

Relational Algebra (Part 2)

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Summary of Relational Operators

Operator	Notation	Meaning
Selection	$\sigma_{arphi}(R)$	choose rows
Projection Ass	ig-дүү Rroje	tc <mark>haose ddelp</mark> ns
Union Intersection Difference	Rttps://powco	
Cartesian product Join Natural-join	$R_1 \times R_2$ $R_1 \bowtie_{\varphi} R_2$ $R_1 \bowtie R_2$	combine tables
Renaming	$ \begin{array}{c c} \rho_{R'(A_1,,A_n)}(R) \\ \rho_{R'}(R) \\ \rho_{(A_1,,A_n)}(R) \end{array} $	rename relation and attributes

A Complete Set of Relational Operators

- The following six operators constitute a complete set:
 - selection σ ; Assignment Project Exam Help
 - projection π ; https://powcoder.com
 - renaming ρ ; Add WeChat powcoder
 - union ∪;
 - difference –;
 - Cartesian product ×.

A Complete Set of Relational Operators

- Six operators (i.e., selection σ , projection π , renaming ρ , union \cup , difference and Cartesian product \times) constitute a complete set.

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- It means that the other RA operators like intersection and join are not necessary and can hetexor/exection the section and join are not necessary and can hetexor/exection the section and join are not necessary and can hetexor/exection and join are necessary and present and the present and the
 - join: R₁ ⋈_{\varphi} R₂Adel_{\varphi} M₁eChat powcoder
 - intersection: $R_1 \cap R_2 = R_1 (R_1 R_2)$
- Hence, intersection and join do not increase the expressive power of RA.
- Nonetheless it is important to include intersection and join because they are convenient to use and commonly applied in database applications.

Relational Algebra Queries

- The output of each RA operation is a relation, which can be used again as the input for another RA operation.
- RA operations can be nested to arbitrary depth for expressing complex queries, as in antimetic.
 - Parentheses and typece denote the intermediate order of evaluation: from highest to lowest: $\{\sigma, \pi, \rho\}$, $\{\times, \bowtie\}$, $\{\cap\}$, $\{\cup, -\}$
 - Operators with the dame precede was evaluated from left to right.
 - Use brackets if you are not sure.
- A query in RA is a sequence of RA operations and each RA operation takes one or two relations as its input and produces one relation as its output.
- Different from SQL, RA considers relations as sets (not multisets as in SQL). Hence, relations produced by an RA operation have no duplicate tuples.

Hints for Writing RA Queries

- Firstly, identify which relations need to be involved, while ignoring the rest.
- Then break the answer down by considering intermediate relations, i.e., queries may be expressed as a sequence of assignment statements.

Example: $R := \pi_{HTeam,GTeam}(\sigma_{HScore=1}(\rho_{(HTeam,HScore,GScore,GTeam)}(SOCCER)))$ https://powcoder.comUse good names for intermediate relations;

- Keep track of attributed to the tra
- When combining relations, check attribute names and make sure that:
 - attributes that should match are to match.
 - attributes that shouldn't match are not to match.
- When using set operations, make sure that two relations of an operation have the same type (i.e., type compatibility).



• Given the following relation schema:

STUDENT={StudentID, Name, DoB}

• Query 1: Find parison students wish to the with the parison of t

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STUDENT			
StudentID	Name	DoB	
457	Lisa	18-Oct-1993	
458	Mike	16-May-1990	
459	Peter	18-Oct-1993	

• Given the following relation schema:

```
STUDENT={StudentID, Name, DoB}
```

• Query 1: Find parison students wie have the light though Show their names.

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```
\pi_{R_1.Name,R_2.Name}(\sigma_{R_1.StudentID} < R_2.StudentID(\sigma_{R_1.DoB} = R_2.DoB(\rho_{R_1}(STUDE))) < Coder
```

```
SELECT R_1.name, R_2.name

FROM Student AS R_1, Student AS R_2

WHERE R_1.DoB = R_2.DoB AND R_1.StudentID < R_2.StudentID;
```

- Why do we need $\sigma_{R_1.StudentID < R_2.StudentID}$ in the above query?
- Why do we need to use renaming in the above query?

• Given the following relation schema:

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Query 1: Find pairs of students who have the same birthday. Show their names.
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- (1). $\pi_{R_1.Name,R_2.Name}(\sigma_{R_1.StudentID < R_2.StudentID}(\sigma_{R_1.DoB=R_2.DoB}(\rho_{R_1}(STUDENT) \times \rho_{R_2}(STUDENT)))$
- (2). $\pi_{Name,Name'}(\sigma_{StudentID < StudentID'}(STUDENT \bowtie \rho_{S(StudentID',Name',DoB)}(STUDENT))$

 Query 1: Find pairs of students who have the same birthday. Show their names.

(1).
$$\pi_{R_1.Name,R_2.Studentib}$$
 (Project Example 1.5 tudentib (

If evaluating our queries over the following relation, what will be the result?

STUDENT		
StudentID	Name	DoB
457	Lisa	18-Oct-1993
458	Mike	16-May-1990
459	Peter	18-Oct-1993

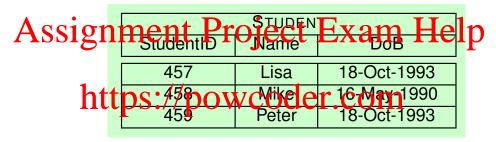


• Query 1 (solution 1): $\pi_{R_1.Name,R_2.Name}(\sigma_{R_1.StudentID} < R_2.StudentID}(\sigma_{R_1.DoB=R_2.DoB}(\rho_{R_1}(STUDENT)))$.



	A del (SWE) Hara (STUDENT) der				
R ₁ .StudentID	R_1 .Name	R₁.DoB	R ₂ .StudentID	R_2 .Name	R ₂ .DoB
457	Lisa	18-Oct-1993	457	Lisa	18-Oct-1993
457	Lisa	18-Oct-1993	458	Mike	16-May-1990
457	Lisa	18-Oct-1993	458	Peter	18-Oct-1993
458	Mike	16-May-1990	457	Lisa	18-Oct-1993
458	Mike	16-May-1990	458	Mike	16-May-1990
458	Mike	16-May-1990	458	Peter	18-Oct-1993
458	Peter	18-Oct-1993	457	Lisa	18-Oct-1993
458	Peter	18-Oct-1993	458	Mike	16-May-1990
458	Peter	18-Oct-1993	458	Peter	18-Oct-1993

• Query 1 (solution 1): $\pi_{R_1.Name,R_2.Name}(\sigma_{R_1.StudentID} < R_2.StudentID(\sigma_{R_1.DoB} = R_2.DoB(\rho_{R_1}(STUDENT)))$.



$R' = \sigma_R A_0 c_0 c_0 c_0 c_0 c_0 c_0 c_0 c_0 c_0 c$					
R ₁ .StudentID	R_1 .Name	R ₁ .DoB	R ₂ .StudentID	R ₂ .Name	R ₂ .DoB
457	Lisa	18-Oct-1993	457	Lisa	18-Oct-1993
457	Lisa	18-Oct-1993	459	Peter	18-Oct-1993
458	Mike	16-May-1990	458	Mike	16-May-1990
459	Peter	18-Oct-1993	457	Lisa	18-Oct-1993
459	Peter	18-Oct-1993	459	Peter	18-Oct-1993

π R $_1$. Name , R $_2$. Name $(\sigma$ R $_1$. StudentID $<$ R $_2$. StudentID $(R'))$		
R ₁ .Name	R ₂ .Name	
Lisa	Peter	

• Query 1 (solution 2): $\pi_{Name,Name'}(\sigma_{StudentID < StudentID'}(STUDENT))$.



RACTUDENTE Chatchen Ware, de l'STUDENT) StudentID Name DoB StudentID' Name' 18-Oct-1993 459 457 Lisa Peter 459 Peter 18-Oct-1993 457 Lisa 459 18-Oct-1993 459 Peter Peter 18-Oct-1993 457 457 Lisa Lisa 458 16-May-1990 Mike 458 Mike

$\pi_{Name,Name'}(\sigma_{StudentID} < StudentID'(R'))$		
Name	Name'	
Lisa	Peter	

• Given the following relation schemas:

STUDENT={StudentID, Name, DoB}
ENROL={StudentID, CourseNo, Semester, EnrolDate}

• Query 2: Which stigents have her interm land purse? Show their IDs and names.

h	https://powcoder.com		
A	StudentID Name DoB		
ſ	456	Tom	Wcoder 02-Jan-1991
	457	Lisa	18-Oct-1993
	458	Mike	16-May-1990

Enrol			
StudentID	CourseNo	Semester	EnrolDate
456	COMP2400	2010 S2	02-Jul-2010
458	COMP2400	2010 S2	23-Jun-2010
458	COMP2600	2010 S2	05-Aug-2010



• Given the following relation schemas:

STUDENT={StudentID, Name, DoB}
ENROL={StudentID, CourseNo, Semester, EnrolDate}

• Query 2: Which stigents and names.

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Hints:

- (1) All the students
- (2) Students who have enrolled in at least one course

Answer: Students in the result (1) but not in the result (2).

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STUDENT={StudentID, Name, DoB}
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 - (1) All the students https://powcoder.com

Add We Chrantp (STUDENT)

(2) Students who have enrolled in at least one course

$$R_2 := \pi_{StudentID}(\mathsf{ENROL})$$

Answer: Students in the result (1) but not in the result (2)

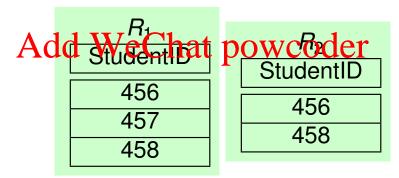
$$\pi_{StudentID,Name}((R_1-R_2)\bowtie \mathsf{STUDENT})$$

- Query 2: Which students have never enrolled in any course? Show their IDs and names.
- If evaluating our query over the following relations, what will be the result?
 - $R_1 := \pi_{St} A_{SS}$ Significant Project Exam Help
 - $R_2 := \pi_{StudentID}(ENROL)$
 - π_{StudentID, Name}((https://powdeficom

Add We Chat POWCOGER		
456	Tom	02-Jan-1991
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π StudentID,Na	$_{me}((R_1-R_2)\bowtie STUDENT)$
StudentID	Name
457	Lisa

• Given the following relation schemas:

STUDENT={StudentID, Name, DoB}
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• Query 3: Which stigents have bring out of the country of the cou

https://powcoder.com		
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456	Tom	Wcoder 02-Jan-1991
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Enrol				
StudentID	CourseNo	Semester	EnrolDate	
456	COMP2400	2010 S2	02-Jul-2010	
457	COMP2400	2010 S2	08-Jul-2010	
458	COMP2400	2010 S2	23-Jun-2010	
458	COMP2600	2010 S2	05-Aug-2010	



Given the following relation schemas:

STUDENT={StudentID, Name, DoB}
ENROL={StudentID, CourseNo, Semester, EnrolDate}

• Query 3: Which still the Project of the Project of the Course COMP2400? Show their IDs and names.

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Hints: Add WeChat powcoder

- (1) Students who have enrolled in the course COMP2400.
- (2) Students who have enrolled in a course but not COMP2400.

Answer: Students in the result (1) but not in the result (2).

• Given the following relation schemas:

```
STUDENT={StudentID, Name, DoB}
ENROL={StudentID, CourseNo, Semester, EnrolDate}
```

- Query 3: Which still the Printer of the Printer o
 - (1) Students who have enrolled in the course COMP2400.

$$R_1: Add Mic Chate power dor (ENROL))$$

(2) Students who have enrolled in a course but not COMP2400.

$$R_2 := \pi_{StudentID}(\sigma_{CourseNo \neq `COMP2400'}(ENROL))$$

Answer: Students in the result (1) but not in the result (2).

$$\pi_{StudentID,Name}((R_1 - R_2) \bowtie \mathsf{STUDENT}) = \\ \pi_{StudentID,Name}((\pi_{StudentID}(\sigma_{CourseNo=`COMP2400`}(\mathsf{ENROL})) \\ -\pi_{StudentID}(\sigma_{CourseNo\neq`COMP2400`}(\mathsf{ENROL}))) \bowtie \mathsf{STUDENT})$$

- Query 3: Which students have only enrolled in the course COMP2400? Show their IDs and names.
- If evaluating our query over the following relations, what will be the result?

 - $R_1 := \pi_{StudentID}(\sigma_{CourseNo='COMP2400'}(ENROL))$ $R_2 := \pi_{StudentID}(\sigma_{CourseNo='COMP2400'}(ENROL))$
 - $\pi_{StudentID,Name}((R_1 R_2) \bowtie STUDENT)$

https://powcoder.com		
StudentID	Name	DoB
Add ₄₅₆ ec	natapo	W620d F1991
457	Lisa	18-Oct-1993
458	Mike	16-May-1990

ENROL				
StudentID	CourseNo	Semester	EnrolDate	
456	COMP2400	2010 S2	02-Jul-2010	
457	COMP2400	2010 S2	08-Jul-2010	
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458	COMP2600	2010 S2	05-Aug-2010	

- Query 3: Which students have only enrolled in the course COMP2400?
 Show their IDs and names.
- If evaluating our query over the following relations, what will be the result?
 - $R_1 := \pi_{StudentID}(\sigma_{CourseNo='COMP2400'}(ENROL))$
 - $R_2 := \pi_{Stassignment} Project(Exam)Help$
 - $\pi_{StudentID,Name}((R_1 R_2) \bowtie STUDENT)$ • https://powcoder.com



$\pi_{StudentID,Name}((R_1-R_2)\bowtie STUDENT)$		
StudentID	Name	
456	Tom	
457	Lisa	



More Hints for Writing RA Queries

Pay attention to keywords like not, never, only, always, exactly, etc. which often indicates the use of **difference** in the corresponding RA queries.

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To show "never":

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 Find all the (combinations of) tuples that are involved.
- Use difference 40 do Wast Those that Mark Colored.
- To show "only" and "always":
 - Find all the (combinations of) tuples that are involved.
 - Use difference to subtract those that didn't always occur.

Equivalence of RA and SQL Queries (1)

Each RA query can be easily re-written in SQL, or vice versa.

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- Selection: $\sigma_{\varphi}(R)$ corresponds to SELECT DISTINCTPS: FROM CORRESPOND
- Projection: $\pi_A A dd$ (W) corresponds to der SELECT DISTINCT A_1, \ldots, A_n FROM R;
- Renaming: $\rho_{S(B_1,...,B_n)}(R)$ (with attributes $A_1,...,A_n$ in R) corresponds to

SELECT A_1 AS B_1, \ldots, A_n AS B_n FROM R AS S;

Equivalence of RA and SQL Queries (2)

• Union: $R_1 \cup R_2$ corresponds to

```
SELECT * FROM R_1 UNION SELECT * FROM R_2 Assignment Project Exam Help Intersection: R_1 \cap R_2 corresponds to
```

SELECT * FRONTIPS IN PERSECULAR FROM R2

• Difference: $R_1 - R_2$ (with attributes A_1, \ldots, A_n) corresponds to Add WeChat powcoder SELECT * FROM R_1 EXCEPT SELECT * FROM R_2 SELECT DISTINCT * FROM R_1 WHERE NOT EXISTS

(SELECT * FROM R_2

WHERE $R_1.A_1 = R_2.A_1$ AND ... AND $R_1.A_n = R_2.A_n$)

SQL eliminates duplicate tuples in the resulting relations of set operations UNION, INTERSECT and EXCEPT.

Equivalence of RA and SQL Queries (3)

- Cartesian Product: $R_1 \times R_2$ corresponds to SELECT Assignment Project Exam Help
- Join: $R_1 \bowtie_{\varphi} R_2$ the theorem is a specific production of the second sec

```
SELECT DISTINCT * FROM R_1 INNER JOIN R_2 ON \varphi; (\varphi may contain =, <, \le, >, \ge, \ne)
```

• Natural-Join: $R_1 \bowtie R_2$ corresponds to

```
SELECT DISTINCT * FROM R_1 NATURAL JOIN R_2;
```

Outer joins are not considered in the traditional relational algebra, as well as aggregation.



Summary

RA is a **procedural query language** defined in the relational model.

An RA query it sets suggester at procedure fox against flucting the result (i.e., implement the query).

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RA is not used as a query language by users.

- Add WeChat powcoder
 RA is used for the internal representation and processing of SQL queries in relational DBMSs, which is a basis of query optimisation techniques.
- Thus, to understand how SQL queries are processed and how they can be optimised, we first need to understand relational algebra.