COMP2022: Formal Languages and Logic

Assignment Project Exam Help

Joseph Godbehere

https://powcoder.com

6th September, 2018



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Equivalence of FA and Regular Expressions

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Proving if a language is, or is not, regular

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► Equivalence of FA and Regular Expressions

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Proving if a language is, or is not, regular

EQUIVALENCE OF REGEX AND FA

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Proof Show at the Serice program of the Excom

- RegEx ⇒ FA:
 Show that for each RegEx, there exists an NFA which recognises the length of the power of the po
- FA ⇒ RegEx:
 Show that for each NFA, there exists a RegEx which recognises the same language

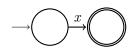
FROM REGEX TO FA: ATOMIC CASES

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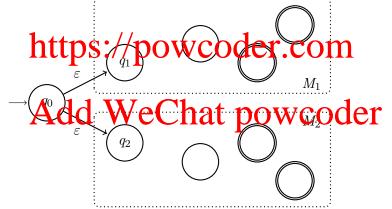
Automaton for $x \in \Sigma$



NFA FOR REGULAR OPERATIONS: UNION

Let M_1 and M_2 be automata recognising $L(R_1)$ and $L(R_2)$

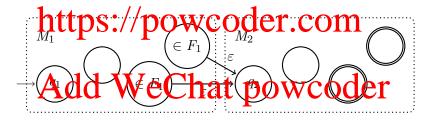
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NFA FOR REGULAR OPERATIONS: CONCATENATION

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Then an automaton M for $R_1 \circ R_2$ is:



Reminder: the accept states of M_1 are not accept states in M

NFA FOR REGULAR OPERATIONS: STAR CLOSURE

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1. Construct automata for the atomic regular expressions a, b, cASSIGNMENT PROPERTY OF THE PROPERTY OF THE

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1. Construct automata for the atomic regular expressions a, b, cASSIGNMENT OF THE PROPERTY OF THE PROPERTY

3. Use the Concatenation operation to find an automaton for bc^{\star}

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- 3. Use the Concatenation operation to find an automaton for bc^\star

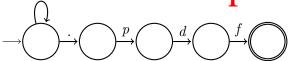
From NFA to RegEx: Simple examples

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This one gives $(a \mid b \mid \dots \mid Y \mid Z)^*.pdf$

a...Add WeChat powcoder



From NFA to RegEx: Simple examples

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1*00*1(0 | 1)*

CONCEPT

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- 1. Convert the NFA to a Generalised NFA (GNFA)
 - Only one start state, no incoming transitions

 Only one accept state, no outgoing transitions

 Thrunsitions de eribed by RegEX
- 2. Progressively eliminate all states between the start and accept stated WeChat powcoder
- 3. The transition between the start and the accept state is now a regular expression describing ${\cal L}$

GENERALISED NFA (GNFA)

The start state q_s is non-accepting and has no incoming transitions

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There is exactly one transition between each ordered pair of states, labelled with a RegEx.

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 $\{abc, abca, abcbb, aaaaaabc\} \subseteq L$

GENERALISED NFA (GNFA)

The start state q_s is non-accepting and has no incoming transitions

Assignmenta Project Exam Help

There is exactly one transition between each ordered pair of states, labelled with a RegEx.

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We do not show the \emptyset transitions (why not?) $\{abc, abca, abcbb, aaaaaabc\} \subseteq L$

CONVERTING AN NFA TO A GNFA

Create a new non-accepting start state q_s , with a arepsilon-transition to

the original start state $Project\ Exam\ Help$ Create a new accept state q_a with ε -transitions from the original accept states, which are no longer accepting.

Label the transitions between every ordered pair (q_i,q_i) of states from the NFA as the upion of the atomic RegExcles ribing each transition from q_i to q_j in the NFA.



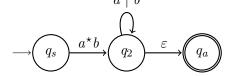
SIMPLE EXAMPLE: ELIMINATE STATE q_1



There is only one way to pass through q: https://powcoder.com

 $q_1
ightarrow q_1$ any number of times

We set in Cransition q_s Charles upon of the new c_g and it's old value (\emptyset). This is $\varepsilon a^*b \mid \emptyset$, which simplifies to a^*b

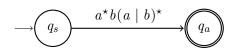


Simple example: eliminate state q_2



There is only one why to pass through a er. com_{a^*b}

 $Add \stackrel{q_2 \rightarrow q_2 \text{ any number of times}}{\text{Add powcoder}} ^{(a|b)^{\star}}$



The language of the original automaton is $a^*b(a \mid b)^*$

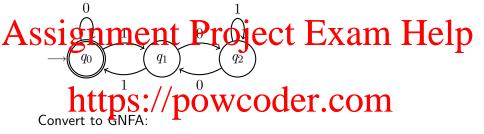
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https://powsøder.com

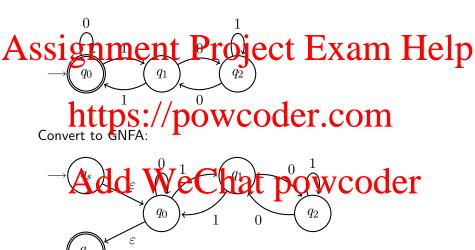
Add $(R_1)(R_2)^*(R_3)$ with the expression (R_4)

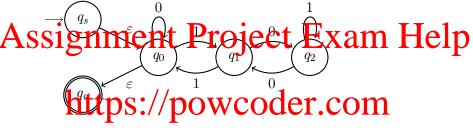
Note:

- ightharpoonup Possibly $q_i = q_i$
- lacktriangle Recall that pairs are ordered, so we also consider (q_j,q_i)
- ▶ If there is no transition R_x , then $R_x = \emptyset$



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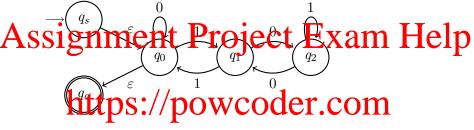




We can eliminate the states in any order. Eliminate q_0 .

All paid of states Wt Exist In which are not of througher

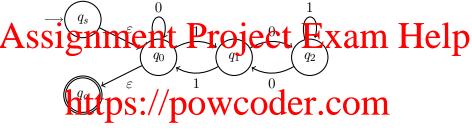
- _
- •
- ightharpoons



We can eliminate the states in any order. Eliminate q_0 .

All paid of takes Wth exist provides provided the paid of takes (q_s, q_1) :

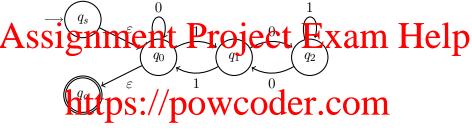
- $\blacktriangleright (q_s, q_a):$
- $ightharpoonup (q_1, q_1):$
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All parades Wt exist have been determined by the parades which are not been all parades with the property of the parades with the parades with

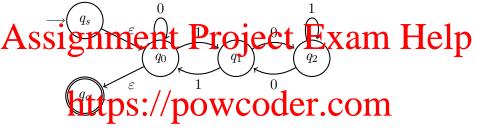
- $(q_s, q_1) : R_1 = \varepsilon,$
- $\blacktriangleright (q_s, q_a):$
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- $ightharpoonup (q_1, q_a):$



We can eliminate the states in any order. Eliminate q_0 .

All paid of tales with expositions which are not of throughout $(q_s,q_1):R_1=\varepsilon,R_2=0,$

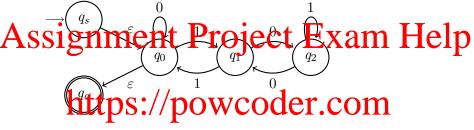
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All paid of tales with excisit properties which are not of throughout $(q_s,q_1):R_1=\varepsilon,R_2=0,R_3=1,$

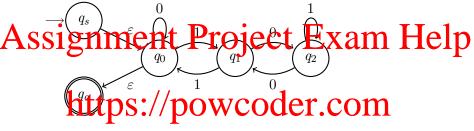
- $\blacktriangleright (q_s, q_a)$:
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We can eliminate the states in any order. Eliminate q_0 .

All pains of states with transitions which are not 10-through com

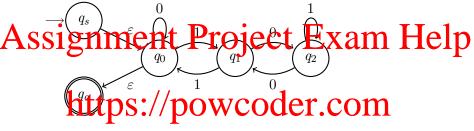
- $(q_s, q_1): R_1 = \varepsilon, R_2 = 0, R_3 = 1, R_4 = 0$
- $\blacktriangleright (q_s, q_a):$
- $ightharpoonup (q_1, q_1):$
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All pains of states with transitions which are not 1/1 through 1/10

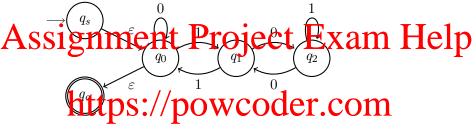
- $(q_s, q_1): R_1 = \varepsilon, R_2 = 0, R_3 = 1, R_4 = \emptyset \Rightarrow \varepsilon 0^* 1 \mid \emptyset$
- $\blacktriangleright (q_s, q_a):$
- $ightharpoonup (q_1, q_1):$
- $ightharpoonup (q_1, q_a):$



We can eliminate the states in any order. Eliminate q_0 .

All pains of states with transitions which are not through you

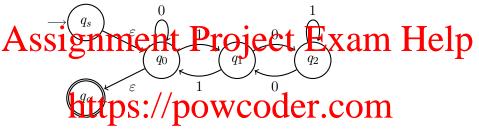
- $(q_s, q_1): R_1 = \varepsilon, R_2 = 0, R_3 = 1, R_4 = \emptyset \Rightarrow \varepsilon 0^*1 \mid \emptyset = 0^*1$
- $\blacktriangleright (q_s, q_a):$
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All pains of states with transitions which are not through an

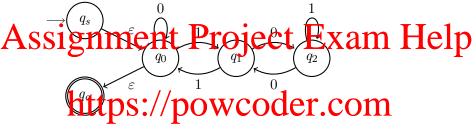
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- $ightharpoonup (q_1, q_1):$
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We can eliminate the states in any order. Eliminate q_0 .

Ill paid of states with expositions which are not of through $(q_s,q_1):R_1=\varepsilon,R_2=0,R_3=1,R_4=\emptyset\Rightarrow \varepsilon 0^\star 1\mid \emptyset$

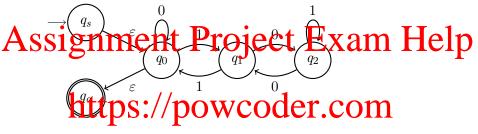
- $ightharpoonup (q_s, q_a): R_1 = \varepsilon, R_2 = 0,$
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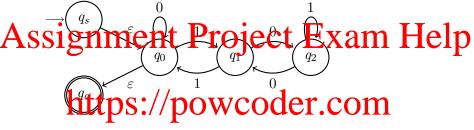
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- $ightharpoonup (q_1, q_a):$



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Ill paid of states with expositions which are not of through $(q_s,q_1):R_1=arepsilon,R_2=0,R_3=1,R_4=\emptyset\Rightarrowarepsilon^*$

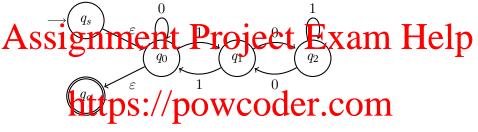
- \blacktriangleright $(q_s, q_a): R_1 = \varepsilon, R_2 = 0, R_3 = \varepsilon, R_4 = \emptyset$
- $ightharpoonup (q_1, q_1):$
- $ightharpoonup (q_1, q_a):$



We can eliminate the states in any order. Eliminate q_0 .

Ill paid of states with expositions which are not obtained by $(q_s,q_1):R_1=\varepsilon,R_2=0,R_3=1,R_4=\emptyset \Rightarrow \varepsilon 0^*1 \mid \emptyset=0^*1$

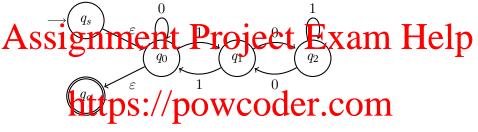
- $(q_s, q_a): R_1 = \varepsilon, R_2 = 0, R_3 = \varepsilon, R_4 = \emptyset \Rightarrow \varepsilon 0^* \varepsilon \mid \emptyset$
- $ightharpoonup (q_1, q_1):$
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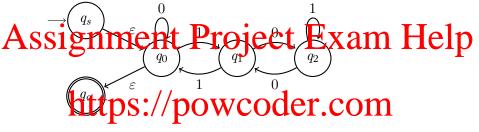
- \blacktriangleright $(q_s, q_a): R_1 = \varepsilon, R_2 = 0, R_3 = \varepsilon, R_4 = \emptyset \Rightarrow \varepsilon 0^* \varepsilon \mid \emptyset = 0^*$
- $ightharpoonup (q_1, q_1):$
- $ightharpoonup (q_1, q_a):$



We can eliminate the states in any order. Eliminate q_0 .

Ill paid of states with expositions which are not through core $(q_s,q_1):R_1=\varepsilon,R_2=0,R_3=1,R_4=\emptyset \Rightarrow \varepsilon 0^*1 \mid \emptyset=0^*1$

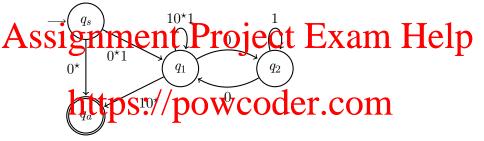
- $(q_s, q_a): R_1 = \varepsilon, R_2 = 0, R_3 = \varepsilon, R_4 = \emptyset \Rightarrow \varepsilon 0^* \varepsilon \mid \emptyset = 0^*$
- $(q_1, q_1): R_1 = 1, R_2 = 0, R_3 = 1, R_4 = \emptyset \Rightarrow 10^*1 \mid \emptyset = 10^*1$
- $ightharpoonup (q_1, q_a):$



We can eliminate the states in any order. Eliminate q_0 .

All pain of states with Exansitions which are not through doing

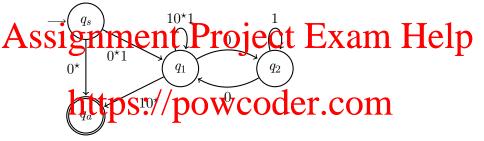
- $(q_s, q_1): R_1 = \varepsilon, R_2 = 0, R_3 = 1, R_4 = \emptyset \Rightarrow \varepsilon 0^* 1 \mid \emptyset = 0^* 1$
- $(q_s, q_a): R_1 = \varepsilon, R_2 = 0, R_3 = \varepsilon, R_4 = \emptyset \Rightarrow \varepsilon 0^* \varepsilon \mid \emptyset = 0^*$
- $(q_1, q_1): R_1 = 1, R_2 = 0, R_3 = 1, R_4 = \emptyset \Rightarrow 10^*1 \mid \emptyset = 10^*1$
- $(q_1, q_a): R_1 = 1, R_2 = 0, R_3 = \varepsilon, R_4 = \emptyset \Rightarrow 10^* \varepsilon \mid \emptyset = 10^*$



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All pairs of states with transitions which are not \emptyset through q_2 :

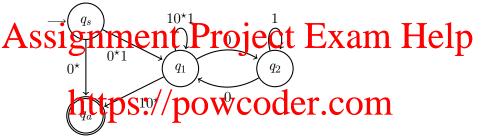
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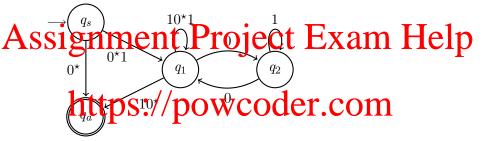
All pairs of states with transitions which are not \emptyset through q_2 :

 $ightharpoonup (q_1, q_1):$



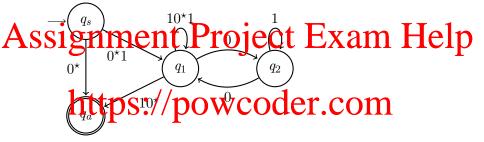
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$$ightharpoonup (q_1, q_1) : R_1 = 0,$$



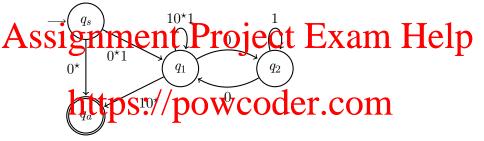
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$$ightharpoonup (q_1, q_1): R_1 = 0, R_2 = 1,$$



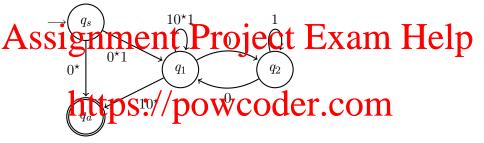
We ca Aelining to We states than arden Eliminate coder

$$ightharpoonup (q_1, q_1): R_1 = 0, R_2 = 1, R_3 = 0,$$



We ca Aelining to We states than arden Eliminate oder

$$ightharpoonup (q_1, q_1): R_1 = 0, R_2 = 1, R_3 = 0, R_4 = 10^*1$$

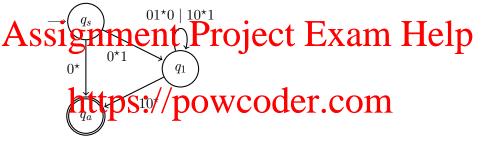


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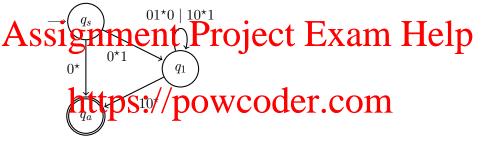
All pairs of states with transitions which are not \emptyset through q_2 :

$$(q_1, q_1): R_1 = 0, R_2 = 1, R_3 = 0, R_4 = 10^*1 \Rightarrow 01^*0 \mid 10^*1$$

Much easier!



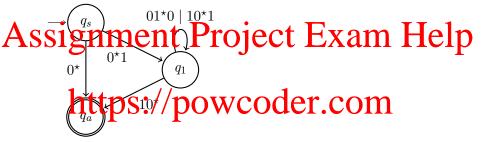
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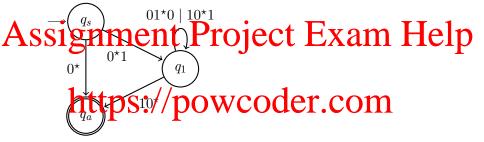
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All pairs of states with transitions which are not \emptyset through q_1 :

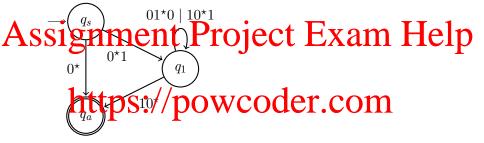
 $ightharpoonup (q_s, q_a)$:



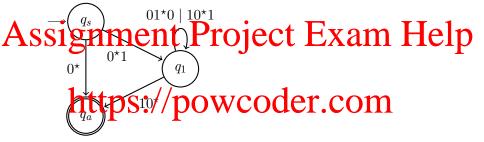
$$ightharpoonup (q_s, q_a) : R_1 = 0^*1,$$



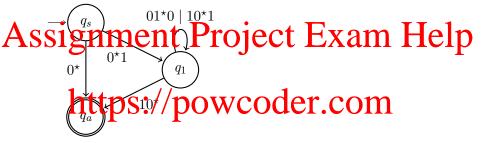
$$ightharpoonup (q_s, q_a): R_1 = 0^*1, R_2 = 01^*0 \mid 10^*1,$$



$$ightharpoonup (q_s, q_a): R_1 = 0^*1, R_2 = 01^*0 \mid 10^*1, R_3 = 10^*,$$



$$ightharpoonup (q_s, q_a): R_1 = 0^*1, R_2 = 01^*0 \mid 10^*1, R_3 = 10^*, R_4 = 0^*$$



All pairs of states with transitions which are not \emptyset through q_1 :

 $(q_s, q_a): R_1 = 0^*1, R_2 = 01^*0 \mid 10^*1, R_3 = 10^*, R_4 = 0^*$ so $(R_1)(R_2)^*(R_3) \mid (R_4) = 0^*1(01^*0 \mid 10^*1)^*10^* \mid 0^*$

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So, 0 1 (1) 10 W Coder Cognises binary strings which are divisible by 3.

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So, 0 1 (1) 10 2 W Coder Cognises binary strings which are divisible by 3.

Eliminating states in a different order can result in a different, but equivalent RegEx.

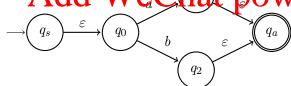
e.g. eliminating q_2 , q_1 , then q_0 yields: $(1(01^*0)^*1|0)^*$

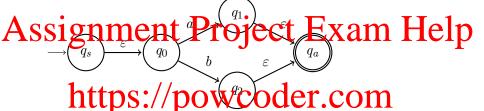
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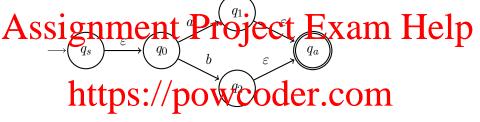
As GNFA:

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Eliminate q_2 :



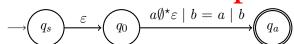
Eliminate q_2 :

Add WeChat powcoder $\xrightarrow{q_s} \xrightarrow{\varepsilon} \xrightarrow{q_0} \xrightarrow{q_a} \xrightarrow{q_a}$

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Eliminate q_0 :

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Simplify, to get the expected: hat powcoder

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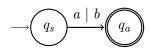
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Eliminate q_0 :

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 $\underbrace{\mathsf{https:/\!/\!powcoder.com}}_{q_s} \overset{\text{https:/\!/\!powcoder.com}}{\underset{q_a}{\longrightarrow}} \underbrace{}_{q_a}$

Simplify, to get the expected: hat powcoder



SUMMARY

Algorithm to convert an NFA to a RegEx:

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- ► Only one accept state, no outgoing transitions
- https://powcoder.com

SUMMARY

Algorithm to convert an NFA to a RegEx:

Assignmento Preject A Extra Help Only one start state, no incoming transitions

- ► Only one accept state, no outgoing transitions
- ► Transitions described by RegEx

2. Progressively eliminate all states between start and accept

- ► For each pair (q_i, q_j) where $q_i, q_j \in Q \setminus \{q_{elim}\}$
- ▶ Replace arrow $q_i \rightarrow q_j$ with $((R_1)(R_2)^*(R_3) \mid (R_4))$, where

Add Ray is the Region of the Region of the Coder

- $ightharpoonup R_3$ is the RegEx on transition $q_{elim} o q_i$
- ▶ R_4 is the RegEx on transition $q_i \rightarrow q_j$

SUMMARY

Algorithm to convert an NFA to a RegEx:

Assignmento Preject AEM Help

- ► Only one accept state, no outgoing transitions
- ► Transitions described by RegEx
- 2. Progressively ellmpass and states between scarling ccept
 - ► For each pair (q_i, q_j) where $q_i, q_j \in Q \setminus \{q_{elim}\}$
 - ▶ Replace arrow $q_i \to q_j$ with $((R_1)(R_2)^*(R_3) \mid (R_4))$, where

Add Ray Regres of transition to the Coder

- $ightharpoonup R_3$ is the RegEx on transition $q_{elim} o q_i$
- $lackbox{ }R_4$ is the RegEx on transition $q_i
 ightarrow q_j$
- 3. The transition between the start and the accept state is now a regular expression describing ${\cal L}$

OUTLINE

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Equivalence of FA and Regular Expressions

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Proving if a language is, or is not, regular

PROVING IF A LANGUAGE IS REGULAR or not

Recall the definition:

A SA A B TO THE EXITE XIM TO THE POPULATION OF THE PROPERTY OF THE PRO

Supple the prove it regular How code recording to the prove it?

Proving if a language is regular or not

SSAGAMENT PROJECT STANDED Which recognises it.

Supplied and supplied to the supplied of the s

- ► Devise a DFA which recognises it, or
- Add We Chat powcoder

PROVING IF A LANGUAGE IS REGULAR or not

Recall the definition: SANGAMENT PROTOCEXITS XIAM TO HELD which recognises it.

Supplied and supplied to the s

- Devise a DFA which recognises it, or
- Add eg Weichiat it powcoder

What if the language was not regular? How can we prove that no suitable automata exists? We can use the pumping lemma for regular langauges

Pumping s using y

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Suppose some string \underline{s} exists, passing through M:

- ► FArdet a Wie Cstheatthpowcoder
- ▶ from q_i back to q_i , using a string $y \neq \varepsilon$, then
- ▶ from q_i to some accept state $f \in F$, using a string z

Pumping s using y

Assignment Project Exam Help



Suppose some string \underline{s} exists, passing through M:

- ► FArde Wie Ghathpowcoder
- \blacktriangleright from q_i back to q_i , using a string $y \neq \varepsilon$, then
- ▶ from q_i to some accept state $f \in F$, using a string z

Then $s = xyz \in L$, and $xy^kz \in L$ for all k > 0e.g. if x = aa, y = b, z = c, then $\{aac, aabc, aabbc, ...\} \subseteq L$

Long strings in finite automata

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Suppose Mist Pwith states and $s \in L(M)$ but $d \in R^{n+1}$

Long Strings in finite automata

Assignment Project Exam Help



Suppose M is a DFW with n states, and $s \in L(M)$ but |a| = n + 1

Then there exists at least one state which was visited more than once (q_i) , and a substring $y \neq \varepsilon$ corresponding to the path followed between the two of those visits.

Long strings in finite automata

Assignment Project Exam Help



Suppose M is a DFW with n states, and $s \in L(M)$ but |A| = n + 1

Then there exists at least one state which was visited more than once (q_i) , and a substring $y \neq \varepsilon$ corresponding to the path followed between the two of those visits.

Hence we can $pump \ s$ to find other strings in the language

FINITE AUTOMATA, INFINITE LANGUAGES

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FINITE AUTOMATA, INFINITE LANGUAGES

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Supplettips in finitipowicoder.com

- ightharpoonup L is regular, so a DFA M exists which recognises it.
- L is an infinite set over a finite alphabet, so it must include a btaliolon votes at powcoder
- ► Therefore words exist which can be *pumped*

PUMPING LEMMA FOR REGULAR LANGUAGES

Assignment gether the sets F when the F pumping length) such that for any string $s \in L$ of length at least p, then s may be divided into three pieces, s = xyz, such that:

- 1. |y| = |y| = 0 (i.e. $y \neq \varepsilon$)
- 3. $|xy| \le p$

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If a language does not satisfy this lemma, then it cannot be regular

Using the pumping Lemma

We can (only) use the purping lemma to pipye that a language is 1 pipye is 1

- Proof by contradiction:

 1. Detail Proof by contrad
 - 2. Choose an appropriate string in the language
 - This is often the hardest part of the proof Wedust Work Market Brown Coder
 - 3. Apply the lemma to find a contradiction
 - 4. Thereby deduce that the assumption is false
 - ▶ i.e. The language cannot be regular

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Assignment $L = \{a^n b^n | n \ge 0\}$ is not regular Assignment examted Exam Help

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Show that $L = \{a^n b^n | n \ge 0\}$ is not regular ASSISSIMMENT TELLIPORT EXAMT Help

2. Then there exists some p > 0 satisfying the pumping lemma.

https://powcoder.com

Show that $L = \{a^n b^n | n \ge 0\}$ is not regular ASSISSIMMENT TELLIPORT EXAMT Help

2. Then there exists some p > 0 satisfying the pumping lemma.

- 3. Let $s = a^p b^p$ (note: the same p as above!) https://powcoder.com
 - Add WeChat powcoder

Assignment $L = \{a^n b^n | n \ge 0\}$ is not regular Assignment reparoject Exam Help

2. Then there exists some p > 0 satisfying the pumping lemma.

- 3. Let $s = a^p b^p$ (note: the same p as above!)
- 4. https://pow.coler.com

4.1 xy $z \in L$ for all $k \ge 0$ (i.e. we can pump y)

- 4.2 |y| > 0
- Add WeChat powcoder

Show that $L = \{a^n b^n | n \ge 0\}$ is not regular ASSISHMENT report Exam Help

2. Then there exists some p > 0 satisfying the pumping lemma.

- 3. Let $s = a^p b^p$ (note: the same p as above!)
- 4. In Expression Property 4.1 xy $z \in L$ for all $k \ge 0$ (i.e. we can pump y)
 - 4.2 |y| > 0
- 5. And by We Chat powcoder b's)

Assignment $E = \{a^n b^n | n > 0\}$ is not regular the pulled of the property of the pulled the pulled $E = \{a^n b^n | n > 0\}$ is not regular. Then there exists some p > 0 satisfying the pumping lemma.

- 3. Let $s = a^p b^p$ (note: the same p as above!)
- 4. https://powdeochricom

4.1 $xy z \in L$ for all $k \ge 0$ (i.e. we can pump y)

- 4.2 |y| > 0
- 5. The ddy We Chat powcoder b's
- 6. Let k=2. Then xy^kz has more a's than b's, so $xy^kz \not\in L$

Show that $L = \{a^n b^n | n \ge 0\}$ is not regular ASSISSIMPLE TOJECT Exam Help

- 2. Then there exists some $p \geq 0$ satisfying the pumping lemma.
- 3. Let $s = a^p b^p$ (note: the same p as above!)
- 4. In the present of the convergence of the conver
- 5. Addy We Chat powcoderb's)
- 6. Let k=2. Then xy^kz has more a's than b's, so $xy^kz \notin L$
- 7. Lines 6 and 4.1 form a contradiction, therefore the assumption is false (i.e. L is *not* regular.)

Introduction

So far we have seen two different, but equivalent, methods of State and Ingles in the Lione Gal regulax explesion. Telp which describe regular languages

We have a proven that some a grages, such as $\{0^n1^n\mid n\geq 0\}$, cannot be described using FA or RE.

Today we will introduce context-free grammars (CFG), which describe the last category of languages CNO context free languages

Later, will see grammars called *regular grammars*, which describe exactly *regular languages*

Grammars

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A granta p Set of pie Wicco 6 to 16 to 16 to 16 a language

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The language generated is the set of all strings which can be
derived from the grammar

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 $S \to 0S1$ Recursive case: if $S \in L$ then $0S1 \in L$

 G_1 generally specifically G_1 generally G_2 generally G_1 generally G_2 generally

How does it derive 0001112 Add WeChat powcoder

Assignment Project Exam Help

 $S \to 0S1$ Recursive case: if $S \in L$ then $0S1 \in L$

 G_1 generally specifically G_1 generally G_2 generally G_1 generally G_2 generally

How does it derive 0001112 How does it derive 0001112 hat powcoder

Assignment Project Exam Help

 $S \to 0S1$ Recursive case: if $S \in L$ then $0S1 \in L$

 G_1 generates an already know is not regular

How does it derive 0001112 have Chat powcoder Add wising rule $S \rightarrow 0S1$

Assignment Project Exam Help

S o 0S1 Recursive ca

Recursive case: if $S \in L$ then $0S1 \in L$

 G_1 generates an already know is not regular

How does it derive 0001112 $\overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 0001112}}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 0001112}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 0001112}}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 000112}}}{\overset{\text{How does it derive 000112}}}}} \overset{\text{How does it derive 000112}}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 000112}}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 000112}}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 000112}}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 000112}}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 000112}}}{\overset{\text{How does it derive 000112}}}} \overset{\text{How does it derive 000112}}}{\overset{\text{How does it derive 000112}}}}} \overset{\text$

 $\Rightarrow 00S11$

using rule $S \rightarrow 0S1$

Assignment Project Exam Help

 $S \rightarrow 0S1$ Recursive case: if $S \in L$ then $0S1 \in L$

 G_1 generates is an expectation of the property of the prop

How does it derive 0001112 hat powcoder Add wising rule $S \to 0S1$

 $\Rightarrow 00S11$

 $\Rightarrow 000111$

using rule $S \to 0S1$

using rule $S \rightarrow 01$

Assignment Project Exam Help

 $NounPhrase \rightarrow \mathsf{the}\ Noun$

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 $Verb \rightarrow likes \mid sees$

What And do Weenerheat powcoder

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 $NounPhrase \rightarrow \mathsf{the}\ Noun$

https://pp.ody.com

 $Verb \rightarrow \mathsf{likes} \mid \mathsf{sees}$

What An used do of general at powcoder { the girl likes the girl, the girl likes the ball,

the girl likes the girl, the girl sees the girl, the ball likes the girl, the ball sees the girl,

the girl sees the ball, the ball likes the ball, the ball sees the ball

Assignment Project Exam Help language

Non-termin s://powcoder.com

- ► A finite set of symbols used to generate the strings.
- * Add We Chat powcoder

Start symbol

► The variable used to start every derivation

Production rules

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substituted for a *variable*:

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Production rules

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substituted for a *variable*:

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A variable can have many rules:

Add gir We Chat powcoder

 $Noun \rightarrow \mathsf{ball}$

 $Noun \rightarrow \mathsf{quokka}$

Production rules

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substituted for a *variable*:

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A variable can have many rules: They can be written together:

Add gir We Chat powg coder kka

 $Noun \rightarrow \mathsf{ball}$

 $Noun \rightarrow \mathsf{quokka}$

ANOTHER EXAMPLE

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 $T \rightarrow a \mid b \mid \dots$ https://powcoder.com

This is a grammator lambda calculus expressions coder

The variables are S. That powcoder

- \triangleright S is the start variable
- ▶ The terminals are $a, b, ..., (,), \lambda, ...$ (i.e. atoms and operators)

Some common notational conventions

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- \blacktriangleright A, B, C, ... and S are variables
- hittps://plowcoder.com
- ightharpoonup ..., X, Y, Z are either terminals or variables
- ...A., dyc a very ing of terminals and/or variables
 $\alpha, \beta, \gamma, ...$ are strings of terminals and/or variables

NIL

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This https://powcoder.com

If you need to use both and they are different, then you could rename the dead We Chat powcoder

- ▶ $NIL = PAIR \ TRUE \ TRUE$, for Church Lists
- ► *NILTREE*, for your tree encoding

Example answer

 $(\mathit{HEAD}\ z)$ should be the head of list z

 $HEAD = \lambda z.FIRST (SECOND z)$

STEE SEAN IN THE INTERPOLATION OF THE LAX RAPITALITY, SEE 19 We just need to get the first expression from the second pair.

Example: head of $\{1, 2, 3\}$ should be 1

https://powcoder.com

- $= HEAD (CONS 1 \{2,3\})$ (list notation)
- $= HEAD (PAIR \ TRUE \ (PAIR \ (1 \ \{2,3\})))$ (defn. of CONS)
- = (AFORT (Ween atripowred (en. of HEAD
- $= FIRST (SECOND (PAIR TRUE (PAIR 1 \{2,3\}))))$
- $= FIRST (PAIR 1 \{2,3\}))$ (reduced SECOND)
- = 1 (reduced FIRST)

IMMUTABLE DATA STRUCTURES

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Data structures encoded in lambda calculus are immutable.

- ► https://powcoder.com
- ► Instead, we return a new expression

Example: Delete the second element of a list

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 $DELETE_SECOND = \lambda z.CONS (HEAD z) (TAIL (TAIL z))$ https://powcoder.com

- ► CONS to make a new list using:
- the head of the old list hat powcoder
- - ▶ i.e. we skipped the second element

Example: Insert e to the second position of a LIST

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INSERTED NO POWCOCE COM (TAIL z))

- CONS a new list using that powcoder

 - the tail of the old list

RECURSIVE DATA STRUCTURES

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► Each position has a reference (link) to the next one

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Church Lists are similar, except instead of linking to the next node, they link to the list which starts with the next node

- ► And twe Chat powcoder

 head is the element stored at the start of the list

 - ► tail is the sublist containing all the remaining elements

RECURSIVE DATA STRUCTURES

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Except instead of liviking to wingle their have definub-tree and a right sub-tree.

In you Asistent West That eep obwice of the which will take a number to store, and two trees (which will be the left and right children).

JAVA EXAMPLE

```
Assignment Project Exam Help
    public final Tree left;
    public final Tree right;
    https://powcoder.com.
      this . element = element;
     Add dg We Chat powcoder
```

MAKETREE in the assignment is like writing: new Tree(e,a,b);

RECURSIVE FUNCTIONS

Simple recursion, condition decides if you're at the base case

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You can have more complicated logic if you want:

- ▶ If x < 5 and y < 5 then y (base case)
- ▶ If x < 5 and $y \ge 5$ then f(1, x) (recursive case)
- ▶ If $x \ge 5$ and x = y then f(y, x) (recursive case)
- ▶ If $x \ge 5$ and $x \ne y$ then 3 (base case)

HELPER FUNCTIONS

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- ► To make long/complex expressions easier to read
- To reduce repetition if you need the expression in several plet ps.//powcoder.com

Example: dMAX function when atturn the larger of two numbers would be helpful when calculating the height of a tree

LISP

I discourage you from trying to directly implement your lambda

SECTION PROPERTY OF BY STATE PROPERTY OF THE P

1 recontet p.Sng//spowscoolerg.com

- ► A Church pair can be represented by a Lisp list with only two elements
- ► AndolistWeephat poweoder

Then you can just use standard Lisp list operations to manipulate your data, instead of needing to implement all your lambda calculus expressions directly.

LISP

OUTLINE

```
Don't forget to indentity Doode to make it easier to see what is 1p being applied to what. Most errors people have shown me were 1p just scope errors.
```

```
(defaulto of doing an if statement (defaulto statement (if (...);; some condition Add; We case at powcoder )
```

Assignment Project Exam Help https://powcoder.com ;; true 2 Add We Chat powcoder

LISP

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You don't need any notation we haven't provided in tutorials or lectures.

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Look back at the earlier two finds and solutions for some tode example Add Wechair powcoder

Regular Expressions

► What they are and how to use them

Assignment Project Exam Help Equivalence of FA and Regular Expressions

- Convert an NFA to a RegEx
- https://powcoder.com

Proving if a language is, or is not, regular

- Pumping Lemma

Grammars (basic concepts)

Lambda calculus revision