



Assignment Project Exam Help

Normalisation – Part 2

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From BCNF to 3NF

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Facts

(1) There exists an algorithm that can generate a **lossless decomposition** into BCNF.

(2) However, a BCNF-decomposition that is **both lossless and dependency-preserving** does not always exist.

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- 3NF is a **less restrictive normal form** such that a lossless and dependency preserving decomposition can always be found.



3NF - Definition

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- A relation schema R is in **3NF** if whenever a non-trivial FD $X \rightarrow A$ holds in R , then X is a **superkey** or A is a **prime attribute**.
- 3NF allows data redundancy but excludes relation schemas with certain kinds of FDs (i.e. partial FDs and transitive FDs).

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Normalisation to 3NF

- Consider the following FD of ENROL:

- $\{\text{StudentID}, \text{CourseNo}, \text{Semester}\} \rightarrow \{\text{ConfirmedBy_ID}, \text{StaffName}\},$
- $\{\text{ConfirmedBy_ID}\} \rightarrow \{\text{StaffName}\}.$

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StudentID	CourseNo	Semester	ConfirmedBy_ID	StaffName
123456	COMP2400	2010 S2	u12	Jane
123458	COMP2400	2008 S2	u13	Linda
123458	COMP2600	2008 S2	u13	Linda

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- Is ENROL in 3NF?

- $\{\text{StudentID}, \text{CourseNo}, \text{Semester}\}$ is the only key.
- ENROL is not in 3NF because $\{\text{ConfirmedBy_ID}\} \rightarrow \{\text{StaffName}\},$
 $\{\text{ConfirmedBy_ID}\}$ is not a superkey and $\{\text{StaffName}\}$ is not prime attribute.



Normalisation to 3NF

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- Algorithm for a dependency-preserving and lossless 3NF-decomposition

Input: a relation schema R and a set Σ of FDs on R .

Output: a set S of relation schemas in 3NF each having a set of FDs

- Compute a **minimal cover** Σ' for Σ and start with $S = \emptyset$
- Group FDs in Σ' by their left-hand-side attribute sets
- For each distinct left-hand-side X_i of FDs in Σ' that includes $X_i \rightarrow A_1, X_i \rightarrow A_2, \dots, X_i \rightarrow A_k$
 - Add $R_i = X_i \cup \{A_1\} \cup \{A_2\} \dots \cup \{A_k\}$ to S
- Remove all redundant ones from S (i.e., remove R_i if $R_i \subseteq R_j$)
- if S does not contain a superkey of R , add a key of R as R_0 into S .
- Project the FDs in Σ' onto each relation schema in S

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$R_1 = X_1 A_1 \dots A_K$
...
 $R_n = X_n A$

$X_1 \rightarrow A_1$
...
 $X_n \rightarrow A$

\dots

$X_1 \rightarrow A_K$
...

A minimal cover

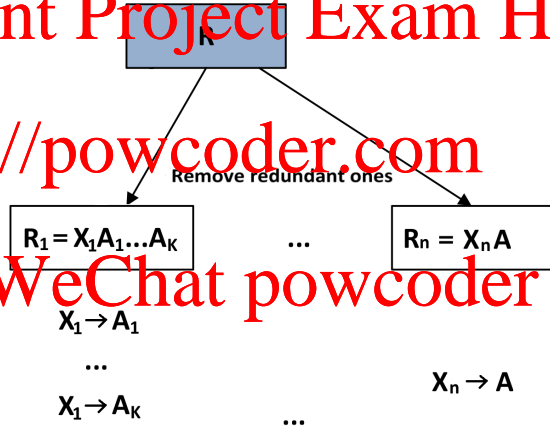


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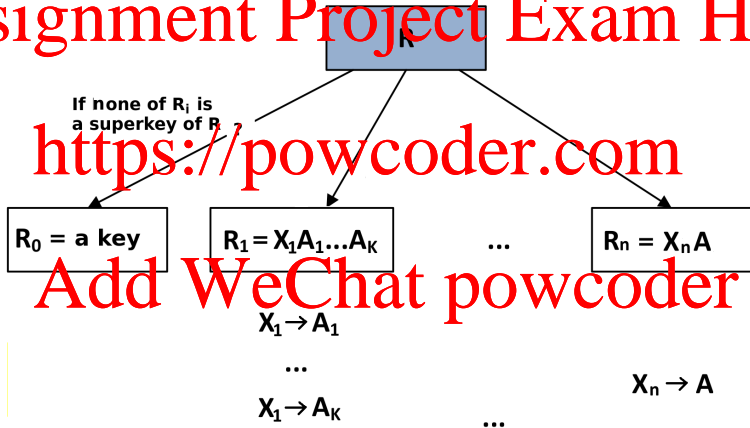
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Minimal Cover – The Hard Part!

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Let Σ be a set of FDs. A **minimal cover** Σ_m of Σ is a set of FDs such that

- 1 Σ_m is equivalent to Σ , i.e., start with $\Sigma_m = \Sigma$;
- 2 **Dependent:** each FD in Σ_m has only a single attribute on its right hand side, i.e., replace each FD $X \rightarrow \{A_1, \dots, A_k\}$ in Σ_m with $X \rightarrow A_1, \dots, X \rightarrow A_k$;
- 3 **Determinant:** each FD has as few attributes on the left hand side as possible, i.e., for each FD $X \rightarrow A$ in Σ_m , check each attribute B of X to see if we can replace $X \rightarrow A$ with $(X - B) \rightarrow A$ in Σ_m ;
- 4 Remove a FD from Σ_m if it is redundant.



Minimal Cover

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Theorem:

The minimal cover of a set of functional dependencies Σ always exists but is not necessarily unique.

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- **Examples:** Consider the following set of functional dependencies:

$$\Sigma = \{A \rightarrow BC, B \rightarrow C, C \rightarrow A, C \rightarrow AB\}$$

Σ has two different minimal covers:

- $\Sigma_1 = \{A \rightarrow B, B \rightarrow C, C \rightarrow A\}$
- $\Sigma_2 = \{A \rightarrow C, C \rightarrow B, B \rightarrow A\}$



Minimal Cover - Examples

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- The set $\{A \rightarrow B, B \rightarrow C, A \rightarrow C\}$ can be reduced to $\{A \rightarrow B, B \rightarrow C\}$ because $\{A \rightarrow C\}$ is implied by the other two.
- Given the set of FDs $\Sigma = \{B \rightarrow A, D \rightarrow A, AB \rightarrow D\}$, we can compute the minimal cover of Σ as follows:

- start from Σ ;
- check whether all the FDs in Σ have only one attribute on the right hand side (look good);
- determine if $AB \rightarrow D$ has any redundant attribute on the left hand side ($AB \rightarrow D$ can be replaced by $B \rightarrow D$);
- look for a redundant FD in $\{B \rightarrow A, D \rightarrow A, B \rightarrow D\}$ ($B \rightarrow A$ is redundant);

Therefore, the minimal cover of Σ is $\{D \rightarrow A, B \rightarrow D\}$.



Normalisation to 3NF – Example

- Consider ENROL again:

- $\{ \text{StudentID}, \text{CourseNo}, \text{Semester} \} \rightarrow \{ \text{ConfirmedBy_ID}, \text{StaffName} \}$
- $\{ \text{ConfirmedBy_ID} \} \rightarrow \{ \text{StaffName} \}$

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StudentID	CourseNo	Semester	ConfirmedBy_ID	StaffName
..

- Can we normalise ENROL into 3NF by a lossless and dependency preserving decomposition?

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Normalisation to 3NF – Example

- Consider ENROL again:

- $\{\text{StudentID}, \text{CourseNo}, \text{Semester}\} \rightarrow \{\text{ConfirmedBy_ID}, \text{StaffName}\}$
- $\{\text{ConfirmedBy_ID}\} \rightarrow \{\text{StaffName}\}$

StudentID	CourseNo	Semester	ConfirmedBy_ID	StaffName
..

- A **minimal cover** is $\{\{\text{StudentID}, \text{CourseNo}, \text{Semester}\} \rightarrow \{\text{ConfirmedBy_ID}\}, \{\text{ConfirmedBy_ID}\} \rightarrow \{\text{StaffName}\}\}$.

- Hence, we have:

- $R_1 = \{\text{StudentID}, \text{CourseNo}, \text{Semester}, \text{ConfirmedBy_ID}\}$ with $\{\text{StudentID}, \text{CourseNo}, \text{Semester}\} \rightarrow \{\text{ConfirmedBy_ID}\}$
- $R_2 = \{\text{ConfirmedBy_ID}, \text{StaffName}\}$ with $\{\text{ConfirmedBy_ID}\} \rightarrow \{\text{StaffName}\}$
- Omit R_0 because R_1 is a superkey of ENROL.



3NF - Exercises

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- Let us do some exercises for the 3NF-decomposition algorithm

• **Exercise 1:** $R = \{A, B, C, D\}$ and $\Sigma = \{A \rightarrow B, B \rightarrow C, AC \rightarrow D\}$:

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• **Exercise 2:** $R = \{A, B, C, D\}$ and $\Sigma = \{AD \rightarrow B, AB \rightarrow C, C \rightarrow B\}$:

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3NF - Exercises

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- Let us do some exercises for the 3NF-decomposition algorithm

• **Exercise 1:** $R = \{A, B, C, D\}$ and $\Sigma = \{A \rightarrow B, B \rightarrow C, AC \rightarrow D\}$:

- $\{A \rightarrow B, B \rightarrow C, A \rightarrow D\}$ is a minimal cover.
- $R_1 = ABD, R_2 = BC$ (omit R_0 because R_1 is a superkey of R)
- The 3NF-decomposition is $\{ABD, BC\}$.

• **Exercise 2:** $R = \{A, B, C, D\}$ and $\Sigma = \{AD \rightarrow B, AB \rightarrow C, C \rightarrow B\}$:

- Σ is its own minimal cover.
- $R_1 = ABD, R_2 = ABC, R_3 = CB$ (omit R_3 because $R_3 \subseteq R_2$ and omit R_0 because R_1 is a superkey of R)
- The 3NF-decomposition is $\{ABD, ABC\}$.

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