The University of Melbourne School of Computing and Information Systems

# Assignment Project Fam Help Declarative Programming

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## Welcome to Declarative Programming

Lecturer: Peter Schachte

# Assi ignificantila Projects. Exam Help There will be two pre-recorded one-hour lectures per week, plus one live

There will be two pre-recorded one-hour lectures per week, plus one live one-hour practical meeting for questions, discussion, and demonstrations.

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You should have already been allocated a workshop. Please check your personal timetable after the lecture.

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### Grok

We use Grok to provide added self-paced instructional material, exercises, ANSI STATE TO LEAST THE PROJECT EXAM HE You can be sess Grok by following the link from the subject LMS page.

If you are unable to access Grok or find that it is not working correctly, please emailttps://powcoder.com

Grok University Support <uni-support@groklearning.com>

from your university email account and explain the problem.

If you have leading was reaction to the power of the post a message to the subject LMS discussion forum.

### Workshops

The workshops will reinforce the material from lectures, partly by asking Augusto apply it to small scale programming task Tam Help To get the most out of each workshop, you should read and attempt the exercises before your workshop. You are encouraged to ask questions, discuss, and actively engage in workshops. The more you put into workshop, the most you vilgatwice themer. Com

Workshop exercises will be available through Grok, so they can be undertaken even if you are not present in Australia. Sample solutions for each set of workshop which will be painted through Golf.

Most programming questions have more than one correct answer; your answer may be correct even if it differs from the sample solution.

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### Resources

The lecture notes contain copies of the slides presented in lectures, plus

Some additional material Project Exam Help
All subject materials (lecture notes, workshop exercises, project specifications etc) will be available online through the LMS.

The recommended text/(which is available of line) is Power of the Powe

Other recommended resources are listed on the LMS.

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### **Assessment**

The subject has the following assessment components:

## Assignment Project Exam Help 15% larger Prolog project, due in Week 6 or 7

0% short Haskell project, is due in Week 8 or 9 (optional)

# 

To pass the subject (get 50%) you must pass both the project component and the example of the control of the project component and the example of the control of the contro

The exam is closed book, and will be held during the usual examination period after the end of the semester. Practice versions of the final exam are available on the LMS.

## **Academic Integrity**

All assessment for this subject is *individual*; what you submit for assessment must be your work and *your work alone*.

Assignmentsh PremiewicEssen freelp tutorials and other unassessed exercises.

We are well aware that there are many online sources of material for subjects the trippe; you meen curaged to learn from any online sources, and from other students, but do not submit for assessment anything that is not your work alone.

Do not store your project work in a public bithub or other repository.

We use sophisticated software to find code that is similar to other submissions this year or in past years. Students who submit another person's work as their own or provide their work for another student to submit in whole or in part will be subject to disciplinary action.

### How to succeed

Declarative programming is substantially different from imperative

Arogramming Project Exam Help Even after you can understand declarative code, it can take a while before you can master writing your own.

If you have been writing imperative code all jour programming life, you will probably try to write imperative code even in Caecharative language. This often does not work, and when it does work, it usually does not work well.

Writing declarative code requires a different mindset, which takes a while to acquire Add  $WeChat\ powcoder$ 

This is why attending the workshops, and practicing, practicing and practicing some more are *essential* for passing the subject.

## Sources of help

During contact hours:

# Assignment Projetefor Exam Help Ask the demonstrator in your workshop.

Outside contact hours:

- The https://paowercoder.comt)
- Email (if not of interest to everyone)
- Attend my consultation hours (see LMS for schedule)
  Email to Culculus an appointment powcoder

Subject announcements will be made on the LMS.

Please monitor the LMS for announcements, and the discussion forum for detailed information. Read the discussion forum before asking questions; questions that have already been answered will not be answered again.

## **Objectives**

On completion of this subject, students should be able to:

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- write medium size programs in a declarative language;
- write programs in which different components use different languages;
- select attrop Ste/an Dosw Go Grodnet alma project.

These objectives are not all of equal weight; we will spend almost all of our time of the first two objectives.

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#### Content

Introduction to logic programming and Prolog

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- Introduction to functional programming and Haskell
- Declarative programming techniques
- · Tool 1 to Stiff powice of steelen
- Interfacing to imperative language code

This subject will track the Haskell and Prolog, with an emphasis on Haskell. Add Wechat powcoder

For logistical reasons, we will begin with Prolog.

## Why Declarative Programming

Declarative programming languages are quite different from imperative

# And shift oriented language Project Exam Help

- They give you a different perspective: a focus on what is to be done, rather than how.
- The work at a higher level of abstractiber com
- They make it easier to use some powerful programming techniques.
- Their clean semantics means you can do things with declarative programs that you can't do with conventional programs;

The ultimate objective of this subject is to widen your horizons and thus to make you better programmers, and not just when using declarative programming languages.

## Imperative vs logic vs functional programming

Imperative languages are based on commands, in the form of instructions

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• Commands have an effect, such as to update the computation state, and later code may depend on this update.

Logic programming languages are based on finding values that satisfy a set of constraints.

- Constraints may have multiple solutions or none at all.
   Constraints on not have an effect powcoder

Functional languages are based on evaluating expressions.

- Expressions are evaluated.
- Expressions do not have an effect.

### Side effects

Code is said to have a *side effect* if, in addition to producing a value, it also modifies some state or his an observable interaction with cilling fanctions of the outside world. For example, a function might

- modify a global or a static variable,
- mod fy the of its a fuments wooder.com
   raise an exception (e.g. divide by zero),
- write data to a display, file or network,
- read data roth a key board, house file or network or der
   call other side-effecting functions.

## An example: destructive update

In imperative languages, the natural way to insert a new entry into a table as to middify the table in place paside effect. The effectively descrive the place of the companion of the property of the propert

In declarative languages, you would instead create a new version of the table, but the old version (without the new entry) would still be there.

The price is that the language implementation has to work harder to recover memory and to ensure efficiency.

The benefit is that you don't need to worry what other code will be affected by the change of the ch

The *immutability of data structures* also makes parallel programming *much* easier. Some people think that programming the dozens of cores that CPUs will have in future is the killer application of declarative programming languages.

### **Guarantees**

- If you pass a pointer to a data structure to a function, can you
- Stuir of that the funct processing the data structure, and pass a pointer to that.
- You add a new field to a structure. Can you guarantee that every piece that the post had been what to handle the new field?
  - If not, you will need many more test cases, and will need to find and fix more test. We Chat powcoder
- Can you guarantee that this function does not read or write global variables? Can you guarantee that this function does no I/O?
  - If the answer to either question is "no", you will have much more work to do during testing and debugging, and parallelising the program will be a *lot* harder.

## Some uses of declarative languages

- In a US Navy study in which several teams wrote code for the same Sex proving engages decaying languages like has ell wire productive than imperative languages.
  - Mission Critical used Mercury to build an insurance application in one third the time and cost of the next best quote (which used Java).
  - Ericsson, one of the largest manufacturers of phone network switches, uses Erlang in some of their switches.
  - The statistical machine learning algorithms behind Bing's advertising systemate with the control of the contr
  - Facebook used Haskell to build the system they use to fight spam.
     Haskell allowed them to increase power and performance over their previous system.

### The Blub paradox

Consider Blub, a hypothetical average programming language right in the middle of the power continuum project Exam Help When a knub programmer looks down the power continuum, he knows he is looking down. Languages below Blub are obviously less powerful, because they are missing some features he is used to.

But where bupped ampedooks to the continuum, he does not realize he is looking up. What he sees are merely weird languages. He thinks they are about equivalent in power to Blub, but with some extra hairy stuff Blub is governeign for hint, since thinks in the continuum, he does not realize he is looking up. What he sees are merely weird languages. He thinks they are about equivalent in power to Blub, but with some extra hairy stuff Blub is governeign for hint, since thinks in the continuum, he does not realize he is looking up.

When we switch to the point of view of a programmer using a language higher up the power continuum, however, we find that she in turn looks down upon Blub, because it is missing some things *she* is used to.

Therefore understanding the differences in power between languages requires understanding the most powerful ones.

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### **Logic programming**

Af John von Neumann, which executes a set of instructions step by steil programming languages are based on the lambda calculus of Alonzo Church, in which functions map inputs to outputs.

Logic programming languages are based on the predicate calculus of Gottlob Prege and the concept of a relation, which captures a relationship among a number of individuals, and the *predicate* that relates them.

A function is a special kind of relation that can only be used in one direction imputs to output and clipping have limitations.

While the first functional programming language was Lisp, implemented by John McCarthy's group at MIT in 1958, the first logic programming language was Prolog, implemented by Alain Colmerauer's group at Marseille in 1971.

#### Relations

A relation specifies a relationship; for example, a family relationship. In

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specifies to small part of the parenthood relation, which relates parents to their children the says/that Queen Elizabet Csla-per on the prince Charles

The name of a relation is called a *predicate*. Predicates have no directionality: (i) make what a much spise to ask who is Prince Charles's parent. There is also no promise that there is a unique answer to either of these questions.

#### **Facts**

A statement such as:

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is called a fact. It may take many facts to define a relation:

```
% (A smattens of / nowish of Francism parent (queen_elizabeth, prince_charles).
parent (prince_philip, prince_charles).
parent (prince_charles, prince_william).
parent (princess_diana, prince_william).
parent (princess_diana, prince_william).
parent (princess_diana, prince_harry).
:
```

Text between a percent sign (%) and end-of-line is treated as a comment.

## **Using Prolog**

Most Prolog systems have an environment similar to GHCi. A file containing facts like this should be written in a file whose name begins with a lower case letter and contains only letters, digits, and underscores and ends with ".pl".

A source file can be loaded into Prolog by typing its filename (without the .pl extension between square by kets a time folder round (?-). Prolog prints a message to say the file was compiled, and true to indicate it was successful (user input looks <u>like this</u>):

## ?- [royandd WeChat powcoder

% royals compiled 0.00 sec, 8 clauses true.

?-

### Queries

Once your code is loaded, you can use or test it by issuing *queries* at the Prolog prompt. A Prolog query looks just like a fact. When writer in Source file has loaded into Prolog, it is treated as a true statement. At the Prolog prompt, it is treated as a query, asking if the statement is true.

```
?- parent (prince_william_prince_charles).
false. Add WeChat powcoder
```

### **Variables**

Each predicate argument may be a *variable*, which in Prolog begins with a capital letter or underscore and follows with letters digits, and underscores that makes that query true, and prints the value that makes it true.

If there is more than one answer to the query, Prolog prints them one at a time, pausing to sit more solutions; just hitting enter (return) finishes without more solutions.

## This quer Asta de www eice finds ipowicoder

```
?- parent(prince_charles, X).
X = prince_william ;
X = prince_harry.
```

### Multiple modes

The same parenthood relation can be used just as easily to ask who is a parent of Prince Charles or even who is a parent of whom. Each of these is a different place, based on which arguments are bound (inputs; non-variables) and which are unbound (outputs; variables).

```
parant (In prince / charles) coder.com
= prince_philip.
parent(X, Y
               eChat powcoder
= prince_charles
= prince_philip,
= prince_charles ;
```

## **Compound queries**

Queries may use multiple predicate applications (called *goals* in Prolog and Atoms in predicate logic). The implest way to combine multiple goals is the separate them with a comma. This acks Prolog for all bindings for the variables that satisfy both (or all) of the goals. The comma can be read as "and". In relational algebra, this is called an *inner join* (but do not worry if you do not the proposition of the process of the comma can be read as "and".

```
?- parent(queen_elizabeth, X), parent(X, Y).
X = prince_charles,
Y = prince_charles,
X = prince_charles,
Y = prince_harry.
```

### Rules

Predicates can be defined using *rules* as well as facts. A rule has the form

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where *Head* has the form of a fact and *Body* has the form of a (possibly compound) the structure of the st

```
grandparent(X,Z) :- parent(X, Y), parent(Y, Z).
means "And parent Cif histrepf Who Code It of Z."
```

Rules and facts are the two different kinds of *clauses*. A predicate can be defined with any number of clauses of either or both kinds, intermixed in any order.

### Recursion

Rules can be recursive. Like Haskell, Prolog has no looping constructs, so recursion is widely used. Prolog does not have at well-developed a library of higher excer operations as Haskell, so recursion is used more in Pologo than in Haskell.

A person's ancestors are their parents and the ancestors of their parents.

https://powcoder.com

ancestor(Anc. Desc)

parent(Anc, Desc).

ancestor (Ang., Perchat powcoder ancestor (Ang., Parent).

### **Equality**

Equality in Prolog, written "=" and used as an infix operator, can be used both to bind variables and to speck for equality. Like Haskell, Prolog is a circle of the Christian August 19: reassized parts of the Christian August 19: reassized parts.

```
?- \frac{x = 7}{x = 7}. https://powcoder.com false.
```

 $\frac{x - X}{\text{false.}}$  And WeChat powcoder

?- 
$$X = 7$$
,  $Y = 8$ ,  $X = Y$ . false.

### Disjunction

Goals can be combined with disjunction (or) as well as conjunction (and).

Disjunction is written ":" and sed as an infix operator. Conjunction 1

(1) Shapping the presence (binds lighter) than disjunction, but Telp

parentheses can be used to achieve the desired precedence.

Who are the children of Queen Elizabeth or Princess Diana?

```
?- parent(queen_elizabeth, X); parent(princess_diana, X).

X = prince_charles ;

X = prince_william;

X = prince_litry. We Chat powcoder
```

### **Negation**

Negation in Prolog is written "\+" and used as a prefix operator. Negation has higher (tighter) precedent than both conjutction and disjutction. Be sure to leave a space between the Older on open parenthesis.

Who are the parents of Prince William other than Prince Charles?

```
?- parenttpsi/e-powcodericomes.
X = princess_diana.
```

Disequality in Prolog swritter at an infix "\=". So X \= Y is the same as \+ X = \frac{Add Wechat powcoder}{}

```
?- parent(X, prince_william), X \= prince_charles.
X = princess_diana.
```

### The Closed World Assumption

Prolog assumes that all true things can be derived from the program. This is called the closed world assumption. Of course this is not true for our parent regular (that would require the billiens of charses!)

```
?- \+ parent(queen_elizabeth, princess_anne).
true. https://powcoder.com
```

but Princess Anne is a daughter of Queen Elizabeth. Our program simply does not know but we Chat powcoder. So use negation with great care on predicates that are not complete, such as parent.

## **Negation** as failure

Prolog executes \+ G by first trying to prove G. If this fails, then \+ G ucceeds; if it succeeds, then G fails. This is the led negation in Prolog Failing goals can never bind variables, so any variable bindings made in solving G are thrown away when \+ G fails. Therefore, \+ G cannot solve for any variables, and goals such as these cannot work properly.

Is there anyone of whom Queen Elizabeth is not a parent. Is there anyone who is not Queen Elizabeth?

?- \+ pared die Weichat powcoder

?- X \= queen\_elizabeth. false.

### **Execution Order**

The solution to this problem is simple: ensure all variables in a negated roal are bound before the go problem of the body of a clause) from first to last, so put the goals that will bind the variables in a negation before the negation of (a).

In this case, the property of them is different from Queen Elizabeth.

```
?- (parAtold ) Vrechia, Trower Corer.
X = prince_philip ;
```

### **Datalog**

The fragment of Prolog discussed so far, which omits data structures, is called Datalog. It is a general stion of what is provided by relational databases how provide Datalog features of use Datalog implementation techniques.

```
capital attable. / phore coder.com
continent (austratia, australia) to powcoder
population(australia, 22_680_000).
population(france, 65_700_000).
```

### **Datalog Queries**

```
What is the capital of France?
                 ent Project Exam Help
Capital paris.
What are capitals of European countries?
?- cont performer//powerodente oppal).
Country = france,
Capital = paris.
What European country school property for the country, europe), population (Country,
   Pop > 50_000_000.
Country = france,
Pop = 65700000.
```

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#### **Terms**

In Prolog, all data structures are called *terms*. A term can be atomic or Acompound or it can be a variable parallel by the structure of the parallel by the

Atomic terms include integers and floating point numbers, written as you would expect, and atoms.

An atom begins pith o lower Qseveter Qne ferror with the lower Qseveter Qne ferror with the lower and underscores, for example a, queen\_elizabeth, or banana.

An atom can also be written beginning and ending with a single quote, and have any litter vening craracters alle is 10 Watter expect can be used, for example \n for newline, \t for tab, and \' for a single quote. For example: 'Queen Elizabeth' or 'Hello, World!\n'.

### **Compound Terms**

In the syntax of Prolog, each compound term is a functor (sometimes called function symbol) followed by zero or more arguments: if there are an parguments, they are shown in parentheses, separated by community processing and have the same syntax as atoms.

For examinating Sall/t/epa Wese Great void ten ritten as

Node Leaf 1 (Node Leaf 2 Leaf)

would be written in Prelog syntax as the term node (lear Adod Me Char) powcoder

Because Prolog is dynamically typed, each argument of a term can be *any* term, and there is no need to declare types.

Prolog has special syntax for some functors, such as infix notation.

#### **Variables**

A variable is also a term. It denotes a single unknown term.

# A grisip on the project the Erxnders of letters, digits, and Inderscores.

A single underscore \_ is special: it specifies a different variable each time it appears, further in Haskell pattern matching.

Like Haskell, Prolog is a single-assignment language: a variable can only be bound (assigned) once.

Because the arguments of a compound term can be any terms and variables are terms, variables can appear in terms. VCOCC

For example f(A,A) denotes a term whose functor is f and whose two arguments can be anything, as long as they are the same;  $f(_-,_-)$  denotes a term whose functor is f and has any two arguments.

### **List syntax**

Like Haskell, Prolog has a special syntax for lists.

# Assignment b Project Exam Help Both denote the list with the three elements 1, 2 and 3 by [1, 2, 3].

While Haskell uses x:xs to denote a list whose head is x and whose tail is xs, the Professions which Prolog lacks).

The Prolog syntax for what Haskell would represent with x1:x2:xs is

[X1, X2] Axdd WeChat powcoder

### **Ground vs nonground terms**

A term is a ground term if it contains no variables, and it is a nonground term if it contains at least on Prariable ect Exam Help 3 and f (\$\frac{1}{2}\$ b) are ground terms.

Since Name and f(a, X) each contain at least one variable, they are nonground terms //powcoder.com

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#### **Substitutions**

A *substitution* is a mapping from variables to terms.

Applying experimental Progressive International Progressive Progre

Note that a substitution only replaces variables, never atomic or compound terms .//powcoder.com
For example, applying the substitution  $\{X1 \mapsto leaf, X2 \mapsto 1, X3 \mapsto leaf\}$  to the term node(X1,X2,X3) yields the term node(leaf,1,leaf).

Since you An det how Teaf (1) leaf) from node (X1, X2, XB) by applying a substitution to it, incredital, ip, leaf) vs children of node (X1, X2, X3).

Any ground Prolog term has only one instance, while a nonground Prolog terms has an infinite number of instances.

#### Unification

The term that results from applying a substitution  $\theta$  to a term t is

Alemosted the project Exam Help such that  $u = t\theta$ .

A substitution  $\theta$  unifies/two terms t and u if  $t\theta = u\theta$  Consider the terms f(X, P) and f(a, Y).

Applying a substitution  $\{X \mapsto a\}$  to those two terms yields f(a, b) and f(a, Y), which are more trially identical, so this substitution is not a unifier.

On the other hand, applying the substitution  $\{X \mapsto a, Y \mapsto b\}$  to those terms yields f(a, b) in both cases, so this substitution is a unifier.

### Recognising proper lists

A proper list is either empty ([]) or not ([X|Y]), in which case, the tail of Abelist must be a proper list. We can define a project to recognize these proper\_list([]).

proper\_list([Head|Tail]) :
https://powcoder.com

?- [list].

Worning: list pl:3:

```
Warning: list.pl:3:

Air leton wheeleh attapowcoder
% list compiled 0.00 sec, 1 clauses
true.
```

### **Detour: singleton variables**

Warning: list.pl:3:
Assignment:Project Exam Help

The variable Head appears only once in this clause:

This often indicates a typo in the source code. For example, if Tail were spelled Tie in the place, the world all easy to the Cur Place singleton warning would alert us to the problem.

### **Detour: singleton variables**

In this case, there is no problem; to avoid the warning, we should begin the variable name Head with Punderscore or JET name the variable proper\_list([]).

proper\_list([\_Head|Tail]) :-

## https://powcoder.com

?- [list].

% list compiled 0.00 sec, 1 clauses

true. Add WeChat powcoder

General programming advice: always fix compiler warnings (if possible). Some warnings may indicate a real problem, and you will not see them if they're lost in a sea of unimportant warnings. It is easier to fix a problem when the compiler points it out than when you have to find it yourself.

**Declarative Programming** 

### **Append**

```
Appending two lists is a common operation in Prolog. This is a built in Arcdicate in most Prolog systems, but could castly be implemented as: 1p append([], C, C).
append([A|B], C, [A|BC]):-

https://powcoder.com

?- append([a,b,c],[d,e],List).
```

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This is similar to ++ in Haskell.

#### append is like proper\_list

Compare the code for proper\_list to the code for append:

This is common code of proedical charles a componen follows the structure of that term (as we saw in Haskell).

While the proper\_list predicate is not very useful itself, it was worth designing, as it gives with at the structure of other code that traverses lists. Since types are not declared in vologic predicates like proper\_list can serve to indicate the notional type.

### **Appending backwards**

Unlike ++ in Haskell, append in Prolog can work in other modes:

```
<del>ment Projec</del>t Exam Help
?- append(Front, [3,4], [1,2,3,4])
Front = [1, 2];
r- appear to sak powcoder.com
Front = [].
Back = [a, b, c];
Front = Aldd WeChat powcoder
Front = [a, b],
Back = \lceil c \rceil:
Front = [a, b, c].
Back = []:
false.
```

#### Length

The length/2 built-in predicate relates a list to its length:

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The \_... terms are how Prolog prints out unbound variables. The number reflects when the ariable vas created technique variables all printed differently, we can tell they are all distinct variables.

[\_2956, \_2962, \_2968] is a list of three distinct unbound variables, and each unbound variable can be any term, so this can be any three-element list, as specified by the query.

### Putting them together

How would we implement a predicate to take the front n elements of a

ist in Prolog? Project Exam Help take (N, Est, Front) should hold if Front is the first N elements of List. So length (Front, N) should hold.

Also, appleed (Front // List) should hold Then:
take(N, List, Front):length(Front, N),

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Prolog coding hint: think about *checking* if the result is correct rather than *computing* it. That is, *think of what* instead of *how*.

Then you need to think about whether your code will work the ways you want it to. We will return to that.

#### **Member**

Here is list membership, two ways:

# Assignment Project-Exam Help

```
member2(Elt, [Elt|]).

member2(Elt, [Rest]):- member2(Elt, Rest).

These behave the same, but the second is a bit more efficient because the
```

first builds and ignores the list of elements before Elt in List, and the second does not.

Note the recursive version does not exactly match the structure of our earlier proper\_list predicate. This is because Elt is never a member of the empty list, so we do not need a clause for []. In Prolog, we do not need to specify when a predicate should fail; only when it should succeed. We also have two cases to consider when the list is non-empty (like Haskell in this respect).

#### **Arithmetic**

In Prolog, terms like 6 \* 7 are just data structures, and = does not

ASSIGNMENT Project Exam Help The built predicate 1s/2 (an infix perator) evaluates expressions.

```
?- X = 6 * 7.
X = 6 * https://powcoder.com
?- X is 6 * 7.
X = 42. Add WeChat powcoder
```

#### Arithmetic modes

Use is/2 to evaluate expression

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Unfortunately, square only works when the first argument is bound. This is because is/2 only works if its second argument is ground.

```
X = 25.
?- square(X_ 25
            Arguvite are 102 tuific w/10 m the lated
```

ERROR: is/2: Arguments are not sufficiently instantiated

Later we shall see how to write code to do arithmetic in different modes.

#### **Arithmetic**

Prolog provides the usual arithmetic operators, including:

```
ment (Parolect) Exam Help
  integer division (rounds toward 0)
  modulo (result has same sign as second argument)
 osuma//rimwetoder.com
```

More arithmetic predicates (infix operators; both arguments must be ground expressions): TT 7 < =< AGOss Wee Chat powcoder > >= greater, greater or equal =:= =\= equal, not equal (only numbers)

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### **Interpretations**

In the mind of the person writing a logic program,

# Assingentment throughout this am discourse" (world of the program);

- each functor (function symbol of arity n where n > 0) stands for a function from n entities to one-entity in the domain of discourse; and
- each predicate of arity *n* stands for a particular relationship between *n* entities in the domain of discourse.

This mapping from the ymbos in the program to the world of the program (which may be the real world or some imagined world) is called an *interpretation*.

The obvious interpretation of the atomic formula parent(queen\_elizabeth, prince\_charles) is that Queen Elizabeth II is a parent of Prince Charles, but other interpretations are also possible.

### Two views of predicates

As the name implies, the main focus of the predicate calculus is on

# Ars Signment Project Exam Help You can wink of a predicate with n aguments in two equivalent ways.

- You can view the predicate as a function from all possible combinations of n terms to activith value (i.e. true or folse).
- You can view the predicate as a set of tuples of n terms. Every tuple
  in this set is implicitly mapped to true, while every tuple not in this
  set is implicitly mapped to false.

The task of a predicate definition is to define the mapping in the first view, or equivalently, to define the set of tuples in the second view.

### The meaning of clauses

The meaning of the clause

# Assignment Projectar Sam Help is: for all the terms that A and C may stand for, A is a grandparent of C if

there is a term B such that A is a parent of B and B is a parent of C.

## In mathe https://powcoder.com

 $\forall A \forall C : grandparent(A, C) \leftarrow \exists B : parent(A, B) \land parent(B, C)$ 

The variables appearing in the head are universally quantified over the entire clause, while validables appearing in the head are universally quantified over the body.

### The meaning of predicate definitions

A predicate is defined by a finite number of clauses, each of which is in the form of an implication. A fact puch as parent (Tueen elizabethelp) represents this implication. Exam Help

```
(A = queen\_elizabeth \land B = prince\_charles)
To represent the meaning of the Medicale, Great Gisunction of the
bodies of all the clauses:
(A = And Ozab We Chath Dowcoder
    (A = prince\_philip \land B = prince\_charles) \lor
    (A = prince\_charles \land B = prince\_william) \lor
    (A = prince\_charles \land B = prince\_harry) \lor
    (A = princess\_diana \land B = prince\_william) \lor
    (A = princess\_diana \land B = prince\_harry)
```

 $\forall A \forall B : parent(A, B) \leftarrow$ 

### The closed world assumption

To implement the closed world assumption, we only need to make the mplication arrow go both P'' O'' Exam Help

```
(A = queen\_elizabeth \land B = prince\_charles) \lor (A = prince\_philip \land B = prince\_charles) \lor (A = prince\_philip \land B = prince\_charles) \lor (A = prince\_charles \land B = prince\_harry) \lor (A = princess\_diana \land B = prince\_william) \lor (A = princess\_diana \land B = prince\_harry) \bigcirc (A = princess\_diana \land B = prince\_harry) \bigcirc (A = princess\_diana \land B = prince\_harry)
```

This means that A is not a parent of B unless they are one of the listed cases.

Adding the reverse implication this way creates the *Clark completion* of the program.

### **Semantics of logic programs**

A logic program P consists of a set of predicate definitions. The semantics of this program (its meaning) the set of its logical consequences as program the logical consequences as program of the semantics.

A ground atomic formula a is a logical consequence of a program P if P makes a true.

A negated strong promit production of P if a is not a logical consequence of P.

For most logic programs, the set of ground atomic formulas it entails is infinite (as the set is constituted at the set of ground atomic formulas it entails is infinite (as the set is constituted at the set of ground atomic formulas it entails is infinite (as the set of groun

### Finding the semantics

You can find the semantics of a logic program by working backwards.

Anstead of reasoning from a query to find a satistying substitution, you present the program to find what ground queries will succeed.

The immediate consequence operator  $T_P$  takes a set of ground unit clauses C and produces the set of ground unit clauses implied by C together Mthtppogram DOWCOGET.COM

This always includes all ground instances of all unit clauses in P. Also, for each clause  $H: -G_1, \ldots, G_a$  in P, if C contains instances of  $G_1, \ldots, G_n$ , then the cores and in this tance of this talk pirothered to the stalk pirothered to

Eg, if 
$$P = \{q(X, Z) : -p(X, Y), p(Y, Z)\}$$
 and

$$C = \{p(a,b).p(b,c).p(c,d).\}, \text{ then } T_P(C) = \{q(a,c).q(b,d).\}.$$

The semantics of program P is always  $T_P(T_P(T_P(\cdots(\varnothing)\cdots)))$   $(T_P \text{ applied infinitely many times to the empty set}).$ 

### **Procedural Interpretation**

The *logical* reading of the clause

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says "for all X, Y, Z, if X is parent of Y and Y is parent of Z, then X is grandparent X is properties and X is parent of Y and Y is parent of Z.

The procedural reading says "to show that X is a grandparent of Z, it is sufficient to show that X is a parent of Y and Y is a parent of Z".

SLD resolated Wreek, in latent playing oder

#### **SLD** Resolution

The consequences of a logic program are determined through a simple but

```
q:- b1 https://powcoder.com
```

## \*\* Add WeChat powcoder

it is sufficient to show any of

```
?- p, b1a, b1b, r.
?- p, b2a, b2b, r.
:
```

#### SLD resolution in action

E.g., to determine if Queen Elizabeth is Prince Harry's grandparent:

## Assignment Project Exam Help

with this program

we unify query goal grandparent (queen\_elizabeth, prince\_harry) with clause national parent (x 12), apply the visiting substitution to the clause, yielding the resolvent. Since the goal is identical to the resolvent head, we can replace it with the resolvent body, leaving:

?- parent(queen\_elizabeth, Y), parent(Y, prince\_harry).

#### SLD resolution can fail

Now we must pick one of these goals to resolve; we select the second.

# The griegon has sent (tau Projec tou Finx many select by resolve with parent (Y, prince hary):

```
parent (prince_charles, prince_harry).
parent https://powcoder.com
```

We choose the second. After resolution, we are left with the query (note the unifying substitution is applied to both the selected clause and the query):

query): Add WeChat powcoder

?- parent(queen\_elizabeth, princess\_diana).

No clause unifies with this query, so resolution fails. Sometimes, it may take many resolution steps to fail.

#### SLD resolution can succeed

Selecting the second of these matching clauses led to failure:

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This does not mean we are through: we must backtrack and try the first matching date of the own coder.com

?- parent(queen\_elizabeth, prince\_charles).

There is an a cling to consider the fove. The query succeeds.

#### Resolution

This derivation can be shown as an SLD tree:

# Assignment-Project-Exam Help

parent(queen\_elizabeth, Y), parent(Y, prince\_harry).

parent (queen\_elizabeth, prince\_charles). princess\_diana).

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#### Order of execution

The order in which goals are resolved and the order in which clauses are tried does not matter for correctness (in pure Piplog), but it does natter for correctness (in pure Piplog), but it does natter for correctness (in pure Piplog), but it does natter for correctness (in pure Piplog), but it does natter for correctness (in pure Piplog), but it does natter before parent (Y, prince\_harry) is more efficient, because there is only one clause matching the former, and two matching the latter.

pareA(deh\_Wateh, h) prince\_narry).

pareA(deh\_Wateh, h) tarpowrochery).

parent(prince\_charles, prince\_harry).

#### **SLD** resolution in Prolog

At each resolution step we must make two decisions:

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which clauses matching the selected goal to pursue

(though there may only be one choice for either or both).

Our procedure was somewhat hapfrazard when decisions needed to be made. For pure logic programming, this does not matter for correctness. All goals will need to be resolved eventually; which order they are resolved in does not change the wisces. All matching clauses may need to be tried; the order in which we try them determines the order solutions are found, but not which solutions are found.

Prolog always selects the first goal to resolve, and always selects the first matching clause to pursue first. This gives the programmer more certainty, and control, over execution.

#### **Backtracking**

When there are multiple clauses matching a goal, Prolog must remember which one to go back to it necessary. It must be able to return the property of the track was in whether the tirst matching clause. This is all done with a choicepoint.

When a got fails Brolog pakerwisto the host recent child epoint, removing all variable bindings made since the choicepoint was created, returning those variables to their unbound state. Then Prolog begins resolution with the next matching clause, repeating the process until Prolog detects that there are no marchiat bing clauses, at which point it removes that choicepoint. Subsequent failures will then backtrack to the next most recent choicepoint.

#### **Indexing**

Indexing can greatly improve Prolog efficiency

Mosto loggest the with autopatically ceast ar index for a redictes of as parent 2 (Prolog uses name/arity to refer to predicates) with multiple clauses the heads of which have distinct constants or functors. This means that, for a call with the first argument bound, Prolog will immediately jump to the fits page that in twee to detect that matches, and so on.

If the first argument is unbound, then all clauses will have to be tried.

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#### **Indexing**

If some clauses have variables in the first argument of the head, those clauses will be tried at the appropriate time regardless of the call. Indexing the head behaviour. Ensider:

```
p(a, z).
p(b, y)https://powcoder.com
p(x, x).
```

For the call  $p(\mathbf{d}^{J})$ , and lause will be tried in order for  $p(\mathbf{b}^{J})$ , the first clause will be tried, then the third, then fourth. For  $p(\mathbf{b}^{J})$ , the second, then third, clause will be tried. For  $p(\mathbf{c}, J)$ , only the third clause will be tried.

#### **Indexing**

Some Prolog systems, such as SWI Prolog, will construct indices for Arguments other than the first For parent /2, SWI Prolog will not provide poth arguments, so finding the children of a parent of parents of a child poth benefit from indexing.

Just as important as jumping directly to the first matching clause, indexing left plots when it first place. Even with only two clauses, such as for append/3 indexing an substantially improve performance.

append/3 Aindexing Wetchilly improve performance. der

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#### List Reverse

To reverse a list, put the first element of the list at the end of the reverse

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Tappend (CB; /[AP, CBAy COUCL COILI

reverse/2 is an SWI Prolog built-in, so we use a different name to avoid conflict. Add WeChat powcoder

#### List Reverse

The mode of a Prolog goal says which arguments are bound (inputs) and which are unbound (outputs) when the predicates called Help rev1/2 works as intended when the first argument is ground and the second is free, but not for the opposite mode.

Prolog hangs at this point. We will use the Prolog debugger to understand why. For now, hit control-C and then 'a' to abort.

#### The Prolog Debugger

To understand the debugger, you will need to understand the Byrd box

Anodel Think of goal executions a box with a port for each way to enter

Another Exam Help

A conventional language has only one way to enter and one way to exit;

Prolog has two of each.

The four bluggers of each.

The four bluggers of each.



Turn on debugger with trace, and off with nodebug, at the Prolog prompt.

#### Using the Debugger

The debugger prints the current port, execution depth, and goal (with the current variable bindings) at each step. Call: (8) rev1([b], \_12834) ? creep Call: (9) rev1([], \_12834) ? creep Call: (9) lists:append([], [b], 12838) (9) lists:append([], [b], [b]) ? creep Exit: (8) rev1([b], [b]) ? creep list Varoed Nata (at) () 2W/C? Exit: (8) lists:append([b], [a], [b, a])? creep Exit: (7) rev1([a, b], [b, a]) ? creep = [b, a].

"lists:" in front of append is a module name.

#### Reverse backward

Now try the "backwards" mode of rev1/2. We shall use a smaller test

```
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Call: (7) rev1(_11553, [a]) ? creep

Call: (8) rev1(_11661, _11671) ? creep

Exit (5) rev1([p[0]) creep

Call: (8) lists:append([], [_11660], [a]) ? creep

Exit: (8) lists:append([], [a], [a]) ? creep

Exit: (7) rev1([a], [a]) ? creep

X = [a] Add WeChat powcoder
```

#### Reverse backward, continued

after showing the first solution, Prolog goes on forever like this:

```
Redo: (8) rev1(_11661, _11671) ? creep
SSE STREET Project Exam Help
Exit: (9) lists:append([], [_11663], [_11663]) ? creep
Exit: (8) rev1([_11663], [_11663]) ? creep
Call: (8) lists:append([_11,663], [_11660], [a]) ? creep
Call: (10) rev1(11667, _11677) ? creep
Exit: (10) rev1([], []) ? creep
Call: (10) lists:append([], [_11666], _11681) ? creep
Exit: (10) Aistel appendit [1666] h [11666] h [200] COCCT
Exit: (9) rev1(11666] 116601) 7 areas
Call: (9) lists:append([_11666], [_11663], _11684) ? creep
Exit: (9) lists:append([_11666], [_11663], [_11666, _11663]) ? creep
Exit: (8) rev1([_11663, _11666], [_11666, _11663]) ? creep
Call: (8) lists:append([_11666, _11663], [_11660], [a])
Fail: (8) lists:append([_11666, _11663], [_11660], [a])
```

#### Infinite backtracking loop

```
Assignment Project Exam Help

append (CB, [A], CBA).
```

```
The problem is the gap of WV. (a) restrict pal rev1(BC, CB), append (CB, [A], [a]). The call rev1(BC, CB) produces an infinite backtracking sequence of solutions \{BC \mapsto [], CB \mapsto []\}, \{BC \mapsto [Z], CB \mapsto [Z]\} \{BC \mapsto [Y, Z], CB \mapsto [Z, Y]\},.... For each of these solutions (CB) and (CB) are fally However.
```

append([], [A], [a]) succeeds, with  $\{A \mapsto [a]\}$ . However, append([Z], [A], [a]) fails, as does this goal for all following solutions for CB. This is an infinite backtracking loop.

#### Infinite backtracking loop

We could fix this problem by executing the body goals in the other order:

# Assignment Project Exam Help append (CB, [A], CBA),

But this definition does now coder, com

```
?- rev2(X, [a,b]).

X = [b, Add WeChat powcoder]
```

#### Working in both directions

The solution is to ensure that when rev1 is called, the first argument is always bound to a list. We do this by observing that the length of a list must always be the same as that of its reverse. When same length/21 succeeds, and he length the same length is length.

```
rev3(ABC, CBA):-

same_length(ABC, CBA),

pttps://powcoder.com
```

```
same_length([], []).
same_length([_|Xs], [_|Ys]) :-
```

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```
?- \frac{\text{rev3}(X, [a,b])}{X = [b, a]}.

?- \frac{\text{rev3}([a,b], Y)}{Y = [b, a]}.
```

#### More on the Debugger

Some useful debugger commands:

### Assignment Project Exam Help

- c creep to the next port (also space, enter)
- s skip over goal; go straight to exit or fail port

### https://powergodering.mings done since starting it;

a abort whole debugging session

### Addy We Chart poweoder

- remove spypoint from this predicate
- I leap to the next spypoint
- **b** pause this debugging session and enter a "break level," giving a new Prolog prompt; end of file reenters debugger

#### More on the Debugger

Built-in predicates for controlling the debugger:

Assignment py Pito jeste, wam Help

nospy(Predspec) Remove the spypoint from Predspec.

debug Turn on the debugger and leap to first spypoint

nodebug Turn off the debugger

A "PredspA" (il a predatte med atmed to WCOCET

#### Using the debugger

Note the r (retry) debugger command restarts a goal from the beginning, "time travelling" back to the pre when starting to execute that grad The s (sep) command skips forward in time, over the whole executi a goal, to its exit or fail port.

This leads to a quick way of tracking down host bugs: Hubs://bowcoder.com

- 1 When you arrive at a call or redo port: skip.
- If you come to an exit port with the correct results (or a correct fail o If you come to an incorrect exit or fail port: retry, then creep.

Eventually you will find a clause that has the right input and wrong output (or wrong failure); this is the bug. This will not help find infinite recursion, though.

#### **Spypoints**

For larger computations, it may take some time to get to the part of the computation where the bug lies. Usually you will have a good idea, or 1 guestes, which predicates you suspect of being bugs (usually the predicates you have edited most recently). In cases of infinite recursion you may suspect certain predicates of being involved in the loop. In these destroying who would be seen that the seen the seen that the se debuggers, when Prolog reaches any port of a predicate with a spypoint set, Prolog stops and shows the port. The 1 (leap) command tells Prolog to run quietly intil it reaches a spypoint. Use the spy(pred) goal at the Prolog prompered a spysoint on the named predicate remove one. You can also add a spypoint on the predicate of the current debugger port with the + command, and remove it with -.

#### **Documenting Prolog Code**

Your code files should have two levels of documentation – file level documentation and predicate level comments. Each file should gat with a mineral sharp of the file; its author, the date of the file; its author, the file; its author, the date

Comments should be provided above all significant and lentivial predicates in a consistent format. These comments should identify: the meaning of each argument; what the predicate does; and the modes in which the redicate is wrighted to predicate DOWCOGET

An excellent resource on coding standards in Prolog is the paper "Coding guidelines for Prolog" by Covington et al. (2011).

#### Predicate level documentation

The following is an example of predicate level documentation from Assignment Project Exam Help

```
%% remove_duplicates(+List, -Result)
%
% Removes the duplicates in List, giving Result.
% Elements and log defeat the two of the COM
% unified with lach other; thus, a partly
% uninstantiated element may become further
% instantiated during testing. If several elements
% match, the partly the coreservent powcoder
```

Predicate arguments are prefaced with a: + to indicate that the argument is an input and must be instantiated to a term that is not an unbound variable; - if the argument is an output and may be an unbound variable; or a? to indicate that the argument can be either an input or an output.

#### Managing nondeterminism

This is a common mistake in defining factorial:

```
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No is N - 1,
```

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#### Managing nondeterminism

This is a common mistake in defining factorial:

# Assignment Project Exam Help No is N - 1,

https://powcoder.com

```
?- fact(5, F).
F = 120 Add WeChat powcoder
ERROR: Outdoor
```

fact(5,F) has only one solution, why was Prolog looking for another?

#### **Correctness**

The second clause promises that for all n,  $n! = n \times (n-1)!$ . This is wrong for sign = 1 and sign = 1 are clause applies, later clauses are still tried. After finding 0! = 1,

The simple solution is to ensure each clause is a correct (part of the) definition TUPS.//POWCOGET.COM

Prolog thinks  $0! = 0 \times -1!$ ; tries to compute  $-1!, -2!, \dots$ 

```
fact(0, 1).
fact(N, A)dd WeChat powcoder
```

```
N1 is N - 1,
fact(N1, F1),
F is F1 * N.
```

#### **Choicepoints**

This definition is correct, but it could be more efficient.

When a dausa incredis but the remainder claused that could pass be proceed, evolog will leave a choicepoult so it can later backtrack and try the later clause.

In this case, backtracking to the second clause will fail unless N>0. This test is quick. However, as long as the choicepoint exists, it inhibits the very important last call optimisation (discussed later). Therefore, where efficiency matters, it is important to make your recursive predicates not leave choicepoints when they should be deterministic COCCT. In this case, N=0 and N>0 are mutually exclusive, so at most one

In this case, N=0 and N>0 are mutually exclusive, so at most one clause can apply, so fact/2 should not leave a choicepoint.

#### If-then-else

We can avoid the choicepoint with Prolog's if-then-else construct:

### Assignment Project Exam Help

https://powcoder.com

F is F1 \* N

Add WeChat powcoder
The -> is treated like a conjunction (,), except that when it is crossed,

The -> is treated like a conjunction (,), except that when it is crossed, any alternative solutions of the goal before the ->, as well as any alternatives following the ; are forgotten. Conversely, if the goal before the -> fails, then the goal after the ; is tried. So this is deterministic whenever both the code between -> and ;, and the code after the ;, are.

#### If-then-else caveats

However, you should prefer indexing (discussed next time) and avoid

Af-then-else, when you have a poice, if-then-else usually leads to ode that will get work throughly in multiple modes. For example, appendicular be written with if-then-else:

This may appear correct, and may follow the logic you would use to code it in another language, but it is not appropriate for Prolog.

#### If-then-else caveats

With that definition of ap:

### Assignment Project Exam Help

?- ap(https://powcoder.com

?- 
$$ap(L, M, [a,b,c,d,e])$$
.  
L = [], Add WeChat powcoder  
M = [a, b, c, d, e].

Because the if-then-else commits to binding the first argument to [] when it can, this version of append will not work correctly unless the first argument is bound when append is called.

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# Assignment Project Fam Help Declarative Programming

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Section 5

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#### Tail recursion

A predicate (or function, or procedure, or method, or...) is tail recursive

of the only recursive call on a pexecution of that predicate is the list code

executed before returning to the called For example, the usual definition

of append/3 is tail recursive, but rev1/2 is not:

```
append https://powcoder.com
append(B, C, BC).
```

```
 \begin{array}{c} \text{rev1([]A[A]WeChat powcoder} \\ \text{rev1([A]BC], CB),} \\ \text{append(CB, [A], CBA).} \end{array}
```

#### Tail recursion optimisation

Like most declarative languages, Prolog performs tail recursion

Applimisation (TRO). This is important for declarative languages in the property of the process of the property of the process of the pr

Note that TRO is more often directly applicable in Prolog than other languages in the Society of the Weist Company of the Prolog while append/3 in Prolog is tail recursive, ++ in Haskell is not, because the last operation performed is (:), not ++.

However another optimisation can permit TRO for this code.

#### The stack

To understand TRO, it is important to understand how programming languages (not just Prolog) implement call and the first process of the programming languages (not just Prolog) implement call and the first process of th

But if all a will do after calling 1 is return to a, then there is no need to preserve as later rights. Wolfg can release b's frame before calling c, as shown to the right. When c is finished, it will return directly to a. This is called *last call optimisation*, and can save significant stack space.

#### TRO and choicepoints

Tail recursion optimisation is a special case of last call optimisation where the last call is recursive. This is espeassagamentio Projecte Swam Help Without PRO, this would require a stack frame for each iteration, and would quickly exhaust the stack. With TRO, tail recursive predigates execute in constant stack Growth b However, if b leaves a choicepoint, it sits on the stack Choicepoint above b's frame, "freezing" that and all earlier frames so that they are not reclaimed. This is necessary by cause when Prolog backtracks to that choicepoint, b's arguments must be ready to try the next matching clause for The same is true if c or any predicate called later leaves a choicepoint, but choicepoints before the call to b do not interfere.

#### Making code tail recursive

Our factorial predicate was not tail recursive, as the last thing it does is

Note that Prolog's if-then-else construct does not leave a choicepoint. A choicepoint is created, but is removed as soon as the condition succeeds or fails. So fact would be subject to TRO, if only it were tail recursive.

#### Adding an accumulator

We make factorial tail recursive by introducing an accumulating parameter or just an accumulator. This is an extra parameter to the predicate that holds a partially computed result.

Usually the base case for the recursion will specify that the partially computed result is actually the result. The recursive clause usually computed partial whole design and states in the recursive goal.

The key to getting the implementation correct is specifying what the accumulator mans and hope it relates to the final result. To see how to add an accumulator, determine what is done after the recursive call, and then respecify the predicate so it performs this task, too.

#### Adding an accumulator

For factorial, we compute fact (N1, F1), F is F1 \* N last, so the tail Accursive version will need to perform the multiplication too. We nust perform the multiplication too.

In most cases, it is not difficult to see how to transform the original definition to the tail recursive one.

```
https://powcoder.com
              fact1(N, A, F) :-
Add WeChat powcoder
   fact(N1, F1),
                      N1 is N-1,
   F is F1 * N
                      A1 is A * N.
                       fact1(N1, A1, F)
```

## Adding an accumulator

Finally, define the original predicate in terms of the new one. Again, it is

Another way to think about writing atail recursive implementation of a predicate is to realise that it will essentially be a loop, so think of how you would write it as a while loop, and then write that loop in Prolog.

https://powcoder.com

```
fact(N, F) :- fact1(N, 1, F).
fact1(N, A, F) :-
fact1(N, A, F
```

Another approach is to systematically transform the non-tail recursive derivation into an equivalent tail occursive predicate. Start by defining a predicate of the work of the recursive call to fact (N, F2) by the definition of fact/2. This is called *unfolding*.

Next we move the final goal into both the *then* and *else* branches.

## Assignment Project Exam Help

The next step is to simplify the arithmetic goals.

## Assignment Project Exam Help

```
\begin{array}{c} F2 = 1, & F = A \\ httpis_0, //powcoder, com, \\ N1 \text{ is } N-1, & \text{fact}(N1, F1), \\ Addis WeChat) powcoder \\ F \text{ is } F2 * A \\ \end{array}
```

Now we utilise the associativity of multiplication. This is the insightful

Now part of the computation can be moved before the call to fact/2.

 $Add^{is} \overset{\mathtt{Fl}}{W} \overset{\mathtt{e}(\mathtt{N} \times \mathtt{A})}{e} at \ powerder$ 

The final step is to recognise that the last two goals look very much like the body of the original definition of fact 1/2, with the substitution of fact 1/2, with the substitution place those two goals with the polycomes are clause head with that substitution applied. This is called folding.

## **Accumulating Lists**

The tail recursive version of fact is a constant factor more efficient, because it behaves like a loop cometimes accumulators can make an addressification of the complexity of the complexity asymptotic complexity, for example replacing append/3 (linear time) with list construction (constant time).

https://powcoder.com
rev1([A|BC], CBA) :rev1(BC, CB),
And CEWAP CE hat powcoder

This definition of rev1/2 is of quadratic complexity, because for the  $n^{th}$  element from the end of the first argument, we append a list of length n-1 to a singleton list. Doing this for each of the n elements gives time proportional to  $\frac{n(n-1)}{2}$ .

#### Tail recursive rev1/2

The first step in making a tail recursive version of rev1/2 is to specify the work of revE2 with that Help appearing the work of revE2 with that Help

```
% rev(BCD, A, DCBA)
% DCBA https://powcoder.com
```

We could develop this by transformation as we did for fact1/3, but we implement it directly here. We begin with the base case, for BCD = []:

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#### Tail recursive rev1/2

For the recursive case, take BCD = [B|CD]:

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We can use our rev/3 predicate to compute that:

rev([B|CD], A, DCBA) :rev(CD, [B|A], DCBA).

#### Tail recursive rev1/2

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At each recursive step, this code removes an element from the head of the input list and the step is therefore a constant, so the overall cost is linear in the length of the list.

Accumulator lists worklike a tack the last element of the accumulator is the first element that was added to it, and so on. Thus at the end of the input list, the accumulator is the reverse of the original input.

## **Difference pairs**

The trick used for a tail recursive reverse predicate is often used in Prolog: a predicate that generales a list takes an extra argument specifying what should come after the list. This works the need to append to the list.

In Prolog, if you do not know what will come after at the time you call the predicate, you can pass an unbound variable, and bind that variable when you do know with Should to be the the predicate a list have two arguments, the first is the list produced, and the second is what comes after. This is called a difference pair, because the predicate generates the difference between the first and second list.

```
flatten(empty, List, List).
flatten(node(L,E,R), List, List0) :-
    flatten(L, List, List1),
    List1 = [E|List2],
    flatten(R, List2, List0).
```

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## Homoiconicity

Prolog is a *Homoiconic* language. This means that Prolog programs can manipulate Prolog programs Project Exam Hell The builter predicate clause (+Head, -Body) allows a running program to access the clauses of the program.

clausttps://powcoder.com

Many SWAProbg "bulk no such apappants" was them, Prolog detects that they are undefined, discovers that they can be auto-loaded, quietly loads the, and continues the computation.

Because append/3 hasn't been auto-loaded yet, clause/2 can't find its code.

### clause/2

If we call  ${\tt append/3}$  ourselves, Prolog will load it, so we can access its

```
nt Proiect Exam He
 append([a],[b],L).
 = [a, b].
               owcoder.com
        d WeChat powcoder
   [7184|7192]
Body = append(_7186, Y, _7192).
```

### A Prolog interpreter

This makes it very easy to write a Prolog interpreter:

There is a more complete definition, supporting disjunction and negation, in interp.pl in the examples directory.

## **Higher Order Programming**

The call/1 built-in predicate executes a term as a goal, capitalising on Prolog's homoiconicity.

```
**Signment Project Exam Help

X = append([], [1], [1]),

A = [],

B = [1] https://powcoder.com

A = [1],

B = [];

false.

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```

This allows you to write a predicate that takes a goal as an argument and call that goal.

This is called *higher order programming*. We will discuss it in some depth when we cover Haskell.

## Currying

It is often useful to provide a goal omitting some arguments, which are supplied when the goal is called This allows the same goal to be used provided with different arguments. Sect Exam Help

To support this, many Prologs, including SWI, support versions of call of higher arity. All arguments to call/n after the goal (first) argument are added as extra property in the wood of the collinear colli

```
?- X=append([1,2],[3]), call(X, L).
X = append(11d 21W31) Chat powcoder
L = [1,2]
```

When some arguments are supplied with the goal, as we have done here, they are said to be "curried". We will cover this in greater depth later.

## Writing higher-order code

It is fairly straightforward to write higher order predicates using call/n. For example, this predicate will apply a predicate to corresponding

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```
maplist(P, [X|Xs], [Y|Ys]):-
```

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```
?- maplist(length_[[a,b],[a],[a,b,c]], Lens).

Lens = Add. WeChat powcoder

2- length(List_2) maplist(same_length(List), List)
```

```
?- length(List,2), maplist(same_length(List), List).
List = [[_9378, _9384], [_9390, _9396]].
```

This is defined in the SWI Prolog library. There are versions with arities 2–5, allowing 1–4 extra arguments to be passed to the goal argument.

#### All solutions

Sometimes one would like to bring together all solutions to a goal.

Prolog's all solutions predicates do exactly this. Exam Help set of (Template, Goal, List) binds List to sorted list of all distinct instances of Template satisfying Goal

Templatican be any term usually containing some of the variables appearing in the D. On completion, settly sinus as Data gument, but does not further bind any variables in the Template.

?- setofA-c prewe, hat powcoder List = [duchess\_kate-prince\_george, prince\_charles-prince\_harry, prince\_charles-prince\_william, prince\_philip-prince\_charles, prince\_william-prince\_george, princess\_diana-prince\_harry, princess\_diana-prince\_william, queen\_elizabeth-prince\_charles].

#### **All solutions**

If Goal contains variables not appearing in Template, setof/3 will backtrack over each distinct binding of these variables, for each of them binding List to the list of intances of Template for that binding the property of the binding of the property of the binding of the bin

```
?- setof(C, parent(P, C), List).
P = duchess_kate,
List = [prince george]
P = prince george/powcoder.com
List = [prince_harry, prince_william];
P = prince_philip,
List = [prince_tharles]
                    eChat powcoder
List = [prince_george] ;
P = princess_diana,
List = [prince_harry, prince_william] ;
P = queen_elizabeth,
List = [prince_charles].
```

## **Existential quantification**

Use existential quantification, written with infix caret (^), to collect tolutions for a template regardless of the bindings of some of the variable

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E.g., to find all the people in the database who are parents of any child:

```
?- seto respective to the seto respective to
```

## Add WeChat powcoder

#### **Unsorted solutions**

The bagof/3 predicate is just like setof/3, except that it does not sort

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```
?- bagof(P, C^parent(P, C), Parents).
Parents = [queen_elizabeth, prince_philip, prince_charles,
prince_hatler princes diama princes diama, prince_william,
duchess_kate]
```

Solutions are collected to the order they are produced. This it not purely logical, because the order of solutions thou door matter. Not should the number of times a solution is produced.

## Input/Output

Prolog's Input/Output facility does not even try to be pure. I/O

Aperations are executed when they are reached recording to Propose 1p

Prolog has builtin predicates to read and write arbitrary Prolog terms. Prolog also allows users to define their own operators. This makes Prolog very convenient for applications involving structured by

```
?- op(800, xfy, wibble).

true.

?- read(A.dd WeChat powcoder)

I: p(x,[1,2],X>Y wibble z).

X = p(x, [1, 2], _1274>_1276 wibble z).

?- write(p(x,[1,2],X>Y wibble z)).

p(x,[1,2],_1464>_1466 wibble z)

true.
```

## Input/Output

write/1 is handy for printing messages:

```
*Signmente Project Exam Help
hello world!
true.
?- write('world!'), write('hello ').
world!hattps://powcoder.com
true.
```

This demonstrates that Polog's input/output predicates are non-ligical. These should be equivalent, because conjunctions by the commutative of

Code that performs I/O must be handled carefully — you must be aware of the modes. It is recommended to isolate I/O in a small part of the code, and keep the bulk of your code I/O-free. (This is a good idea in any language.)

## **Comparing terms**

All Prolog terms can be compared for ordering using the built-in predicates

but most usefully, within these classes, terms are ordered as one would expect: number of some of the sound terms are ordered first by arity, then alphabetically by functor, and finally by arguments, left-to-right. It is best to use these only for ground terms.

## ?- hell Acid WeChat powcoder true.

?- 
$$X @< 7, X = foo.$$

$$X = foo$$

?- 
$$X = foo, X @< 7.$$

false

## Sorting

There are three SWI Prolog builtins for sorting ground lists according to the @< ordering; sort /2 sort plist, removing diplicates, msort /2 sorts a list, without removing duplicates, and key sort perably sorts list of the terms, only comparing X parts:

```
?- sort([h,e,],!,o], L).

?- msort([h,e,1,1,o], L).

L = [e, h, 1, 1, o].

?- keys Atd Ca, W. e. C, hat 3 powcoder

L = [3-b, 3-c, 3-a, 7-a, 8-d].
```

### **Determining term types**

Ariables nent Project Exam Help rule.

- integer(3).

true.

- integer(a).

?- integer(a): false. https://powcoder.com ?- integer(X).

false.

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Similarly, float/1 recognises floats, number recognises either kind of number, atom/1 recognises atoms, and compound/1 recognises compound terms. All of these fail for variables, so must be used with care.

## Recognising variables

han an unbound variable and pround 1 holds for any term other than an unbound variable and pround 1 holds for ground term this provides travelsing the whole term Olsing these or the predicates in the previous slide can make your code behave differently in different modes.

But they can also be used to write code that works in multiple modes. Here is a hit text works of Wenc 20 hat works in multiple modes. Here is a hit text work of the length is known:

```
len2(L, A)dd WeChat powcoder
-> L = []
; N1 is N - 1,
        L = [_|L1],
        len2(L1, N1)
```

).

### Recognising variables

This version works when the length is unknown:

```
Assignment Project Exam Help
    N1 \text{ is } N0 + 1.
This code chooses between the two coder.com
 len(L, N) :-
    And We Chat powcoder
       nonvar(N)
    -> throw(error(type_error(integer, N),
                 context(len/2, '')))
       len1(L, 0, N)
```

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## **Constraint (Logic) Programming**

An imperative program specifies the exact sequence of actions to be executed by the computer.

A functional program specifies how the result of the program is to be computed at a more abstract level. One can read function definitions as suggesting an order of actions, but the language implementation can and sometimes will be step to the two der die to zyres of the execution, and various optimizations.

A logic program is in some ways more declarative, as it specifies a set of equality constraints that the terms of the splitting ways got a set of the searches for a solution.

A constraint program is more declarative still, as it allows more general constraints than just equality constraints. The search for a solution will typically follow an algorithm whose relationship to the specification can be recognized only by experts.

## **Problem specification**

The specification of a constraint problem consists of

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- a set of constraints, with each constraint involving one or more variables, and
- an https://powcoder.com

The job of the constraint programming system is to find a *solution*, a set of assignments of values to variables (with the value of each variable being drawn from its tomain) what atis its all the possworts of the constraint of

The objective function, if there is one, maps each solution to a number. If this number represents a cost, you want to pick the cheapest solution; if this number represents a profit, you want to pick the most profitable solution.

## Kinds of constraint problems

There are several kinds of constraints, of which the following four are the most common. Most CP systems handle only one or two kinds. Help in Herbraud constraint systems, the variables represent terms, and the basic constraints are unifications, i.e. they have the form  $term_1 = term_2$ . This is the constraint domain implemented by Prolog.

In finite domain or D constraint systems, each variable's domain has a finite number of elements.

In boolean satisfiability or SAT systems, the variables represent booleans, and each contract as extended to the truth of an extended using logical operations such as AND, OR, NOT and implication.

In *linear inequality* constraint systems, the variables represent real numbers (or sometimes integers), and the constraints are of the form  $ax + by \le c$  (where x and y are variables, and a, b and c are constants).

#### **Herbrand Constraints**

Herbrand constraints are just equality constraints over Herbrand terms—

exactly what we have been using since we started with Prolog. Help
In Prolog we can constrain variables to be equal, and Prolog will succeed
if that is possible, and fail if not.

```
?- length(Word, 5), reverse (Word, Word), Word=[r,a,d,a,r].
Word = Add, WreChat powcoder

?- length(Word, 5), reverse (Word, Word), Word=[r,a,d,a,r].
### The control of th
```

#### Search

Prolog normally employs a strategy known as "generate and test" to earch for variable bindings that satisfy constraints. Nondetermitistic goals generate setential solutions; later goals test those solutions, imposing further constraints and rejecting some candidate solutions.

The first goal generates single-digit numbers, the second tests that it is even, and the third that its square quarter in the Share of the second tests that it is

Constraint logic programming uses the more efficient "constrain and generate" strategy. In this approach, constraints on variables can be more sophisticated than simply binding to a Herbrand term. This is generally accomplished in Prolog systems with attributed variables, which allow constraint domains to control unification of constrained variables.

### **Propagation**

The usual algorithm for solving a set of FD constraints consists of two

Atens: propagation and labeling roject Exam Help In the propagation step, we try to reduce the domain of each variable as much as possible.

For each constraint, we/check whether the constraint rules out any values in the current abmens of any of the variables in the constraint. If it does, then we remove that value from the domain of that variable, and schedule the constraints involving that variable to be looked at again.

# The propagatol Gep Wse Chat powcoder

- if every variable has a domain of size one, which represents a fixed value, since this represents a solution;
- if some variable has an empty domain, since this represents failure; or
- if there are no more constraints to look at, in which case propagation can do no more.

### Labelling

If propagation cannot do any more, we go on to the *labelling* step, which

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- partitions its current domain (of size n) into k parts  $d_1, ..., d_k$ , where usually k=2 but may be any value satisfying  $2 \le k \le n$ , and
- recursively possible to the chosen variable to  $d_i$ .

Each recursive invocation also consists of a propagation step and (if needed) applying type the vilote ton putation there is sists of alternating propagation and labelling steps.

The labelling steps generate a search tree. The size of the tree depends on the effectiveness of propagation: the more effective propagation is at removing values from domains, the smaller the tree will be, and the less time searching it will take.

### **Prolog Arithmetic Revisted**

In earlier lectures we introduced a number of built-in arithmetic predicates, Ancluding (i.s.) /2 (=:=) /2, D=) /2 and (=< )2. Recall that these predicate countries in the large count

example, only works when its second argument is ground.

The CLP(FD) library (constraint logic programming over finite domains) provides replacements for these lower-level arithmetic predicates. These new predicates are called *arithmetic constraints* and can be used in both directions (i.e., in,out and out,in).

# **CLP(FD) Arithmetic Constraints**

CLP(FD) provides the following arithmetic constraints:

```
Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> equals Expr<sub>2</sub>

EXPRING FOR EXPLANATION

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is less than Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>1</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>2</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>3</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>3</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>3</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>3</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>3</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>3</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>3</sub>

Expr<sub>1</sub> #= Expr<sub>2</sub> Expr<sub>3</sub> is greater than or equal to Expr<sub>3</sub>

Expr<sub>3</sub> Expr<sub>4</sub> is greater than or equal to Expr<sub>3</sub>

Expr<sub>3</sub> Expr<sub>4</sub>
```

# - 25 #- Add WeChat powcoder

X in  $-5 \/5$ .

$$X = 5$$

# Propagation and Labelling with CLP(FD)

Recall that the domain of a CLP(FD) variable is the set of all integers. We deduce or restrict the domain of these variables with the use of CLP(FD) constraints. When a constraint is posted, the library automatically recise the domains of relevant variables if necessary. This is called propagation.

As we saw in the Sudoku example, sometimes propagation alone is enough to reduce the tip shoot and while to the tip shoot and to tell Prolog to perform the labelling step.

label/1 is an enumeration predicate that searches for an assignment to each variable in dist was estimated by the control of t

```
?- \frac{25 \# X * X, label([X])}{25 \# 5}
```

# Propagation and Labelling with CLP(FD)

What we expressed in Prolog using generate-and-test

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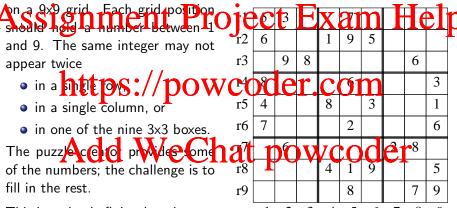
would be expressed with constrain and generate as:

#### And with labelling:

```
X = 6.
```

#### Sudoku

Sudoku is a class of puzzles played



This is a classic finite domain constraint satisfaction problem.

c1 c2 c3 c4 c5 c6 c7 c8 c9

#### Sudoku as finite domain constraints

You can represent the rules of sudoku as a set of 81 constraint variables Ar1c1 11c2 etc) each with the domain 1.9 and 27 all-different L

For example, the constraint for the top left box would be all\_different([r1c1, r1c2, r1c3, r2c1, r2c2, r2c3, r3c1, r3c2, r3c3]).

Initially, the transfer of leach a We C 1.01 through the lue of a variable e.g. by setting r1c1 = 5, this means that the other variables that share a row, column or box with r1c1 (and that therefore appear in an all-different constraint with it cannot be 5, so their domain tan be reduced to Augus We Chat powcoder

This is how the variables fixed by our example puzzle reduce the domain of r3c1 to only [1..2], and the domain of r5c5 to only [5].

Fixing r5c5 to be 5 gives us a chance to further reduce the domains of the other variables linked to r5c5 by constraints, e.g. r7c5.

# Sudoku in SWI Prolog

Using SWI's library(clpfd), Sudoku problems can be solved:

```
Assignment Project Exam Help
length(Rows, 9), maplist(same_length(Rows), Rows),
append(Rows, Vs), Vs ins 1..9,

https://distinct.Rowsder.com
maplist(all_distinct, Columns),
Rows = [A,B,C,D,E,F,G,H,I],
Aldes A, We Chast powerser, I).
```

# Sudoku in SWI Prolog

```
Assignment Project Exam Help
     https://powcoder.com
     Add; W;e,Chat; powcoder
        [\_,\_,\_,\_,8,\_,-,7,9]],
    sudoku(Puzzle),
    write(Puzzle).
```

#### Sudoku solution

In less than  $\frac{1}{20}$  of a second, this produces the solution:

```
ssignment. Project Exam Help
     [6.7.2. 1.9.5. 3.4.8]
     [1,9,8,3,4,2,5,6,7]
   https://powcoder.com
     [4,2,6,8,5,3,7,9,1]
      ,1,3, 9,2,4, 8,5,6],
      ad WeChat powcoder
     [2,8,7, 4,1,9, 6.3,5]
     [3.4.5, 2.8.6, 1.7.9]]
```

### **Linear inequality constraints**

Suppose you want to make banana and/or chocolate cakes for a bake sale, and you have 10 kg of flour, 10 bananas 1.2 kg of sugar, 1.5 kg of butter and 700 grams of cocol on hand. On tan charge \$4.00 for 1 banana cake and \$6.50 for a chocolate one. Each kind of cake requires a certain quantity of each ingredient. How do you determine how many of each cake to make the assternations were registed entirely entirely. To solve such a problem, you need to set up a system of constraints saying, for example, that the number of each kind of cake times the amount of flour needs of that kind of cake must add to no more than

You also need to specify that the number of each kind of cake must be non-negative. Finally, you need to define your revenue as the sum of the number of each kind of cake times its price, and specify that you would like to maximise revenue.

### **Linear inequality constraints**

We can use SWI Prolog's library(clpr) to solve such problems. This Assignment Project Exam Help  $?-\{250*B + 200*C = < 10000\},$  $\{2*B = < 30\},$ thttps://pow.coder.com  $\{75*C = < 700\},\$  $\{B>=0\}, \{C>=0\},$ Add Wechat poweoder B = 12.0C = 2.0.

So we can make \$61.00 by making 12 Banana and 2 Chocolate cakes.

Revenue = 61.0

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# **Functional programming**

The basis of functional programming is equational reasoning. This is a

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 if two expressions have equal values, then one can be replaced by the other.

You can set the simpler and simpler, until it is as simple as possible. Suppose x = 2 and y = 4, and you start with the expression x + (3 \* y):

```
Step 0: Axdd3 WeChat powcoder
```

```
step 2: 2 + (3 * 4)
```

```
step 3: 2 + 12
```

step 4: 14

#### Lists

Of course, programs want to manipulate more complex data than just

to define their own types, using a much more expressive type system than the type system of e.g.  $C_1$ 

Nevertheless, the most fremently used type in this ker pograms is probably the builtin list type.

The notation [] means the empty list, while x:xs means a nonempty list whose here (irrelement) is epresented by the wriable x. (all the remaining elements) is represented by the variable xs.

The notation ["a", "b"] is syntactic sugar for "a": "b": []. As in most languages, "a" represents the string that consists of a single character, the first character of the alphabet.

#### **Functions**

A function definition consists of equations, each of which establishes an equality between the left and part hand sides of the equal sign. Help len (x:xs) = 1 + len xs

Each equilition typically/expects the input arguments to conform to a given pattern; if and waxes are two patterns.

The set of patterns should be *exhaustive*: at least one pattern should apply for any possible call.

It is good programming style to ensure that the set of patterns is also

exclusive, which means that at most one pattern should apply for any possible call.

If the set of patterns is both exhaustive and exclusive, then *exactly one* pattern will apply for any possible call.

### Aside: syntax

In most languages, a function call looks like f(fa1, fa2, fa3).

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If the second argument is not fa2 but the function g applied to the single argument ga1, then in Haskell you would need to write nttps://powcoder.com

since Haskell would interpret f fa1 g ga1 fa3 as a call to f with four arguments.

In Haskell And de n Ware hesta at not be the Good et st of a function call, but parentheses may be needed around individual arguments. This applies on the left as well the right hand sides of equations.

This is why the recursive call is len xs and not len(xs), and why the left hand side of the second equation is len (x:xs) instead of len x:xs.

### More syntax issues

Comments start with two minus signs and continue to the end of the line.

# The principality of the period parties of attention of the period parties of the period

Suppose line1 starts in column *n*, and the following nonblank line, line2, starts in following. The offside rule says that the column of the following nonblank line, line2, starts in following nonblank line, line2, starts in following nonblank line.

- if m > n, then line2 is a continuation of the construct on line1;
- if m = n, then line2 is the start of a new construct at the same level as line3; dd WeChat nowcoder
- if m < n, then line2 is either the continuation of something else that line1 is part of, or a new item at the same level as something else that line1 is part of.

This means that the structure of the code as shown by indentation must match the structure of the code.

#### Recursion

The definition of a function to compute the length of a list, like many

Alaskell functions, reflect the pucture of the date a list is either more properties. The properties are a list is either more properties.

The first equation for len handles the empty list case.

this is called the base case. This is called the base case.

# Add WeChat powcoder

#### Recursion

The definition of a function to compute the length of a list, like many

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https://powcoder.com

The second equation handles nonempty lists. This is called the *recursive* case, since it contains we call the powcoder

len (x:xs) = 1 + len xs

#### Recursion

The definition of a function to compute the length of a list, like many

Alaskell functions, reflect the Pucture of the date a list is either motion

Alaskell functions, reflect the Pucture of the date a list is either motion

Alaskell functions are flect the Pucture of the date at list is either motion.

The first equation for len handles the empty list case.

This is called the base case.

The second equation handles nonempty lists. This is called the *recursive* case, since it contains we call the powcoder

len (x:xs) = 1 + len xs

If you want to be a good programmer in a declarative language, you have to get comfortable with recursion, because most of the things you need to do involve recursion.

# Using a function

```
len []
Assignment Project Exam Help Given a function definition like this, the Haskell implementation can use the
to replace calls to the function with the right hand side of an applicable
equation.
            ttps://powcoder.com
step 1: 1 + len ["b"] -- ("b":[])
step 2: 1 + 1 + len []
step 3: Add WeChat powcoder
```

step 5: 2

### **Expression** evaluation

To evaluate an expression, the Haskell runtime system conceptually executes a loop, each iteration of which consists of these steps:

# looks for a function call in the current expression.

- searches the list of equations defining the function from the top downwards, looking for a matching equition,
- sets the values of the variables in the matching pattern to the corresponding parts of the actual arguments, and
- replaces the left hand side of the equation with the right hand side.

The loop stops when the current expression contains no function calls, not even calls to such builtin "functions" as addition.

The actual Haskell implementation is more sophisticated than this loop, but the effect it achieves is the same.

#### Order of evaluation

len []

The first step in each iteration of the loop, "look for a function call in the Aurrent expression", can find Project Exam Help

#### **Church-Rosser theorem**

In 1936, Alonzo Church and J. Barkley Rosser proved a famous theorem, which says that for the rewriting system known is the lambda of fully regardless of the black in which the original terms of subterms are rewritten the final result is always the same.

This theorem also holds for Haskell and for several other functional programming an Sees (tog) with Older. Com

This is not that surprising, since most modern functional languages are based on one variant or another of the lambda calculus.

We will ight Cle ord of Clua in the High Wreso ( to two since in most cases it does not matter. We will come back to the topic later.

The Church-Rosser theorem is *not* applicable to imperative languages.

# Order of evaluation: efficiency

```
Assignment Project Exam Help
```

https://powcoder.com

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# Order of evaluation: efficiency

```
Assignment Project Exam Help
```

```
0: all_pos_[-1, 2]//powcoder.com
1: -1 > nttps://powcoder.com
2: False && all_pos [2]
```

3: False

# Add WeChat powcoder

all\_pos [] = True

evaluation order A:

# Order of evaluation: efficiency

```
Assignment Project Exam Help
```

# Add WeChat powcoder

6: False && True

7: False

all\_pos [] = True

# Imperative vs declarative languages

In the presence of side effects, a program's behavior depends on history;

that is the order of evaluation project Exam Help Because understanding an effectful program requires thinking about all possible histories, side effects often make a program harder to understand.

When deteloping larger/programs or working in teams, managing side-effects is entrol and difficult, Haskel guarantees the assence of side-effects.

What really distinguishes pure declarative languages from imperative languages is that they work allows determined by the content of the languages is that they work allows determined by the content of the languages from imperative languages from impera

There is only one benign exception to that: they do allow programs to generate exceptions.

We will ignore exceptions from now on, since in the programs we deal with, they have only one effect: they abort the program.

### Referential transparency

The absence of side effects allows pure functional languages to achieve referential transparency, which means that an expression can be replaced with its value. This requires that the expression has no dide effects and ippure, i.e. always returns the same results on the same input.

By contrast, in imperative languages such as C, functions in general are not pure no

Impure functional languages such as Lisp are called impure precisely because the permitted description and permitted descriptions are not referentially transparent.

# Single assignment

One consequence of the absence of side effects is that assignment means comething different in a functional language that has imperativeled parties and the company of the consequence of the absence of side effects is that assignment means the company of the consequence of the absence of side effects is that assignment means the company of the consequence of the absence of side effects is that assignment means the company of the consequence of the

- In conventional, imperative languages, even object-oriented ones (including Chava/and Python) each dariable has a current value (a garbage value if not yet initialized), and assignment statements can change the current value of a variable.
- In functional languages, variables are single assignment, and there are no assignment statement. Yn all define with the output you cannot redefine it. Once a variable has a value, it has that value until the end of its lifetime.

### **Giving variables values**

Haskell programs can give a variable a value in one of two ways.

# Assignment Project Exam Help

This defines pi to be the given value in the expression represented by the dots. It does not define/pi anywhere else.

The implicit way is to put the variable in a pattern on the left hand side of an equation:

len (x:X) dd+Wrechat powcoder

If len is called with a nonempty list, Haskell will bind x to its head and xs to its tail.

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# The Haskell type system

Haskell has a strong, safe and static type system.

The corporary magniful the programmes to be a pointer, as one can in C with (char \*) 42.

The safe part means that a running program is guaranteed never to crash due to a type error (\*C program that deletered the above pointer would almost certainly crash.)

The static part means that types are checked when the program is compiled method the region in all powcoder

This is partly what makes the *safe* part possible; Haskell will not even start to run a program with a type error.

# **Basic Haskell types**

Haskell has the usual basic types. These include:

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- The native integer type is called Int. Values of this type are 32 or 64 bits in size, depending on the platform. Haskell also has a type for integer of points were der.com
- The usual floating-point type is Double. (Float is also available, but its use is discouraged.)
- The Araded ty Well that powcoder

There are also others, e.g. integer types with 8, 16, 32 and 64 bits regardless of platform.

There are more complex types as well.

#### The types of lists

In Haskell, list is not a type; it is a *type constructor*.

## Giversary over 17 the part of the continue of

You can have lists of any type. For example,

- [Bo Titp Sype of Street of Content of Street of Street
- [[Int]] is the type of lists of lists of native integers.

These are smith to Live est spatan parkets of the rer, and LinkedList<LinkedList<Integer>> in Java.

Haskell considers strings to be lists of characters, whose type is [Char]; String is a synonym for [Char].

The names of types and type constructors should be identifiers starting with an upper case letter; the list type constructor is an exception.

#### ghci

The usual implementation of Haskell is ghc, the Glasgow Haskell

```
Signment Project Exam Help $ ghci $ ...

Prelude let x = 2/powcoder.com

Prelude x + (3 * y)

14
```

The prelide is haskell's standard fibrary. powcoder

ghci uses its name as the prompt to remind users that they can call its functions.

#### Types and ghci

You can ask ghci to tell you the type of an expression by prefacing that

Axpression with it. The compand is the tell phai to print the two as the compand is the tell phai to print the two as

```
Prelude> :t "abc"
"abc" [Char] Prelude LDS://powcoder.com
Prelude> "abc"
"abc"
    Add WeChat powcoder
```

The notation x: y says that expression x is of type y. In this case, it says "abc" is of type [Char].

it is ghci's name for the value of the expression just evaluated.

#### **Function types**

You can also ask ghci about the types of functions. Consider this

Aunction, which checks whether list is empty: Exam Help is Empty (\_:\_) = False

(\_ is a spicial pattern that matches anything er.com

If you ask ghoi about its type, you get

```
> :t isEmpty
isEmptyA:ded-WeChat powcoder
```

A function type lists the types of all the arguments and the result, all separated by arrows. We'll see what the a means a bit later.

#### **Function types**

Programmers should declare the type of each function. The syntax for this As similar to the notation printed by give: the function name, a double p

module Emptiness where

isEmptyhttps://powcoder.com
isEmpty [] = True
isEmpty \_ = False

Declaring the green of whether is equired ploy to post one green ing style. The Haskell implementation will infer the types of functions if not declared.

Haskell also infers the types of all the local variables.

Later in the subject, we will briefly introduce the algorithm Haskell uses for type inference.

#### **Function type declarations**

With type declarations, Haskell will report an error and refuse to compile the file of the declared type of a function is incompatible with its definition. It's also appear or if a call to the function is incompatible with its declared type.

Without leclarations. Haskell will report an irror if the types in any call to any function are incompatible with its dentitien. Haskell will never allow code to be run with a type error.

Type declarations improve Haskell's error messages, and make function definition and lesselve messages and make function definition and lesselve messages.

#### **Number types**

Haskell has several numeric types, including Int, Integer, Float, and Couble A plain integer constant belongs to all protein. So what he type we are 13 12 X and Help

```
Prelude> :t 3
3 :: Num p => p
Prelude | Prelud
```

In these massages a thin or types, not varieties. They are variables that stand for types, not varieties.

The notation  $Num\ p$  means "the type p is a member of type class Num". Num is the class of numeric types, including the four types above.

The notation  $3 :: Num p \Rightarrow p$  means that "if p is a numeric type, then 3 is a value of that type".

#### Number type flexibility

The usual arithmetic operations, such as addition, work for any numeric

### nment Project Exam He (+) :: (Num a) => a -> a -> a

The nota nttps://pow/corebetfatGostm arguments and returns a result, all of which have to be of the same type (since they are denoted by the same type variable, a), which in this case must be a member of the type that powcoder. This flexibility is nice, but it does result in confusing error messages:

```
Prelude> [1, True]
  No instance for (Num Bool) arising from the literal '1'
```

#### if-then-else

-- Definition A

signment Project Exam Help if-then-elses in imperative languages in that

- the disetatrois not opposite wooder.com
   the then and else arms are expressions, not statements.

### Add WeChat powcoder

#### **Guards**

-- Definition B

## Assignment Project Exam Help

| n > 0 = iota (n-1) ++ [n]

Definition B uses guards to specify cases. Note the first line does not end with an 'fitted Stard/lip petwecoce of the one that case, much as in definition A.

Note that the second guard specifies n>0. What should happen if you do iota A37 What we explain that the second guard specifies n>0. What should happen if you definition A?

#### **Structured definitions**

Some Haskell equations do not fit on one line, and even the ones that do

Ait are often better split agrospeveral Guards are only one example of p

-- Definition C

iota n =

if https://powcoder.com

## \*Add-WeChat powcoder

The offside rule says that

- the keywords then and else, if they start a line, must be at the same level of indentation as the corresponding if, and
- if the then and else expressions are on their own lines, these must be *more* indented than those keywords.

#### Parametric polymorphism

Here is a version of the code of len complete with type declaration:

## Assignment Project Exam Help

```
len [] = 0
len (_;xs) = 1 + len xs

This function, like many of the sir Haskelf, is polymorphic. The phrase "poly morph" means "many shapes" or "many forms". In this context, it means that len can process lists of type t regardless of what type t is, i.e. regardless of what the form of the ements is WCOCET
```

The *reason* why len works regardless of the type of the list elements is that it does not do anything with the list elements.

This version of len shows this in the second pattern: the underscore is a placeholder for a value you want to ignore.

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#### Type definitions

Like most languages, Haskell allows programmers to define their own types. The simplest type definions define types that are similar the languages that are similar the languages are similar to leave the simplest type definions define types.

data Gender = Female | Male
data Role = Staff | Student

This define the Stype Devy Cold Che Colm wo values Female and Male, while the type called Role has the two values Staff and Student.

Both type are as construct a type are types, they each construct a type.

The four values are also called *data constructors*. Given zero arguments, they each construct a value (a piece of data).

The names of type constructors and data constructors must be identifiers starting with upper-case letters.

#### **Using Booleans**

You do not have to use such types. If you wish, you can use the standard Boolean type instead like thi

# Time Project Exam Help

```
intended usage: show1 isFemale isStaff
                  7 "female staff"
show1 True True
show1 False True
show1 False False = "male student"
```

### Veletrat powcoder

- let isFemale = True
- let isStaff = False
- show1 isFemale isStaff

#### Using defined types vs using Booleans

> show1 isFemale isStaff
> show1 isStaff eisFema Project Exam Help

The problem with using Booleans is that of these two calls to show1, only one matches the programmer's intention, but since both are type correct (both surply two Boolean arguments). High competition catcher correct switch the arguments.

```
show2 :: Gender -> Role -> String
```

With short, the kell carry and will be the program any angine out it switch. This makes the program safer and the programmer more productive.

In general, you should use separate types for separate semantic distinctions. You can use this technique in any language that supports enumerated types.

#### Representing cards

Here is one way to represent standard western playing cards:

## Assignmenta Project Exam Help

= R2 | R3 | R4 | R5 | R6 | R7 | R8 | R9 | R10

https://powcoder.com

data Card = tard Suit Rank

The types Suit and Rank would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type Card would be enumerated types in C, while the type C and type C and

On the right hand side of the definition of the type Card, Card is the name of the *data constructor*, while Suit and Rank are the types of its two arguments.

#### **Creating structures**

data Card = Card Suit Rank

appearance), but (from its second appearance) also the name of the data constructor which constructs the "structure" from its arguments.

In languages like C creating a structure and filling it in requires a call to malloc of its equivalent, Pheck of its return value, and an assignment to each field of the structure. This typically takes several lines of code.

In Haskell, you can construct a structure just by writing down the name of the data constructor, who were by in argument, why this One Tub Ace. This typically takes only part of one line of code.

In practice, this seemingly small difference has a significant impact, because it removes much clutter (details irrelevant to the main objective).

#### **Printing values**

Many programs have code whose job it is to print out the values of a given type in a way that is meaningful to the program ner. Such functions are particularly useful adving various forms of tesus girds.

The Haskell approach is use a function that returns a string. However, writing such functions by hand can be tedious, because each data constructor equivasity on the constructor of the

```
showrank :: Rank -> String
showrank R2 = "R2"
showrank R2 = "R2"
we Chat powcoder
...
```

#### **Show**

The Haskell prelude has a standard string conversion function called show.

Aust as the arithmetic function are applicable to all types that free the type class Num, this function is applicable to all types that are members of the type class Show.

You can tell Haskell that the show function for values of the type Rank is showrant: Itps://powcoder.com

instance Show Rank where show = showrank

This of course requires defining showrank. If you don't want to do that, you can get Hatel to define the flow function of the local fine deriving Show to the type's definition, like this:

```
data Rank =
    R2 | R3 | R4 | R5 | R6 | R7 | R8 |
    R9 | R10 | Jack | Queen | King | Ace
    deriving Show
```

#### Eq and Ord

Another operation even more important than string conversion is

To be able to use Haskell's == comparison operation for a type, it must be in the Eq type class. This can also be done automatically by putting deriving Eq at the end of a type definition.

To compare values of a type for order (using Care), the type must be in the Ord type class, which can also be done by putting deriving Ord at the end of a type definition. To be in Ord, the type must also be in Eq.

To derive rutibe typ Vace paratesis pow COCCT data Suit = Club | Diamond | Heart | Spade deriving (Show, Eq, Ord)

#### Disjunction and conjunction

data Suit = Club | Diamond | Heart | Spade

A value Cype Suit is either a Club or a Diamond or a Heart or a Spade. This disjunction of values corresponds to an enumerated type.

A value of type Card contains a value of type Suit and a value of type Rank. This contains of values corresponds to a structure type.

In most imperative languages, a type can represent either a disjunction or a conjunction, but not both at once.

a conjunction, but not both at enge.

Haskell and read languages to not have provided provided to the provided prov

#### Discriminated union types

Haskell has discriminated union types, which can include both disjunction

systems that allows them to be combined in this way are often called algebraic type systems, and their types algebraic types.

data Joker Colpressed Proceder. Com

data JCard = NormalCard Suit Rank | JokerCard JokerColor

data board Normarodra barb ham | bonorodra bonorodro

# A value of type J Carris constructed to either using the Normal Card constructor, in which case it contains a

- either using the NormalCard constructor, in which case it contains a
  value of type Suit and a value of type Rank,
- or using the JokerCard constructor, in which case it contains a value of type JokerColor.

#### Discriminated vs undiscriminated unions

In C, you could try to represent JCard like this:

```
AssignmentuProject Exam Help
struct Skercard_struct { ...};
union card_union {
struct_normalcard_struct_normal;
struct_pscard_powcoder.com
};
```

but you wouldn't know which field of the union is applicable in any given case. In Haket you work at apparture of the lata postructor of

Note that unlike C's union types, C's enumeration types and structure types are special cases of Haskell's discriminated union types.

Discriminated union types allow programmers to define types that describe *exactly* what they mean.

#### Maybe

In languages like C, if you have a value of type \*T for some type T, or in Anguages like lava, if you have a value of some non-primitive type call parties will be a value of some non-primitive type call parties will be a value of some non-primitive type call parties will be a value of type \*T for some type T, or in Anguages like C, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you have a value of type \*T for some type T, or in Anguages like Lava, if you hav

If not, the value represents a value of type T. If yes, the value *may* represent a value of type T, or it may represent nothing. The problem is, often the represent a value of type T, or it may represent nothing. The problem is, often the represent a value of type T, or it may represent nothing. The problem is,

And even if the value **must** not be null, there's no guarantee it won't be. This can lead to segfaults or NullPointerExceptions.

In Haskell to the light of the

data Maybe t = Nothing | Just t

For any type t, a value of type Maybe t is either Nothing, or Just x, where x is a value of type t. This is a polymorphic type, like [t].

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#### Representing expressions in C

```
signment Project Exam Help
typedef struct expr_struct *Expr;
struct https://powcoder.com
   ExprKind kind;
           walue: expr_NUM */
ham ve hate powcoder
                    /* if EXPR BINOP */
   Binop
           binop;
                    /* if EXPR_UNOP */
   Unop
           unop;
           subexpr1; /* if EXPR_BINOP or EXPR_UNOP */
   Expr
           subexpr2; /* if EXPR_BINOP */
   Expr
};
                                  4 日 ) 4 周 ) 4 達 ) 4 達 )
```

typedef enum {

#### Representing expressions in Java

```
Assignment Project Exam Help
```

```
public class NumExpr extends Expr {
    inthttps://powcoder.com
    ... implementation of abstract methods ...
}

public Account powcoder
    String name;
    ... implementation of abstract methods ...
}
```

#### Representing expressions in Java (2)

```
public class BinExpr extends Expr {
 ssignment Project Exam Help
   Expr arg2;
   ... implementation of abstract methods ...
    https://powcoder.com
public class UnExpr extends Expr {
  ExpA dd WeChat powcoder
   ... implementation of abstract methods ...
```

#### Representing expressions in Haskell

```
Assignment Project Exam Help
```

```
| Binop Binopr Expr Expr | Unop Unopr Expr | https://powcoder.com | data Binopr Flus | Minus Times | Divide | data Unopr = Negate
```

As you car see this it is much more direct definition of the set of values that the programmer wants to represent POWCOCCI

It is also much shorter, and entirely free of notes that are meaningless to the compiler and understood only by humans.

#### Comparing representions: errors

By far the most important difference is that the C representation is quite

# Arssignment Project Exam Help You can access a field when that field is not meaningful, e.g. you can

- You can access a field when that field is not meaningful, e.g. you can access the subexpr2 field instead of the subexpr1 field when kind is EXPLUNOP.
- You can loge to init plus some of the fields, e.g. You can forget to assign to the name field when setting kind to EXPR\_VAR.
- You can forget to process some of the alternatives, e.g. when switching of the vivide did, our may in the vivide four enum values.

The first mistake is literally impossible to make with Haskell, and would be caught by the Java compiler. The second is guaranteed to be caught by Haskell, but not Java. The third will be caught by Java, and by Haskell if you ask ghc to be on the lookout for it.

#### **Comparing representions: memory**

The C representation requires more memory: seven words for every expression, whereas the Java and Haskell representations needs the law for the kind, and three for arguments members).

Using unions can make the C representation more compact, but only at the expense of more complexity, and therefore a higher probability of programmer letters://powcoder.com

Even with unions, the C representation needs four words for all kinds of expressions. The Java and Haskell representations need only two for numbers and carriables wide free or expression with the property operators.

This is an example where a Java or Haskell program can actually be *more efficient* than a C program.

#### **Comparing representions: maintenance**

Adding a new kind of expression requires:

### Assignment Project Examillelp

C: Adding a new alternative to the enum and adding the needed members to the type, and adding code for it to all functions

#### https://bowcoder.com Haskell Adding a new alternative, with arguments, to the type, and

Haskell Adding a new alternative, with arguments, to the type, and adding code for it to all functions handling that type

### Adding a Awdedati Wife presinate prowcoder

**Java:** Adding a new method to the abstract Expr class, and implementing it for each class

C: Writing one new function

Haskell Writing one new function

#### **Switching on alternatives**

```
is_static :: Expr -> Bool

is_static expr =

cashtops://powcoder.com

Number _ -> True

Variable _ -> False

Anot d expri = Cashtatic expri powcoder

is_static expr1 && is_static expr2
```

This function figures out whether the value of an expression can be known statically, i.e. without having to know the values of variables.

#### Missing alternatives

If you specify the option -fwarn-incomplete-patterns, ghc and ghci

Avil warn about any missing Proatives, both in Case expression Inching

Sets Programme Troject Exam Help

This option is particularly useful during program maintenance. When you add a new alternative to an existing type, all the switches on values of that type in the program control of the type in the program of the type in the program of the program

If you always compile the program with this option, the compiler will tell you all the with the in the gogram that must be writing der

Without such help, programmers must look for such switches themselves, and they may not find them all.

#### The consequences of missing alternatives

If a Haskell program finds a missing alternative at runtime, it will throw an exception, which (unless caugh and handled) will abort the program. Without edefault case, a C program would simply go on and silently compute an incorrect result. If a default case is provided, it is likely to just print an error message and abort the program. C programmers thus have to do moet dripton. Haskell programmer less to detupt the level of safety offered by Haskell.

If an abstract method is used in Java, this gives the same safety as Haskell. However, however, however alone for tetting to write method for a subclass will just inherit the (probably wrong) behaviour of the superclass.

#### Binary search trees

Here is one possible representation of binary search trees in C:

# Assignment Project Exam Help

```
int value; // powcoder.com

BST right;
```

};

### Here it is Atdd: We Chat powcoder

```
data Tree = Leaf | Node String Int Tree Tree
```

The Haskell version has two alternatives, one of which has no associated data. The C version uses a null pointer to represent this alternative.

#### Counting nodes in a BST

countnodes :: Tree -> Int

```
ssignment Project Exam Help
  1 + (countnodes 1) + (countnodes r)
int coulittps://powcoder.com
  if (tree == NULL) {
  *Add WeChat powcoder
        countnodes(tree->left) +
        countnodes(tree->right);
```

213 / 419

#### Pattern matching vs pointer dereferencing

The left-hand-side of the second equation in the Haskell definition Anaturally gives names to each of the fields of the mode that actually need has a used they are used in the right wand side. An The D

These variables do not have to be declared, and Haskell infers their types.

The C version refers to these fields using syntax that dereferences the pointer tree and accesses one of the fields of the structure it points to.

The C code is longer, and using Haskell-like names for the fields would

```
BST 1 = Add ef We Chat powcoder
BST r = tree->right;
```

. . .

#### Searching a BST in C (iteration)

```
int search_bst(BST tree, char *key, int *value_ptr)

Assignment Project Exam Help
```

```
cmp_result = strcmp(key, tree->key);
      ps://powcoder.com
      return TRUE:
   } else if (cmp_result < 0) {</pre>
  Add: WeChat powcoder
      tree = tree->right;
return FALSE;
```

search\_bst :: Tree -> String -> Maybe Int

#### Searching a BST in Haskell

```
Assignment Project Exam Help
```

```
sk < k = search_bst l sk
oth
ttps://poweoder.com
```

- If the search succeeds, this function returns Just v, where v is the searched-for value.
- If the decide ils Wree as hats powcoder
- We could have used Haskell's if-then-else for this, but guards make the code look much nicer and easier to read.

#### Data structure and code structure

The Haskell definitions of countnodes and search but have similar

## an equation handling the case where the tree is empty (a Leaf), and

- an equation handling the case where the tree is nonempty (a Node).

The type wet to process in Distwice Iso the M functions have two equations: one for each alternative.

This is quite a common occurrence:

- a functional see Wile Chartuc DOWN COCKETS all or a selected part of that data structure, and
- what the function needs to do often depends on the shape of the data, so the structure of the code often mirrors the structure of the data.

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# Assignment Broject Exam Help Declarative Programming

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#### Writing code

Consider a C function with two loops, and some other code around and Assignment Project Exam Help straight line code A 10 https://powcoder.com loop 2 straight line code C ld WeChat powcoder

◆ロト ◆部 ト ◆ 恵 ト ◆ 恵 ・ 夕 へ ②

#### The functional equivalent

```
loop1func base case
Assignment Project Exam Help
                                       loop2func base case
                                       loop2func recursive case
                                     https://powcoder.com
                                                                                                        let \dots = \dots in
                                                                                                    \overset{\text{let}}{\overset{\text{let}}{A}}\overset{\text{d}}{\overset{\text{d}}{\overset{\text{levolute}}{\overset{\text{let}}{\overset{\text{let}}{A}}}}}\overset{\text{def}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{let}}}{\overset{\text{let}}{\overset{\text{let}}}{\overset{\text{let}}{\overset{\text{let}}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}{\overset{\text{let}}}{\overset{\text{let}}}{\overset{\text{let}}}{\overset{\text{let}}}{\overset{\text{let}}}{\overset{\text{let}}}{\overset{\text{let}}}{\overset{\text{let}}}{\overset{\text{let}}}{\overset{\text{let}}{\overset{\text{let}}}{\overset{let}}}}{\overset{\text{let}}{\overset{let}}}{\overset{\text{let}}{\overset{let}}}}{\overset{\overset{let}}{\overset{\overset{let}}{\overset{let}}}}{\overset{l
                                                                                                      let r2 = loop2func ... in
```

The only effect of the absence of iteration constructs is that instead of writing a loop inside somefunc, the Haskell programmer needs to write an auxiliary recursive function, usually outside somefunc.

. . .

#### Example: C

```
int f(int *a, int size)
ssignment Project Exam Help
  int first_gt_target;
  whattps://poweoder.com
  i++:
  first_gt_target = a[i];
  return 3 * first_gt_target;
```

#### **Example: Haskell version**

```
f :: [Int] -> Int
Assignments Project Exam Help
          (x:xs) \rightarrow
        https://ptweodergtcomet in
  skip_init_le_zero :: [Int] -> [Int] skip_inA derowe(1 hat powcoder skip_init_le_zero (x:xs) =
      if x <= 0 then skip_init_le_zero xs else (x:xs)
  find_gt :: [Int] -> Int -> Int
  find_gt (x:xs) target =
      if x <= target then find_gt xs target else x
```

#### Recursion vs iteration

Functional languages do not have language constructs for iteration. What iterative language program po with iteration, functional language programs and the language programs are languaged by the language programs and the language programs are languaged by the language constructs for iteration. What iteration is a supplied to the language constructs for iteration. What is a supplied to the language constructs for iteration. What is a supplied to the language constructs for iteration. What is a supplied to the language constructs for iteration. What is a supplied to the language constructs for iteration. What is a supplied to the language constructs for iteration is a supplied to the language constructs for iteration.

For a programmer who has known nothing but imperative languages, the absence of iteration can seem like a crippling limitation.

In fact, it is not a limitation at all. Any loop can be implemented with recursion, but some recursions are difficult to implement with iteration.

There are several viewpoints to consider;

- How does this affect the process of wating code?
- How does this affect the reliability of the resulting code?
- How does this affect the productivity of the programmers?
- How does this affect the efficiency of the resulting code?

#### C version vs Haskell versions

The Haskell versions use lists instead of arrays, since in Haskell, lists are

### Assignment Project Exam Help With -fw2n-incomplete-pattern, Haskell will warn you that

- there may not be a strictly positive number in the list;
- ther https://poweodertecome list,

and that these situations need to be handled.

The C compiler cannot generate such warnings. If the Haskel code operated an array, W Haskell Ambier 3 Converted CT

The Haskell versions give meaningful names to the jobs done by the loops.

#### Reliability

The names of the auxiliary functions should remind readers of their tasks.

These functions should give the meaning of the arguments, and describe the relationship between the arguments and the return value.

This description should allow readers to construct a correctness argument for the function PS. / POWCOGET. COM

The imperative language equivalent of these function descriptions are *loop* invariants, but they are as rare as hen's teeth in real-world programs.

argument gives programmers a chance to notice situations where the (implicit or explicit) correctness argument doesn't hold water.

The fact that such writing down occurs much more often with functional programs is one factor that tends to make them more reliable.

#### **Productivity**

Picking a meaningful name for each auxiliary function and writing down its documentation takes time. Project Exam Help This cost unposed on the original author of the code is repaid manyfold when

- other members of the team read the colle and find it easier to read and understant. POWCOUEL. COM
- the *original author* reads the code much later, and finds it easier to read and understand.

Properly counted ed wickers, where crede was income or not, can be reused. Separating the code of a loop out into a function allows the code of that function to be reused, requiring less code to be written overall.

In fact, modern functional languages come with large libraries of prewritten useful functions.

#### **Efficiency**

The recursive version of e.g. search\_bst will allocate one stack frame for pack node of the tree it travers, while the iterative version will be partially allocate one stack frame for the partial to ject Exam Help

The recursive version will therefore be less efficient, since it needs to allocate, fill in and then later deallocate more stack frames.

The recursive version will also need more stack space. This should not be a problem for search\_bst, but the recursive versions of some other functions can run out of stack space.

However, and the force tive natural way to be the optimization of recursive code. In many cases, they can take a recursive algorithm in their source language (e.g. Haskell), and generate iterative code in their target language.

#### **Efficiency in general**

Overall, programs in declarative languages are typically slower than they would be if written in C. Depending on which declarative language and purpose the slowdown can range from a few percent to huge integer factors, such as 10% to a factor of a 100.

However, pobliping ages to the fact, their programs will typically be significantly slower than corresponding Haskell programs.

In general he higher the lose of hoperamoving two does for the programmer), the slower its programs will be on average. The price of C's speed is the need to handle all the details yourself.

The right point on the productivity vs efficiency tradeoff continuum depends on the project (and component of the project).

#### **Sublists**

Suppose we want to write a Haskell function

### Assignment Project Exam Help

that returns a list of all the "sublists" of a list. A list a is a sublist of a list b iff every element of a appears in b in the same order, though some elements by the Second of the sublists appear in the resulting list.

For example:

How would you implement this?

#### **Declarative thinking**

Some problems are difficult to approach imperatively, and are much easier to think about declaratively. Project Exam Helr

The imperative approach is procedural: we devise a way to solve the problem step by step. As an afterthought we may think about grouping the steps into chunks (methods, procedures, functions, etc.)

The declarative approach treaks now the problem at chunks (functions), assembling the results of the chunks to construct the result.

You must be careful in imperative languages, because the chunks may not compose the file-everte the flight approvement of the languages.

#### Recursive thinking

One especially useful approach is recursive thinking: use the function you Arssignment Project Exam Help

- Determine how to produce the result for the whole problem from the result for the garts of the myself requester case).

  Determine the solution for the smallest part of the input (base case).

Keep in mind the specification of the problem, but it also helps to think of concrete Andel WeChat powcoder

For lists, (1) usually means generating the result for the whole list from the list head and the result for the tail; (2) usually means the result for the empty list.

This works perfectly well in most imperative languages, if you're careful to ensure your function composes. But it takes practice to think this way.

#### **Sublists again**

Write a Haskell function:

```
Assignmental Project Exam Help sublists "ABC" = ["ABC", "AB", AC", "A", "BC", "B", "C", ""]
 sublists "BC" = ["BC", "B", "C", ""]
How can helpfore [//FDOW/COCHETECOTITE,""] from ["BC", "B", "C, ""] and A?
It is just ["BC", "B", "C", ""] with A added to the front of each string,
followed ba "We Chart powcoder
For the base case, the only sublist of [] is 1] itself, so the list of sublists
of [] is [[]].
```

#### **Sublists again**

The problem becomes quite simple when we think about it declaratively (recursively). The sublists of Dist is the sublists of its tail both with and without the head of the list added to the work of each cubic. The problem is added to the work of each cubic.

```
sublists:: [a] -> [[a]]
sublists [t-p][]/powcoder.com
sublists (t-p)[]/powcoder.com
where restSeqs = sublists es
```

```
addToEach h [] = [] That powcoder
addToEach h (t:ts) = (h:t):addToEach h ts
```

#### Immutable data structures

In declarative languages, data structures are *immutable*: once created, Abey cannot be changed so Pat do you do aif you do need to Pate 1

You create another version of the data structure, one which has the change you want to make, and use that version from then on.

However, 11 Dant to / you and a Cottle Color well. You will definitely want to do so if some part of the system still needs the old version (in which case imperative code must also make a modified copy).

### The old vaid a We Chat powcoder

- because both old and new are needed, as in sublists
- to implement undo
- to gather statistics, e.g. about how the size of a data structure changes over time

#### **Updating a BST**

Note that *all* of the code of this function is concerned with the job at hand; there is no code concerned with memory management.

In Haskell As in the value management is outworked by the garbage collector.

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#### Polymorphic types

Our definition of the tree type so far was this:

## Assignmentd Project Exam Help This type assumes that the keys are strings and the values are integers.

However, the functions we have written to handle trees (countnodes and search\_list do not really care about the tyles of the keys and values.

We could also define trees like this:

data Tree k v = Leaf | Node k v (Tree k v) (Tree k v)

In this case land values, and Tree is a type constructor, which constructs a new type from two other types.

#### Using polymorphic types: countnodes

With the old, monomorphic definition of Tree, the type declaration or

## Assignment Project Exam Help

With the new, polymorphic definition of Tree, it will be

countri**ptips://powcoder.com**Regardless of the types of the keys and values in the tree, countriodes will

count the number of nodes in it.

The exact And a de Wke then a tes. powcoder

#### Using polymorphic types: search\_bst

countnodes does not touch keys or values, but search\_bst does perform to the conference of the confere

```
will not vertified by the reason is that search but contains these two tests:
```

- a comparison for equality: sk == k, and
- a corrector Wee Chat powcoder

#### Comparing values for equality and order

Some types cannot be compared for equality. For example, two functions Ahould be considered equal if to all sets of input argument values, they compute the same result. Unfortunately, it has been proven that testing whether two functions are equal is undecidable. This means that building an algorithm that is guaranteed to decide in finite time whether two functions at tensis: ith pib wcoder.com Some types that can be compared for equality cannot be compared for order. Consider a set of integers. It is obvious that  $\{1, 5\}$  is not equal to  $\{2, 4\}$ , but using the standard method of set comparison (set inclusion), they are otherwise incomparable, notice can be said to be greater than the other.

#### Eq and Ord

In Haskell,

## Assignment Project ExempeHelp belong to the type class Eq, white

• comparison for order can only be done on values of types that belong to the type class of powcoder.com

Membership of trd implies membership of Eq, but not vice versa.

The declaration of search\_bst should be this:

search AddrdW-eChat-powGoder

The construct  $Ord\ k =>$  is a type class constraint; it says search\_bst requires whatever type k stands for to be in Ord. This guarantees its membership of Eq as well.

#### Data.Map

The polymorphic Tree type described above is defined in the standard Aibrary with the name Mapy in the module Data Mapy You can implify it polymers the generation.

import Data.Map as Map

The key https://powcoder.com

```
insert :: Ord k => k -> a -> Map k a -> Map k a

Map.lookup :: Ord k => k -> Map k a -> Maybe a

(!)Addrdw = (ap k at > b ) WCOinte Toperator

size :: Map k a -> Int
```

... and many, many more functions; see the documentation.

#### **Deriving membership automatically**

data Suit = Club | Diamond | Heart | Spade

## Assignment Project Exam Help

The automatically created comparison function takes the order of data constructors from the order in the declaration diself: constructor listed earlier is less than a constructor listed later (e.g. Club < Diamond).

If the two values being compared have the same top level data constructor the attornativally created comparison function compares their arguments in the front effect right this preasure of present types must also be instances of Ord. If the corresponding arguments are not equal, the comparison stops (e.g. Card Club Ace < Card Spade Jack); if the corresponding argument are equal, it goes on to the next argument, if there is one (e.g. Card Spade Ace > Card Spade Jack). This is called *lexicographic* ordering.

#### Recursive vs nonrecursive types

data Tree = Leaf | Node String Int Tree Tree

Assignment Project Exam Help
Tree is a ecursive type because some of its data constructors have arguments of type Tree.

Card is a non-recursive type because none of its data constructors have an arguments of type pard! POWCOTET.COTT

A recursive type needs a nonrecursive alternative, because without one, all values of the type would have infinite size.

values of the type would have infinite size.

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#### Mutually recursive types

Some types are recursive but not *directly* recursive.

## Assignment Project Exam Help

- | BoolOp BoolOp BoolExpr BoolExpr
- CompOp CompOp IntExpr IntExpr
- data Interes://powcoder.com
  - = IntConst Int
    - | IntOp IntOp IntExpr IntExpr
- In a mutually recursive set of types, it is enough for one of the types to

In a mutually recursive set of types, it is enough for one of the types to have a nonrecursive alternative.

These types represent Boolean- and integer-valued expressions in a program. They must be mutually recursive because comparison of integers returns a Boolean and integer-valued conditionals use a Boolean.

#### Structural induction

Code that follows the shape of a nonrecursive type tends to be simple.

### Assignment Project Exam Help

Consider a recursive type with one nonrecursive data constructor (like Leaf in Tree) and one recursive data constructor (like Node in Tree). A function that follows the procure of the root will follow have

- an equation for the nonrecursive data constructor, and
- an equation for the recurrive that a constructor coder

Typically, recursive calls will occur only in the second equation, and the switched-on argument in the recursive call will be *strictly smaller* than the corresponding argument in the left hand side of the equation.

#### **Proof by induction**

You can view the function definition's structure as the outline of a correctness argument. Project Exam Help The argument is a proof by induction on n, the number of data

constructors of the switched-on type in the switched-on argument.

- Base 15 S=1/190 he in the function correctly handles the case where n=1.
- Induction that: Assume the induction hypothesis: the function correctly bandles all cases where k = 1 this Mypothesis implies that all the recursive calls are correct. If the second equation is correct, then the function correctly handles all cases where  $n \le k + 1$ .

The base case and the induction step together imply that the function correctly handles all inputs.

### **Formality**

Acreet respectively requires a formal specification of the expected relationship between each function's arguments and its result.

Typical software development projects do not do formal proofs of correctness, regardless of what kind of language their code is written in.

However, projects using functional languages do tend to use *informal* correctness arguments slightly more often.

The support of this provide by the ligin programme using consists of nothing more than a natural language description of the criterion of correctness of each function. Readers who want a correctness argument can then construct it for themselves from this and the structure of the code.

### Structural induction for more complex types

If a type has *nr* nonrecursive data constructors and *r* recursive data constructors, what happens Project > Elike Bool Exp Help

You can do structural induction on such types as well.

Such functions will typically have ar nonrecursive equations and r recursive equations, but not always. Sometimes you need mole than one equation to handle a constructor, and sometimes one equation can handle more than one constructor. For example, sometimes all base cases need the same hearment. We Chat powcoder

Picking the right representation of the data is important in every program, but when the structure of the code follows the structure of the data, it is particularly important.

#### Let clauses and where clauses

```
assoc_list_to_bst ((hk, hv):kvs) =
```

## Assignment Project Exam Help

A let clause let name = expr in mainexpr introduces a name for a value to be used in the main expression.

A where clause main expr where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the same meaning, but has the definition where name = expr has the definition where = expr has the definition = expr has the definition = expr has the definition = expr has the ex

Which one you want to use depends on where you want to put the emphasis.

But you can only use where clauses at the top level of a function, while you can use a let for any expression.

### **Defining multiple names**

You can define multiple names with a single let or where clause:

## Assignment Project Exam Help

in mainexpr

https://powcoder.com

mainexpr where

namAddr We Chat powcoder

The scope of each name includes the right hand sides of the definitions of the following names, as well as the main expression, unless one of the later definitions defines the same name, in which case the original definition is shadowed and not visible from then on.

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### First vs higher order

First order values are data.

### Acsopenment Project Exams Help

Third order values are functions whose arguments and results are first or second order values.//powcoder.com
In general, nth order value are functions whose arguments and results are

In general, nth order values are functions whose arguments and results are values of any order from first up to n-1.

Values that belong to an order higher than first are higher order values. Java 8, released mid-2014, supports higher order programming. C also supports it, if you work at it. Higher order programming is a central aspect of Haskell, often allowing Haskell programmers to avoid writing recursive functions.

IntList filter(Bool (\*f)(int), IntList list)

### A higher order function in C

```
ssignment Project Exam Help
  if (list == NULL) {
     return NULL:
                powcoder.com
       ((*f)(list->head)) {
        new_list = checked_malloc(sizeof(*new_list));
        return new_list;
     } else {
        return filtered_tail;
     }
```

### A higher order function in Haskell

Haskell's syntax for passing a function as an argument is much simpler than C's syntax. All you need to do is wrap the type of the higher order argument in parentheses to tell haskel to one argument.

```
filter :: (a -> Bool) -> [a] -> [a]

filter https://powcoder.com

if f x then x:fxs else fxs

where fxs = filter f xs
```

Even though it is ignificant, sho treath is forcing is countly corregeneral than the C version, since it is polymorphic, and thus works for lists with *any* type of element.

filter is defined in the Haskell prelude.

### Using higher order functions

You can call filter like this:

```
ignment Project Exam Help
   filter is_long ["a", "abc", "abcde"] ...
given definitely style powcoder.com
is_even :: Int -> Bool
is_even x = if (mod x 2) == 0 then True else False
                YeChat powcoder
is_pos x = if x > 0 then True else False
is_long :: String -> Bool
is_long x = if length x > 3 then True else False
```

### Backguote

Modulo is a built-in infix operator in many languages. For example, in C or Java; 5 modulo 2 would be pritten; 5 % 21 ASSIGNMENT Project Exam Help Taskell uses mod for the modulo operation, but Haskell allows you to make any function an infix operator by surrounding the function name with

backquotes (backticks, written '). s://tpowcoder.com

is\_even :: Int -> Bool

operators written with backquotes have high precedence and associate to

the left.

It's also possible to explicitly declare non-alphanumeric operators, and specify their associativity and fixity, but this feature should be used sparingly.

### **Anonymous functions**

In some cases, the only thing you need a function for is to pass as an argument to a higher order function like filter in such cases, reiders may find Smore convenient if the call contained the dominition of the function, not its name.

In Haskell, anonymous functions are defined by *lambda expressions*, and you use the life sis. / powcoder.com

```
... filter (\x -> x 'mod' 2 == 0) [1, 2, 3, 4] ... 
... filter (\s -> length s > 3) ["a", "abc", "abcde"] ...
```

This notation is sed to the amount of the companion of th

In the lambda calculus, each argument is preceded by a lambda, and the argument list is followed by a dot and the expression that is the function body. For example, the function that adds together its two arguments is written as  $\lambda a.\lambda b.a + b$ .

### Map

(Not to be confused with Data.Map.)

the Hasker prelude.) Given a function and a list, map applies the function to every member of the list.

```
map :: https://powcoder.com
map f (x:xs) = (f x):(map f xs)
```

Many things that an imporative programmer would do with a loop, a functional regerammen would do with a do to war constitution.

```
get_names :: [Customer] -> [String]
get_names customers = map customer_name customers
```

This assumes that customer\_name is a function whose type is Customer -> String.

### Partial application

Given a function with n arguments, partially applying that function means triving it its first k arguments. Where k < n

The result of the partial application is a closure that records the identity of the function and the values of those k arguments.

This closure behaves as/a/function with n-k arguments. A call of the closure leads to all of the original function with both sets of arguments.

```
is_longer :: Int -> String -> Bool
is_longer limit wellength x > limit
Add WeChat powcoder
... filter (is_longer 4) ["ab", "abcd", "abcdef"] ...
```

In this case, the function is\_longer takes two arguments. The expression is\_longer 4 partially applies this function, and creates a closure which records 4 as the value of the first argument.

### Calling a closure: an example

```
Assignment Project Exam Help
```

```
... filter (is_longer 4) ["ab", "abcd", "abcdef"] ...
In this can the Se of powil cook of the Connes:
```

• is\_longer 4 "ab"

filter f (x:xs) =

- is\_langed d "We Chat powcoder"

Each of these calls comes from the higher order call f x in filter. In this case f represents the closure is\_longer 4. In each case, the first argument comes from the closure, with the second being the value of x.

### **Operators and sections**

If you enclose an infix operator in parentheses, you can partially apply it by

Prelude map (\*3) [1, 2, 3] [3,6,9]

You can attans notation with a least the Cottn guments.

Prelude> map (5 'mod') [3, 4, 5, 6, 7]
[2,1,0,5,5]
Prelude man (1 mow 32 (3 14 at powcoder
[0,1,2,0,1]

### Types for partial application

In most languages, the type of a function with *n* arguments would be

## Serbing like ment Project Exam Help

where at1, at2 etc are the argument types, (at1, at2, ... atn) is To allow the function to be partially applied by supplying the first argument, you need a function with a different type:

### f:: at A dat Wethat powcoder This function takes a single value of type at 1, and returns as its result

another function, which is of type (at2, ... atn) -> rt.

### **Currying**

You can keep transforming the function type until every single argument is supplied separately:

## Aupplied separately: ent Project Exam Help

The transformation from a function type in which all arguments are supplied together to a function type in which the arguments are supplied one by one is eather currying.

In Haskell, all function types are curried. This is why the syntax for function types is what it is. The arrow that makes function types is right associative, solle second correction flow of www. Solid of the parenthesization implicit in the first:

```
is_longer :: Int -> String -> Bool
is_longer :: Int -> (String -> Bool)
```

### Functions with all their arguments

Given a function with curried argument types, you can supply the function ats first argument, then its second, then its third and so on Whatelp Happens Gen you have supplied then the Live Exam Help

is\_longer 3 "abcd"

There are two things you can get wooder.com

- a closure that contains all the function's arguments, or
- the result of the evaluation of the function.

In C and in Cold the Unitages, there would be will see later, they are equivalent.

### **Composing functions**

Any function that makes a higher order function call or creates a closure (e.g. by partially applying another function) is a second order function. This means that both filter and its carters are second order functions.

filter has a piece of data as an argument (the list to filter) as well as a function (the filtering function). Some functions do not take *any* piece of data as a guine it Solution (the Dignitude of the COM)

The builtin operator '.' composes two functions. The expression  ${\tt f}\,$  .  ${\tt g}\,$  represents a function which first calls g, and then invokes {\tt f}\, on the result:

### (f g)AddgWeChat powcoder

### Composing functions: some examples

Suppose you already have a function that sorts a list and a function that Acturns the head of a list if it is one you can then compute the left is: Project Exam Help

```
minimum = head . sort
```

If you also have a function that reverses a list you can also compute the maximum with ery little extra code.

```
maximum = head . reverse . sort
```

This shows that functions created by composition, such as reverse sort, can themselves be part of further compositions.

This style of programming is sometimes called *point-free style*, though *value-free style* would be a better description, since its distinguishing characteristic is the absence of variables representing (first order) values.

### Composition as sequence

Function composition is one way to express a sequence of operations.

### Assignment Project Exam Help

- You start with the input, x.
- You compute step1f x.
- You https://powcoder.com
- You compute step3f (step2f (step1f x)).

This idea is the basis of monads, which is the mechanism Haskell uses to do input out the Wechan powcoder

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### **Higher order programming**

Higher order programming is widely used by functional programmers.

### Assignment Project Exam Help

- code reuse,
- a higher level of abstraction, and
- a set of taking solution to the cuent depintered property.

In programs written by programmers who do not use higher order programming, you frequently find pieces of code that have the same structure but sippliffeevt pieces of the code in the tructure of the code in the

Such code typically qualifies as an instance of the copy-and-paste programming *antipattern*, a pattern that programmers should strive to avoid.

#### **Folds**

We have already seen the functions map and filter, which operate on

# The other lass of popular higher order functions on lists are the reduction operations, which reduce a list to a single value.

The usual reduction operations are folds. There are three main folds: left, right and balanced. / DOWCOGET. COM

left 
$$((((I \odot X_1) \odot X_2)...) \odot X_n)$$
right  $(We (X_1 \odot X_2) \odot (X_3 \odot X_4)) \odot ...$ 
balanced  $((X_1 \odot X_2) \odot (X_3 \odot X_4)) \odot ...$ 

Here  $\odot$  denotes a binary function, the folding operation, and I denotes the identity element of that operation. (The balanced fold also needs the identity element in case the list is empty.)

#### **FoldI**

```
foldl :: (v \rightarrow e \rightarrow v) \rightarrow v \rightarrow [e] \rightarrow v
ssignment Project Exam Help
   let newbase = f base x in
   foldl f newbase xs
.https://powcoder.com
suml = foldl (+) 0
productAdd WeChat powcoder
productl = foldl (*) 1
concatl :: [[a]] -> [a]
concat1 = fold1 (++) []
```

#### **Foldr**

```
foldr :: (e -> v -> v) -> v -> [e] -> v
    ssignment Project Exam Help
                               let fxs = foldr f base xs in
                               f x fxs
   sumr = https://powcoder.com
    productr = foldr (*) 1
You can defind the product of the content of the co
and foldr because addition and multiplication on integers, and list
append, are all associative operations.
```

#### **Balanced fold**

```
balanced fold :: (e -> e -> e) -> e -> [e] -> e
ssignment Project Exam Help
balanced_fold f b l@(_:_:_) =
  let
        ps not powcoder.com
     value1 = balanced_fold f b half1
     Add WeChat powcoder
```

splitAt n 1 returns a pair of the first n elements of 1 and the rest of 1. It is defined in the standard Prelude.

#### More folds

The Haskell prelude defines sum, product, and concat.

Assessing and learning the respective former and the lister empty. For such cases, the Haskell Prelude defines:

fold11:: (a -> a -> a) -> [a] -> a
foldr1 https://powcoder.com

that compute

fold  $o[X_1, X_2, \dots, X_n] = (X_1 \odot (X_2 \odot \dots X_n))$ 

maximum = foldr1 max
minimum = foldr1 min

You could equally well use foldl1 for these.

### Folds are really powerful

You can compute the length of a list by summing 1 for each element, instead of the element itself. To if we can define function that takes parallel and the length of the element itself. To if we can use that define parallel length.

const https://powcoder.com

length = foldr ((+) . const 1) 0
You can map over a list with foldr: powcoder

map f = foldr ((:) . f) []

#### Fold can reverse a list

snoc :: [a] -> a -> [a] snoc tlhttps://powcoder.com

reverse = foldl snoc []

But the Harkett Delute Ceres a fination provide concentration of the con

flip :: 
$$(a \rightarrow b \rightarrow c) \rightarrow b \rightarrow a \rightarrow c$$
  
flip f x y = f y x

reverse = foldl (flip (:)) []

#### **Foldable**

But what about types other than lists? Can we fold over them?

## Acysigmment Project Exam Help Prelude sum (Just 7)

https://powcoder.com

In fact we can fold over any type in the type class Foldable

Prelude Clarwe Chat powcoder foldr :: Foldable t => (a -> b -> b) -> b -> t a -> b

We can declare our own types to be instances of Foldable by defining foldr for our type; then many standard functions, such length, sum, etc. will work on that type, too.

### List comprehensions

Haskell has special syntax for one class of higher order operations. These two implementations of quicks of do the same thing, with the first using the conventions higher order code, and the second using life comprehensions.

```
qs1 [] = []
qs1 (x:xs) = qs1 littles ++ [x] ++ qs1 bigs
where tps://powcoder.com
    littles = filter (<x) xs
    bigs = filter (>=x) xs
```

### 4s2 [] Add WeChat powcoder

### List comprehensions

List comprehensions can be used for things other than filtering a *single* list.

### Assignments Project Exam Help

- a template (an expression, which is often just a variable)
- one or more generators (each of the form var <- list),</li>
- zero https://poweoder.com
- zero or more let expressions defining local variables.

## Some more examples We Chat powcoder

```
rows = "12345678"
chess_squares = [[c, r] | c <- columns, r <- rows]
```

```
pairs = [(a, b) | a \leftarrow [1, 2, 3], b \leftarrow [1, 2, 3]]

nums = [10*a+b | a \leftarrow [1, 2, 3], b \leftarrow [1, 2, 3]]
```

### **Traversing HTML documents**

Types to represent HTML documents:

# Assignment Project Exam Help

HTML\_text String

Hattps://powcoder.com

data Font\_tag = Font\_tag (Maybe Int) (Maybe String)

### Add WeChat powcoder

- = Colour\_name String
- Hex Int
- RGB Int Int Int

font sizes in html :: HTML -> Set Int -> Set Int

### **Collecting font sizes**

```
Assignment Project Exam Help
            font_sizes_in_elt :: HTML_element -> Set Int -> Set Int
            font_sizestinelt/MTML_text code \bar{\text} \bar{\text
                                   let
                                                           Font_tag maybe_size _ _ = font_tag
                                                  Add by English powcoder
                                                                                   Just fontsize -> Data.Set.insert fontsize sizes
                                    in
                                                           font_sizes_in_html html newsizes
            font_sizes_in_elt (HTML_p html) sizes =
                                   font_sizes_in_html html sizes
```

4 日 ) 4 周 ) 4 達 ) 4 達 )

### **Collecting font names**

```
font_names_in_html :: HTML -> Set String -> Set String
Assignment Project Exam Help
  font_names_in_elt :: HTML_element -> Set String -> Set String
  font_nametin_elt /HTML text conder in names m = font_nametin_elt /HTML text conder in names m =
      let
          Font_tag _ maybe_name _ = font_tag
        Add hing English powcoder
              Just fontname -> Data.Set.insert fontname names
      in
          font_names_in_html html newnames
  font_names_in_elt (HTML_p html) names =
      font_names_in_html html names
```

### **Collecting any font information**

```
font_stuff_in_html :: (Font_tag -> a -> a) -> HTML -> a -> a

Afont_stuff_in_html frements_stuff_= Exam Help
```

```
font_stuff_in_elt :: (Font_tag -> a -> a) ->
    HTML element -> a -> a -> a) ->
font_stuff_ip_St./f pro_wec_Oder_com
font_stuff_in_elt f (HTML_font font_tag html) stuff =
    let newstuff = f font_tag stuff in
    font_stuff_in_elt f (HTML_primm) pro_wecoder
    font_stuff_in_elt f (HTML_primm) pro_wecoder
    font_stuff_in_html f html stuff
```

### Collecting font sizes again

```
font sizes in html' :: HTML -> Set Int -> Set Int
issigningent Project Exam Help
```

accumulate\_font\_sizes font\_tag sizes = lettes: powcoder.com Nothing ->

### Add WeChat powcoder Data. Set. insert fontsize sizes

Using the higher order version avoids duplicating the code that traverses the data structure. The benefit you get from this scales linearly with the complexity of the data structure being traversed.

### Comparison to the visitor pattern

The function font\_stuff\_in\_html does a job that is very similar to the ob that the visitor design partern would do in an object-oriented Impulge theraverse a data structure, invoking a function a conor more selected points in the code. However, there are also differences.

- In the Haskell version, the type of the higher order function makes it clear whether the code executed at the selected points just gathers information, or whether it modifies the traversed data structure. In Java, the invoked code is imperative, so it can do either.
- rigon Weden a deportment of Wever Oeke Te classes that correspond to Haskell types in the data structure (in this case, HTML and HTML\_element).
- In the Haskell version, the functions that implement the traversal can be (and typically are) next to each other. In Java, the corresponding methods have to be dispersed to the classes to which they belong.

#### Libraries vs frameworks

The way typical libraries work in any language (including C and Java as well as Haskell) is that code Pitten by the programmer calls furctions in the library of the librar

In some cases, the library function is a higher order function, and thus it can call back a function supplied to it by the programmer.

Application transworks are intraries but they are not typical libraries, because they are intended to be the top layer of a program.

When a program uses a framework, the framework is in control, and it calls function witten by the programmer in the work is in control, and it

For example, a framework for web servers would handle all communication with remote clients. It would itself implement the event loop that waits for the next query to arrive, and would invoke user code only to generate the response to each query.

### Frameworks: libraries vs application generators

Frameworks in Haskell can be done like this, with framework simply being Assignment Project Exam Help

Main = Gramework plugin1 plugin2 plugin3

```
plugin https://powcoder.com
plugin3 = ...
```

This approach could also be used in other languages, since even C and Java support allock vocations in the programmer is then expected to modify. This approach throws abstraction out the window, and is much more error-prone.

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### Representation of C programs in gcc

The gcc compiler has one main data type to represent the code being compiled. The node type is argiant union which has different fields for different finds of entiries. A node can represent, amongst other things,

- a data type,
- a validitips://powcoder.com
- a statement.

Every link of a property of property of the can-represent-everything type.

When Stallman chose this design in the 1980s, he was a Lisp programmer. Lisp does not have a static type system, so the Blub paradox applies here in reverse: even C has a better static type system than Lisp. It's up to the programmer to design types to exploit the type system.

### Representation of if-then-elses

To represent if-then-else expressions such as C's ternary operator

## Assignment Project Exam Help

the relevant union field is a structure that has an array of operands, which should have exactly three elements (the condition, the then part and the else part) half three should be expressions der.com

This representation is subject to two main kinds of error.

- The array of operands could have the wrong number of operands.
- Any Aerald n twarray could point to the wrong kind of tree node.

gcc has extensive infrastructure designed to detect these kinds of errors, but this infrastructure itself has three problems:

- it makes the source code harder to read and write;
- if enabled, it slows down gcc by about 5 to 15%; and
- it detects violations only at runtime.

### **Exploiting the type system**

A well designed representation using algebraic types is not vulnerable to sither kind of error, and is no Publect any of those three kinds of problems.

```
= Const Const
```

https://powcoder.com

Unop Unop Expr

Call String [Expr]

### 'Add WeChat powcoder

```
data Binop = Add | Sub | ...
data Unop = Uminus | ...
data Const = IntConst Int | FloatConst Double | ...
```

#### Generic lists in C

```
typedef struct generic_list List;
assignment Project Exam Help
   List
         *tail;
};
    https://powcoder.com
List
      *int_list;
List
    Add WeChat powcoder
int
for (p = int_list; p != NULL; p = p->tail) {
   item = (int) p->head;
   ... do something with item ...
}
```

### Type system expressiveness

Programmers who choose to use generic lists in a C program need only the list type and therefore on the control of the control

The other alternative in a C program is to define and use a separate list type for every element type of item that the program wants to put into a list. This is type safe, but requires repeated duplication of the functions that operate on lists. Any bugs in those those functions must be fixed in each copy Add WeChat powcoder

Haskell has a very expressive type system that is increasingly being copied by other languages. Some OO/procedural languages now support generics. A few such languages (Rust, Swift, Java 8) support *option types*, like Haskell's Maybe. No well-known such languages support full algebraic types.

#### **Units**

One typical bug type in programs that manipulate physical measurements as unit confusion, such as adding 2 meters and 3 feet, and thinking the result is 5 meters. Many climate Orbite was lost because of such a bug.

Such bugs can be prevented by wrapping the number representing the length in a data constructor giving its unit.

data Language DOWCOder.com

```
meters_to_length :: Double -> Length
meters_tA_length W ech mat powcoder
```

```
feet_to_length :: Double -> Length
feet_to_length f = Meters (f * 0.3048)
```

```
add_lengths :: Length -> Length -> Length
add_lengths (Meters a) (Meters b) = Meters (a+b)
```

#### Different uses of one unit

Sometimes, you want to prevent confusion even between two kinds of Auantities measured in the sap units ect Exam Help For example, many operating systems represent time as the number of seconds elapsed since a fixed epoch. For Unix, the epoch is 0:00am on 1 Jan 1970.

data Dunttps://powcoder.com

data Time = SecondsSinceEpoch Int

add\_durations (Seconds a) (Seconds b) = Seconds (a+b)

```
add_duration_to_time :: Time -> Duration -> Time
add_duration_to_time (SecondsSinceEpoch sse) (Seconds t) =
    SecondsSinceEpoch (sse + t)
```

### Different units in one type

Sometimes, you cannot apply a fixed conversion rate between different units. In such applications, each operation may reed to do conversion in demand a whatever rate is applicable at the time of its execution.

data Money

- antops://powcoder.com
- | GBP\_pounds Double

For financial applications, using Doubles would not be a good idea, since accounting use that were the mentioned transfer of property specific during methods (e.g. for interest calculations) that binary floating point numbers do not satisfy.

One workaround is to use fixed-point numbers, such as integers in which 1 represents not one dollar, but one one-thousandth of one cent.

### Mapping over a Maybe

Suppose we have a type

# Assignment-Project Exam Help

giving a list of all the marks for each student.

(A type declaration like this declares that Marks is an alias for Map String Ut 11 Sjust/tle Cyve Lize Cleans Godhar].)

We want to write a function

that returns Just the total mark for the specified student, or Nothing if the specified student is unknown. Nothing means something different from Just 0.

### Mapping over a Maybe

This definition will work, but it's a bit verbose:

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Nothing -> Nothing

https://powcoder.com

studentTotal marks student = sumAnd dokWselenhats powcoder

but it's a type error:

Couldn't match expected type 'Maybe Int' with actual type 'Int'

#### The Functor class

If we think of a Maybe a as a "box" that holds an a (or maybe not), we want to apply a function inside the box leaving the box in place by replacing its content with the result of the function.

That's actually what the map function does: it applies a function to the contents of a list, returning a list of the results.

What we want pt Sapply process of a Maybe a, returning a Maybe b. We want to map over a Maybe.

The Functor type class is the class of all types that can be "mapped" over. This dide [avoices of the last of the

#### The Functor class

You can map over a Functor type with the fmap function:

# Assignment Project Exam Help

This gives us a much more succinct definition:

Functor is defined in the standard prelude, so you can use fmap over Maybes (and lists) without importing anything.

The standard prelude also defines a function <\$> as an infix operator alias for fmap, so the following code will also work:

sum <\$> Map.lookup student marks

#### **Beyond** Functors

Suppose our students work in pairs, with either teammate submitting the Assignment Project Exam Help
pairTotal :: Marks -> String -> Maybe Int

to return the total of the assessments of two students, or Nothing if either or both on teleprents are powerful elocation.

This code works, but is disappointingly verbose:

```
pairTotal marks student1 student2 =
case studentTVL1C rks realier to WCOCCT

Nothing -> Nothing

Just t1 -> case studentTotal marks student2 of

Nothing -> Nothing

Just t2 -> Just (t1 + t2)
```

### Putting functions in Functors

Functor works nicely for unary functions, but not for greater arities. If we Ary to use fmap on a binary for tion and a May be we wind up with a payment Project Exam Help

Remembering the type of fmap,

fmap: https://powcoder.com
if we take f to be Maybe, a to be Int and b to be Int -> Int, then we

if we take f to be Maybe, a to be Int and b to be Int -> Int, then we see that

fmap (+AddentWeCarlatdpowcoder

returns a value of type Maybe (Int -> Int).

So all we need is a way to extract a function from inside a functor and fmap that over another functor. We want to apply one functor to another.

### Applicative functors

Avhich can be applied to other functors, defined by the Applicative class. The most important function of the Applicative class is

(<\*>) :: f (a -> b) -> f a -> f b which do https://powcoder.com

Happily, Maybe is in the Applicative class, so the following definition works:

# pairTotal dd WeChat2powcoder

let mark = studentTotal marks
in (+) <\$> mark student1 <\*> mark student2

#### Applicative

The second function defined for every Applicative type is

# Assignment Project Exam Help

which just inserts a value into the applicative functor. For the Maybe class, pure = Just. For lists, pure = (:[]) (creating a singleton list).

For example the Santed polymer of the scroll scroll 100, we could do:

(100-) <\$> studentTotal marks student

In fact, every Applicative must also be a Functor, just as every Ord type must be Eq.

### Lists are Applicative

<\*> gets even more interesting for lists:

```
Assignments definite to the line of the latest and something and the latest and the l
```

You can think of <\*> as being like a Cartesian product, hence the "\*".

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#### any and all

Other useful higher-order functions are

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For example, to see if eyery word in a list contains the letter 'e':

```
Prelude all (elem ', p') ["eclectic", "elephant", "legion"]
True
```

# To check if a dd contains a Chart powcoder

```
Prelude> any (\x ->  elem x "aeiou") "sky" False
```

### flip

If the order of arguments of elem were reversed, we could have used furrying rather than the bulk projection. The filelp function takes a function and returns the function with the order of the parguments flipped.

```
Prelude any (flip elem "aeiou") "hmmmm"
False Add WeChat powcoder
```

The ability to write functions to construct other functions is one of Haskell's strengths.

#### **Monads**

Monads build on this strength. A *monad* is a type constructor that depresents a computation. These computations can then be computed to create other computations and so on the power of manads lies in the programmer's ability to determine *how* the computations are composed. Phil Wadler, who introduced monads to Haskell, describes them as "programmable projections" OWCOGET.COM.

A monad M is a type constructor that supports two operations:

- A sequencing operation, denoted >>=, whose type is
   M a A G W e nat powcoder
- An identity operation, denoted return, whose type is a -> M a.

#### **Monads**

Think of the type M a as denoting a computation that produces an a, and possibly carries something extra particular that something extra particular of whether an error hap occurred so far.

- You far take a value of type a and use the (misnamed) identity operation to wrap it in the monad of type constructor.
- Once you have such a wrapped value, you can use the sequencing operation to perform an operation on it. The >>= operation will unwrap its fort any ment and that typical will in our few function given to it as its second argument, which will return a wrapped up result.

### The Maybe and MaybeOK monads

The obvious ways to define the monad operations for the Maybe and

Alaybelk type constructors are these Maybelk Example of the library of the Maybelk Constructors are the Maybelk Constructor

https://powcoder.com

Totall I base I

In a sequence of calls to >>=, as long as all invocations of f succeed, (returning Just x or OK x), you keep going.

Once you get a failure indication, (returning Nothing or Error m), you keep that failure indication and perform no further operations.

### Why you may want these monads

Suppose you want to encode a sequence of operations that each may fail.

```
Assignment Project Exam Help
maybe_head [] = Error "head of empty list"
https://powcoder.com
maybe_sqrt : Int -> MaybeOK Double
maybe_sqrt x =
   if A dd WeChat, powcoder
   else
```

Error "sqrt of negative number"

How can you encode a sequence of operations such as taking the head of a list and computing its square root?

### Simplifying code with monads

```
maybe_head :: [a] -> MaybeOK a
TSSignment Project Exam Help
-- definition not using monads
maybe_https://powcoder.com
      Error msg -> Error msg
    Add WeChat powcoder
-- simpler definition using monads
maybe_sqrt_of_head 1 =
   maybe_head 1 >>= maybe_sqrt
```

### I/O actions in Haskell

Haskell has a type constructor called IO. A function that returns a value of Aype In the for some the will return a value of type the but can also do input and of type the functions of the will return the sound of type the sound of the so

Haskell has several functions for reading input, including

```
getLinehttps://gpowcoder.com
```

Haskell has several functions for writing output, including

```
putStr Addin We Chat powcoder
putStrLn :: String
```

print :: (Show a) => a -> IO ()

The type (), called *unit*, is the type of 0-tuples (tuples containing zero values). This is similar to the void type in C or Java. There is only one value of this type, the empty tuple, which is also denoted ().

### Operations of the I/O monad

The type constructor IO is a monad.

# Absignment Project Exam Help

The sequencing operation: f >>= g

- calls the Say of Own Own in tune of the may be meaningful or may be (),
- 2 calls g rf (passing the return value of f to g), which may do I/O, and which will return a value registrate also may be meaningful or may be (),
- returns rg (inside IO) as the result of f >>= g.

You can use the sequencing operation to create a chain of any number of I/O actions.

### Example of monadic I/O: hello world

hello :: IO ()

# Assignment Project Exam Help

\\_ -> putStrLn "world!"

# This codhtstps0/actpoweedder.com

- The first is a call to putStr. This prints the first half of the message, and returns ().
- and returns ().

  The second can northwas flaton pathwas against and ignores the result of the first action, and then calls putStrLn to print the second half of the message, adding a newline at the end.

The result of the action sequence is the result of the last action.

### **Example of monadic I/O: greetings**

```
greet :: IO ()
ssignmentu Project Exam Help
 >>=
 \_ -> getLine
 >>= https://powcoder.com
    putStr "Where are you from? "
    Add:WeChat powcoder
    \town ->
     let msg = "Welcome, " ++ name ++
             " from " ++ town
      in putStrLn msg
```

#### do blocks

Code written using monad operations is often ugly, and writing it is usually dedious. To address both contents. Haskell provides do blocks. These are merely syntactic sugar for sequences of morad operations, but they make the code much more readable and easier to write.

```
A do block starts with the keyword do, like this:

hello https://powcoder.com

putStr "Hello, "

putStrLn "world"

Add WeChat powcoder
```

#### do block components

Each element of a do block can be

## Assignmentur more clue sxigmped outperson, as the calls to putStr and putStrLn below (just call the function),

- an I/O action whose return value is used to bind a variable, (use https://bevariable.com.bind a variable to a nun-monadic value (use let var = expr (no in)).

```
greet :: IO ()
greet = do
   put Addet We Chatopow coder
   name <- getLine
   putStr "Where are you from? "
   town <- getLine
   let msg = "Welcome, " ++ name ++ " from " ++ town
   putStrLn msg
```

#### **Operator priority problem**

Unfortunately, the following line of code does not work:

### Assignment, Project Exam. Help

The reason is that due to its system of operator priorities, Haskell thinks that the main function being invoked here is not putStrLn but ++, with its left argumen Dang put 30.WiCodOT.COM

This is also the reason why Haskell accepts only the second of the following equations. It parses the left hand side of the first equation as (len x): A, or ds law (ex) hat powcoder

```
len x:xs = 1 + len xs
len (x:xs) = 1 + len xs
```

#### Working around the operator priority problem

There are two main ways to fix this problem:

## Assignment Project Exam Help

The first simply uses parentheses to delimit the possible scope of the ++

operator. https://powcoder.com

The second user another perator, \$, which has lower priority than ++, and thus binds less tightly.

The main function invoked on the line is thus \$. Its first argument is its left operand declunction prostration is the second argument is its right operand: the expression "Welcome, " ++ name ++ " from " ++ town, which is of type String.

\$ is of type (a -> b) -> a -> b. It applies its first argument to its second argument, so in this case it invokes putStrLn with the result of the concatenation.

#### return

```
If a function does I/O and returns a value, and the code that computes

The return value does not do po you will need to invoke the return the last operation of the do block. The last operation of the last operation of the last operation of the last operation of the last operation.
```

```
main :: IO ()
main = do
    putstingsease power der.com
    len <- readlen
    putStrLn $ "The length of that string is " ++ show len</pre>
```

### ${\tt readlen} Add_{\tt nt} We Chat\ powcoder$

```
readlen = do
    str <- getLine
    return (length str)</pre>
```

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### I/O actions as descriptions

Haskell programmers usually think of functions that return values of type to the doing I/O as well as returning a value of type to While this is suitably correct, the care some situacione of which it is dot becaute C enough.

The correct way to think about such functions is that they return two https://powcoder.com

- a value of type t, and

• a description of and/O operation.

The monadic operator >>= can then be understood as taking descriptions of two I/O operations, and returning a description of those two operations being executed in order.

The monadic operator return simply associates a description of a do-nothing I/O operation with a value.

#### Description to execution: theory

Every complete Haskell program must have a function named main, whose signature should be Project Exam Help

As in C, this is where the program starts execution. Conceptually,

- the the system;
- the runtime system calls main, which returns a description of a sequence of I/O operations; and
- the rations stew enter heatscripe were of er operations.

#### Description to execution: practice

In actuality, the compiler and the runtime system together ensure that each O operation is executed as Toph as its description has been computed.

- provided that the description is created in a context which guarantees
  that the description will end up in the list of operation descriptions
  returned by main, and
- provided that all the previous operations of that list have also been executed.

The provisions are never since hat powcoder

• you don't want to execute an I/O operation that the program does

- you don't want to execute an I/O operation that the program does not actually call for, and
- you don't want to execute I/O operations out of order.

### **Example: printing a table of squares directly**

```
main :: IO ()
     gnment Project Exam Help
   print_table 1 10
print_table pur max powerder.com
    cur > max = return ()
     Add We Chat powcoder
      print_table (cur+1) max
table_entry :: Int -> String
table_entry n = (show n) ++ "^2 = " ++ (show (n*n))
```

### Non-immediate execution of I/O actions

Amean that this 1/O action will executed a description of an 1/O action, does not that this 1/O action will executed am Help Haskell programs can pass around descriptions of 1/O operations. They cannot peer into a description of an 1/O operation, but they can nevertheless do things with them, such as

- build up lists of 1/0 actions, and oder.com
- put I/O actions into binary search trees as values.

Those lists and trees whiter be processed further and programmers can, if they wish, take the descriptions of I/O actions out of those data structures, and have them executed by including them in the list of actions returned by main.

### Example: printing a table of squares indirectly

```
main = do
Assignment Project Exam Help
     execute_actions (take 10 row_actions)
 table_anttips." powcoder.com
 show_entry :: Int -> 10 ()
show_entry dd wte(In hate powcoder
  execute_actions :: [IO ()] -> IO ()
  execute actions [] = return ()
  execute_actions (x:xs) = do
     X
```

execute\_actions xs

#### Input, process, output

A typical batch program reads in its input, does the required processing,

And prints its output Project Exam Help A typical exteractive program goes through the same three stages once for each interaction.

In most programs, the vast majority of the ode is in the middle (processing) stage. S. / POW COCET. COM

In programs written in imperative languages like C, Java, and Python, the type of a function (or procedure subroutine or method) does not tell you whether the function was constant powcoder

In Haskell, it does.

### I/O in Haskell programs

In most Haskell programs, the vast majority of the functions are not I/O functions and they do no input or output. They merely build, access and transform data structures, and do cargulations. The code that does I/O a thin veneer on top of this bulk.

This approach has several advantages.

- A unit test for a non-to function is a record of the values of the arguments and the expected value of the result. The test driver can read in those values, invoke the function, and check whether the result—native. The driver are beauty and the content of the values of the arguments are content of the values of the arguments and the values of the arguments and the values of the content of the values of the arguments and the expected value of the result. The test driver can read in those values, invoke the function, and check whether the result.
- Code that does no I/O can be rearranged. Several optimizations exploit this fact.
- Calls to functions that do no I/O can be done in parallel. Selecting the best calls to parallelize is an active research area.

#### **Debugging printfs**

One standard approach for debugging a program written in C is to edit

Your code to insert debugging prints to show you what input your buggy

fametion is called with and what results to computes.

In a program written in Haskell, you can't just insert printing code into functions not already in the IO monad.

Debugging prints are only used for debugging, so you're not concerned with where the output from debugging prints appears relative to other output. This is where the function unsafePerformIO comes in: it allows you to perform output the output miles of purple be wrong.

Do not use unsafePerformIO in real code, but it is useful for debugging.

#### unsafePerformIO

The type of unsafePerformIO is IO  $t \rightarrow t$ .

# Assignment Project, Exama Help type 10 t. unsafePerformIO calls this function.

- The function will return a value of type t and a description of an I/O oper right ps://powcoder.com
   unsafePerformIO executes the described I/O operation and returns
- unsafePerformIO executes the described I/O operation and returns the value.

### Here is an Add: We Chat powcoder

```
sum :: Int -> Int -> Int
sum x y = unsafePerformIO $ do
   putStrLn ("summing " ++ (show x) ++ " and " ++ (show y))
   return (x + y)
```

#### The State monad

The State monad is useful for computations that need to thread information throughout the computation. It allows such information to be transparently passed around a computation, and accessed and replaced purpose when needed. That is, it allows an imperative style of programming without losing Haskell's declarative semantics.

This code to prove the code of the code of

```
data Tree a = Empty | Node (Tree a) a (Tree a)
```

# type In Arde Triving Show powcoder

```
incTree :: IntTree -> IntTree
incTree Empty = Empty
incTree (Node 1 e r) =
   Node (incTree 1) (e + 1) (incTree r)
```

#### Threading state

If we instead wanted to add 1 to the leftmost element, 2 to the next element, and so on, we would peed to pass an integer into our function saying what to add to the *next* element. This requires more complex code:

### Introducing the State monad

```
The State monad abstracts the type s \rightarrow (v,s), hiding away the s
Aart Haskell's do notation alloys us to focus or the y part of the left
  incTree2 · · IntTree -> IntTree
  incTree2 tree = fst (runState (incTree2' tree) 1)
        https://powcoder.com
  incTree2' :: IntTree -> State Int IntTree
  incTree2' Empty = return Empty
  incTree Add Trwe Chat powcoder
     n <- get -- gets the current state
     put (n + 1) -- sets the current state
     newr <- incTree2' r</pre>
     return (Node newl (e+n) newr)
```

### **Abstracting the state operations**

In this case, we do not need the full generality of being able to update the integer state in arbitrary ways he only update operation we need is an increment. We can tweefere provided version of the state monad that is specialized for this task. Such specialization provides useful documentation, and makes the code more robust.

type chttps://powcoder.com

```
withCounter:: Int -> Counter a -> a
withCounterlinit WeChat powcoder
```

```
nextCount :: Counter Int
nextCount = do
    n <- get
    put (n + 1)
    return n</pre>
```

#### Using the counter

Now the code that uses the monad is even simpler:

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#### Eager vs lazy evaluation

In a programming language that uses eager evaluation, each expression is evaluated as soon as it gets bond to a variable either explicitly in an assignment etatement, of implicitly our gar call. (Weath implicitly assigned each actual parameter expression to the corresponding formal parameter variable.)

In a programming Sng/4gp (a We Care this fine the evaluated until its value is actually needed. Typically, this will be when

- the program wants the value as input to an arithmetic operation, or
- the part of Can Wo match hattue Jan W Good of 1
- the program wants to output the value.

Almost all programming languages use eager evaluation. Haskell uses lazy evaluation.

#### Lazyness and infinite data structures

Lazyness allows a program to work with data structures that are conceptually infinite, as long 19the program tooks at only a finite fart of the many latest attack the conceptual the latest the lates

For example, [1..] is a list of all the positive numbers. If you attempt to print it out, the printout will be infinite, and will take infinite time, unless you interpt to print it out. Dowcoder.com

On the other hand, if you want to print only the first n positive numbers, you can do that with take n [1..].

Even though the scondard entire to execute.

-- returns the (infinite) list of all primes

#### The sieve of Eratosthenes

```
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prime_filter :: [Integer] -> [Integer]

prime_filter (:: [Integer] -> [Integer]

prime_filter (x:xs)

powcoder.com

x:prime_filter (filter (not . ('divisibleBy' x)) xs)

-- n 'dAiddByWenshatdpowcoder

divisibleBy n d = n 'mod' d == 0
```

#### Using all\_primes

To find the first n primes:

## Assignment Project Exam Help

To find all primes up to n:

## tal Hittps://powcoder.com

Lazyness allows the programmer of all\_primes to concentrate on the function's task, without having to also pay attention to exactly how the program wents to lected how many parties a concentrate on the

Haskell automatically interleaves the computation of the primes with the code that determines how many primes to compute.

#### Representing unevaluated expressions

In a lazy programming language, expressions are not evaluated until you need their value. However, until then, you do need to remember the code whose execution will compute that a light CCL X and The p

In Haskell implementations that compile Haskell to C (this includes GHC), the data structure you need for that is a pointer to a C function, together with all the tree structure.

This representation is sometimes called a *suspension*, since it represents a computation whose evaluation is temporarily suspended.

It can also decided a porte since at lso poet of the carry out a computation if its result is needed.

Historically inclined people can also call it a *thunk*, because that was the name of this construct in the first programming language implementation that used it. That language was Algol-60.

#### Parametric polymorphism

Parametric polymorphism is the name for the form of polymorphism in which types like [a] and Trepk v and functions like length Intitions with identically regardless of what types the type variables stand for.

The implementation of parametric polymorphism requires that the values of all types leren sentable in Marin of mental Without this, the code of e.g. length wouldn't be able to handle lists with elements of all types.

That "sand amount of memory" hillsy picethy betthe more sixes the machine, which is the size of a pointer. Anything that does not fit into one word is represented by a pointer to a chunk of memory on the heap.

Given this fact, the arguments of the function in a suspension can be stored in an array of words, and we can arrange for all functions in suspensions to take their arguments from a single array of words.

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#### **Evaluating lazy values only once**

Many functions use the values of some variables more than once. This

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| px = x/: takeWhile p xs | Thttps://powcoder.com

You need to know the value of x to do the test p x, which requires calling the function in the suspension representing x; if the test succeeds, you will again need to the theorem of x and x is the test succeeds.

To avoid redundant work, you want the first call to x's suspension to record the result of the call, and you want all references to x after the first to get its value from this record.

Therefore once you know the result of the call, you don't need the function and its arguments anymore.

#### Call by need

Operations such as printing, arithmetic and pattern matching start by

Ansuring their argument is at least partially evaluated. Help

They will make sure that at least the top level data constructor of the value is determined. However, the arguments of that data constructor may remain suspensions.

For example, consider the maten of the second argument of takeWhile against the patterns [] and (p:ps). If the original second argument is a suspension, it must be evaluated enough to ensure its top-level constructor is determined of it is two clien the first argument most be project to x. Whether x needs to be evaluated will depend on what the first argument (function) does.

This is called "call by need", because function arguments (and other expressions) are evaluated only when their value is needed.

#### **Control structures and functions**

(a) ... if (x < y) f(x); else g(y); ...

```
Assignment Project Exam Help
   int ite(bool c, int t, int e)
   { if (c) then return t; else return e; }
  call to both.
   \stackrel{\text{(c)}}{\dots} \stackrel{\text{if } x < y \text{ then } f \ x \text{ else } g \ y \dots}{\text{(d)}} \stackrel{\text{(d)}}{\dots} \stackrel{\text{Add}}{\text{dd}} \stackrel{\text{(d)}}{\text{Wethat}} \stackrel{\text{powcoder}}{\text{powcoder}}
   ite :: Bool -> a -> a -> a
   ite c t e = if c then t else e
  In Haskell, (c) will execute a call to only one of f and g, and thanks to
```

lazyness, this is also true for (d).

#### Implementing control structures as functions

Without lazyness, using a function instead of explicit code such as a dequence of if-then-elses could be undecessary ion-termination practically the second processory ion-termination practically the second processory ion-termination practically the second processor in the second processor is a second processor in the second processor in the second processor is a second processor in the second processor in the second processor in the second processor in the second processor is a second processor in the sec

Lazyness' guarantee that an expression will not be evaluated if its value is not needed allows programmers to define their own control structures as functions <a href="https://powcoder.com">https://powcoder.com</a>

For example, you can define a control structure that returns the value of one of three expressions, with the expression chosen based on whether an expression chosen based on the control of the chosen based on the chosen

#### Using lazyness to avoid unnecessary work

minimum = head . sort

Anthe surfar, this exact like two vereful method for properties the minimum since sorting is usually done with an  $O(n^2)$  or  $O(n \log n)$  algorithm, and min should be doable with an O(n) algorithm.

However, in this case, the evaluation of the lorted list can stop after the materialization of the first element!

If sort is implemented using selection sort, this is just a somewhat higher overhead version of the direct code for min.

overhead version of the direct code for min. Add WeChat powcoder

#### Multiple passes

```
output_prog chars = do

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```

```
let prog = parse tokens
let prog_str = show prog
putrups://powcoder.com
```

This function takes as input one data structure (chars) and calls for the construction of four more (anno\_chars, tokens, prog and prog\_str).

### This kind A range truttle edurs frequent pior execute T

#### The effect of lazyness on multiple passes

With eager evaluation, you would completely construct each data structure

before starting construction Phenest Exam Help The maximum memory needed at any one time will be the size of the largest data structure (say pass n), plus the size of any part of the previous data structure (pass n-1) needed to compute the last part of pass n. All other membry be ga/bar GW ted beotelfen COM

With lazy evaluation, execution is driven by putStrLn, which needs to know what the next character to print (if any) should be. For each character to printe of those data structures needed to figure that out.

The memory demand at a given time will be given by the tree of suspensions from earlier passes that you need to materialize the rest of the string to be printed. The maximum memory demand can be significantly less than with eager evaluation.

#### Lazy input

In Haskell, even input is implemented lazily.

but it returns the string lazily: it reads the next character from the file only when the rest of the program needs that character.

```
parse_proffile file name docoder.com

fs ntteps of perame coder.com

let tokens = scan (annotate_chars 1 1 fs)

return (parse_prof [] tokens)
```

When the nan indulation of the of suspensions.

Only when those suspensions start being forced will the input file be read, and each call to evaluate\_suspension on that tree will cause only as much to be read as is needed to figure out the value of the forced data constructor.

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#### **Effect of lazyness on performance**

Lazyness adds two sorts of overhead that slow down programs.

- Assignments Projectes Examented p most of them are evaluated, so eventually they also need to be unpacked.
  - Ever protection a value must first check check the prince has been materialized yet.

However, lazyness can also speed up programs by avoiding the execution of computation of a large energy of the computation of t

Whether the dominant effect is the slowdown or the speedup will depend on the program and what kind of input it typically gets.

The usual effect is something like lotto: in most cases you lose a bit, but sometimes you win a little, and in some rare cases you win a lot.

#### **Strictness**

Theory calls the value of an expression whose evaluation loops infinitely or Ahrows an exception "bottom Project Exam Help A function is strict if it always needs the values of all its arguments. In formal terms, this means that if any of its arguments is  $\bot$ , then its result will also be  $\bot$ .

The addition that is proceeding the last lecture is nonstrict.

Some Haskell compilers including GHC include strictness analysis, which is a compile has viose to stand the Odd Wile for from Ind figure out which of its functions are strict and which are nonstrict.

When the Haskell code generator sees a call to a strict function, instead of generating code that creates a suspension, it can generate the code that an imperative language compiler would generate: code that evaluates all the arguments, and then calls the function.

#### Unpredictability

Besides generating a slowdown for most programs, lazyness also makes it harder for the programmer to understand where the program is pending most of its time and what parts of the program allocate most of its C memory.

This is because small changes in exactly where and when the program demands a fatto or value an course ge clanges in what arts of a suspension tree are evaluated, and can therefore cause great changes in the time and space complexity of the program. (Lazy evaluation is also called demand driven computation.)

The main problem is that it is very hard for programmers to be simultaneous aware of all the relevant details in the program.

Modern Haskell implementations come with sophisticated profilers to help programmers understand the behavior of their programs. There are profilers for both time and for memory consumption.

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## **Memory efficiency**

(Revised) BST insertion code:

## 

As discussed earlier, this greates new data structures instead of destructive notifying the structure powerful powerful

The advantage of this is that the old structure can still be used.

The disadvantage is new memory is allocated and written. This takes time, and creates garbage that must be collected.

#### **Memory efficiency**

Insertion into a BST replaces one node on each level of the tree: the node on the path from the root to the insertion site. Exam Help In (mostly) balanced trees with n nodes, the height of the tree tends to be about  $log_2(n)$ .

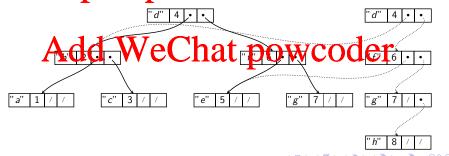
Therefore the number of hodes allocated duling an insertion tends to be logarithmic in the size of the tree. COURT COURT

- If the old version of the tree is not needed, imperative code can do better it invest a ocate only be new node.
- If the old version of the tree is needed timperative code will do worse: it must copy the entire tree, since without that, later updates to the new version would update the old one as well.

#### **Reusing memory**

When insert\_bst inserts a new node into the tree, it allocates new versions of every node on the path from the root to the insertion point. However, every other node in the tree will become part of the new tree ap well as the old one.

This shows what happens when you insert the key "h" into a binary search tree that aread portains prower Coder.com



#### Deforestation

As we discussed earlier, many Haskell programs have code that follows this

## Assignment Project Exam Help • You start with the first data structure, ds1.

- You traverse ds1, generating another data structure, ds2.
- You nteps: //pn/w/dole en. com/ds3.

If the programmer can restructure the code to compute ds3 directly from ds1, this should speed up the program, for two reasons:

- the new version does not need to create ds2, and
- the new version does one traversal instead of two.

Since the eliminated intermediate data structures are often trees of one kind or another, this optimization idea is usually called *deforestation*.

## **Simple Deforestation**

In some cases, you can deforest your own code with minimal effort. For

# Assignment Froject Exam Help

is equivalent to

```
The second treps or support, Woode and Charles in the second treps or support, who are support, who are support, which is the second treps of the
```

You can combine two calls to filter in a similar way:

```
is always and das WeChat powcoder

filter (\x -> x >= 0 & x < 10) list
```

#### filter\_map

```
filter_map :: (a -> Bool) -> (a -> b) -> [a] -> [b]

Afisteignment Project Exam Help
```

The one pass juntion performs exactly the same task as the two pass function, but those the job with pholist those wo, and does not create an intermediate list.

One can also write similarly deforested combinations of many other pairs of higher order functions, such as map and foldl.

## **Computing standard deviations**

four\_pass\_stddev :: [Double] -> Double

```
Assignment Project Exam Help
    count = fromIntegral (length xs)
    sum = foldl (+) 0 xs
    https://powcoder.com
```

```
(sqrt (count * sumsq - sum * sum)) / count
```

## square Adde We Cehat powcoder square x = x \* x

This is the simplest approach to writing code that computes the standard deviation of a list. However, it traverses the input list three times, and it also traverses a list of that same length (the list of squares) once.

#### Computing standard deviations in one pass

data StddevData = SD Double Double Double ignment. Project Exam Help one\_pass\_stddev xs = let ininttps://powcoder.com SD (c + 1.0) (s + x) (sq + x\*x)SD count sum\_sumsq = foldl update\_sd init\_sd xs (sqrt (count \* sumsq - sum \* sum)) / count

#### **Cords**

Repeated appends to the end of a list take time that is quadratic in the

In imperative languages, you would a loid this quadratic behavior by keeping a pointer to the tail of the list, and destructively updating that tail.

In declarative languages, the usual solution it to switch from lists to a data structure that supports appends means there. These are usually called cords. This is one possible cord design; there are several.

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append\_cords :: Cord a -> Cord a -> Cord a append\_cords a b = Branch a b

## Converting cords to lists

The obvious algorithm to convert a cord to a list is

# Assignment Project Exam Help

```
cord_to_list (Leaf x) = [x]
cord_to_list (Branch a b) =
    (conttopst/a/powcoder.com
```

Unfortunately, it suffers from the exact same performance problem that cords were designed to avoid.

The cord change (Levi 12 Le 11 a) the the Wt equator converts to a list may itself be one branch of a bigger cord, such as Branch (Branch (Leaf 1) (Leaf 2)) (Leaf 3).

The list [1], converted from Leaf 1, will be copied twice by ++, once for each Branch data constructor in whose first operand it appears.

#### **Accumulators**

With one exception, all leaves in a cord are followed by another item, but the second equation puts an only list behind all leaves, which is the latter two equations make the same mistake for empty and branch cords.

Fixing the performance problem requires telling the conversion function what list of tens blows to converte conversion function what list of tens blows to arrange using an accumulator.

```
cord_to_list :: Cord a -> [a]
cord_toAidd=WdeClhat powcoder
```

#### Sortedness check

The obvious way to write code that checks whether a list is sorted:

```
sorted! [_] = True

sorted! [_] = True

sorted! (x1:x2:xs) = x1 <= x2 && sorted! (x2:xs)

However, the edge that looks at each list element handles three alternatives (lists of length zero, one and more).
```

It does this because each cortedness comparison needs  $\it two$  list elements, not one. Add we can powcoder

#### A better sortedness check

```
Assignment Project Exam Help
```

```
sorted_lag :: (Ord a) => a -> [a] -> Bool
sorted_lag xp (x2:xs p = x1 <= x2 && sorted_lag x2 xs
```

In this version, the code that looks at each list element handles only two alternative. The falle of the previous element, the element that the current element should be compared with, psupplied separately.

#### **Optimisation**

You can use :set +s in GHCi to time execution.

```
ment Project Exam Help
                                                                                                                                                                                                                                      (sorted.hs, interpreted)
 [1 of 1] Compiling Sorted
Ok, modules loaded: Sorted.
*Sorted the street of the stre
True
(50.11 secs, 32,811,594,352 bytes)
*Sorted Asdel 2 Weehat powcoder
True
 (40.76 secs, 25,602,349,392 bytes)
```

The sorted2 version is about 20% faster and uses 22% less memory.

## **Optimisation**

However, the Haskell compiler is very sophisticated. After doing ghc -dynamic -c -03 sorted.hs, we get this:

Assignment Project Exam Help
Ok, modules loaded: Sorted.

Prelude Sorted> :set +s

Preludettps://powcoder.com

(2.89 secs, 8,015,369,944 bytes)

Prelude Forted week2 [1.100000000]
True Add Wechat powcoder

(2.91 secs, 8,002,262,840 bytes)

Compilation gives a *factor* of 17 speedup and a factor of 3 memory savings. It also removes the difference between sorted1 and sorted2. *Always* benchmark your compiled code when trying to speed it up.

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Declarative Programming

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## Foreign language interface

Many applications involve code written in a number of different languages; Aleclarative languages are no present in this respect. There are many present in this respect to the present in this respect to the present in the present i

- to interface to existing code (especially libraries) written in another language;
   to write performance Pittal code in a language (typically)
- to write performance critical code in a lower-level language (typically C or C++);
- to write each part of an application in the most appropriate language;
- as a way the lace My Eastan at print own Color Grage to another, by replacing one piece at a time.

Any language that hopes to be successful must be able to work with other languages. This is generally done through what is called a *foreign* language interface or foreign function interface.

## **Application binary interfaces**

In computer science, a platform is a combination of an instruction set

Architecture (ISA) and an operating system, such as x86/Windows 10 1p

Associated The Daris Project Exam Help

Each platform typically has an application binary interface, or ABI, which dictates such things as where the callers of functions should put the function farting Sandwheet Action of the first the result.

By compiling different files to the same ABI, functions in one file can call functions in a separately compiled file, even if compiled with different compilers  $Add\ WeChat\ powcoder$ 

The traditional way to interface two languages, such as C and Fortran, or Ada and Java, is for the compilers of both languages to generate code that follows the ABI.

#### Beyond C

ABIs are typically designed around C's simple calling pattern, where each function is compiled to machine language, and each function call passes some number of inputs, calls another known function, possibly returns of result, and is then finished.

This model does not work for lazy languages like Haskell, languages like Prolog or Mertin Shar support worder from Targuages like Prolog, Python, and Java that are implemented through an abstract machine, or even languages like C++ where function (method) calls may invoke different code each time they creat excuted.

In such languages, code is not compiled to the normal ABI. Then it becomes necessary to provide a mechanism to call code written in other languages. Typically, calling C code through the normal ABI is supported, but interfacing to other languages may also be supported.

#### **Boolean functions**

One application of a foreign interface is to use specialised data structures and algorithms that would be difficult or inefficient to implement in the Project Exam Help

Some applicatations need to be able to efficiently manipulate Boolean formulas (Boolean functions). This includes the following primitive values and operations://powcoder.com

- true, false
- Boolean variables: eg: a, b, c, ...
- Operated and W. e Chat, power of defec.
- Tests: satisfiability (is there any binding for the variables that makes a formula true?), equivalence (are two formulas the same for every set of variable bindings?)

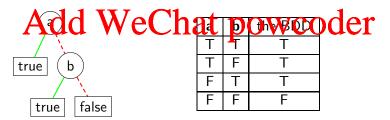
For example, is  $a \leftrightarrow b$  equivalent to  $\neg((a \land \neg b) \lor (\neg a \land b))$ ?

## **Binary Decision Diagrams**

Deciding satisfiability or equivalence of Boolean functions is NP-complete,

system of the control of the control

With a truth assignment for each variable, the value of the formula can be determined by the sing from the voct, following then branch for true variables and else branch for false variables.



#### **BDDs** in Haskell

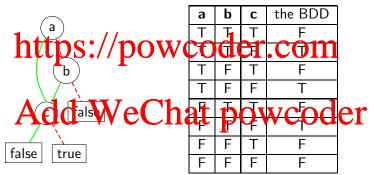
We could represent BDDs in Haskell with this type:

## Assignment Project Exam Help

```
The meaning of a BDD is given by:
    mean https://powcoder.com
                                  = false
    meaning BFalse
     \begin{array}{c} \text{meaning (Ite v two)} = (\text{was meaning t}) \lor (\neg v \land \text{meaning e}) \\ \text{Add WeChat powcoder} \end{array} 
So for example, meaning (Ite a BTrue (Ite b BTrue BFalse))
                   = (a \land true) \lor (\neg a \land (b \land true \lor (\neg b \land false)))
                    = a \lor (\neg a \land b \lor false)
                    = a \lor b
```

#### **ROBDDs**

Reduced Ordered Binary Decision Diagrams (ROBDDs) are BDDs where labels are in increasing order from root to leaf, no node has two identical ANSI BINMONIC TO THE SAME SAME TO THE PORTION OF THE PORTION

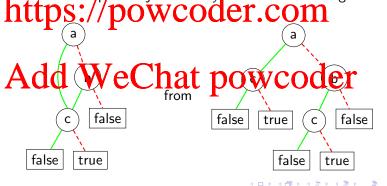


By sharing the c node, the ROBDD is smaller than it would be if it were a tree. For larger ROBDDs, this can be a big savings.

#### **Object Identity**

ROBDD algorithms traverse DAGs, and often meet the same subgraphs depended by They greatly benefit from caching: recording results of past operations to reuse without repeating the competation and the past past of the competation and the past of the past

Caching requires efficiently recognizing when a node is seen again. Haskell does not have the concept of *object identity*, so it cannot distinguish



#### **Structural Hashing**

Building a new ROBDD node ite(v, thn, els) must ensure that:

## Assignment-Project-Exam Help

of for any Boolean formula, there is only one ROBDD node with that semantics.

The first bathipes by change was oder icontaining the

The second is achieved by structural hashing (AKA hash-consing): maintaining a hash table of past calls ite(v, thn, els) and their results, and always return in the past result where call is repeated OCCT

Because of point 1 above, satisfiability of an ROBDD can be tested in constant time (meaning r is satisfiable iff  $r \neq false$ )

Because of point 2 above, equality of two ROBDDs is also a constant time test (meaning  $r_1 = meaning \ r_2$  iff  $r_1 = r_2$ )

#### Impure implementation of pure operations

(We haven't cheated NP-completeness: we have only shifted the cost to Auilding ROBDDs ent Project Exam Help Yet ROBDD operations are purely declarative. Constructing ROBDDs, conjunction, disjunction, negation, implication, checking satisfiability and equality, etc., are all pure. This is an example of usin property councile to the code.

In fact, all declarative code running on a commodity computer does that: these CPUs work through impurity. Even adding two numbers on a modern CPU works by descriptive y acting the resister to another.

If you are required to work in an imperative or object-oriented language, you can still use such languages to build declarative abstractions, and work

with them instead of working directly with impure constructs.

#### robdd.h: C interface for ROBDD implementation

```
extern robdd *true_rep(void); /* ROBDD true */

Axsignmenter roject / RxsanasHe
extern 2bdd *variable_rep(in var); /* ROBDD for var */
 extern robdd *conjoin(robdd *a, robdd *b);
 extern robdd *disjøin(robdd *a, robdd *b);
 extern https://powcoder.com
 extern robdd *implies(robdd *a, robdd *b);
 extern int district heat power could be true? */
 extern int robdd_label(robdd *f); /* label of f */
 extern robdd *robdd_then(robdd *f); /* then branch of f */
 extern robdd *robdd_else(robdd *f); /* else branch of f */
```

#### Interfacing Haskell to C

For simple cases, the Haskell foreign function interface is fairly simple. You

As sign import ccall "C name" Haskell name :: Haskell type

But how shall we represent an ROBDD in Haskell?

C primiti ettps vert poweredelsket omg,

In Haskell, we want to treat ROBDDs as an opaque type: a type we cannot pecking the weaking to pass at to, proceed the treat from, foreign functions.

The Haskell Word type represents a word of memory, much like an Int. However Word is not opaque, as we can confuse it with an integer, or any Word type.

#### newtype

Declaring type BoolFn = Word would not make BoolFn opaque; it would just be an alias for Word and could be passed as a Word Hord Exam Word We can reake it opaque with a data Boolfn = Boolfn Word

declaration. We could convert a Word w to a BoolFn with BoolFn w, and convert a BoolFn b to a Word with

https://powcoder.com

But this would box the word, adding an extra indirection to operations.

Instead wedechred WeChat powcoder

newtype BoolFn = BoolFn Word deriving Ea

We can only use newtype to declare types with only one constructor, with exactly one argument. This avoids the indirection, makes the type opaque, and allows it to be used in the foreign interface.

foreign import ccall "true\_rep"

#### The interface

```
foreign import ccall "false_rep"
                                   false
foreign import ccall "is_true"
                                   isTrue
                                            :: BoolFn->Bool
                                   isFalse :: BoolFn->Bool
foreign import ccall "is false"
foreign import ccall "robdd_then"
                                   minThen :: BoolFn->BoolFn
foreign import ccall "robdd_else"
                                   minElse :: BoolFn->BoolFn
foreign import ccall "conjoin"
                                   conjoin :: BoolBinOp
foreign import ccall "disjoin"
                                   disjoin :: BoolBinOp
                                   negation:: BoolFn->BoolFn
foreign import ccall "negate"
foreign import ccall "implies"
                                   implies :: BoolBinOp
```

4 日 > 4 周 > 4 目 > 4 目 >

:: BoolFn

true

#### Using it

To make C code available, compile it and pass the object file on the ghc or ghci command line.

TES sespondent Projective warmm; at edp in Boolff. hs, robdd.c and robdd.r in the examples directory.)

```
nomad% pcc -c -Wall/robdd.c nomad% pttpSid//pOwcoder.com
GHCi, version 8.4.3: http://www.haskell.org/ghc/
Prelude> :1 BoolFn.hs
[1 of 1 Acapiting Food That (Pool Fr. ha cinterpreted )
0k, one module loaded. That (Pool Fr. ha cinterpreted )
*BoolFn> (variable 1) 'disjoin' (variable 2)
((1) \mid (^1 \& 2))
*BoolFn> it 'conjoin' (negation $ variable 3)
((1 & ~3) | (~1 & 2 & ~3))
```

#### **Interfacing to Prolog**

The Prolog standard does not standardise a foreign language interface.

Fach Prolog system has its of Papproach. Exam Help The SWIP rolog approach does most of the work on the C side, rather than in Prolog. This is powerful, but inconvenient.

In an SWL Prolog source file, the declaration er.com: use\_foreign\_library(swi\_robdd).

will load a compiled C library file that links the code in swi\_robdd.c, which form the interface teleprolegies at the optivities of the code in swi\_robdd.c,

These are compiled and linked with the shell command:

swipl-ld -shared -o swi\_robdd swi\_robdd.c robdd.c

#### Connecting C code to Prolog

The swi\_robdd.c file contains C code to interface to Prolog:

## Assignment Project Exam Help

```
PL_register_foreign("boolfn_node", 4, pl_bdd_node, 0);
PL_register_foreign("boolfn_true", 1, pl_bdd_true, 0);
PL_register_foreign("boolfn_false_1_1 pl_bdd_false, 0);
PL_register_foreign("boolfn_conjorn, 3, pl_bdd_and, 0);
PL_register_foreign("boolfn_disjoin", 3, pl_bdd_or, 0);
PL_register_foreign("boolfn_negation", 2, pl_bdd_negate, 0);
PL_register_foreign("boolfn_negation", 2, pl_bdd_negate, 0);
PL_register_foreign("boolfn_negation", 2, pl_bdd_negate, 0);
```

This tells Prolog that a call to boolfn\_node/4 is implemented as a call to the C function pl\_bdd\_node, etc.

### Marshalling data

A C function that implements a Prolog predicate needs to convert between Prolog ferms and C data struPires This is call to marshalling dather. static foreign\_t pl\_bdd\_and(term\_t f, term\_t g, term\_t result\_term) { void https://powcoder.com && PL\_is\_integer(g) && PL\_get\_pointer(f, &f\_nd) return PL\_unify\_pointer(result\_term, (void \*)result); } else { PL\_fail;

### Making Boolean functions abstract in Prolog

To keep Prolog code from confusing an ROBDD (address) from a number, we wrant the address in a hood pn/1 term, much like we did in Hastell We must all this markety; it is most easily done in Prolog code.

```
% conjoin(+BFn1, +BFn2, -BFn)
% BFn hitthe conjoin(trien of BFn1 ded BFn2 conjoin(F, Conjoin(F, G, FG).
```

We can make groups with BLOs lar anything nicely by adding a clause for user portray/1:

### Using it

```
nomad% swipl-ld -shared -o swi_robdd swi_robdd.c robdd.c
           nent Pro1ect Exa
Welcome to SWI-Prolog (threaded, 64 bits, version
1 ?- [boolfn].
true.
     https://powcoder.com
2 ?- variable(1,A), variable(2,B), variable(3,C),
    disjoin(A,B,AB), negation(C,NotC), conjoin(AB,NotC,X)
 *dd WeChat powcoder
C = ((3)),
AB = ((1) \mid (^1 \& 2)),
NotC = ((^3)),
X = ((1 \& ~3) | (~1 \& 2 \& ~3)).
```

### Impedance mismatch

Declarative languages like Haskell and Prolog typically use different representations for similar data. For example, what would be represented as an array in C or Java.

The consequence of this is that in each language (declarative and imperative) the Court of Charles included the consequence of this is that in each language (declarative and imperative) the Court of Charles included the consequence of this is that in each language (declarative and imperative) the consequence of this is that in each language (declarative and imperative) the consequence of this is that in each language (declarative and imperative) the consequence of this is that in each language (declarative and imperative) the consequence of this is that in each language (declarative and imperative) the consequence of this is that in each language (declarative and imperative) the consequence of the consequen

This problem, usually called *impedance mismatch*, is the reason why most cross-language not reason why most repeated the property of the reason why most values of primitive types.

### Comparative strengths of declarative languages

- Programmers can be significantly more productive because they can work at a significantly higher level of abstraction. They can focus on Set when the structure of the significantly higher level of abstraction. They can focus on responsibility it is to free a data structure.
- Processing of symbolic data is significantly easier due to the presence of algebraic data types and parametric polymorphism.
- Programe gan be sign ficurtly more reliable, because III
  - you cannot make a mistake in an aspect of programming that the language automates (e.g. memory allocation), and
  - the compiler can ratch many more kinds of errors.
- What debugging is still needed is easier because you can fump backward in time.
- Maintenance is significantly easier, because
  - the type system helps to locate what needs to be changed, and
  - the typeclass system helps avoid unwanted coupling in the first place.
- You can automatically parallelize declarative programs.

### Comparative strengths of imperative languages

• If you are willing to put in the programming time, you can make the Spigmmenfunt Project Exam Help

Most existing software libraries are written in imperative languages. Using them in declarative languages is harder than using them in another imperative language (due to dissimilarity of basic concepts), while right of a program interfaces to an existing library, this argues for writing the program in the language of the library:

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- There is a much greater variety of programming tools to choose from (debuggers, profilers, IDEs etc).
- It is much easier to find programmers who know or can quickly learn the language.

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### **Parsing**

A parser is a program that extracts a structure from a linear sequence of

# Assignment Project Exam Help For example, a parser is responsible for taking input like:

and producing posts strip to represent general and producture of the input:



### Using an existing parser

The simplest parsing technique is to use an existing parser. Since every programming language must have a parser to parse the program if may passe the programming language must have a parser to parse the programming parser.

A Domain Specific Language (DSL) is a small programming language intended for a narrow domain. Often these are embedded in existing languages, letter of the room was the host language for functionality outside that domain.

If a DSL can be parsed by extending the host language parser, that makes the DSL pared or enterty to the language.

Prolog handles that quite nicely, as we saw earlier. The  ${\tt read}/1$  built-in predicate reads a term. You can use  ${\tt op}/3$  declarations to extend the language.

### **Operator precedence**

Operator precedence parsing is a simple technique based on operator's:

Arssingenmentors project Exam Help association whether repeated infix operators associate to the left, right, or neither (eg, whether a-b-c is (a-b)-c or

file for an error); and the file for commerce for the file for the fil

In Prolog, the op/3 predicate declares an operator:

### Add: We Chat ipowcoder

where *precedence* is a precedence number (larger number is *lower* precedence; 1000 is precedence of goals), *fixity* is a two or three letter symbol giving fixity and associativity (f indicates the operator, x indicates subterm at *lower* precedence, y indicates subterm at *same* precedence), and *operator* is the operator to declare.

### **Example: Prolog imperative for loop**

```
:- op(950, fx, for). :- op(940, xfx, in).
Assignment Project Exam Help
 for Generator do Body :-
       ( call(Generator),
      https://powcoder.com
          true
      Add WeChat powcoder
 Var in Low .. High :-
       between(Low, High, Var).
 Var in [H|T] :-
       member(Var, [H|T]).
```

### **Example: Prolog imperative for loop**

```
?- for X in 1 .. 4 do format('~t~d~6|^ 2 = ~d~n', [X, X^2]).
    ignment Project Exam Help
true.
        tps://powcoder.com
   ; Parity = odd
   for Atdd WeChatarbowcoder
   3 is odd
   5 is odd
   7 is odd
  11 is odd
true.
```

### **Haskell operators**

Haskell operators are simpler, but more limited. Haskell does not support

Arefix of postfix operators Project Exam Help

Declare and infix operator with:

https://powcoder.com
where associativity is one of:

infixl left associative infix operator infix outlass cattle infinantiopowcoder

infix non-associative infix operator

and *precedence* is an integer 1–9, where lower numbers are *lower* (looser) precedence.

### Haskell example

This code defines % as a synonym for mod in Haskell:

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```
(%) :: Integral a => a -> a -> a

a % b hattps://powcoder.com
```

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#### **Grammars**

Parsing is based on a grammar that specifies the language to be parsed.

Grammars are defined in terms of terminals, which are the symbols of the Ansise grid interint is, which are betify a light in a tegore Grammars are defined by a set of rules of the form:

(nonterminal  $\cup$  terminal)\*  $\rightarrow$  (nonterminal  $\cup$  terminal)\* more repetitions, and the part on the left of the arrow must contain at least one non-terminal. Most commonly, the left side of the arrow is just a

> expression  $\rightarrow$  expression +, expression expression  $\rightarrow$  expression '-' expression expression  $\rightarrow$  expression '\*' expression expression  $\rightarrow$  expression '/' expression

 $expression \rightarrow number$ 

#### **Definite Clause Grammars**

Prolog directly supports grammars, called definite clause grammars

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- Nonterminals are written using a syntax like ordinary Prolog goals.
- Terminals are written between backquotes.
- The left and right sides are separated with ==> (instead of :-).
   Parts on the right side are separated with commas.
- Empty terminal is written as [] or ''

### For example, the doctor are fairly and the written as a Prolog DCC.

```
expr --> expr, '+', expr.
expr --> expr, '-', expr.
expr --> expr, '*', expr.
expr --> expr, '/', expr.
expr --> number.
```

### Producing a parse tree

A grammar like this one can only be used to test if a string is in the defined language: usually we want to produce a list a structure (Hierselphicular) the languistic stricture of the language.

This is done very easily in a DCG by adding arguments, ordinary Prolog terms, to the nonterminals.

```
https://powcoder.com
expr(E1+E2) --> expr(E1), '+', expr(E2).
expr(E1-E2) --> expr(E1), '-', expr(E2).
expr(E1+E2) --> expr(E1) (*', expr(E2).
expr(E1+E2) --> number(N).
```

We will see a little later how to define the number nonterminal.

### Recursive descent parsing

DCGs map each nonterminal to a Prolog predicate that

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To use a grammar in Prolog, use the built-in phrase/2 predicate:

phrase(*qonterminal,string*). For example:

https://powcoder.com

?- phrase(expr(Expr), '3+4\*5').

ERROR: Stack limit (1.0Gb) exceeded

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This exposes a weakness of recursive descent parsing: it cannot handle left

This exposes a weakness of recursive descent parsing: it cannot handle left recursion.

#### Left recursion

A grammar rule like

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is *left recursive*, meaning that the first thing it does, before parsing any terminals, is to call itself recursively. Since DCGs are transformed into similar or property property property property property itself recursively without consuming any input, so it is an infinite recursion.

But we can transform our grammar to remove left recursion:

- Renam did cursive electrate province coder nonterminal.
- ② Add a rule for A\_rest that matches the empty input.
- Then add A\_rest to the end of the non-left recursive rules.

#### Left recursion removal

This is a little harder for DCGs with arguments: you also need to

Aransform the arguments t Project Exam Help Replace the argument of non-left recursive rules with a fresh variable, usp the original argument of the rule as the first argument of the rule as the rule as the rule argument of the rule argument o nonterminal, and that fresh variable as the second. So: s://powcoder.com

would be transformed to:

expr(E)AddabeW)eCphat(powcoder

### Left recursion removal

For non-recursive rules, use the argument of the left-recursive nonterminal as the first head argument and a fresh variable as the second the lead as the first argument of the lead as the first argument of the lead and of the \_tail call. So:

expr(Ehttps://powcoder.com

would be transformed to:

 ${\tt expr\_re} \textbf{A}(\textbf{dd}) \textbf{WeChat}^2 \textbf{poweoder}^{\tt R)}.$ 

### **Ambiguity**

With left recursion removed, this grammar no longer loops:

```
Expr = 3-(4-5);

Expr = 3-(4-5);

Expr = 3-4-5;

false. https://powcoder.com

?- phrase(expr3(Expr), '3+4*5').

Expr = 3+4*5;

Expr = A3cto WeChat powcoder

false.
```

Unfortunately, this grammar is ambiguous: negation can be either left- or right-associative, and it's ambiguous whether + or \* has higher precedence.

### Disambiguating a grammar

The ambiguity originated in the original grammar: a rule like

# Assignment Project Exam Help

applied to input "3-4-5" allows the first expr to match "3-4", or the second to match "4-5".

The solutation into separate nonterminals, one for each precedence level. The above rule should become:

### expr(E-AddxpWeChatrpowcoder

before eliminating left recursion.

### Disambiguating a grammar

This finally gives us:

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### **Handling terminals**

The "terminals" in a grammar can be whatever you like. Traditionally, Ayntax analysis is divided into paical analysis (alto called tokeniting) and paising 18 nment Project Exam Help

Lexical analysis uses a simpler class of grammar to group characters into tokens, while eliminating meaningless text, like whitespace and comments. Tools are available for writing cokenisers but CI can write them by hand or use the same grammar tool as you used for parsing, such as a DCG.

We will take that approach. Add WeChat powcoder

### **DCG** for parsing numbers

In addition to allowing literal 'strings' as terminals DCGs allow you to write lists as terminals (in fact, 'strings' are just lists of ASCII codes).

TEST SAIS AN MICH Mite ordinal To Ge coile Acasim (Furth) praces . If this code fails, the rule will fail. We can also use if->then; else in DCGs.

```
number https://powcoder.com
   [C], { '0' = C, C =< '9' },
   { NO is C -'0' },
   number rest (NO, C) hat powcoder

   ( [C], { '0' =< C, C =< '9' }
   -> { N1 is NO * 10 + C - '0' },
        number_rest(N1,N)
   ; { N = NO }
}
```

#### Demo

Finally, we have a working parser.

```
signment Project Exam Help
Value = -6;
false.
** https://pow.coder.com
E = 3+4*5.
Value = 23 in the false. Add WeChat powcoder
?- phrase(expr(E), '3*4+5'), Value is E.
E = 3*4+5
Value = 17:
false.
```

### **Going beyond**

This is just the beginning. Take Programming Language Implementation

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DCGs can run backwards, generating text from structure:

• Hasken Idder Was Chatspowcoder

Read type class for parsing Haskell expressions; opposite of Show.

ReadP More general, more efficient string parser.

Parsec Full-fledged file parsing.

