# COMP30026 Models of Computation Assignment Project Exam Help

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Lecture Week 2 Part 2 (Zoom)

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#### This Lecture is Being Recorded



On the island of Knights and Knaves, everyone is a knight or knave.

Assignment Project Exam Help Today there is a census on the island!

You are a census taker, going from house to house. Fill in what you know about tach of these the Wicksey Cer. COM

• In house 1: Husband: We are both knaves.

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- In house 3: Husband: If I am a knight then so is my wife.

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If you like these puzzles, Raymond Smullyan has written several books that you will like.

#### Logic and Computer Science

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Before we get to more sophisticated logic and its applications, let us establish a vocabulary and some important concepts.

"The teams ship/tenew empeater are manalical logic will be as fruitful in the next century as that between analysis and physics in the last."

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#### Validity and Satisfiability

Assignment Project Exam Help Otherwise it is non-valid.

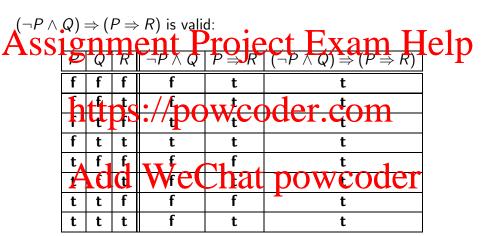
It is unsanstituted in the stem of the item of the ite

A valid propositional formula is a tautology.

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An unsatisfiable propositional formula is a contradiction.

#### Tautology Example



#### Logically, "Valid" Means Vacuous

# As sale nine of the point of th

But in formal logic, a valid statement is not that laudable; in a sense it is void of the protection o

"If Trump is sane then Trump is sane" tells us nothing about whether Trump is sane then trump is sane winter winter the action of the trump is sane.

You don't even have to know who Trump is, or what it means to be sane, in order to agree: The statement is inherently true.

#### Validity Checking in Haskell

Given a truth table for a proposition P, it is easy to check if P is

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To check the validity of 3-place Haskell predicate:

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To check the validity of 3-place Haskell predicate:

Poll 2: What does a function to check satisfiability look like?

#### Contradiction Example

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Again, we can just complete the truth table. However, it is often possible to apply faster/reasoning.coder.com

In this case, P and Q are conjuncts of the formula, so if a truth assignment maps either to  $\mathbf{f}$ , the formula evaluates to  $\mathbf{f}$ .

And if P and dre Wothen appearat, premise Compose  $(\neg t \Leftrightarrow (\neg t \lor t))$ , which again evaluates to f.

#### Substitution Preserves Validity + Unsatisfiability

Validity is preserved by substitution of propositional letters by

# Assignment Project Exam Help We saw that $(\neg P \land Q) \Rightarrow (P \Rightarrow R)$ is valid, and hence

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(Different letters call of replaced by the same formula allt of course, all occurrences or a letter must be replaced by the same formula.)

A formula is unsatisfiable iff its negation is valid.

It follows that substitution also preserves unsatisfiability.

is valid.

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No — a counter-example is easy:

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No — a counter-example is easy:

Take P in tithing learly proprotes The experience Thy  $Q \wedge \neg Q$ .

The fact that P can be made true does not mean we cannot also make if false.

make if false. Add WeChat powcoder In fact, the typical propositional formula can be made both true and

In fact, the typical propositional formula can be made both true and false; it will simultaneously be satisfiable and non-valid.

#### Models, Logical Consequence, and Equivalence

# Assignment of the attruth assignment of the appropriational formular of the properties of the second of the second

G is a logical consequence of F iff every model of F is a model of G as well.  $\frac{\text{https://powcoder.com}}{\text{In that case we write } F \models G}$ 

If  $F \models G$  and  $G \models F$  both folds that is F and G are (logically) equivalent.

In that case we write  $F \equiv G$ 

#### Poll 4

Of the following statements, which allow us to conclude  $P \Rightarrow Q$ ?

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- P https://powcoder.com
- $(P \lor R) \stackrel{\bullet}{\Rightarrow} Q$
- ¬P Add WeChat powcoder
- $P \Rightarrow (Q \vee R)$
- $(P \Rightarrow Q) \lor R$

#### Poll 4

Of the following statements, which allow us to conclude  $P \Rightarrow Q$ ?

## Assignment Project Exam Help

- $P = \frac{\text{https://powcoder.com}}{(P \lor R) \Rightarrow Q}$

- ¬P Add WeChat powcoder
- $P \Rightarrow (Q \vee R)$
- $(P \Rightarrow Q) \lor R$

Which of the statements are logical consequences of  $P \Rightarrow Q$ ?



#### Substitution Preserves Logical Equivalence

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```
If F \equiv G and F' and G' are the results of replacing each occurrence of letter F' (in both) with formula H, then F' \equiv G.
```

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#### Interchange of Equivalents

# Replacing equals by equals yields equals. If Assignment Project Exam Help

- $\bigcirc$   $F \equiv G$ , and
- https://powcoder.com

then  $H \equiv H'$ .

Interchange of Quiv terces totor totor totor totor.

It also preserves logical consequence, validity, and unsatisfiability.

Unlike substitution, it even preserves satisfiability.

#### Some Equivalences

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Commutativity:  $P \wedge Q \equiv Q \wedge P$ 

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 $P \wedge (Q \wedge R) \equiv (P \wedge Q) \wedge R$ Associativity:

Add WeChat powcoder putivity:  $P \land (Q \lor R) \equiv (P \land Q) \lor (P \land R)$ 

Distributivity:

 $P \lor (Q \land R) \equiv (P \lor Q) \land (P \lor R)$ 

#### More Equivalences

 $\Leftrightarrow$  and  $\oplus$  are also commutative and associative.

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De Morgan:  $\neg(P \land Q) \equiv \neg P \lor \neg Q$ 

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Implication:  $P \Rightarrow Q \equiv \neg P \lor Q$ 

Contrapolited We Chat powcoder  $P \Rightarrow \neg Q \equiv Q \Rightarrow \neg P$ 

$$P \Rightarrow \neg Q \equiv Q \Rightarrow \neg P$$
$$\neg P \Rightarrow Q \equiv \neg Q \Rightarrow P$$

Biimplication:  $P \Leftrightarrow Q \equiv (P \land Q) \lor (\neg P \land \neg Q)$ 

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#### Last Equivalences

Let  $\bot$  be any unsatisfiable formula and let  $\top$  be any valid formula.

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Negation from absurdity: 
$$P \Rightarrow \bot \equiv \neg P$$

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 $P \land \top \equiv P$ 

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Contradiction:  $P \land \neg P \equiv \bot$ 

Excluded middle:  $P \lor \neg P \equiv \top$ 

Which of these claims hold?

- P https://powcoder.com  $(P \Rightarrow Q) \land (P \Rightarrow R) \equiv P \Rightarrow (Q \land R)$
- $\overset{\bullet}{\text{Add}}\overset{(P\Rightarrow R)}{\text{WeChat}}\overset{(Q\Rightarrow R)}{\text{Powcoder}}$

#### Next Week Same Time Tune In

# Assignment Project Exam Help Learn how symbolic manipulation beats truth tables.

We shall he did a second a second a second

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Mechanising deduction based on propositional logic

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#### Exit Puzzle for People Who Like Puzzles

Long before Covid-19. Mr. Sprith and his wife invited four other 1p with some of the others. Of course, nobody shook hands with their partner, or themselves, and nobody shook hands with the same person the 1ps://powcoder.com

After that, Mr. Smith asked everyone how many times they shook somebody's hand. He received different answers from all nine!

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How many times did Mrs. Smith shake hands?

Answers to the discussion board