### COMP2022: Formal Languages and Logic

# Assignment Project Exam Help

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### https://powcoder.com

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#### OUTLINE

# Assignment Project Exam Help

- Concepts (Operators, FV, Reductions)
- ► Recursion (fixed point, using it)

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- ► Functional Programming
- ► Automata Theory

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- ► Regular languages
- ► NFA

### **OPERATORS**

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Notation: (A ⋅ B)
 Expression B is applied to expression A

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### **OPERATORS**

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- Expression B is applied to expression A
- ► Abstraction

### Add Wis abstracted at powcoder

Right associative:  $(\lambda abcdef.M) = (\lambda a.(\lambda b.(\lambda c.(\lambda d.(\lambda e.(\lambda f.M))))))$ 

#### Free Variables

# Assignmente Pribojectpresixamed Help inductively like this:

https://powcoder(weensan atom)
$$FV(MN) = FV(M) \cup FV(N) \qquad (M, N \text{ are expressions})$$

$$FV(\lambda x. M) = FV(M) - \{x\}$$
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Any variable in an expression that is not free, is bound.

### REWRITING

- Add We Chat powcoder
  - $(xyz\lambda x.(zxz))[y := B] \equiv (xBz\lambda x.(zxz))$
  - $(xyz\lambda x.(zxz))[z := C] \equiv (xyC\lambda x.(CxC))$

#### $\alpha$ -REDUCTION

- https://powcoder.com
- ► VALUE a We able that powcoder

  ► Do not choose a symbol that is already in the expression

  - $\blacktriangleright$  It's usually easiest to start with the innermost  $\lambda$

### $\beta$ -REDUCTION

- Preduces an application into an abstraction nttps://powcoder.com
- Note: the free occurrences of x in M are exactly the set of our details with a constant the constant of t
- ightharpoonup Do lpha-reductions first if necessary

#### $\eta$ -REDUCTION

# Assignment Project Exam Help If x is not free in M (i.e. $x \notin FV(M)$ ), then we can write:

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#### Naming

- $\blacktriangleright$  If more than one  $\lambda$  uses the same label
- https://plewithordern!com

- To fix them:

  Application of the property of t
  - ► Always rename to a label not already in use
  - $\blacktriangleright$  Work from the innermost  $\lambda$  to the outermost one

### FIXED POINT COMBINATORS

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we shttps://powcoder.com

i.e. some input X exists which, when applied to Contact again.

#### FIXED POINT THEOREM

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### 2. https://poweoder.com

$$\forall F \ F(YF) = YF$$

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- $\blacktriangleright$  i.e. for any function F, YF is a fixed point of F.
- ► Proven last week
- ► Very useful for recursion

#### RECURSION

Recursive functions often look like this:

# Assignment Project Exam Help $F = (\lambda xyz. (\text{condition}) (\text{base case}) (\text{recursive case calls } F))$

If we heed more castes, we can just add thore logic We can't directly refer to the function F within itself

We can define it like this instead:

# Add WeChat powcoder $H = (\lambda fxyz.(\text{condition})(\text{base case})(\text{recursive case calls } f))$

F = Y H

# $H = (\lambda fxyz. (\text{condition}) (\text{base case}) (\text{recursive case calls } f))$ $Assignment\ Project\ Exam\ Help$

Evaluation: NTLPS://powcoder.com

$$F \ a \ b \ c = (Y \ H) \ a \ b \ c$$
 $= H \ (Y \ H) \ a \ b \ c$ 
 $= H \ (Y \ H) \ a \ b \ c$ 
 $= (Xyz.(condition)(base)(call(s) \ to \ (Y \ H))) \ a \ b \ c$ 

Notice that we managed to call (Y H) = F from within F

recursion!

#### REDUCING THE Y COMBINATOR.

# Assignment Project Exam Help We don't need to reduce (Y H) directly

- $\blacktriangleright$  In the recursive calls, it expands to H (Y H), then we reduce The (1 H) will disappear when we reach the base cases

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### EXAMPLE: LAST WEEK'S TUTORIAL QUESTIONS

We wanted a function that would build a list  $\{x_1...x_n\}$  from an

# szigniment<sup>n</sup> Project Exam Help

- $\triangleright$  Recurse *n* times
- Fach recursion consumes up one argument
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# HAdd 15We Chat (powerer

▶ Prepend the next argument to the list with (CONSet), and recursively call f list (n-1) with the remaining arguments

### EXAMPLE: LAST WEEK'S TUTORIAL QUESTIONS

```
= H (Y H) NIL 3 a b c
```

- $= \left( \frac{1}{1} \frac{1}{1}$
- = ... = FALSE NIL ( $\lambda e.(Y H)$  ( $CONS \ e \ NIL$ ) ( $PRED \ 3$ ))  $a \ b \ c$ = ... = Ace (Ace Ace Ace
- $= \dots = (Y \ H) \ (CONS \ a \ NIL) \ (PRED \ 3) \ b \ c$
- $= \dots = (Y H) (CONS \ a \ NIL) \ 2 \ b \ c$
- $= \ldots = (\textit{Y H}) (\textit{CONS b} (\textit{CONS a NIL})) \ 1 \ \textit{c}$
- $= \ldots = (\textit{Y H}) \; (\textit{CONS c} \; (\textit{CONS b} \; (\textit{CONS a NIL})) \; 0$
- $= \dots = (CONS \ c \ (CONS \ b \ (CONS \ a \ NIL)))$

### EXAMPLE: LAST WEEK'S TUTORIAL QUESTIONS Reversing a list:

```
= (\lambda a \underset{(a,b,a)}{\textbf{https:}} / / a \underset{(a,b,a)}{\textbf{powcoder.com}}
= Y H \{c,b,a\} NIL
=H(Y H) \{c, b, a\} NIL
= (\langle fa \text{Astd}) b \text{VTeC} (\text{Pat(HPOW)COOLET}a} \text{NIL}
= \dots = (Y \ H) \ (TAIL \{c, b, a\}) (CONS \ (HEAD \{c, b, a\}) \ NIL)
= \dots = (Y \ H) \{b, a\} (CONS \ c \ NIL)
= ... = (Y \ H) \{b, a\}\{c\}
= ... = (Y H) \{a\}\{b, c\}
= ... = (Y \ H) \ NIL\{a, b, c\}
= ... = \{a, b, c\}
                                                                                             18/63
```

#### NOTATION

# We've mostly been using the = sign everywhere. This isn't strictly personal strictly been using the = sign everywhere. This isn't strictly personal strictly

We could have used more precise notation, such as:

- https://powcoder.com
- $M \equiv N : M$  is equivalent to N (has the same effect)
- $ightharpoonup M woheadrightarrow_{\beta} N : M \beta$ -reduces to N
- ►  $M =_{\beta} N : M$  is β-convertable to N

We've avoided using these so far for the sake of simplicity

### $\beta$ -NORMAL FORM

# Assignment Project Exam Help Not all expressions have normal forms

• e.g.  $(\lambda x.xx)(\lambda x.xx)$  does not have a normal form https://powcoder.com

Normalisation Theorem: If a normal form exists, it can always be found by following the leftmost reduction

- because the leftmost reduction roops infinitely
- $\blacktriangleright$   $(\lambda ab.b)((\lambda x.xx)(\lambda x.xx))$  has a normal form,  $(\lambda b.b)$ , even though following the reduction on the right would not have found it

### $\beta$ -EQUIVALENCE

# Assignment Project Exam Help

- This doesn't necessarily mean we can β-reduce between them directly! https://powcoder.com
- ► e.g.
  - $(\lambda xy.x)ab$  and  $(\lambda xy.x)ac$  both reduce to a for fore-theyer  $\beta$ -equivalent  $(\lambda xy.x)ac$  between them:

▶ We've been using this property often, without stating it

### $\beta$ -EQUIVALENCE

# Assignment of Provident Examino Help

 $YF =_{\beta} F(YF)$ , but neither  $YF \twoheadrightarrow_{\beta} F(YF)$  nor  $F(YF) \twoheadrightarrow_{\beta} YF$ https://powcoder.com
Turing discovered another fixed point combinator

 $\Theta \equiv (\lambda xy.y(xxy))(\lambda xy.y(xxy))$ , which has the property that

<sup>OF</sup> Afdd WeChat powcoder

There are an infinite number of fixed point combinators in untyped lambda calculus!

#### CHURCH-ROSSER THEOREM

# Assignment $P_1$ reject is smanned the p

This https://wpoew.cig.6ch.tGoth.der in which we reduce the subexpressions doesn't change the result.

We do need be writtle literateful sometimes, as some parts do not lead to the normal form, although they remain  $\beta$ -equivalent to it!)

### COMPUTATIONAL POWER

Lambda calculus can compute all the computable (recursive)

# Assignment Project Exam Help

- ▶ Proof is beyond the scope of this course
- ► Key points:

### http://www.desingle.com

► Lambda Calculus is consistent (you can't prove false statements)

A frameworm (competists we can find it (Normalisation Electem)

Essentially, given any problem you can express with set theory (i.e. maths), then *if* it's possible to solve (compute) it, lambda calculus can do so.

### COMPUTATIONAL POWER

### Assignment Project Exam Help

The **furth D.S. ing** by **points who is little and** and Turing machines have the same computational power.

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The proof is relatively simple. If we have time at the end of the course, we will show you.

WHY?

# Assignmenticher object at Examinth lelp use the functional paradigm?

= is https://powcoder.com

- They day ed Water computation provey coder

  They are not the same
- Some things are *easier* with each approach

#### Positive traits of functional paradigm

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- ► Lazy evaluation
  - ► Easy to work with vast / infinite data sets
- ► Inttonshiposino had concuestino of the concuestion of the concursion of the conc
  - e.g. Map / ford / reduce templates allow us to define ways to 'crawl' over our data. Performing different transformations now just becomes arguments to these methods, instead of

### And when hat powcoder

- ► Inherent immutability
  - Our functions define relationships between the existing structure and the one we want
  - ► Notions like undo/redo become almost trivial

### HYBRID LANGUAGES

# Assignment Project Exam Help NOT an either/or choice.

### https://powcoder.com

Most languages blend imperative and functional paradigms:

\* A dad C Python hat powcoder

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- ► Regular languages
- ► NFA

#### ALAN TURING

Assignment Project Example Help
philosopher, code breaker, visionary

- Created abstract machines called *Turing*Power of the power of the p
  - ► Church-Turing thesis

### Add Wechat powcoder

- ► The Imitation Game
- ► Enigma code breaker

#### NOAM CHOMSKY



of classes of formal languages (applies to human language and computer theory)

# Regular (DFA) Regular (PDA) Regular (PDA) Recursively-

#### ALPHABET

# Assignment Projecty Exam Help

For elantitos://powcoder.com

- ▶ All lower case letters:  $\Sigma = \{a, b, c, ..., z\}$
- Anhaduderi WeChat powcoder
- ► Set of signals used by a protocol

#### STRING

# Assignment seure from tols roxamex melp

- ▶ The *length* of a string w, denoted |w|, is equal to the number The string of the string over the alphabet Σ

  denotes the set of all strings over the alphabet Σ
- $\triangleright$   $\varepsilon$  (epsilon) denotes the *empty string*

### Adda We Chat powcoder

- xy = the concatenation of two strings x and y
- $x^n$  the string x repeated n times

#### STRING

# Assignment seure je ot s roxamex Help

- The *length* of a string w, denoted |w|, is equal to the number of symbols in the string e.g. if x = ebcd then |x| = 4
- The string of the string over the alphabet Σ

  denotes the set of all strings over the alphabet Σ
- ightharpoonup  $\varepsilon$  (epsilon) denotes the *empty string*

### Add ab We Chat powcoder

- ightharpoonup xy =the concatenation of two strings x and y
- $ightharpoonup x^n$  the string x repeated n times

#### Powers of an Alphabet

# Assignment Project Exam Help

Let  $\Sigma$  be an alphabet, then:

- ► https://powcoder.com ►  $\Sigma^* = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \cup ...$  (i.e. all strings, including  $\varepsilon$ )
- $\blacktriangleright \ \Sigma^+ = \Sigma^1 \cup \Sigma^2 \cup \Sigma^3 \cup \dots$  (i.e. all strings except  $\varepsilon)$ Add WeChat powcoder

#### LANGUAGES

## Assignment Project Exam Help

ightharpoonup Let L be the language of all strings consisting of n 0s followed by n 1s:

## https://poweoder.com

- ► Let *L* be the language of all strings with an equal number of 0s and 1s:
- Add = Wie Coll hat 101 power of the empty language power of the empty language
  - ▶ Beware:  $\{\varepsilon\}$  is NOT  $\emptyset$

#### THE MEMBERSHIP PROBLEM

## Assignment Project Exam Help

Given a string  $w\in \Sigma^*$  and a language L over  $\Sigma,$  decide whether or not  $w\in L$ 

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Example:

Let wA 10001 WeChat powcoder

Does w belong to the language of strings with an equal number of

0s and 1s?

#### OUTLINE

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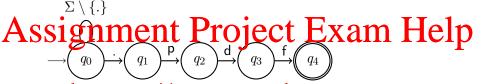
- Concepts (Operators, FV, Reductions)
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- ► Functional Programming
- ► Automata Theory

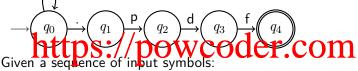
### Add Wethat powcoder

- ► Regular languages
- ► NFA



Form hypother probes clother mountin

- ▶ Information is represented by the *state* (circles)
- Tansiliod rules Varrors Hefine state changes according to imput U
- ightharpoonup Start state is denoted  $\rightarrow$
- ► Accept state(s) denoted by double circle
- lacktriangle The set of all possible input symbols is the *alphabet*,  $\Sigma$



- ► Begin in the *start* state
- Follow one transition for lack symbol in the input string
- After reading the entire input string:
  - ▶ The input is *accepted* if the automaton is in an *accept* state
  - ► The input is *rejected* if it is not

 $\Sigma \setminus \{.\}$ 

## Assignment Project Exam Help

Example input "example.pdf":

- https://poweoder.com
- $\blacktriangleright$  moves to  $q_1$  when it scans "."
- $\blacktriangleright$  then  $q_2$  for 'p',  $q_3$  for 'd',  $q_4$  for 'f'
- after all input it scanned, we ended in an accept state the education of t

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- after all input it scanned, we ended in an accept state therefore example pot is largeted OWCOGET

- ▶ .pdf
- ▶ pdf
- ► example.pd
- example.pdf.pdf

 $\Sigma \setminus \{.\}$ 

# Assignment Project Exam Help

Example input "example.pdf":

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- after all input it scanned, we ended in an accept state therefore example por is ladepted OWCOGET

- ► .pdf **Yes**
- ▶ pdf
- ► example.pd
- example.pdf.pdf

 $\Sigma \setminus \{.\}$ 

# Assignment Project Exam Help

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- after all input it scanned, we ended in an accept state therefore example pot is largeted OWCOGET

- ► .pdf **Yes**
- ▶ pdf **No**
- ► example.pd
- example.pdf.pdf

 $\Sigma \setminus \{.\}$ 

# Assignment Project Exam Help

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- after all input to scanned, we ended in an accept state the earlier example pot in a part of the earlier of the

- ► .pdf **Yes**
- ▶ pdf **No**
- example.pd No
- example.pdf.pdf

 $\Sigma \setminus \{.\}$ 

# Assignment Project Exam Help

Example input "example.pdf":

- https://poweoder.com
- $\blacktriangleright$  moves to  $q_1$  when it scans ".
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- after all input to scanned, we ended in an accept state the earlier example pot in a part of the earlier of the

- ► .pdf **Yes**
- ▶ pdf **No**
- example.pd No
- ► example.pdf.pdf No(!)

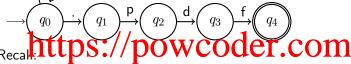
## Assignment Project Exam Help

 $\xrightarrow{q_0} \xrightarrow{p} \xrightarrow{q_2} \xrightarrow{d} \xrightarrow{q_3} \xrightarrow{f} \xrightarrow{q_4}$ Recall: 1ttps://powcoder.com

▶ Information is represented by the *state* (circles)

What information is represented by state  $q_1$ ? By  $q_2$ ? Oder

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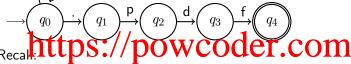


▶ Information is represented by the *state* (circles)

## What information is represented by state q1? By q2. Oder

 $ightharpoonup q_1$ : We have scanned any number of letters, followed by "."

## Assignment Project Exam Help



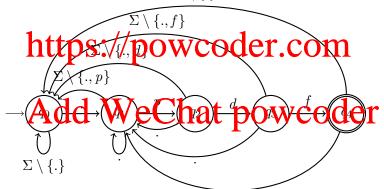
► Information is represented by the *state* (circles)

## What information is represented by state q1? By q2. Oder

- $ightharpoonup q_1$ : We have scanned any number of letters, followed by "."
- $ightharpoonup q_2$ : We have scanned any number of letters, followed by ".p"

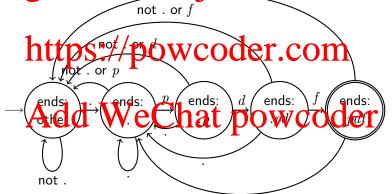
#### Our first valid DFA

A properly defined DFA will have a transition for every symbol,



#### ALTERNATIVE NOTATION

You can be more descriptive if you like:



#### DETERMINISTIC FINITE AUTOMATA (DFA)

- 1. They have a finite set of states
- 2. https://powcoder.com
  3. They have one start state
- 4. They have a behaviour given by transitions
- 5. They have accept state(s) the phase symbol from each state r

#### DETERMINISTIC FINITE AUTOMATA (DFA)

## Assignment Project Exam Help

A finite automaton is a 5-tuple  $(Q, \Sigma, \delta, q_0, F)$  where

- 1. hittpis set bled the state der.com
  2. \( \Sigma \) is a finite set colled the alphabet,
- 3.  $\delta: Q \times \Sigma \to Q$  is the transition function,
- 4. question of accept states powcoder

  5. F \( \) Q is the set of accept states powcoder

#### DRAW A DFA FROM THE DEFINITION

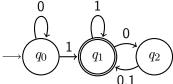
Let  $M_1 = (Q, \Sigma, \delta, q_0, F)$  where:

- 3.  $\delta: Q \times \Sigma \to Q$  is given by  $q_0 \quad q_0 \quad q_1$   $q_1 \quad q_2 \quad q_1 \quad q_2 \quad q_2$
- 4.  $q_0 \in Q$  is the start state
- Now Add www.eChat powcoder

#### Draw a DFA from the definition

Let  $M_1 = (Q, \Sigma, \delta, q_0, F)$  where:

- 3.  $\delta: Q \times \Sigma \to Q$  is given by  $q_0 q_0 q_1$   $q_1$   $q_2$   $q_2$   $q_1$   $q_2$   $q_2$   $q_1$   $q_2$   $q_1$   $q_2$   $q_2$   $q_2$   $q_2$   $q_2$   $q_1$   $q_2$   $q_2$   $q_2$   $q_1$   $q_2$   $q_2$   $q_2$   $q_1$   $q_2$   $q_2$   $q_2$   $q_2$   $q_1$   $q_2$   $q_1$   $q_2$   $q_1$   $q_2$   $q_1$   $q_2$   $q_$
- 4.  $q_0 \in Q$  is the start state
- Now And Day W: eChat powcoder



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We charped descriped wooder.com

- 2.  $\Sigma =$
- 3. Add-WeChat powcoder
- 4. The start state is:
- 5. The set of accept states is: F =



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- 2.  $\Sigma =$
- 3. Add-WeChat powcoder
- 4. The start state is:
- 5. The set of accept states is: F =



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- 2.  $\Sigma = \{0, 1\}$
- 3. Add-WeChat powcoder
- 4. The start state is:
- 5. The set of accept states is: F =



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- 2.  $\Sigma = \{0, 1\}$
- 3. Add WeChatapowcoder
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- 2.  $\Sigma = \{0, 1\}$
- 3. Add WeChatapowcoder
- 4. The start state is:  $q_1$
- 5. The set of accept states is: F =



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2. 
$$\Sigma = \{0, 1\}$$

- 4. The start state is:  $q_1$
- 5. The set of accept states is:  $F = \{q_2\}$



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- 1.  $Q = \{ \mathbf{q}, q_2 \}$
- 2.  $\Sigma = \{0, 1\}$
- 3. Add We Chat 10 W coder
- 4. The start state is:  $q_1$
- 5. The set of accept states is:  $F = \{q_2\}$

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#### FORMAL DEFINITION OF COMPUTATION

## Assignment Project Exam Help Let $M = (Q, \Sigma, \delta, q_0, F)$ be a finite automaton, and

Let  $w=(\mathcal{Q}, \mathcal{Z}, \theta, q_0, T)$  be a finite automaton, and Let  $w=w_1w_2\cdots w_n$  be a string over the alphabet  $\Sigma$ 

Then M accepts w iff there exists a sequence of states  $r_0r_1\cdots r_n$  from Q which satisfy the following three conditions:

- 1.  $r_0 = q_0$
- 2. And WeChat powcoder

#### LANGUAGE OF AN AUTOMATON

- $\blacktriangleright$  Let A be a language, and M be an automaton.
- $\begin{array}{c} & \text{ he cay that } \underline{M} / \text{ecognises } A \text{ if and only if } \\ & POWCOGET. \\ & A = \{w | M \text{ accepts } w\} \end{array}$
- We often the partial anguage recognised by M as I(M)
   E(M) is the set of all strings labeling paths from the start
- $\blacktriangleright$  L(M) is the set of all strings labelling paths from the start state of M to any accept state in M

#### REGULAR LANGUAGE

A language is regular if and only if there exists a finite automaton Assisherment Project Exam Help

Exercise

Prove that  $A = \{w | w \text{ is the empty string or ends with a } 0\}$  is a regular property regular regu

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#### REGULAR LANGUAGE

A language is regular if and only if there exists a finite automaton

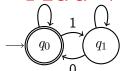
#### ssignment Project Exam Help Exercise:

Prove that  $A = \{w | w \text{ is the empty string or ends with a } 0\}$  is a

regul hattps://powcoder.com Solution:

The following DFA recognises A, therefore A must be regular:

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#### Examples of Regular Languages

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#### Examples of Regular Languages

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even number of 0s follow the last 1}

#### EXAMPLES OF REGULAR LANGUAGES

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What is the language recognised by the automaton obtained by inversing the accept and start states in  $M_2$ ?

#### Examples of Regular Languages

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What is the language recognised by the automaton obtained by inversing the accept and start states in  $M_2$ ?

#### Designing finite automata

"Reader as Automaton" method: The states encode what you need to remember about the string as you are reading it.
SESINGENIALENTE | DIVIDENTATION XIALINGER IS THE | DIVIDENTE | DIVIDE language consisting of strings with an odd number of 1s.

We need to remember:

- There has been an odd number of 1s so far

So we will need exactly two states. Then it just remains to add the transit And delive the ctal had recent states coder

#### DESIGNING FINITE AUTOMATA

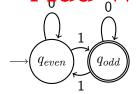
"Reader as Automaton" method: The states encode what you need to remember about the string as you are reading it.

Sample 111 | Division Cuttmator Xing | Division Cuttmator X

We need to remember:

- https://powdoder.com
- ► There has been an odd number of 1s so far

So we will need exactly two states. Then it just remains to add the transitioned delive the ctal and transitioned delive the ctal and transitioned delive the ctal and transitioned delivers.



Devise an automaton which accepts the language of strings which

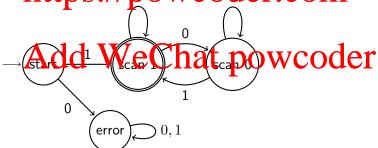
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- ▶ Whether or not the string began with 1
- Whether or not the last character seanned was a 1 https://powcoder.com

Devise an automaton which accepts the language of strings which

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- ▶ Whether or not the string began with 1
- ► Whether or not the last character scanned was a 1 nttps://powcoder.com



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What do we need to remember?

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What do we need to remember?

A: String so far has no 11, does not end in 1 https://powcoder.com

#### EXAMPLE 3

Devise an automaton which accepts the language of binary strings

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What do we need to remember?

- ► A: String so far has no 11, does not end in 1
  ► Intip S far h DO NY LOCAL CARDON

Devise an automaton which accepts the language of binary strings

# Assignment Project Exam Help

What do we need to remember?

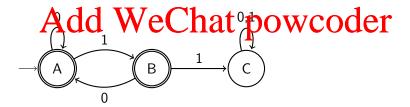
- ► A: String so far, has no 11, does not end in 1
- https://powcoder.com
- ► C: Consecutive 1s have been seen

Devise an automaton which accepts the language of binary strings

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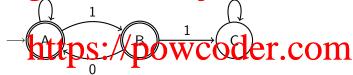
What do we need to remember?

- ► A: String so far, has no 11, does not end in 1
- https://powcoder.com
- ► C: Consecutive 1s have been seen



Let  $L = \{w | w \in \{0, 1\}^* \text{ and } w \text{ does not contain consecutive } 1s\}$ 

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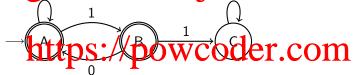


Is the string 101 in L?

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Let  $L = \{w | w \in \{0, 1\}^* \text{ and } w \text{ does not contain consecutive } 1s\}$ 

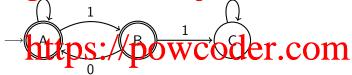
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Is the string 101 in L?

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Assignment Project Exam Help

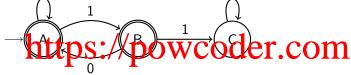


- ► SArdad WeChat powcoder

  ► Follow transition 1 to reach B

Let  $L = \{w | w \in \{0, 1\}^* \text{ and } w \text{ does not contain consecutive } 1s\}$ 

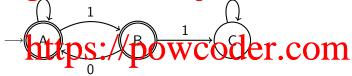
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- Add WeChat powcoder
- $\blacktriangleright$  Follow transition 1 to reach B
- ightharpoonup Follow transition 0 to reach A

Let  $L = \{w | w \in \{0, 1\}^* \text{ and } w \text{ does not contain consecutive } 1s\}$ 

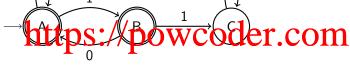
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- Add WeChat powcoder
- $\blacktriangleright$  Follow transition 1 to reach B
- ightharpoonup Follow transition 0 to reach A
- $\blacktriangleright$  Follow transition 1 to reach B

Let  $L = \{w | w \in \{0, 1\}^* \text{ and } w \text{ does not contain consecutive } 1s\}$ 

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- Add WeChat powcoder
- $\blacktriangleright$  Follow transition 1 to reach B
- ightharpoonup Follow transition 0 to reach A
- $\blacktriangleright$  Follow transition 1 to reach B
- ightharpoonup The result is an accepting state, so 101 is in the language

#### ERROR STATE(S)

An error state is any state from which it is impossible to reach an Sacapps at 1 Specific Property Less from the diagram. All elp missing transitions point to an unseen error state.

You must write "error states not shown" if you omit them. https://powcoder.com
These DFA are equivalent and both have two states



(error states not shown)

???

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With httpp sate, power offer inic ormata can you devise?

#### OUTLINE

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- Concepts (Operators, FV, Reductions)
- ► Recursion (fixed point, using it)

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- ► Functional Programming
- ► Automata Theory

- ► Regular languages
- ► NFA

#### Non deterministic Finite Automata (NFA)

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- ▶ no choice in the computation ⇒ deterministic https://powcoder.com

#### NFA

- can have any number of transitions per input from each state
   so some deposor to combination paget W Cracket listic
- $\blacktriangleright$  can also have  $\varepsilon$ -transitions, i.e. transitions which the automaton can follow without scanning any input

#### Non deterministic Finite Automata (NFA)

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per powcoder.com

#### Review

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► Automata Theory

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- ► DFA diagrams
- ► Using a DFA to do pattern matching

- ► Regular languages
- Definition
- ► How to prove that a language is regular
- ► Introduction to NFA