COMP2022: Formal Languages and Logic

Assignment Project Exam Help

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https://powcoder.com

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OUTLINE

- ► Context-Free Grammars (CFG)
- Context-Free Languages (CFL) Oder.com
- Ambiguity
- Recursive Grammars & Chat powcoder
- ► Types of Grammar

Introduction

Assignmento diffe, beginventes Help describing languages: finite automata and regular expressions, which describe regular languages

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We have already proven that some languages, such as

We have already proven that some languages, such as $\{0^n1^n \mid n \geq 0\}$, cannot be described using FA or RE.

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Today we will introduce *context-free grammars (CFG)*, which describe the next category of languages, the *context-free languages*

Grammars

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A grantapset of power of the wife a language

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The language generated is the set of all strings which can be
derived from the grammar

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 $S \to 0S1$ Recursive case: if $S \in L$ then $0S1 \in L$

 G_1 greaters and provided the second seco

How does it derive 0001112 Add WeChat powcoder

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 $S \to 0S1$ Recursive case: if $S \in L$ then $0S1 \in L$

 G_1 greaters and provided the second seco

How does it derive 0001112 How does it derive 0001112 hat powcoder

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 $S \to 0S1$ Recursive case: if $S \in L$ then $0S1 \in L$

 G_1 generates an already know is not regular

How does it derive 0001112 have Chat powcoder Add WeChat powcoder using rule $S \rightarrow 0S1$

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 $S \rightarrow 0S1$ Recursive case: if $S \in L$ then $0S1 \in L$

 G_1 generates is an expectation of the second se

How does it derive 000111? Add WeChat powcoder $Add \sum_{n=1}^{\infty} Add \sum_{n=1}^{\infty} Chat powcoder$

 $\Rightarrow 00S11$

using rule $S \rightarrow 0S1$

 $S \rightarrow 0S1$

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 G_1 generates and already know is not regular

How does it derive 0001112 have Chat powcoder Add will prove Add will grule $S \rightarrow 0S1$

 $\Rightarrow 00S11$

 $\Rightarrow 000111$

using rule $S \rightarrow 0S1$

using rule $S \rightarrow 01$

Recursive case: if $S \in L$ then $0S1 \in L$

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 $NounPhrase \rightarrow \mathsf{the}\ Noun$

https://pase verb Noun Phrase com

 $Verb \rightarrow likes \mid sees$

What And do Wenerheat powcoder

Assignment Project Exam Help

 $NounPhrase \rightarrow \mathsf{the}\ Noun$

$http^{\textit{VerbPhrase}}_{\textit{Nopn}} \vec{o} \vec{v}^{\textit{Verb}}_{\textit{pirt}} \vec{c}^{\textit{NounPhrase}}_{\textit{ball}} \text{com}$

 $Verb \rightarrow \mathsf{likes} \mid \mathsf{sees}$

What An used do of general at powcoder { the girl likes the girl, the girl likes the ball,

the girl likes the girl, the girl sees the girl, the ball likes the girl, the ball sees the girl,

the girl sees the ball, the ball likes the ball, the ball sees the ball

Assignment Project Exam Help language

Non-termings://powcoder.com

- ► A finite set of symbols used to generate the strings.
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Start symbol

► The variable used to start every derivation

Production rules

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Define strings of *variables* and *terminals* which can be substituted for a *variable*:

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Production rules

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substituted for a *variable*:

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A variable can have many rules:

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 $Noun \rightarrow \mathsf{ball}$

Noun o quokka

Production rules

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substituted for a *variable*:

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A variable can have many rules: They can be written together:

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 $Noun \rightarrow \mathsf{ball}$

 $Noun \rightarrow \mathsf{quokka}$

ANOTHER EXAMPLE

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 $T \rightarrow a \mid b \mid \dots$ https://powcoder.com

This is a grammator lambda calculus expressions coder

The variables are S. That powcoder

- \triangleright S is the start variable
- ▶ The terminals are $a, b, ..., (,), \lambda, ...$ (i.e. atoms and operators)

Some common notational conventions

- \blacktriangleright A, B, C, ... and S are variables
- hittps://blowcoder.com
- \blacktriangleright ..., X, Y, Z are either terminals or variables
- ...A, α a electrical of terminals and/or variables

CONTEXT-FREE GRAMMAR (CFG)

A context-free grammar is a grammar where every production rule

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ho α is a string of terminals and/or variables (possibly ϵ)

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CONTEXT-FREE GRAMMAR (CFG)

A context-free grammar is a grammar where every production rule

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 $ightharpoonup \alpha$ is a string of terminals and/or variables (possibly ϵ)

Conthittps://arporwood/enacom

Example:

 $\{a^nb^n\mid n\in N\}$ is not a regular language (no finite automata exists regularly but we can arrive this correctific language, because the following grammar generates it:

$$S \to aSb \mid \varepsilon$$

CFG: FORMAL DEFINITION

- \triangleright V is a finite set of variables
- https://powcoder.com
- PAs digite Wife and design the probability of the p
- $lackbox{lack} S \in V$ is a special variable called the Start Symbol

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More formely S: #/powerder.com

V =

Add WeChat powcoder

Assignment Project Exam Help

More for the St. #/powerder.com

V =

Add WeChat powcoder

```
More formally S. \neq / P over C oder. C of T = \{0,1\} V = \{S\} Add V = \{S\} Add V = \{S\} S \to 01 S \to 0S1
```

Assignment SProject Exam Help

 $VerbPhrase \rightarrow Verb\ NounPhrase$

https://power.com

More farmally GWe Chat powcoder

V =

S =

P =

Assignment SProject Exam Help

 $VerbPhrase \rightarrow Verb\ NounPhrase$

https://pogwcoder.com

 $\overset{\text{More farmally } G}{\underset{T}{\text{More farmally } G}} \overset{\text{More farmally } F}{\underset{\text{the, girl, ball, likes, sees}}{\text{where bounded}}} \text{owcoder}$

V =

S =

P =

Assignment SProject Exam Help

 $VerbPhrase \rightarrow Verb\ NounPhrase$

https://poder.com

```
More farmally G the, girl, ball, likes, sees V = \{S, NounPhrase, VerbPhrase, Noun, Verb\}
```

S =

--

P =

Assignment SProject Exam Help

 $VerbPhrase \rightarrow Verb\ NounPhrase$

https://pop.ggirl ball der.com

```
More farmally G the, girl, ball, likes, sees V = \{S, NounPhrase, VerbPhrase, Noun, Verb\} S = S P = \{S, NounPhrase, VerbPhrase, Noun, Verb\}
```

Assignment SProject Exam Help

 $VerbPhrase \rightarrow Verb\ NounPhrase$

https://powerceder.com

```
More farmally G_2 The hard power of the, girl, ball, likes, sees Y = \{S, NounPhrase, VerbPhrase, Noun, Verb\}
S = S
P = (\text{set of seven rules above})
```

LANGUAGE OF A GRAMMAR

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Language of a Grammar

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Notation:

 $\alpha \Rightarrow \beta$ defices that α derives it in one or more steps

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Language of a Grammar

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Notation:

 $\alpha \Rightarrow \beta$ means it derives it in one or more steps

The language of the settle L(G) and L(G) and L(G) by L(G) and L(G) by L(G) by L(G) and L(G) by L(G) by L(G) and L(G) by L(

Language of a Grammar

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Notation:

 $\alpha \Rightarrow \beta$ means it derives it in one or more steps

The larguage of the settle L(G) is the settle L

If two grammars generate the same langauge, then they are equivalent.

- Assign with the start Project Exam Help one of its productions
 - until the string is composed only of terminal symbols https://powcoder.com

Assign with the start Project Exam Help one of its productions

 $\begin{tabular}{ll} $\textbf{https://powcoder.com} \end{tabular}$

Example, derivation of 000111 from this grammar:

Assignment Project Exam Help one of its productions

https://powcoder.com

Example, derivation of 000111 from this grammar:

Assignment Project Exam Help one of its productions

https://powcoder.com

Example, derivation of 000111 from this grammar:

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 $\Rightarrow 00S11$

 $\Rightarrow 000S111$

 \Rightarrow

Assignment Project Exam Help one of its productions

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Example, derivation of 000111 from this grammar:

Adds:WeChat powcoder

 $\Rightarrow 00S11$

 $\Rightarrow 000S111$

 $\Rightarrow 000111$

Assignmental Project the leftmost variable first Assignment and the project of the leftmost variable first are the leftmost va

Example: "the girl sees the ball"

 $S \Rightarrow N$ https://powcoder.com

Assitement derivation: always derive the leftmost variable first Assitement always derive the leftmost arrange first always derive the left always derive the lef

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- ** He firl Werb Phresse Chat powcoder

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- ⇒ the girl VerbPhrese ⇒ the girl VerbPhrese Chat powcoder
- \Rightarrow the girl sees NounPhrase

Leftmost derivation: always derive the leftmost variable first ssignment Project Exame Help

Example: "the girl sees the ball"

- \Rightarrow the Noun VerbPhrase
- ⇒ the girl VerbPhrese ⇒ the girl VerbPhrese Chat powcoder
- \Rightarrow the girl sees NounPhrase
- \Rightarrow the girl sees the *Noun*

Leftmost derivation: always derive the leftmost variable first ssignment Project Exame Help

Example: "the girl sees the ball"

 $S \Rightarrow N$ and the second process of the secon

- \Rightarrow the Noun VerbPhrase
- ⇒ the girl VerbPhrese ⇒ the girl VerbPhrese Chat powcoder
- \Rightarrow the girl sees NounPhrase
- \Rightarrow the girl sees the *Noun*
- \Rightarrow the girl sees the ball

A Statement derivation: always derive the leftmost variable first A Statement of the left of the left

Example: "the girl sees the ball"

 $S \Rightarrow N$ hours S is a superbolar S in S is a superbolar S in S

 \Rightarrow the Noun VerbPhrase

- \Rightarrow NounPhrase Verb NounPhrase
- ⇒ the girl NerbPhrese ⇒ the girl NerbPhrese ⇒ the girl NerbPhrese Chat powcoder
- \Rightarrow the girl sees NounPhrase
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Leftmost derivation: always derive the leftmost variable first ssignment Project Exam Help

Example: "the girl sees the ball"

 $S \Rightarrow N$ and the second process of the secon

 \Rightarrow the Noun VerbPhrase

- $\Rightarrow NounPhrase Verb NounPhrase$
- ⇒ the girl VerbPhrese hat powcoder

 NumPhrese NounPhrase Verb the Noun

 ⇒ the girl VerbPhrese hat powcoder
- \Rightarrow the girl sees NounPhrase
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- \Rightarrow the girl sees the ball

Leftmost derivation: always derive the leftmost variable first ssignment Project Exam Help

Example: "the girl sees the ball"

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 \Rightarrow the Noun VerbPhrase

- $\Rightarrow NounPhrase Verb NounPhrase$
- $\Rightarrow \text{ the girl } Verb Phrese \\ \Rightarrow \text{ the grad } Num Ferse \\ \text{ hat } Pop Wis Contest \\ \text{ all } \\$
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Leftmost derivation: always derive the leftmost variable first ssignment Project hax arm fHelp

Example: "the girl sees the ball"

$S \Rightarrow N$ https://powcoder.com/hrase

 \Rightarrow the Noun VerbPhrase

- $\Rightarrow NounPhrase Verb NounPhrase$
- $\Rightarrow NounPhrase Verb$ the Noun
- ⇒ the girl VerbPhrase hat NounPhrase Verb the NounPhrase Verb the
- \Rightarrow the girl sees NounPhrase

 $\Rightarrow NounPhrase$ sees the ball

- \Rightarrow the girl sees the *Noun*
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Leftmost derivation: always derive the leftmost variable first ssignment Project Box am filelp

Example: "the girl sees the ball"

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Leftmost derivation: always derive the leftmost variable first ssignment Project Box am filelp

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 \Rightarrow the *Noun* sees the ball

 \Rightarrow the girl sees the ball

 \Rightarrow the girl sees the ball

Context-Free Languages

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Context-Free Languages

A language is context-free if it is generated by a CFG

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The syntax of most programming languages are context-free.

https://poweoder.com $S \to W$ if poweoder.com $S \to I := E$ Add We Chat poweoder $E \to ...$ (description of an expression)

 $I \rightarrow \dots$ (description of an identifier)

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CONTEXT-FREE LANGUAGES

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{Reglartepusees}/powcoder.com

- The union of two CFL is also context-free Coder

 The concatenation of two CFL is also context-free
- ► The star closure of a CFL is also context-free

Assignment Project Exam Help $S \rightarrow AB$ $S \rightarrow AB$ $S \Rightarrow AB$ $S \Rightarrow AB$

https://powcoder.com

What is L(G)?

Assignment Project Exam Help $S \rightarrow AB$ $S \rightarrow AB$ $S \rightarrow AB$ $S \Rightarrow AB$

https://powcoder.com

What is L(G)?

 $\Rightarrow aaaaB$

Assignment Project Exam Help $S \rightarrow AB$ $S \rightarrow AB$ $S \rightarrow AB$ $S \Rightarrow AB$

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What is L(G)?

 $\Rightarrow aaaaB$

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 $\Rightarrow aaaabbbbbb$

Assignment Project Exam Help $S \rightarrow AB$ $S \rightarrow AB$ $S \rightarrow AB$ $S \Rightarrow AB$

https://powcoder.com

What is L(G)?

 $\Rightarrow aaaaB$

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 $\Rightarrow aaaabbbbbb$

i.e.
$$L(G) = L(a^*b^*) = \{a^nb^m \mid n \ge 0, m \ge 0\}$$

More examples

Assignment Project Exam Help 1. $S \rightarrow aSa \mid bSb \mid \varepsilon$

- 2. https://powcoder.com
- 3. $S \rightarrow SS \mid bS \mid a$
- 4. Add_bT WeChat powcoder
- 5. $S \rightarrow aSa \mid bSb \mid a \mid b$

More examples

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- 1. $\{ba^{n+1}b \mid n \ge 0\}$
- 2. https://gpowcoder.com
- 3. Even-length strings in $\{a,b\}^*$ with matching middle symbols \mathbf{Add} \mathbf{WeChat} $\mathbf{powcoder}$
- 4. Binary strings containing more 0's than 1's
- 5. Strings over $\{a, b\}$ with at least three a's

Let M and N be two languages whose grammars have disjoint sets. So between them is the start symbols.

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Let M and N be two languages whose grammars have disjoint sets. Support their start symbols.

Then we can construct a grammar recognising the following languages, with a new start symbol 9.

Let M and N be two languages whose grammars have disjoint sets. Support their start symbols.

Then we can construct a grammar recognising the following languages, with a new start symbol 9.

▶ Union: the grammar for $M \cup N$ starts with $S \rightarrow S_M \mid S_N$

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All other productions remain unchanged (aside for renaming of variables as needed)

Let M and N be two languages whose grammars have disjoint sets Shptinms name transfer persent by Lexistan <math>She p their start symbols.

Then we can construct a grammar recognising the following languages, with a new start symbol 9.

- ▶ Union: the grammar for $M \cup N$ starts with $S \rightarrow S_M \mid S_N$
- $\begin{array}{c} {\color{red} \bullet} \quad \text{Cancatenation the grammar for } MN \text{ starts with } S {\color{red} \bullet} S_M S_N \\ {\color{red} \textbf{Add WeChat powcoder}} \end{array}$

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Let M and N be two languages whose grammars have disjoint sets. SSI CHAMONITO POSTY) LEXAM SHE their start symbols.

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- ▶ Union: the grammar for $M \cup N$ starts with $S \rightarrow S_M \mid S_N$

All other productions remain unchanged (aside for renaming of variables as needed)

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Then $L=M\cup N$ where $M=\{a^n\mid n\geq 0\}, N=\{b^n\mid n\geq 0\}$

So a grammar G_N of N is

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Then $L=M\cup N$ where $M=\{a^n\mid n\geq 0\}, N=\{b^n\mid n\geq 0\}$

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Then $L=M\cup N$ where $M=\{a^n\mid n\geq 0\}, N=\{b^n\mid n\geq 0\}$

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Then $L=M\cup N$ where $M=\{a^n\mid n\geq 0\}, N=\{b^n\mid n\geq 0\}$

So a grammar G_N of N is $S_N \to \varepsilon \mid bS_N$

Using And rule Chat powcoder

$$S \to S_M \mid S_N S_M \to \varepsilon \mid aS_M S_N \to \varepsilon \mid bS_N$$

USING THE CONCATENATION RULE

Assignment Project Exam Help

Then L=MN where $M=\{a^m\mid m\geq 0\}, N=\{b^n\mid n\geq 0\}$

So a grammar G_N of N is $S_N \to \varepsilon \mid bS_N$

USING THE CONCATENATION RULE

Assignment Project Exam Help

Then L=MN where $M=\{a^m\mid m\geq 0\}, N=\{b^n\mid n\geq 0\}$

So a grammar G_N of N is $S_N \to \varepsilon \mid bS_N$

Using the dd at the Chart powcoder

$$S \to S_M S_N$$

$$S_M \to \varepsilon \mid aS_M$$

$$S_N \to \varepsilon \mid bS_N$$

USING THE STAR CLOSURE RULE

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Then https://powcoder.com

So a grammar \mathcal{G}_M of M is

USING THE STAR CLOSURE RULE

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Then https://powcoder.com

So a grammar G_{M} of M is $\mathit{S}_{M} \rightarrow \mathit{aa} \mid \mathit{bb}$

USING THE STAR CLOSURE RULE

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Then https://powcoder.com

So a grammar G_{M} of M is $\mathit{S}_{M} \rightarrow \mathit{aa} \mid \mathit{bb}$

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Using the star closure rule we get:

 $S \to S_M S \mid \varepsilon$ $S_M \to aa \mid bb$

Parsing

Assignment Project Exam Help grammar generates it.

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i.e. To discover the *correct* derivation of the sentence, or the correct parse tree

Parse Tree

A parse tree is a tree labelled by symbols from the CFG

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- ▶ leaf node = a terminal or ε
- hildren of X = the right hand side of a production rule for https://powcoder.com

Parse Tree

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- \blacktriangleright leaf node = a terminal or ε
- hildren of X = the right hand side of a production rule for https://powcoder.com

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Example parse tree for "0011" in $S \rightarrow 0S1 \mid 01$

An in-order traversal of the leaf nodes retrieves the string

PARSE TREE OR DERIVATION TREE

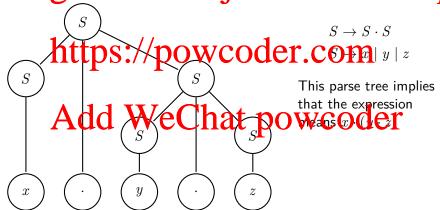
The parse tree defines the (syntactic) meaning of a string in the Assignment Project Exam Help

https://powcoder.com

PARSE TREE OR DERIVATION TREE

The parse tree defines the (syntactic) meaning of a string in the

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NATURAL LANGUAGE PROCESSING (NLP) EXAMPLE

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 $NounPhrase \rightarrow ComplexNoun \mid ComplexNoun PrepPhrase$

 $VerbPhrase \rightarrow ComplexVerb \mid ComplexVerb \mid PrepPhrase$

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 $ComplexNoun \rightarrow Article\ Noun$

Complex Verb Verb NounPhrase Addle WeChat powcoder

 $Noun \rightarrow girl \mid dog \mid stick \mid ball$

 $Verb \rightarrow \mathsf{chases} \mid \mathsf{sees}$

 $Prep \rightarrow with$

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We have no choice but start by deriving

S ⇒ https://powcoder.com

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We have no choice but start by deriving

S ⇒ https://powcoder.com

All the production rules for VerbPhrase produce a ComplexVerb, which Authorized the powcoder

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We have no choice but start by deriving

S ⇒ https://powcoder.com

All the production rules for VerbPhrase produce a ComplexVerb, which Attn hustroduct Verb powcoder

Therefore all strings in the language contain a verb. "a ball" does not contain a verb, so it cannot be accepted by the grammar.

Ambiguity: example

Ambiguity: several meanings for the same sentence.



⇒ Article Noun VerbPhrase

⇒ he Noun VerbPhrase

→ heget lebbase / DOWCOde legels

\Rightarrow height le bbhree / POWCOUE de girl \Rightarrow the girl ComplexVerb \Rightarrow the girl

- ⇒ the girl Verb NounPhrase
- ⇒ the girl chases NounPhrase
- ⇒ the girl chases Complex Volun PropPhrase ⇒ the firl chase strick Num PrepPhrase
- ⇒ the girl chases the Noun PrepPhrase
- \Rightarrow the girl chases the dog PrepPhrase
- \Rightarrow the girl chases the dog $Prep\ ComplexNoun$
- \Rightarrow the girl chases the dog with ComplexNoun
- ⇒ the girl chases the dog with Article Noun
- the giri chases the dog with 217 there 140
- \Rightarrow the girl chases the dog with a Noun
- ⇒ the girl chases the dog with a stick

- \Rightarrow Article Noun VerbPhrase
- ⇒ the Noun VerbPhrase
- ⇒ the girl ComplexVerb PrepPhrase
- ⇒ the girl Verb NounPhrase PrepPhrase
- ⇒ the girl chases NounPhrase PrepPhrase
- the girl chases the North PrepPhil
 - ⇒ the girl chases the dog PrevPhrase
 - ⇒ the girl chases the dog Prep ComplexNoun
 - ⇒ the girl chases the dog with ComplexNoun

 - \Rightarrow the girl chases the dog with $Article\ Noun$
 - \Rightarrow the girl chases the dog with a Noun
 - \Rightarrow the girl chases the dog with a stick

Ambiguity: example

Ambiguity: several meanings for the same sentence.

Assignments Project Extanted Pelp

https://the girl VerbPhrase

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> the girl VerbPhrase

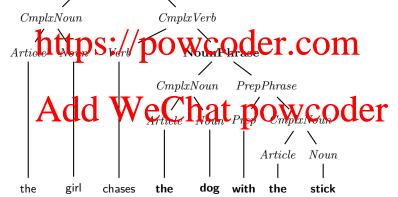
Add Le We Chat powcoder

- \Rightarrow the girl $ComplexVerb\ PrepPhrase$
- \Rightarrow ⁺ the girl chases the dog with a stick

Who has the stick?

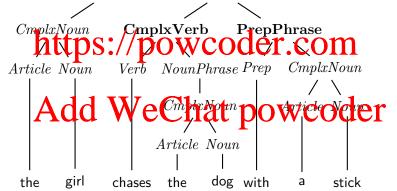
FIRST LEFTMOST DERIVATION TREE

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SECOND LEFTMOST DERIVATION TREE

Assignment Project Exam Help



Ambiguous Grammars

Assignment of ground it is unambigous.

Definition:

Project it is unambigous.

Definition to the property of the property of

Ambiguous Grammars

A SSIGNMENT PROJECT LEXAMINETED parse trees. Otherwise, it is unambigous.

Defin tottps://powcoder.com
A grammar s ambiguous if it contains an ambiguous string.

Each purse tree has only ore leftmost derivation, so this is equivalent to saying that the stand has two defined to derivations.

Ambiguous Grammars

A SSIGNMENT PROJECT I LEXAMINE LE LE P parse trees. Otherwise, it is unambigous.

Defin tottps://powcoder.com
A grammar s ambiguous if it contains an ambiguous string.

Each purse tree has only one leftmost derivation, so this is equivalent to saying that the string has two defined on the derivations.

Similarly for rightmost derivations.

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Rightmost derivations of a - b - c:

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Assignment $\Pr_{E \to \mathcal{F}} \mathcal{F}_{e} \mathcal{E}_{c}$ Exam Help

Rightmost derivations of a - b - c:

https://powcoder.com $E \Rightarrow E - E$ $\Rightarrow E - c$ Add We Chat powcoder $\Rightarrow E - b - c$ $\Rightarrow a - b - c$

i.e.
$$(a - b) - c$$

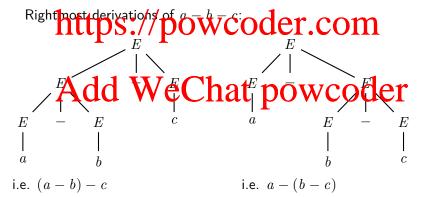
Assignment $\Pr_{E \to \mathcal{F}} \mathcal{F}_{e} \mathcal{E}_{c}$ Exam Help

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 & \text{https://powcoder.com} \\
 & E \Rightarrow E-E \\
 & \Rightarrow E-E \\
 & \Rightarrow E-E-E \\
 & \Rightarrow E-E-E$

i.e.
$$(a - b) - c$$

i.e.
$$a - (b - c)$$

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```
REMOVING AMBIGUITY (EXAMPLE)
Suppose we want a - b - c to always mean (a - b) - c?
```

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REMOVING AMBIGUITY (EXAMPLE)
```

Suppose we want a-b-c to always mean (a-b)-c?

Assignment Project Exam Help $T \rightarrow a \mid b \mid c$

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Suppose we want a-b-c to always mean (a-b)-c?

Introduce a new nonterminal symbol T:

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Now the only rightmost derivation is: https://powcoder.com

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Now the only rightmost derivation is: https://powcoder.com

$$\begin{array}{c}
E \Rightarrow E - T \\
A \stackrel{\rightarrow}{\text{det}} W_c \text{eChat powcoder} \\
E \stackrel{\rightarrow}{\text{det}} V_c \text{eChat powcoder}
\end{array}$$

$$\Rightarrow E - b - c$$

$$\Rightarrow T - b - c$$

$$\Rightarrow a - b - c$$

RECURSION

Assignmente Project Exam Help

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Assignmenter Projection X as the Help

 \blacktriangleright left-recursive: it occurs at the start of the string $X\Rightarrow^+ X\beta$

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Assignmenter Projection X as the Help

- ▶ left-recursive: it occurs at the start of the string $X \Rightarrow^+ X\beta$
- right-recursive:/ir occurs at the end of the string $X \Rightarrow^+ \alpha X$ TUPS://powcoder.com

Assignmenter Projection X ash the Help

- ▶ left-recursive: it occurs at the start of the string $X \Rightarrow^+ X\beta$
- $\begin{array}{c} \bullet \quad \text{right-recursive:/if occurs at the end of the string } X \Rightarrow^+ \alpha X \\ \bullet \quad \text{seff-embedding:/it occurs in Ceurs in Ceurs$

Assirgnmenter Proting containing X at the Help

- ▶ left-recursive: it occurs at the start of the string $X \Rightarrow^+ X\beta$

A gran Andidective et my historia bo in cereivder

Assignmenter Profession Examination

- ▶ left-recursive: it occurs at the start of the string $X \Rightarrow^+ X\beta$
- right-recursive:/ir occurs at the end of the string $X \Rightarrow^+ \alpha X$ seff-embedding:/it occurs in Ceuvening.

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A grammar for an infinite language must contain at least one recursive variable

BALANCED PARENTHESES

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REMOVE LEFT RECURSION

$\begin{array}{c} \textbf{Assignment Project Exam} \\ \textbf{An equivalent grammar without left-recursion:} \ B \rightarrow (B) \mid \mathcal{B}B \mid \mathcal{E} \\ \textbf{An equivalent grammar without left-recursion:} \ B \rightarrow (B)B \mid \mathcal{E} \\ \end{array}$

Left flarsing of ()()() // Is now deterministif: powcoder.com

Remaining	input	Derivation steps		
	()()()	В	start symbol	
\perp Ad	()()()	WeChat	POW/COde	er
110)()()	(B)B	matching terminals	
)()())B	$B \to \varepsilon$	
	()()	$\mid B \mid$	matching terminals	

CLEAN GRAMMARS

Assignment of the control of the con

be reduced to a single variable.

https://powcoder.com

CLEAN GRAMMARS

Assignment definition Project Exame Help there is no reason to distinguish between them. They should

be reduced to a single variable.

https://powcoder.com

No useless variables:

A variable is useless if it cannot appear in the derivation of any string i.e. there is no derivation $S \Rightarrow^+ \alpha X \beta \Rightarrow^+ \sigma$ where σ it Astrictor fermes unidervapines Wing Contest without affecting the language generated by the grammar.

CLEAN GRAMMARS

Signement of Example Help there is no reason to distinguish between them. They should

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https://powcoder.com

A variable is useless if it cannot appear in the derivation of any stying i.e. there is no derivation $S \Rightarrow^+ \alpha X \beta \Rightarrow^+ \sigma$ where σ it astrogof New to Landstva Dies Win Good Cal without affecting the language generated by the grammar.

► No null productions (except for the start symbol)

Types of grammars

We are interested in 4 classes of grammars, depending on the type Assignment throughout Exam Help

```
Type 0 (unrestricted) \chi \to \alpha

Type 1 (context-sensitive) \chi \to \alpha where 1 \le |\chi| \le |\alpha|

Type 3 (regular) \chi \to \alpha where \chi \to \alpha is \chi \to \alpha.
```

Recall the Chomsky Hierarchy from week 1!

Context-free Grammars

Assignment class of Exam. Help

- \blacktriangleright All rules are in the form $A \to \alpha$
- ► Closed under Union, Concatenation and Star Closure
- https://pow.coder.com
- ► Ambiguous grammars
- Add WeChat powcoder

Next lecture:

- ► Push-Down Automata
- ► Parsing