## School of Computing and Information Systems COMP30026 Models of Computation Tutorial Week 8

23–25 September 2020

## Plan

This week's exercises cover formal languages, DFAs, NFAs, and minimization. Exercises 65-67 are important because they teach you a systematic approach to building DFAs for intersection, complements and differences of languages.

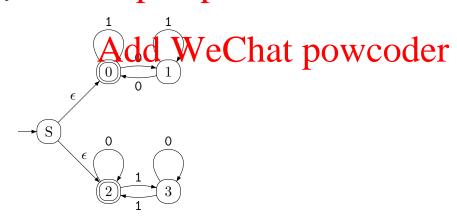
Some of the exercises on automata contestion Sipser, Introduction to the Theory of Computation. Chapter 1, on regular languages, in Chapter 1, on Chapter 1, on regular languages, in Chapter 1, on regular langua

## The exercises ssignment Project Exam Help

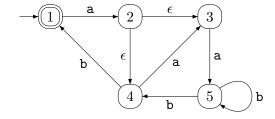
- 63. For two languages  $L_1 = \{ab, c\}$ ,  $L_2 = \{ca, c\}$ , construct a language:
  - (a) LAssign And Medip Exweet Exweet Expenses
  - (b)  $L_1 \circ L_2$
  - (c)  $L_1^*$
  - (d)  $L_1^* \setminus L_2^*$  https://powcoder.com
- 64. Draw DFAs recognising the following languages. Assume that the alphabet  $\Sigma = \{0, 1\}$ .
  - (a) {w | w begin with 1 West what powcoder
  - (b)  $\{w \mid w \text{ is not empty and contains only 0s or only 1s}\}$
  - (c)  $\{w \mid w \text{ contains the substring 0101}\}\ (\text{so } w = x \text{0101} y \text{ for some strings } x \text{ and } y)$
  - (d)  $\{w \mid w \text{ has length at least 3 and its third symbol is 0}\}$
  - (e)  $\{w \mid \text{the length of } w \text{ is at most } 5\}$
  - (f)  $\{w \mid \text{the length of } w \text{ is a multiple of } 3\}$
  - (g)  $\{w \mid w \text{ is any string except 11 and 111}\}$
  - (h)  $\{w \mid \text{every odd position of } w \text{ is a 1}\}$
  - (i)  $\{w \mid w \text{ contains at least two 0s and at most one 1}\}$
  - (j)  $\{w \mid \text{the last symbol of } w \text{ is occurred at least twice in } w\}$
  - (k)  $\{\epsilon, 0\}$
  - (l) The empty set
  - (m) All strings except the empty string
- 65. Each of the following languages is the intersection of two simpler languages. First construct the DFAs for the simpler languages, then combine them using the following idea: If the set of states for DFA  $D_1$  is  $Q_1$  and the set of states for  $D_2$  is  $Q_2$ , we let the set of states for the combined DFA D be  $Q_1 \times Q_2$ . We construct D so that, having consumed a string s, D will be in state  $(q_1, q_2)$  iff  $D_1$  is in state  $q_1$ , and  $p_2$  is in state  $q_2$  when they have consumed s. Throughout this question, assume that the alphabet  $\Sigma = \{a, b\}$ .
  - (a)  $\{w \mid w \text{ has at least three as and at least two bs}\}$

- (b)  $\{w \mid w \text{ has an even number of as and one or two bs}\}$
- (c)  $\{w \mid w \text{ has an odd number of as and ends with b}\}$
- (d)  $\{w \mid w \text{ has an odd number of as and has even length}\}$
- 66. Each of the following languages is the complement of a simpler language. Again, the best way to proceed is to first construct a DFA for the simpler language, then find a DFA for the complement by transforming that DFA appropriately. Throughout this question, assume that the alphabet  $\Sigma = \{a, b\}.$ 
  - (a)  $\{w \mid w \text{ does not contain the substring bb}\}$

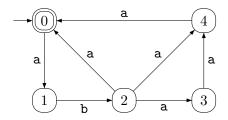
  - (d)  $\{w \mid w \text{ is any string not in } A^* \cup B^*, \text{ where } A = \{a\}, B = \{b\}\}$
  - (e) {w | wAsssirgnmentcoProjecto Exam Help
  - (f)  $\{w \mid w \text{ is any string except a and b}\}$
- 67. The following language is the difference of two simpler languages. First construct DFAs for simple Angrie Angres in the the trade of the tale of tale of the tale of the tale of tale  $\{w \mid \text{the lenght of } w \text{ is a multiple of 2 and is not multiple of 3}\}$
- 68. (An example from Lecture 7)./Use the subset construction method to turn this NFA into an equivalent DFA: DVA: DVA: OVER 1. COM



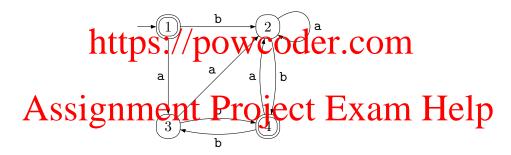
69. Use the subset construction method to turn this NFA into an equivalent DFA:



70. Use the subset construction method to turn this NFA into an equivalent DFA:



71. Find a minimal DFA which is equivalent to this one:



72. Find Aisisi grantent Mechanic Exweelet p

