea (recursion).

Subtraction

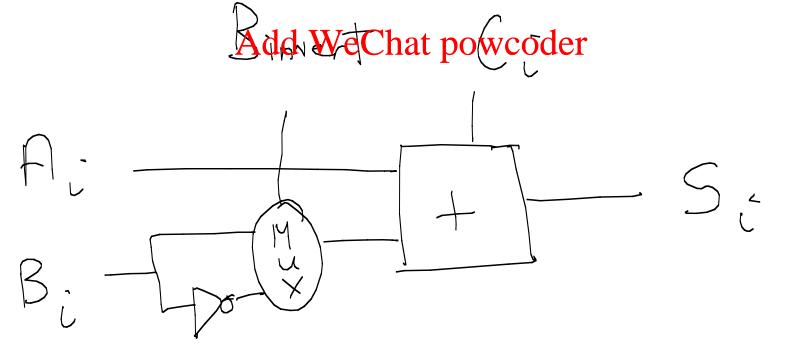
$$y = x + (-y)$$

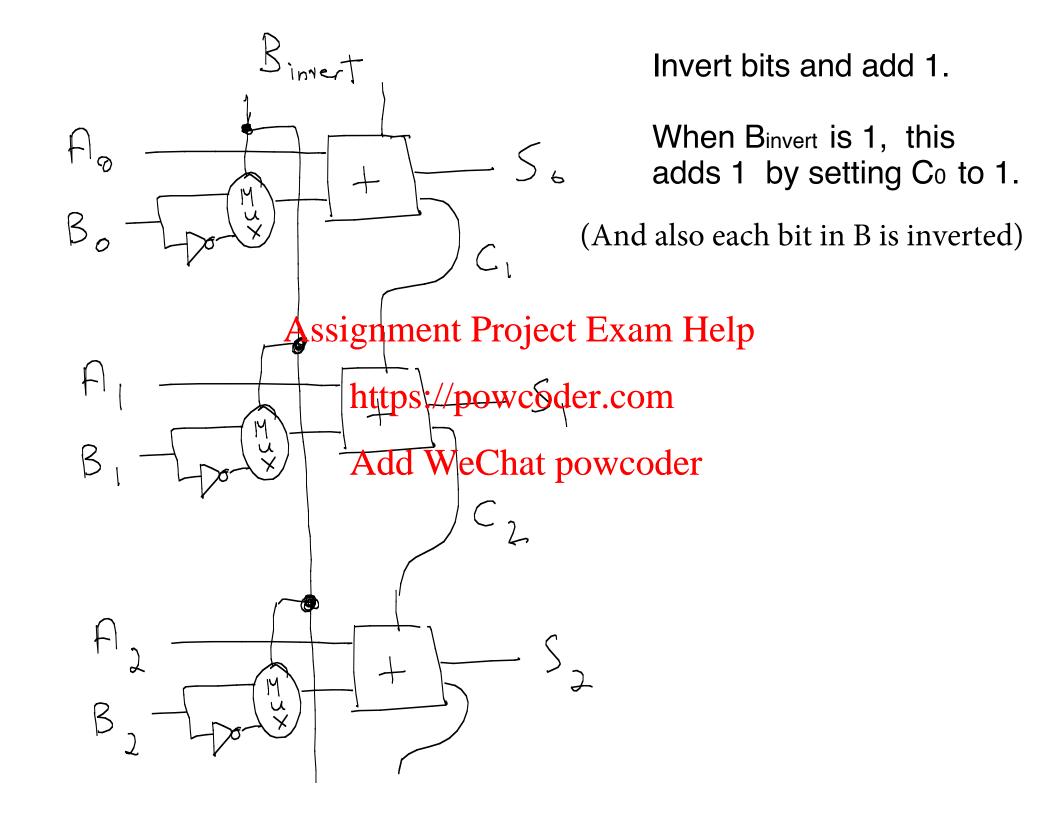
Invert bits and add 1.

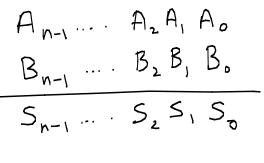


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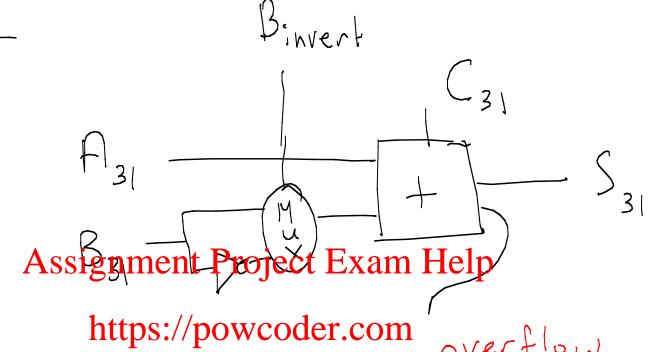
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n = 32

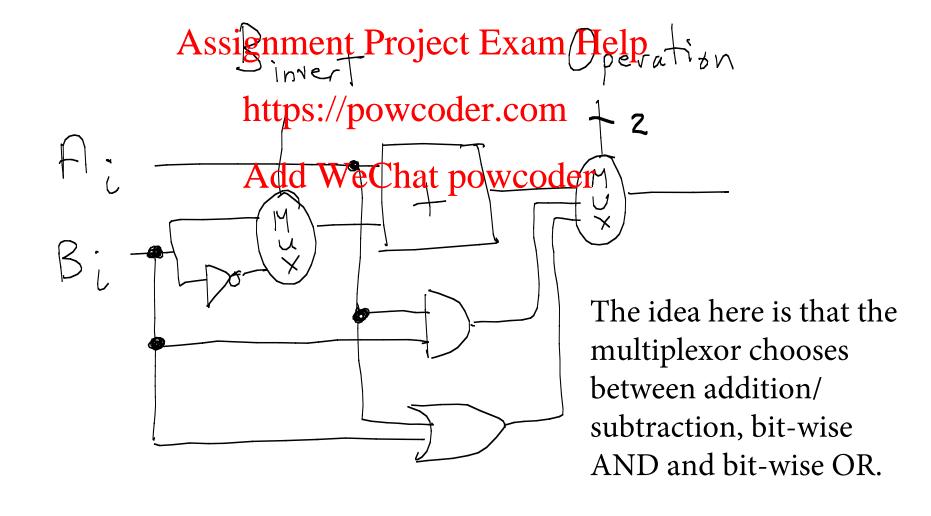


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Binsert	A ₃₁	B ₃₁	531	overflow	 -
D West),
				V	

See Exercises 2

Let's include a bitwise AND and OR.



Arithmetic Logic Unit (ALU)

