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Formal Languages – A Reminder of Terminology

- The alphabet or vocabulary of a formal language is a set of tokens ssignment Project Exam Help • A string over Σ is a sequence of tokens, or the null-string ϵ .
 - ightharpoonup sequence may be empty, giving empty string ϵ

 - A language with alphabet Ws Some Set of Strings over \(\Strings \).
 - ▶ For example, the set of all strings Σ^*
 - ▶ or the set of all strings of even length, $\{w \in \Sigma^* \mid w \text{ has even length}\}$

Notation Add WeChat powcoder

- Σ^* is the set of all strings over Σ .
- Therefore, every language with alphabet Σ is some subset of Σ^* .

Specifying Languages

Languages can be given . . .

- as a finite enumeration, e.g. $L = \{\epsilon, a, ab, abb\}$ ASSISTMENT TREEST COLORS (WEXAM) From p alphabet Σ
 - algebraically by regular expressions, e.g. L = L(r) for regexp r
 - by a httpps://spowcodef.com
 by a grammar (this lecture)

languages

- a concepted have chait lippoist code returned
 - describes how strings are constructed rather than how membership can be checked (e.g. by an automaton)
 - the main tool to describe syntax.

Grammars in general

Formal Definition. A grammar is a quadruple $\langle V_t, V_n, S, P \rangle$ where ASSISPINE TO THE PROPERTY OF A V is a finite set of non-terminal symbols disjoint from V_t

- V_n is a finite set of **non-terminal symbols** disjoint from V_t (Notation: $V = V_t \cup V_n$)
- S is notetingustical in the state of the s
- P is a set of productions, written

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- $\alpha \in V^*V_nV^*$ (i.e. at least one non-terminal in α)
- ▶ $\beta \in V^*$ (i.e. β is any list of symbols)

Example

The grammar

$$\begin{array}{l} \textbf{\textit{G}} = \langle \{\textbf{\textit{a}},\textbf{\textit{b}}\},\ \{\textbf{\textit{S}},\textbf{\textit{A}}\},\ \textbf{\textit{S}},\ \{\textbf{\textit{S}}\rightarrow\textbf{\textit{a}}\textbf{\textit{Ab}},\ \textbf{\textit{a}}\textbf{\textit{A}}\rightarrow\textbf{\textit{a}}\textbf{\textit{a}}\textbf{\textit{Ab}},\ \textbf{\textit{A}}\rightarrow\boldsymbol{\textit{\epsilon}}\}\rangle \\ \textbf{\textbf{Assignment}} \\ \textbf{\textbf{Project Exam Help}} \\ \end{array}$$

• Terminals: {a, b}

- Productions:
- Non-terminals: {\$,A} Stantynos \$ / powcoder €014

- Often, Add list the crodulate, powered ens can be inferred (S is the standard notation for the start symbol)
 - The notation $\alpha \to \beta_1 \mid \cdots \mid \beta_n$ abbreviates the set of productions

$$\alpha \to \beta_1, \quad \alpha \to \beta_2, \quad \dots, \quad \alpha \to \beta_n$$

(like for inductive data types)



Derivations

Intuition.

• A production $\alpha \to \beta$ tells you what you can "make" if you have α :

Assignment Porojectitexam Help • Notation: $\gamma \alpha \rho \Rightarrow \gamma \beta \rho$

Derivations.

- $\alpha \Rightarrow \text{http:gn-be/reprotected energy}$ so \Rightarrow^* is the reflexive transitive closure of \Rightarrow

Language of a grammar.

- informally all strings of terminal symbols that can be generated from the start symbol WECNAL DOWCOUEL
- formally: $L(G) = \{ w \in V_t^* \mid S \Rightarrow^* w \}$

Sentential Forms of a grammar.

- informally: all strings (may contain non-terminals) that can be generated from S
- formally: $S(G) = \{ w \in V^* \mid S \Rightarrow^* w \}$.

Example

Productions of the grammar *G*.

 $S \Rightarrow aAb \Rightarrow aaAbb \Rightarrow aaaAbbb \Rightarrow aaabbb$

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last string baabbb is psentence, others are sentential forms

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Alternative Grammar for the same language

$$S \rightarrow aSb$$
, $S \rightarrow ab$.

(Grammars and languages are not in 1-1 correspondence), and anguages are not in 1-1 correspondence

The Chomsky Hierarchy

By Noam Chomsky (a linguist!), according to the form of productions:

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Unrestricted: (type 0) no constraints.

Context-sensitive: (type 1) the length of the left hand side of each

 $\begin{array}{c} http: \begin{subarray}{c} production must not exceed the length of the right (with one production) powcoder.com \end{subarray}$

Context-free: (type 2) the left of each production must be a *single* non-terminal.

Regular (1/6 3) Wf To the 2 at the graph of the fine is also constrained (details to come).

(There are lots of intermediate types, too.)

Classification of Languages

Definition. A language is $type \ n$ if it can be generated by a type n

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• Every language of type n + 1 is also of type n.

Establishing the Stock of the Company of the Compan

- \bullet give a grammar of type n that generates the language
- usually the easier task eChat powcoder

 Disproving that a language is of type n
 - must show that *no* type *n*-grammar generates the language
 - usually a difficult problem

Example — language $\{a^nb^n \mid n \in \mathbb{N}, n \geq 1\}$

Different grammars for this language

• Unrestricted (type 0):

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 $\underset{\bullet \ \textit{Context-free (type 2)}.}{\textbf{https://powcoder.com}}$

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Recall. We know from last week that there is no DFA accepting L

- We will see that this means that there's no regular grammar
- so the language is context-free, but not regular.

Regular (Type 3) Grammars

Definition. A grammar is *regular* if all its productions are either *right-linear*, i.e. of the form

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or left-linear, i.e. of the form

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- $\begin{array}{c} \bullet \text{ right and left linear grammars are equivalent: they generate the same} \\ \text{language} \\ \end{array}$
- we focus on right linear (for no deep reason)
- i.e. one symbol is generated at a time (cf. DFA/NFA!)
- ullet termination with terminal symbols or ϵ

Next Goal. Regular Grammars generate precisely all regular languages.

Regular Languages - Many Views

Theorem. Let L be a language. Then the following are equivalent:

• *L* is the language generated by a *right-linear grammar*;

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- L is the language accepted by some NFA;
- · L is hettps: //powcoders:com

So far.

- have seen that NFAsyand PFAs generate the same languages (subset construction) Wechat powcoder
- have hinted at regular expressions and NFAs generate the same languages

Goal. Show that NFAs and right-linear grammars generate the same languages.

From NFAs to Right-linear Grammars

Given. Take an NFA $A = (\Sigma, S, s_0, F, R)$.

alphabet, state set, initial state, final states, transition relation

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- terminal symbols are elements of the alphabet Σ ;
- non-terminal symbols are the states S; start DEDSite stpowy COder.com
- productions are constructed as follows:

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Each final state

gives production

$$T \in F \qquad T \to c$$
 (Formally, a transition $T \stackrel{a}{\longrightarrow} U$ means $(T, a, U) \in R$.)

Observation. The grammar so generated is right-linear, and hence regular,

NFAs to Right-linear Grammars - Example

Given. A non-deterministic automaton

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Exercise. Convince yourself that the NFA accepts precisely the words that the grammar generates.

From Right-linear Grammars to NFAs

Given. Right-linear grammar (V_t, V_n, S, P)

terminals, non-terminals, start symbol, productions

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- alphabet is the terminal symbols V_t ;
- states are the non-terminal symbols V_n together with new state S_f (for https://powcoder.com
- start state is the start symbol S;
- final states are S_f and all non-terminals T such that there exists a production of the constructed as follows:

Each production

gives transition

$$T \rightarrow aU$$

$$T \stackrel{a}{\longrightarrow} U$$

Each transition

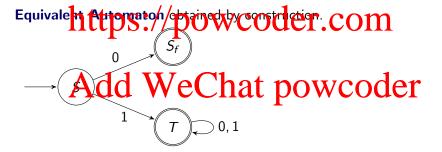
gives transition

Right-linear Grammars to NFAs - Example

Given. Grammar *G* with the productions

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(generates binary strings without leading zeros)



Exercise. Convince yourself that the NFA accepts precisely the words that the grammar generates.

Context-Free (Type 2) Grammars (CFGs)

Recall. A grammar is type-2 or context free if all productions have the Assignment Project Exam Help

where $A \in V_n$ is a non-terminal, and $\omega \in V^*$ is an (arbitrary) string.

- left side is non-terminal
- right htetp Sein powcoder.com
- independent of context, replace LHS with RHS.

In Contrast. Conjext Serisitive glammars may have productions $\alpha A\beta \to \alpha \omega \beta$

• may only replace A by ω if A appears in context $\alpha_-\beta$

Example

Goal. Design a CFG for the language

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L = {
$$a^m b^n c^{m-n} \mid m \ge n \ge 0$$
}

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$$\omega = a^{m-n} \mid a^n b^n \mid c^{m-n}$$

and henchttps.b//powcoder.com

- convenient to not have comparison between n and m
- generate $a^k \dots c^k$, i.e. same number of leading as and trailing c^s
- fill . . Ain the middle by a by i.e. same number of as and bs
 use different non-terminals for both phases of the construction

Resulting Grammar. (productions only)

$$S \rightarrow aSc \mid T$$

 $T \rightarrow aTb \mid \epsilon$

Example ctd.

Grammar

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Example ntypis: //powcoder.com

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 \Rightarrow aaTbc

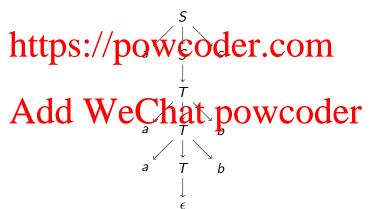
 \Rightarrow aaaTbbc

 \Rightarrow aaabbc

Parse Trees

Idea. Represent derivation as tree rather than as list of rule applications

- describes where and how productions have been applied
- As generated word can be effected at the leaves xam Help



The Power of Context-Free Grammars

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A fun example: http://pd.tips://powicoder.com

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Parse Trees Carry Semantics

Take the code

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where e1, e2 are boolean expressions and s1, s2 are subprograms.

```
Two Readings PS://powcoder.com
if e1 then (if e2 then s1 else s2)
```

and Add WeChat powcoder

```
if e1 then ( if e2 then s1 ) else s2
```

Goal. unambiguous interpretation of the code leading to determined and clear program execution.

Ambiguity

Assignment Project Exam Help Recall that we can present CFG derivations as parse trees.

Until now this was mere pretty presentation; now it will become important.

A contexhttps://powncigaterrecommean be derived by at most one parse tree.

G is **ambiguous** iff there exists any word $w \in L(G)$ derivable by more than one Argure's. We Chat powcoder

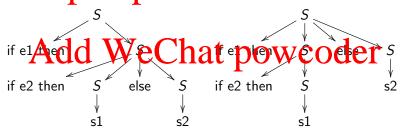
Example: If-Then and If-Then-Else

Consider the CFG

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where **bexp** and **prog** stand for boolean expressions and (if-statement free) programs respectively, defined elsewhere.

The strinhttphen if pho weed cheresevorare trees:



Example: If-Then and If-Then-Else

Assignment Project Exam Help That grammar was ambiguous. But Jere's a grammar accepting the exact same language that is unambiguous:

 $\frac{\text{https://powecoder.com}}{T \rightarrow \text{ir bexp then } T \text{ else } S \mid \text{prog} }$

There is now only one parse for if e1 then if e2 then s1 else s2. This is given on the next see that powcoder

Example: If-Then and If-Then-Else

Assignment Project Exam Help https://powcoder.com if e2 then Add WeChat powcoder

You cannot parse this string as if e1 then (if e2 then s1) else s2.

Reflecting on This Example

Observation.

• more than one grammar for a language

Assing manbiguous tot Project Exam Help

Grammars for Programs.

- ambattps://doppowcoccericom
- replace ambiguous grammar with unambiguous one

Choices for converting where the converting to t

- decide on just one parse tree
- e.g. if e1 then (if e2 then s1) else s2 vs if e1 then (if e2 then s1 else s2)
- in example: we have *chosen* if e1 then (if e2 then s1 else s2)

What Ambiguity Isn't

Question. Is the grammar with the following production ambiguous?

Assignment Project Exam Help Reasoning.

- Suppose that the above production was used
- · we https://powcoder.com

A. This is *not* ambiguity.

- both Aptions ive vs. to the large parse tree worder
 indeed, for context-free languages it doesn't matter what production
- indeed, for context-free languages it doesn't matter what production is applied first.
- thinking about parse trees, both expansions happen in parallel.

Inherently Ambiguous Languages

Q. Can we always remove ambiguity?

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Q. Why is this context free?

A. Note that $L = \{a^i b^j c^k\} \cup \{a^i b^j c^j\}$

- idea htttps: produpio wtcodetwecomon
- $S \to T \mid \overline{W}$ where T is "left" and W is "right"

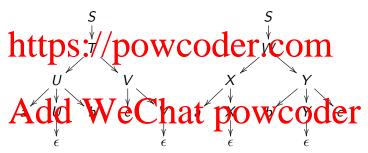
Complete Grand ar We Chat powcoder

```
egin{array}{llll} T & 
ightarrow & UV & W 
ightarrow & XY \ U 
ightarrow & aUb \mid \epsilon & X 
ightarrow & aX \mid \epsilon \ V 
ightarrow & cV \mid \epsilon & Y 
ightarrow & bYc \mid \epsilon \end{array}
```

Inherently Ambiguous Languages

Problem. Both left part $a^ib^ic^k$ and right part $a^ib^jc^j$ has non-empty intersection: $a^ib^ic^i$

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Fact. There is *no* unambiguous grammar for this language (we don't prove this)

The Bad News

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Q. Can we even determine whether an unambiguous grammar exists?

A. If we hterpret "compute" and "determine" as "by means of a program", then possible to the computer and "determine" as "by means of a

- There is no program that solves this problem for all grammars
- input: CFG G, output: appliquous or not. This problem is undecided Wechat powcoder

(More undecidable problems next week!)

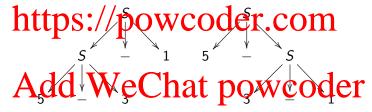
Example: Subtraction

Example.

$$S \rightarrow S - S \mid \text{int}$$

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Ambiguity.



Evaluation.

- left parse tree evaluates to 1
- right parse tree evaluates to 3
- so ambiguity matters!

Technique 1: Associativity

Idea for ambiguity induced by binary operator (think: -)

- ullet prescribe "implicit parentheses", e.g. $a-b-c\equiv (a-b)-c$
- Assignment Project Exam Help

$$S \rightarrow S - int \mid int$$

Result. https://powcoder.com

- 5 3 1 can only be read as (5 3) 1
- this is *left associativity*

Right Association. We Chat powcoder

$$S \rightarrow \text{int} - S \mid \text{int}$$

Idea. Break the symmetry

- one side of operator forced to lower level
- here: force right hand side of i to lower level \bigcirc

Example: Multiplication and Addition

Example. Grammar for addition and multiplication

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Ambiguity.

- also 1 + 2 + 3 is ambiguous but this doesn't matter here.

Take 1. The tick we have just seen at powcoder strictly evaluate from left to right

- but this gives $1+2*3 \equiv (1+2)*3$, not intended!
- **Goal.** Want * to have *higher precedence* than +

Technique 2: Precedence

Example Grammar giving * higher precedence:

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Given e.g. 1 + 2 * 3 or 2 * 3 + 1

- force the part / is otwooder.com so + will be last operation evaluated

- suppose Wetart Whee That in OWCOder
 - stuck, as cannot generate 1+2 from \overline{T}

Idea. Forcing operation with *higher* priority to *lower* level

- three levels: S, (highest), T (middle) and integers
- lowest-priority operation generated by highest-level nonterminal

Example: Basic Arithmetic

Repeated use of + and *: Assignment Project Exam Help $T \rightarrow T * U \mid T/U \mid U$ https://powcoder.com

Main Differences.

- have parentheses to break operator priorities, e.g. (1+3) * 3
 parentheses at lowest ever, so highest priority COGET
- lower-priority operator can be inside parentheses
- expressions of arbitrary complexity (no nesting in previous examples)

Example: Balanced Brackets

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- associativity Seete backty work of Green Conserve)
 - ... two ways of generating (): $S \Rightarrow SS \Rightarrow S \Rightarrow (S) \Rightarrow ()$

Technique 3: Controlling ϵ

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- ϵ can only be derived from ξ all order derived from at powered power derived from a power derived from ϵ
- here: combined with multiple level technique
- ambiguity with ϵ can be easy to miss!

From Grammars to Automata

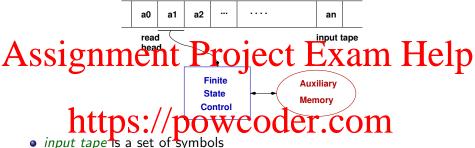
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• regular languages correspond to regular grammars. https://powcoder.com

Q. What automata correspond to context free grammars?

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General Structure of Automata

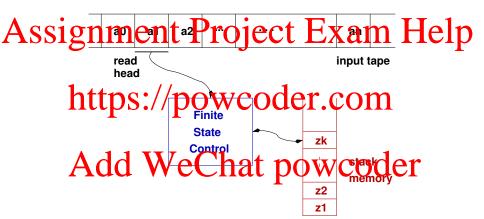


- finite state control is just like for DFAs / NFAs
- symbols are processed and head advances owcoder
 new aspect: auxiliary memory advances

Auxiliary Memory classifies languages and grammars

- no auxiliary memory: NFAs / DFAs: regular languages
- stack: push-down automata : context free languages
- unbounded tape: Turing machines: all languages

Push-down Automata — PDAs



PDAs ctd.

Actions of a push-down automaton

change of internal state

Assimption or popping the tack oject Exam Help

Action dependencies. Actions generally depend on

- current state (of finite state control)
 inpunyable S://powcoder.com
- symbol at the top of the stack

- input strong full wear Chat powcoder
 - machine is in accepting state
 - stack is empty

Variations.

- acceptance with empty stack: input fully read, stack empty
- acceptance with final state: input fully read, machine in final state

Example

Language (that cannot be recognised by a DFA)

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- cannot be recognised by a DFA
- · can https://powfeeder.com
- can be recognised by a PDA

• phase 1: (state S₁) push a s from the input onto the stack

- phase 2: (state S_2) pop a's from the stack, if there is a b on input
- finalise: if the stack is empty and the input is exhausted in the final state (S_3) , accept the string.

Deterministic PDA - Definition

Definition. A deterministic PDA has the form $(S, s_0, F, \Sigma, \Gamma, Z, \delta)$, where Assignates Project steams Fig. 19

- Σ is the *alphabet*, or set of *input symbols*;
- Γ is hetsetyofstadk/sphontane od ene circlinack symbol;
- δ is a (partial) transition function

$$\delta: \mathbf{Addu} \overset{\mathcal{S}}{\text{Ne}} \overset{\mathcal{S}}{\text{Chartanow}} \overset{\mathcal{S}}{\text{Chartanow}} \overset{\mathcal{S}}{\text{Ne}} \overset{\mathcal{S}}{\text{Chartanow}} \overset{\mathcal{S}} \overset{\mathcal{S}}{\text{Chartanow}} \overset{\mathcal{S}}{\text{Chartanow}} \overset{\mathcal{S}}{\text{Chart$$

Additional Requirement to ensure determinism:

- if $\delta(s, \epsilon, \gamma)$ is defined, then $\delta(s, a, \gamma)$ is undefined for all $a \in \Sigma$
- ensures that automaton has at most one execution

Notation

Given. Deterministic PDA with transition function

Notation ttps://powcoder.com

- \bullet $\,\sigma$ is a $\it string$ that replaces top stack symbol
- * final states are unusually underlined (s) powcoder

Rationale.

- replacing top stack symbol gives just one operation for push and pop
- pop: $\delta(s, a, \gamma) = s'/\epsilon$
- push: $\delta(s, a, \gamma) = s'/w\gamma$

Two types of PDA transition

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- ullet automaton reads symbol x
- symlattips://powcoder.com

Non-consuming transitions

- δ contains (s_1, ϵ, s_2) independent of injury sembol hat powcoder
- can happen any time and does not consume input symbol

Example ctd.

```
Language L = \{a^n b^n \mid n \ge 1\}
```

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- ullet starts with Z (initial stack symbol) on stack
- final state is S_3 (underlined)
- transattps://powcoder.com

(δ is partial, i.e. undefined for many arguments)

Example ctd. - Diagrammatically

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Example ctd. — PDA Trace

PDA configurations

• triples: (state, remaining input, stack)

Assignment Project Exam Help Example Execution.

https://power.com(push first a)
$$\Rightarrow (S_1, abbb, aaZ) \qquad \text{(push further a's)}$$

$$\Rightarrow (S_1, bbb, aaaZ) \qquad \text{(push further a's)}$$

$$Add We (Shbb aaZ) \qquad \text{(push further a's)}$$

$$\Rightarrow (S_2, b, aZ) \qquad \text{(pop further a's)}$$

$$\Rightarrow (S_2, \epsilon, Z) \qquad \text{(pop further a's)}$$

$$\Rightarrow (S_3, \epsilon, \epsilon) \qquad \text{(accept)}$$

Accepting execution. Ends in final state, input exhausted, empty stack, 48/59

Example ctd. — Rejection

Assignment Project Exam Help $(S_0, aaba, Z) \Rightarrow (S_1, aba, aZ)$ \Rightarrow (S_1, ba, aaZ)

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- Non-accepting execution.

 No transition possible, ettick Mtalit reaching that et
 - rejection happens when transition function is undefined for current configuration (state, input, top of stack)

Example: Palindromes with 'Centre Mark'

Example Language.

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Deterministic PDA that accepts *L*

- Push the bis onto the stack covered the one when we see c, change state;
- Now try to match the tokens we are reading with the tokens on top of the stack political we go hat powcoder

 If the top of the stack is the empty stack symbol 2, pop it and enter
- the final state via an ϵ -transition. Hopefully our input has been used up too!

Exercise. Define this formally!

Non-Deterministic PDAs

Deterministic PDAs

transitions are a partial function

Assignment Project Exam Help δ : (state, input token or ϵ , top-of-stack) \rightarrow (new state, stack string)

• side condition about ϵ -transitions

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• transitions given by relation

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no side condition (at all).

Main differences

- for deterministic PDA: at most one transition possible
- for non-deterministic PDA: zero or more transitions possible

Non-Deterministic PDAs ctd.

Finite Automata

• non-determinism is convenient

As sui gen't rive extrt property set cutstruction an Help

Push-down automata.

- non-https://poweoder.com
- cannot convert every non-deterministic PDA to deterministic PDA
- there are context free languages that can only be recognised by non-definition to the languages that powcoder
- intuition: non-determinism allows "guessing"

Grammar / Automata correspondence

- non-deterministic PDAs are more important
- they correspond to context-free languages

Example: Even-Length Palindromes

Palindromes of even length, without centre-marks

$$L = \{ww^R \mid w \in \{a, b\}^* \land w^R \text{ is } w \text{ reversed}\}$$

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- intuitive reason: no centre-mark, so don't know when first half of wordistads://powcoder.com

Non-deterministic PDA for L has the transition

$$\delta(s,\epsilon,\gamma) = r/x$$
 • $x \in \{AbG\}$ s in the earling the wave order state.

Intuition

- "guess" (non-deterministically) whether we need to enter "match-and-pop"-state
- automaton gets stuck if guess is not correct (no harm done)

Grammars and PDAs

Assignment, Project, Exams Help equivalent

- for every CFL L there exists a PDA that accepts L
- if L https://pow/www.cru.

Proof. We only do one direction: construct PDA from CFL.

- this is the "interesting" direction for parser generators der other direction quite complex.

From CFG to PDA

Given. Context-Free Grammar $G = (V_t, V_n, S, P)$

Construct non-deterministic PDA $A = (Q, Q_0, F, \Sigma, \Gamma, Z, \delta)$ SS1gnment Project Exam Help States. Q (initial state), Q_1 (working state) and Q_2 (final state).

Alphabet. $\Sigma = V_t$, terminal symbols of the grammar Stack Abtteps://powcoder.com

Initialisation.

Termination.

- if the stack is empty (i.e. just contains Z), terminate
- $\delta(Q_1, \epsilon, Z) \mapsto Q_2/\epsilon$

From CFGs to PDAs: working state

Idea.

- build the derivation on the stack by expanding non-terminals
- Assignifications productions are the productions of the production of the
 - terminate, if the entire input has been consumed

• non-terminals on the tack are replaced by right hand side of

- non-terminals on the stack are replaced by fight hand side of productions
- $\delta(Q_1, \epsilon, A) \mapsto Q_1/\alpha$ for all productions $A \to \alpha$ Pop Terminals. We Chat powcoder

a terminals on the stack are nonned if they match th

- terminals on the stack are popped if they match the input
- $\delta(Q_1,t,t)\mapsto Q_1/\epsilon$ for all terminals t

Result of Construction. Non-deterministic PDA

may have more than one production for a non-terminal.



Example — Derive a PDA for a CFG

Arithmetic Expressions as a grammar:

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1. Initial https://powcoder.com

$$\delta(Q_0, \epsilon, Z) \mapsto Q_1/SZ$$

2. Expan Action in We Chat powcoder

$$\delta(Q_1, \epsilon, S) \mapsto Q_1/S + T$$
 $\delta(Q_1, \epsilon, T) \mapsto Q_1/U$
 $\delta(Q_1, \epsilon, S) \mapsto Q_1/T$ $\delta(Q_1, \epsilon, U) \mapsto Q_1/(S)$
 $\delta(Q_1, \epsilon, T) \mapsto Q_1/T * U$ $\delta(Q_1, \epsilon, U) \mapsto Q_1/\inf$

CFG to PDA ctd.

4. Terminaedd WeChat powcoder

$$\delta(Q_1, \epsilon, Z) \mapsto Q_2/\epsilon$$

 $\delta(Q_1,),)) \mapsto Q_1/\epsilon$

Example Trace

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Assignment Progett Exam Help
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \Rightarrow (Q_1, int * int, T * UZ)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \Rightarrow (Q_1, \text{ int} * \text{int}, \text{ } U*UZ)
                                                                                                                                                                                                                                                  https://powcoder.ct
                                                                                                                                                                                                                                                  Add \ We \overset{\stackrel{\scriptstyle \triangleleft}{\underset{\scriptscriptstyle =}{\stackrel{\scriptscriptstyle \triangleleft}{\stackrel{\scriptscriptstyle \square}{\stackrel{\scriptscriptstyle \square}{\stackrel \square}{\stackrel{\scriptscriptstyle \square}{\stackrel{\scriptscriptstyle \square}{\stackrel{\scriptscriptstyle \square}{\stackrel \square}{\stackrel{\scriptscriptstyle \square}{\stackrel \square}{\stackrel{\scriptscriptstyle \square}{\stackrel \square}{\stackrel \scriptscriptstyle \square}{\stackrel {\stackrel \square}{\stackrel \scriptstyle {\stackrel \square}{\stackrel \scriptstyle \square}{\stackrel \scriptscriptstyle \square}{\stackrel }{\stackrel \scriptscriptstyle \square}{\stackrel \scriptscriptstyle \square}}}}}}}}}}}}}}}}}}}}}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         accept
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