COMP2610 / COMP6261 - Information Theory Assignment Project Exam Help

https://powcoder.com



7 August 2018

Last time

Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder Bayesian parameter etimation

This time

Assignment Project Exam Help

• https://powcoder.com

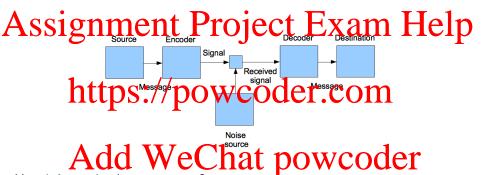
Add WeChat powcoder • Some basic properties of entropy

Outline

- Information Content & Entropy
- Entropy of a Random Variable ssignment Project Exam Help
- Examples: Bernoulli and Categorical Random Variables
 - Maximum Entropy
- powcoder.com
 - Average Code Length
 - Minimum Number of Binary Questions
- Joint Entropy, Conditional Entropy and Profile Coder
- An Axiomatic Characterisation
- Wrapping up

Recap: A General Communication System

How informative is a message?



5/39

Information Content: Informally

Say that a message comprises a single bit (one binary random variable)

Whether or not a coin comes up heads

Assignmento Project Exam Help

Informally, the amount of information in such a message is:

- How unexpected of /surprising, an outebase of random variable is
 - If a coin comes up Heads 99.99% of the time, the message "Tails" is much more informative than "Heads"
 - If I believe my favourite horse will win with 99.99% probability, it is explicitly to have did not at powcoder

Information Content: Informally

Say that a message comprises a single bit (one binary random variable)

Whether or not a coin comes up heads

Assignmento Project Exam Help

Informally, the amount of information in such a message is:

- How unexpected of /surprising, an outebase of random variable is
 - If a coil comes up Heads 99.99% of the time, the message "Tails" is much more informative than "Heads"
 - If I believe my favourite horse will win with 99.99% probability, it is supplying to wood did not at 100 WCOCCT
- How predictable a random variable is
 - ▶ If a coin comes up Heads 99.99% of the time, we can predict the next message as "Heads" and be right most of the time
 - If I believe my favourite horse will win with 99.99% probability, then I believe predicting so to be right most of the time

Information Content: Formally

Intuitively, we measure information of a message in relation to the other

Anessages we could have see Project Exam Help

The property of the project of the

• The message 1 is informative when there is a good chance I might have see pS://powcoder.com

How can we formalise and thus measure information content?

- Information Context of an out of the must leave on its of the fility
- Information content of a random variable must depend on its probability distribution

Information Content of an Outcome: Definition

Assignment Project Exam Help

e.g. $\mathcal{X} = \{\text{Yes, No, Maybe}\}\$ Let p(x) denote the probability of outcome $x \in \mathcal{X}$

The information contents of a cutomat prower and
$$h(x) = \log_2 \frac{1}{p(x)}$$

Information Content of an Outcome: Properties

Assignment Project Exam Help

Outcomes that are rare are deemed to contain more information

Choice ohtatiph Spasis parity coder.com

• If we use \log_2 we measure information in bits

What about the din wise Chat powcoder

Entropy of a Random Variable: Definition

Let X be a discrete r.v. with possible outcomes Fram Help The entropy or the random variable X is the average information content of the outcomes:

https://powcoder.com
$$= \sum_{x} \rho(x) \cdot \log_2 \frac{1}{\rho(x)}$$
Add WeChat powcoder

where we define $0 \log 0 \equiv 0$, as $\lim_{p\to 0} p \log p = 0$.

Some Basic Properties

Non-negativity:

Assignment Projecto Exam Help $\Rightarrow \sum_{x} \rho(x) \log \frac{1}{\rho(x)} \ge 0$ https://powcoder.com

Add WeChat powcoder

Some Basic Properties

Non-negativity:

Assignment Project Lam Help
$$\Rightarrow \sum_{x} p(x) \log \frac{1}{p(x)} \ge 0$$

https://powcoden.com

• Change of base:

Add We Chat powcoder
$$= \sum_{x} p(x) \log_{b} p(x)$$

$$H_b(X) = \log_b a H_a(X)$$

- If we use log₂ the units are called bits
- If we use natural logarithm the units are called nats

Unrolling the Definition

Assignment, Project Exam Help

Pick a rail don topicome x, and see how to repetit probability in

Average information content of each outcome

only on their probabilities of the outcomes probabilities of the o

• Contrast with expectation $\mathbb{E}[X] = \sum_{x} x \cdot p(X = x)$.

What Does Entropy "Mean"?

Not a well posed question.

Angony coen nagreeme interior protect of bury to name to the period of t

Rare outcomes provide more information

Add
$$WeChat^2 powcoder$$

We will see some examples where our definition of entropy arises naturally The main justification is the results we can obtain with it.

- Information Content & Entropy
 - Entropy of a Random Variable
 - Some Basic Properties

Assignment Projector Exam Help Maximum Entropy

- Entro https://powcoder.com
 - Minimum Number of Binary Questions
- Add WeChat powcoder
- 5 An Axiomatic Characterisation
- 6 Wrapping up

Example 1 — Bernoulli Distribution

Let $X \in \{0,1\}$ with $X \sim \text{Bern}(X|\theta)$

Assignment Project Exam Help

Example 1 — Bernoulli Distribution

```
Let X \in \{0,1\} with X \sim \text{Bern}(X|\theta) and \theta = p(X=1)
```

Assignment Project Exam Help

https://powcoder.com

Add WeChat, powcoder

Example 1 — Bernoulli Distribution

Let $X \in \{0,1\}$ with $X \sim \text{Bern}(X|\theta)$ and $\theta = p(X=1)$

Assignment Project Exam Help https://powcoder.com

Add WeChat, powcoder

Concave function of the distribution

Example 1 — Bernoulli Distribution

Let $X \in \{0,1\}$ with $X \sim \text{Bern}(X|\theta)$ and $\theta = p(X=1)$

Assignment Project Exam Help

https://powcoder.com

Add WeChat, powcoder

- Concave function of the distribution
- Minimum entropy \rightarrow no uncertainty about X, i.e. $\theta = 1$ or $\theta = 0$

Example 1 — Bernoulli Distribution

Let $X \in \{0,1\}$ with $X \sim \text{Bern}(X|\theta)$ and $\theta = p(X=1)$

Assignment Project Exam Help

https://powcoder.com

Add WeChat, powcoder

- Concave function of the distribution
- Minimum entropy \rightarrow no uncertainty about X, i.e. $\theta = 1$ or $\theta = 0$
- ullet Maximum when o complete uncertainty about X, i.e. heta=0.5

Example 1 — Bernoulli Distribution

Let $X \in \{0,1\}$ with $X \sim \text{Bern}(X|\theta)$ and $\theta = p(X=1)$

Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

- Concave function of the distribution
- Minimum entropy \rightarrow no uncertainty about X, i.e. $\theta = 1$ or $\theta = 0$
- Maximum when \rightarrow complete uncertainty about X, i.e. $\theta = 0.5$
- For $\theta = 0.5$ (e.g. a fair coin) $H_2(X) = 1$ bit.

Example 2

Assignment Project Exam Help

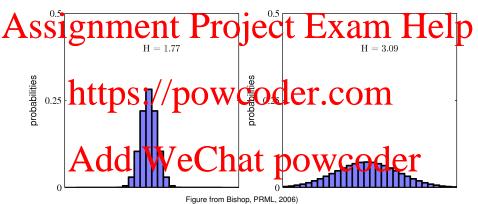
Consider a random variable *X* with uniform distribution over 32 outcomes:

The entropy of this ry is/given by:
$$H(X) = -\sum_{32} p(i) \log_2 p(i) = -\sum_{i=1}^{32} \frac{1}{32} \log_2 \frac{1}{32} = \log_2 32 = 5 \text{ bits.}$$

$$Add We Chat powcoder$$

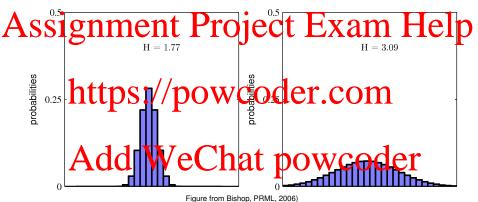
Example 3 — Categorical Distribution

Categorical distributions with 30 different states:



Example 3 — Categorical Distribution

Categorical distributions with 30 different states:



• The more sharply peaked the lower the entropy

Example 3 — Categorical Distribution

Categorical distributions with 30 different states:

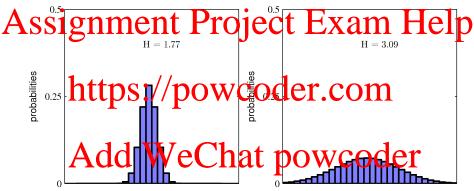


Figure from Bishop, PRML, 2006)

- The more sharply peaked the lower the entropy
- The more evenly spread the higher the entropy

Example 3 — Categorical Distribution

Categorical distributions with 30 different states:

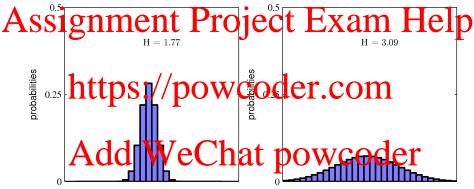


Figure from Bishop, PRML, 2006)

- The more sharply peaked the lower the entropy
- The more evenly spread the higher the entropy
- Maximum for *uniform* distribution: $H(X) = -\log \frac{1}{30} \approx 3.40$ nats
 - When will the entropy be minimum?

Maximum Entropy

Assign a discrete variable paking on values from the set \mathcal{X} Help Let probability of each state, with \mathcal{X} \mathcal{X} \mathcal{X}

https://powcoder.com

Add WeChat powcoder

Maximum Entropy

Assignment Paking on values From the set \mathcal{X} Help

• Den Hethe vector of probabilities with der.com

Add WeChat powcoder

Maximum Entropy

Assider a discrete variable Paking on values From the set & Help

• Den te the vector of probabilities with the community of the positive of the

Note $log_2|\mathcal{X}|$ is the number of bits needed to describe an outcome of X

- Information Content & Entropy
 - Entropy of a Random Variable
 - Some Basic Properties

Assignment Project Exam Help

- Maximum Entropy
- Entropy as Code Length Owcoder.com
 Average Gode Length Owcoder.com
 - Minimum Number of Binary Questions
- Add WeChat powcoder
- 5 An Axiomatic Characterisation
- 6 Wrapping up

Example 4 (from Cover & Thomas, 2006) — 1 of 3

Consider a horse race with 8 horses participating:

Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

Example 4 (from Cover & Thomas, 2006) — 1 of 3

Consider a horse race with 8 horses participating:

Assignment Project Exam Help

Each horse is equally likely to win. How many bits will we need to transmit the identity of the winning horse? 000, 001, 010, ..., 111
 DOWCOGET.COM

Add WeChat powcoder

Example 4 (from Cover & Thomas, 2006) — 1 of 3

Consider a horse race with 8 horses participating:

Assignment Project Exam Help

• Each horse is equally likely to win. How many bits will we need to transmit the identity of the winning horse? 000, 001, 010, ..., 111

Note that the entropy of the corresponding random variable, say X, is:

Add WeChat powcoder

$$H(X) = 8 \times \frac{1}{8} \log_2 8 = 3 \text{ bits.}$$

Example 4 (from Cover & Thomas, 2006) — 1 of 3

Consider a horse race with 8 horses participating:

Assignment Project Exam Help

• Each horse is equally likely to win. How many bits will we need to transmit the identity of the winning horse? 000, 001, 010, ..., 111

Note that the entropy of the corresponding random variable, say X, is:

$$Add \ \, \ \, \overset{H(X) \, = \, 8 \, \times \, \frac{1}{8} \log_2 8 \, = \, 3 \text{ bits.}}{\text{Notice of the power of t$$

Now say that the probabilities of each horse winning are:

$$\left(\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \frac{1}{64}, \frac{1}{64}, \frac{1}{64}, \frac{1}{64}\right)$$

Example 4 (from Cover & Thomas, 2006) — 1 of 3

Consider a horse race with 8 horses participating:

Assignment Project Exam Help

• Each horse is equally likely to win. How many bits will we need to transmit the identity of the winning horse? 000, 001, 010, ..., 111

Note that the entropy of the corresponding random variable, say X, is:

Now say that the probabilities of each horse winning are:

$$\left(\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \frac{1}{16}, \frac{1}{64}, \frac{1}{64}, \frac{1}{64}, \frac{1}{64}\right)$$

What is the average code-length to transmit the identity of the winning horse?

Example 4 (from Cover & Thomas, 2006) — 2 of 3

We see that some horses have higher probability of winning:

We can still use a 3-bit representation

ASSI Some Middle Waster less the loss almost representation

https://powcoder.com

Example 4 (from Cover & Thomas, 2006) — 2 of 3

We see that some horses have higher probability of winning:

 Idea: Use shorter codes for most probable horses and longer codes for the less probable horses.

https://powcoder.com

Example 4 (from Cover & Thomas, 2006) — 2 of 3

We see that some horses have higher probability of winning:

We can still use a 3-bit representation

SS1 90 Wenter and a few many probable borses and leaves a

- Idea: Use shorter codes for most probable horses and longer codes for the less probable horses.
- Let (1s try/representing the horses (states) using the following codes {0, 1, 10, 11, 100, 101, 110, 111, 1000}?

Example 4 (from Cover & Thomas, 2006) — 2 of 3

We see that some horses have higher probability of winning:

- We can still use a 3-bit representation
 SS1 Pontonic Mud by white it is some rosx are in ore treatment.
 - Idea. Use shorter codes for most probable horses and longer codes for the less probable horses.
 - Let us try/representing the horses (states) using the following codes $\{0,1,10,11,100,101,110,111,1000\}?$
 - Decode 010 into 'aba' or 'as'? Ambiguous.
 - We smalled aby the sample of the strings into the corresponding components.

Example 4 (from Cover & Thomas, 2006) — 2 of 3

We see that some horses have higher probability of winning:

 We can still use a 3-bit representation SS1 EMM CALLE A CONTROL OF THE PARTY OF THE

- Idea. Use shorter codes for most probable horses and longer codes for the less probable horses.
- Let us try/representing the borses (states) using the following codes 5.//powcoder.con {0, 1, 10, 11, 100, 101, 110, 111, 1000}?

Decode 010 into 'aba' or 'as'? Ambiguous.

- We shadle ab W the land a data path a Gottle a strings into the corresponding components.
- Represent the horses (states) using the following codes:

{0, 10, 110, 1110, 111100, 111101, 111110, 111111}

E.g. 11001110 \rightarrow ??

Example 4 (from Cover & Thomas, 2006) — 3 of 3

Assignment Project Exam Help

https://powcoder.com

Example 4 (from Cover & Thomas, 2006) — 3 of 3

Example 4 (from Cover & Thomas, 2006) — 3 of 3

Example 4 (from Cover & Thomas, 2006) — 3 of 3

https://powcoder.com

What is the entropy of the corresponding random variable?

$$H(X) = -\left(\frac{1}{2}\log_2\frac{1}{2} + \frac{1}{4}\log_2\frac{1}{4} + \frac{1}{8}\log_2\frac{1}{8} + \frac{1}{16}\log_2\frac{1}{16} + \frac{1}{64}\log_2\frac{1}{64}\right)$$
= 2 bits

23/39

Example 5 (from Cover & Thomas, 2006)

Aet Significant Project Exam Help

https://powcoder.com

Then H(X) = 1.58, and average code length = 1.66

Example 5 (from Cover & Thomas, 2006)

Aet Significant Project Exam Help

https://powcoder.com

Then H(X) = 1.58, and average code length = 1.66

In general Entiony is a lower pound on the average number of bits to transmit the state of a variable.

As we shall see later, we can construct descriptors with average length within 1 bit of the entropy.

What Questions Should We Ask? (From Cover & Thomas, 2006)

Assume that only the followin Process participated in the last rate: Factor Project Exam Help

The corresponding probabilities of winning are give by:

$$p(x)$$
 thtps: $p(x)$ pow coder to $p(x)$ and $p(x)$ and $p(x)$ and $p(x)$ and $p(x)$ are $p(x)$ and $p(x)$ and $p(x)$ are $p(x)$ are $p(x)$ are $p(x)$ and $p(x)$ are $p(x)$ and $p(x)$ are $p(x)$ and $p(x)$ are $p(x)$ and $p(x)$ are $p(x)$ are $p(x)$ and $p(x)$ are $p(x)$ and $p(x)$ are $p(x)$ ar

You want to determine which horse won the race with the minimum number of resployed the stories of t

- (b) What is the minimum expected number of binary questions for this?

What Questions Should We Ask? (From Cover & Thomas, 2006) — Cont'd

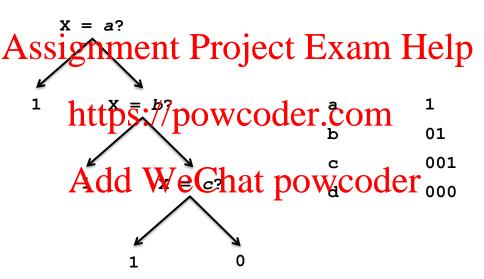
Assignment Project Fxam Help X = a won the race?

If the answer is not then ask about the second most probable winner: has X=b won the lace?

Then $X = A^2$, and $X = A^2$ we Chat powcoder

Note that the series of questions corresponding to an outcome can be seen as a code!

What Questions Should We Ask? (From Cover & Thomas, 2006) — Cont'd



What Questions Should We Ask? (From Cover & Thomas, 2006) — Cont'd

Anset go ha and variable fortes Foxenmu free p minimum number of binary questions:

This is in fact the minimum expected number of binary questions. In general, this number lies between H(X) and H(X) + 1 Add Wellar powcoder

Intuitively, each question reduces our amount of uncertainty in the outcome by attempting to eliminate (or validate) the hard to predict outcomes

- Information Content & Entropy
 - Entropy of a Random Variable
 - Some Basic Properties

Assignment Project Exam Help

- Maximum Entropy
- Entrohttps://powcoder.com
 - Minimum Number of Binary Questions
- Joint FAred don Whe enthyard pro wecoder
- 5 An Axiomatic Characterisation
- Wrapping up

Assignment Project Exam Help distribution p(X, Y) is given by:

https://pox/eqder.com $= \sum_{p(x,y) \log \frac{1}{p(x,y)}} \sum_{p(x,y) \log \frac{1}{p(x,y)}} Add Weenat powcoder$

Independent Random Variables

If X and Y are statistically independent we have that:

Assignment Project Exam Help

https://powcoder.com

Independent Random Variables

If *X* and *Y* are statistically independent we have that:

 $\frac{1}{h} \sum_{y=0}^{h} \sum_{y=0}^{h} p(x) p(y) \left[\log p(x) + \log p(y) \right] \text{ as } p(x,y) = p(x) p(y) \\ \text{powcoder.com}$

Independent Random Variables

If *X* and *Y* are statistically independent we have that:

Assignment Project Exam Help

$$= -\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x) p(y) \left[\log p(x) + \log p(y) \right] \text{ as } p(x,y) = p(x) p(y)$$

$$= -\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x) \log p(x) \sum_{y \in \mathcal{Y}} p(y) - \sum_{y \in \mathcal{Y}} p(y) \log p(y) \sum_{x \in \mathcal{X}} p(x)$$
Add WeChat powcoder

Independent Random Variables

If X and Y are statistically independent we have that:

Assignment of project Exam Help

$$\frac{1}{p(x,y)} = \sum_{x \in \mathcal{X}} p(x) p(y) \left[\log p(x) + \log p(y) \right] \text{ as } p(x,y) = p(x) p(y) \\
\text{https://powcoder.com} \\
= -\sum_{x \in \mathcal{X}} p(x) \log p(x) \sum_{y \in \mathcal{Y}} p(y) - \sum_{y \in \mathcal{Y}} p(y) \log p(y) \sum_{x \in \mathcal{X}} p(x) \\
\text{Add WeChat powcoder} \\
= \sum_{x \in \mathcal{X}} p(x) \log \frac{1}{p(x)} + \sum_{y \in \mathcal{Y}} p(y) \log \frac{1}{p(y)}$$

Independent Random Variables

If *X* and *Y* are statistically independent we have that:

Assignment Project Exam Help

$$= -\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x) p(y) [\log p(x) + \log p(y)] \text{ as } p(x,y) = p(x) p(y)$$

$$= -\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x) \log p(x) \sum_{y \in \mathcal{Y}} p(y) - \sum_{y \in \mathcal{Y}} p(y) \log p(y) \sum_{x \in \mathcal{X}} p(x)$$

$$= -\sum_{x \in \mathcal{X}} p(x) \log p(x) \sum_{y \in \mathcal{Y}} p(y) - \sum_{y \in \mathcal{Y}} p(y) \log p(y) \sum_{x \in \mathcal{X}} p(x)$$

$$= \sum_{x \in \mathcal{X}} p(x) \log \frac{1}{p(x)} + \sum_{y \in \mathcal{Y}} p(y) \log \frac{1}{p(y)}$$

$$= H(X) + H(Y)$$

Independent Random Variables

If *X* and *Y* are statistically independent we have that:

Assignment Project Exam Help

$$= -\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x) p(y) [\log p(x) + \log p(y)] \text{ as } p(x,y) = p(x) p(y)$$

$$= -\sum_{x \in \mathcal{X}} p(x) \log p(x) \sum_{y \in \mathcal{Y}} p(y) - \sum_{y \in \mathcal{Y}} p(y) \log p(y) \sum_{x \in \mathcal{X}} p(x)$$

$$= -\sum_{x \in \mathcal{X}} p(x) \log p(x) \sum_{y \in \mathcal{Y}} p(y) - \sum_{y \in \mathcal{Y}} p(y) \log p(y) \sum_{x \in \mathcal{X}} p(x)$$

$$= \sum_{x \in \mathcal{X}} p(x) \log \frac{1}{p(x)} + \sum_{y \in \mathcal{Y}} p(y) \log \frac{1}{p(y)}$$

$$= H(X) + H(Y)$$

Entropy is additive for independent random variables

Conditional Entropy

The conditional entropy of Y given X = x is the entropy of the probability distribution p(Y|X = x):

https://powcoder.com

Conditional Entropy

The conditional entropy of Y given X = x is the entropy of the probability distribution p(Y|X = x):

The conditional entropy of Y given X is the liverage over Yef the conditional entropy of Y given X = x.

$$Add \overset{H(Y|X)}{\underset{=}{W}} = \sum_{x \in \mathcal{X}} p(x) H(Y|X=x) \\ = \sum_{x \in \mathcal{X}} p(x) \sum_{y \in \mathcal{Y}} p(y|x) \log \frac{1}{p(y|x)}$$

Conditional Entropy

The conditional entropy of Y given X = x is the entropy of the probability distribution p(Y|X = x):

The conditional entropy of Y given X is the liverage over Yef the conditional entropy of Y given X = x.

Add Wethat powcoder
$$= \sum_{x \in \mathcal{X}} p(x) \sum_{y \in \mathcal{Y}} p(y|x) \log \frac{1}{p(y|x)}$$

Average uncertainty that remains about *Y* when *X* is known.

We can re-write the conditional entropy as follows:

Assignment Project Exam Help

https://powcoder.com

We can re-write the conditional entropy as follows:

Assignment Project Exam Help
$$= \sum_{x \in \mathcal{X}} \sum_{p(x)p(y|x) \log \frac{1}{p(y|x)}} \frac{1}{p(y|x)}$$
https://powcoder.com

We can re-write the conditional entropy as follows:

https://power.pow

We can re-write the conditional entropy as follows:

Assignment
$$\sum_{x \in \mathcal{X}} p(x) p(y|x) \log \frac{1}{p(y|x)}$$

https://powcoder.com
$$\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x,y) \log \frac{1}{p(y|x)}$$
Add Wechathpowcoder

We can re-write the conditional entropy as follows:

Assignment
$$\sum_{x \in \mathcal{X}} p(x) p(x) p(x) = \sum_{x \in \mathcal{X}} \sum_{p(x), p(y|x)} p(x) \log \frac{1}{p(y|x)}$$

https://powcoder.com
$$\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x, y) \log \frac{1}{p(y|x)}$$
Add Wec leat powcoder

Note the expectation is not wrt the conditional distribution but wrt the joint distribution p(X, Y)

The joint entropy can be written as:

Assignment Project Exam Help

https://powcoder.com

The joint entropy can be written as:

Assignment Project Exam Help
$$= -\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x,y) [\log p(x) + \log p(y|x)]$$

$$\text{https://powcoder.com}$$

The joint entropy can be written as:

Assignment
$$Project$$
 Exam Help
$$= -\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x, y) [\log p(x) + \log p(y|x)]$$

$$\text{https://project.com/g} p(y|x)$$

$$\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x, y) [\log p(x) + \log p(y|x)]$$

The joint entropy can be written as:

Assignment Project Exam Help
$$= -\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x,y) [\log p(x) + \log p(y|x)]$$

$$\text{https://gpowgodergommg} p(y|x)$$

$$H(x \text{Add}x) \text{Weshat powcoder}$$

The joint entropy can be written as:

Assignment
$$Project$$
 Exam Help
$$= -\sum_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x,y) [\log p(x) + \log p(y|x)]$$

$$\text{https://dep.dep.gom.}_{x \in \mathcal{X}} \sum_{y \in \mathcal{Y}} p(x,y) [\log p(x) + \log p(y|x)]$$

$$H(x \text{Add}x) \text{Weshat-powcoder}$$

The joint uncertainty of *X* and *Y* is the uncertainty of *X* plus the uncertainty of *Y* given *X*

- Information Content & Entropy
 - Entropy of a Random Variable
 - Some Basic Properties

Assignment Project Exam Help

- Maximum Entropy
- https://powcoder.com
 - Minimum Number of Binary Questions
- Add WeChat powcoder
- 6 An Axiomatic Characterisation
- 6 Wrapping up

An Axiomatic Characterisation

Suppose we want a measure H of "information" in a random variable X such that

- H depends on the distribution of X and not the outcomes the heelies The \mathcal{P} for the combination of two variables X, Y is at most the sum the corresponding H values
- The H for the combination of two independent variables X, Y is the sum of the corresponding H values OCT. COM
- Adding outcomes with probability zero does not affect H
- The Hold Bernoulli with parameter prends to Casp CT

Then, the only possible choice for H is

$$H(X) = -\sum_{x} p(x) \log_2 p(x)$$

Outline

- Information Content & Entropy
- Entropy of a Random Variable ssignment Project Exam Help
- Examples: Bernoulli and Categorical Random Variables
 - Maximum Entropy
- powcoder.com
 - Average Code Length
 - Minimum Number of Binary Questions
- Joint Entropy, Conditional Entropy and Profile Coder
- An Axiomatic Characterisation
- Wrapping up

Summary

Entropy as a measure of information content

Assignment Project Exam Help Computation of entropy of discrete random variables

- Entripy and average code length coder.com
- Entropy and minimum expected number of binary questions
- Joint and ditional entropies at in prowed er
- Reading: Mackay $\S 1.2 \S 1.5$, $\S 8.1$; Cover & Thomas $\S 2.1$; Bishop § 1.6

Next time

Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

Mutual information