This assignment is due on Sunday Nov 22, 23:59 and has a coding part and a written part.

- Submit your written part (Problems 1 and 2) as a single pdf on Gradescope.
- Submit your code (Problem 3) on Ed.
- All work must be *done individually* without consulting anyone else's solutions in accordance with the University's "Academic Dishonesty and Plagiarism" policies.
- For clarifications and more details on all aspects of this assignment (e.g., level of justification expected, late penalties, repeated submissions, what to do if you are stuck, etc.) you are expected to regularly monitor the Ed Forum post "Assignment Guidelines".

**Problem 1.** Let  $\Sigma = \{a, b\}$  and consider the language  $L_1 \subseteq \Sigma^*$  of all strings of the form  $a^m u$  where  $m \geq 0$  and u has at most m many as in it. Thus, e.g., aababa and aabba and aa are in  $L_1$ , but aababaabb is not in  $L_1$ .

- 1. Give a context-free proper  $G_1/DOWCO$  the language  $L_1$ .
- 2. Explain why your grammar is correct.
- 3. Explain whether or not  $L_1$  is regular Project Exam Help

Assignment Project Exam Help Problem 2. Let his problem you will design a context-free grammar that generates the language associated with a non-negative integer pointer Let  $\{p, m\}$ . We say that a string  $w \in \Sigma^*$  is a valid counter string if, when read from left to right, and interpreting p as all the Sand powerful Endword from 0, the running sum is non-negative. For instance, ppm and pm and ppmmp are valid counter strings, but pmmp and mpp are not valid counter string.

- 2. Explain why your grammar is correct.
- 3. Explain whether or not  $L_2$  is regular.

**Problem 3.** In this problem you will implement the CYK algorithm and extend it to provide rightmost-derivations and detect ambiguous strings. Your algorithm will have three modes: membership, rightmost-derivation, and ambiguous. Input is read from standard input (stdin). The first line of input indicates which mode is to be executed. The remaining input is the data to act on. Examples of usage, and of input and output are provided in Appendix B.

#### 1. Membership mode

- Input: membership followed by a context-free grammar in Chomsky normalform followed by a sequence of input strings.
- Output: One line per input string, giving the string, a comma, and then 1 if the string is generated by the grammar and 0 otherwise.

#### 2. Rightmost-derivation mode

- Input: rightmost-derivation followed by a context-free grammar in Chomsky normal-form followed by an input string that is generated by the context-free grammar.
- Output: A sequence of lines, each line containing the next step of a *rightmost* derivation of the input string.

#### 3. Ambiguous mode

- Input: ambiguous followed by a context-free grammar in Chomsky normalform followed by a sequence of input strings.
- Output: One line per input string, giving the string, a comma, and then 1 if the string is ambiguous and 0 otherwise.

# https://powcoder.com

### A Marking

## Problem 1 (A marks) nment Project Exam Help

- The first part is for 16 marks. For full credit your context-free grammar should not be more complicated then record the record than the record
- The second part is for Amarka. For Juli eredit tour answer should be clear, and explain why your grammar only generates strings in L<sub>1</sub> and why it generates all strings in L<sub>1</sub>.
- The third partin for 10 marks. An explanation of replacity equires that you provide a DFA, NFA or RE for the language and prove it is correct. An explanation of non-regularity requires that you provide a proof using the PHP as in lectures.

### Problem 2 (25 Act of WeChat powcoder

- The first part is for 10 marks. For full credit your context-free grammar should not be more complicated than needed.
- The second part is for 5 marks. For full credit your answer should be clear, and should explain why your grammar only generates strings in  $L_2$  and why it generates all strings in  $L_2$ .
- The third part is for 10 marks. An explanation of regularity requires that you provide a DFA, NFA or RE for the language and prove it is correct. An explanation of non-regularity requires that you provide a proof using the PHP as in lectures.

#### Problem 3 (50 marks)

- For passing the test-cases:
  - 20 marks for membership mode
  - 10 marks for rightmost derivation mode
  - 10 marks for ambiguous mode.

You are not allowed to hard-code any of the test-cases.

- The remaining 10 marks are based on the overall quality of the code. Quality is judged based on our answers to questions such as:
  - How readable is the code? e.g. commenting, variable naming, space, line length, etc.

- Are the data structures appropriate to the problem? e.g. how the grammars are repre-
- Are the algorithms implemented in a reasonably efficient way?
- How much of the assignment was attempted.

#### $\mathbf{B}$ Input/Output formats

#### Input context-free grammar in Chomsky normal-form

A sequence of lines:

- 1. A comma separated list of variable symbols
- 2. A comma separated list of terminal symbols
- 3. The start variable
- 4. One or more lines of the form: https://powcoder.com • A -> B C
  - A -> a
  - A -> epsilon •
- 5. the string and SSignment Project Exam Help

```
For example Project Exam Help B, C, D, S, T Add WeChat powcoder
A,B,C,D,S,T
a,b
          https://powcoder.com
Τ
          Add WeChat powcoder
    epsilon
     C
    S
B ->
```

... represents the grammar:

```
T \rightarrow AB \mid BA \mid SS \mid AC \mid BD \mid \epsilon
 \mathbf{S} \to \mathbf{A}\mathbf{B} \mid \mathbf{B}\mathbf{A} \mid \mathbf{S}\mathbf{S} \mid \mathbf{A}\mathbf{C} \mid \mathbf{B}\mathbf{D}
\mathbf{C} \to \mathbf{SB}
\mathbf{D} 	o \mathbf{S} \mathbf{A}
\mathbf{A} \rightarrow a
\mathbf{B} \to b
```

#### Membership mode

- 1. The input is a sequence of lines:
  - (a) membership
  - (b) A context-free grammar in Chomsky normal-form (in the format described above)
  - (c) Several strings to check, one on each line, followed by end
- 2. The output is 1 or 0 for each input string, where 1 means the string is generated by the grammar and 0 means it is not, all followed by end.

Here is an example. If the input is:

```
membership
A,B,C,D,S,T
a,b
Τ
Τ
   Α
   В
     Α
             https://powcoder.com
   SS
 -> epsilon Assignment Project Exam Help
      ssignment Project Exam Help
Add WeChat powcoder
   S
   B D
   S B
         https://powcoder.com
   S A
 ->
end
aab
          Add WeChat powcoder
ababab
end
```

the output is:

```
0
1
end
```

#### Rightmost-derivation mode

- 1. The input is a sequence of lines:
  - (a) rightmost-derivation
  - (b) A context-free grammar in Chomsky normal-form (in the format described above)
  - (c) A single non-empty string to derive, followed by end
- 2. The output is a sequence of lines:
  - (a) Each line should be a non-empty string over the alphabet of variables and terminals
  - (b) The sequence of lines should represent a rightmost derivation in which each line yields the next
  - (c) The last line should be end

Here is an example. If the input is:

```
rightmost-derivation
A,B,C,D,S,T
a,b
Т
 ->
   A B
    В
     Α
   SS
 -> A C
 -> B D
 -> epsilon
 -> A B
   S
     S
   B D
   S B
               https://powcoder.com
B -> b
        Assignment Project Exam Help
ab
end
 a pos Assignment Project Exam Help
Add WeChat powcoder
Т
AΒ
          https://powcoder.com
```

which encodes the rightmost derivation that powcoder Add we characterise the rightmost derivation  $Ab \Rightarrow Ab \Rightarrow Ab$ 

of the string ab.

Αb ab end

#### Ambiguous mode

- 1. The input is a sequence of lines:
  - (a) ambiguous
  - (b) A context-free grammar in Chomsky normal-form (in the format described above)
  - (c) Several non-empty strings to check, one on each line, followed by end
- 2. The output is a sequence of lines:
  - (a) The output is 1 or 0 for each input string, where a 1 means the string is ambiguous, and a 0 that it is not

Here is an example. If the input is:

```
ambiguous
A,B,C,D,S,T
a,b
Т
Т
 -> A B
 -> B A
```

```
-> S S
 -> A C
 -> B D
 -> epsilon
 -> S S
      С
 -> S B
 -> S A
B -> b
end
ab
abab
  then the expected output is: https://powcoder.com
end
```

0 Assignment Project Exam Help 0 1

derivations.

https://powcoder.com

Add WeChat powcoder