Assignment Models of Computation Help

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Lecture Week 9

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The automata we saw so far were limited by their lack of memory.

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A pushdown automaton (PDA) is a finite-state automaton, equipped with a stack.

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Fine but Important Points

Based pro(1) impute ymbol, (2) top stack tynbox and (3) the current state, PEA will decide which state to go to next, as well as, what operation apply to the stack.

In one traction sep, Process to the stack, or both (replaces the top stack symbol).

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It may also ignore the input.

Pushdown Automata Formally

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- Q is a finite set of states,
- E interpresimple of the property of the contraction of the contracti
- Γ is the finite stack alphabet,
- $\delta: Q \times \Sigma_{\epsilon} \times \Gamma_{\epsilon} \to \mathcal{P}(Q \times \Gamma_{\epsilon})$ is the transition function,
- % Add WeChat powcoder
- $F \subseteq Q$ are the accept states.

Example Transitions

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If in state q_5 , when reading input symbol a, provided the top of the stack holds, b, consume the a, pop the h, and go to state q_7 . $\delta(q_5, \epsilon, \mathbf{b}) = \{(q_6, \mathbf{a}), (q_7, \mathbf{b})\}$ means:

$$\delta(q_5,\epsilon,\mathtt{b})=\{(q_6,\mathtt{a}),(q_7,\mathtt{b})\}$$
 means:

If in state q_5 , and if the top of the stack holds 'b' either replace that b by a and go to state q_6 , or leave the stack as is and go to state q_7 . In either case do not consume an input symbol.

PDA Example 1

This PDA recognises $\{a^nb^n \mid n > 0\}$:

Assignment Project \xrightarrow{b} $\xrightarrow{\epsilon, \epsilon \to \$}$ $\xrightarrow{q_1}$ $\xrightarrow{b, a \to \epsilon}$ $\xrightarrow{q_2}$ $\xrightarrow{\epsilon, \$ \to \epsilon}$ $\xrightarrow{q_3}$

• $Q = \{q_0, q_1, q_2, q_3\}$ powcoder.com

- $\Sigma = \{a, b\};$
- $\stackrel{\Gamma}{\bullet} \stackrel{\Lambda}{\circ} \stackrel{\Lambda$
- $\delta(q_1, b, a) = \{(q_2, \epsilon)\}, \delta(q_2, b, a) = \{(q_2, \epsilon)\},$ $\delta(q_2, \epsilon, \$) = \{(q_3, \epsilon)\}, \text{ for other inputs } \delta \text{ returns } \emptyset;$
- $q_0 = q_0$;
- $F = \{q_0, q_3\}.$

Acceptance Precisely

The PDA $(Q, \Sigma, \Gamma, \delta, q_0, F)$ accepts input w iff $w = v_1 v_2 \cdots v_n$ with each $v_1 \in \Sigma$, and there are states $r_0, r_1, \ldots, r_n \in Q$ and strings P and P and P are P are P are P and P are P are P are P and P are P are P are P are P are P and P are P are P and P are P are P are P and P are P are P are P are P are P and P are P are P and P are P and P are P are P and P are P are P are P are P and P are P are P are P are P are P are P and P are P are P are P and P are P and P are P are P are P are P and P are P are P and P are P are P and P are P are P are P and P are P and P are P are P and P are P are P are P are P and P are P and

- $r_n \in F$.

Note 1: There is no requirement that $\mathbf{L} = \epsilon$, so the stack may be non-empty when the machine stops (even when it accepts).

Note 2: Trying to pop an empty stack leads to rejection of input, rather than "runtime error".

PDA Example 2

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Let us design a PDA to recognise $\{ww^{\mathcal{R}} \mid w \in \{0,1\}^*\}$, the set of even-length binary palindromes:

 $\frac{\text{even-length binary palindromes:}}{https://powcoder.com}$



PDA Example 2

Assignment Project Exam Help This PDA recognises $\{ww^{\mathcal{R}} | w \in [0,1]^*\}$:

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CFLs Have PDAs as Recognisers

Given a context-free language L (in the form of a grammar), we can

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And, every PDA recognises a context-free language.

Namely, given a CFG G, we show how to construct a PDA P such that L(P) HG WeChat powcoder

The idea is to let the PDA use its stack to store a list of "pending" recogniser tasks.

The construction does not give the cleverest PDA, but it always works.

From Context-Free Grammars to PDAs

Say $B \to xAy$ is a rule in G, and the PDA finds the symbol B on top Assignment Project Exam He stack input input

If it finds the terminal x on top of the stack, and x is the next input symbol, it may consume the input and pop x.

From Context-Free Grammars to PDAs

Construct the PDA like this:

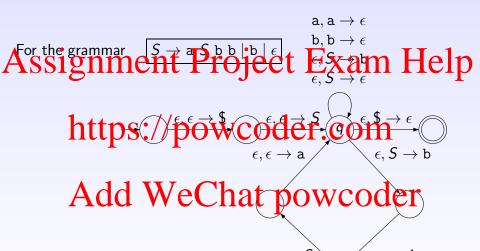
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with a sentential of the grammar's start symbol).

For each rule $A \rightarrow \alpha_1$ We Chat, powcode, $A \rightarrow \alpha_n$

add this loop from q to q:

Example Recogniser



Pumping Lemma for CFLs

There are languages that are not context-free, and again there is a Austrigue market to be used to some analysis of the policy of the context non-context-free:

If A is context-free then there is a number p such that for any string $s \in A$ will be so that A and A are the string A will be so that A and A are the string A are the string A and A are the string A

- uvⁱxyⁱz ∈ A for all i ≥ 0
 |vy|Add WeChat powcoder
- $|vxy| \le p$

We won't prove this lemma, but we give two examples of its use.

Pumping Example 1

 $A = \{ww \mid w \in \{0,1\}^*\}$ is not context-free.

Assume it is, let p be the proping length, take $0^p1^p0^p1^p$. Help By the pumping lemma, $0^p1^p0^p1^p = uvxyz$, with uv^ixy^iz in A for all i > 0, and |vxy| < p.

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00...0011...1100...0011...11

If it straddles the mid vint (t has form $1^{n}0^{m}$ so, pumping down, we are left with $0^{n}1^{n}0^{j}1^{p}$, with i < p, or j < p, or both.

If it is in the first half, uv^2xy^2z will have pushed a 1 into the first position of the second half.

Similarly if vxy is in the second half.

Pumping Example 2

 $B = \{a^n b^n c^n \mid n \in \mathbb{N}\}$ is not context-free.

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By the pumping lemma, $a^p b^p c^p = uvxyz$, with $uv^i xy^i z$ in B for all i.

Either vattips: empoweeder.com

If one of them contains two different symbols from $\{a, b, c\}$ then uv^2xy^2z has symbol with an arrival probability the widness of the probability of the probabi

So both v and y must contain only one kind of symbol. But then uv^2xy^2z can't have the same number of as, bs, and cs.

In all cases we have a contradiction.

Closure Properties for CFLs

Assignment Project Exam Help The class of context-free languages is closed under

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- Kleene star,
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Closure Properties for CFLs

The class of context-free languages is not closed under intersection!

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Consider these two CFLs:

$$https: \sqrt[d]{power oder coder com}$$

Exercise: Prove that they are context-free!

But $C \cap D$ is the language $B = \{a^nb^nc \mid n \in \mathbb{N}\}$ which we just showed is not context-free.

However, we do have: If A is context-free and R is regular then $A \cap R$ is context-free.

Deterministic PDAs

Is a deterministic PDA (a DPDA) as powerful as a PDA?

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 $\underset{\text{but not the context-free}}{\text{https://powcoder.com}} \{\underset{ww^{\mathcal{R}} \mid c \in \Sigma, w \in (\Sigma \setminus \{c\})^*\}}{\text{but not the context-free}} \{\underset{ww^{\mathcal{R}} \mid w \in \Sigma^*}{\text{but not the context-free}} \}$

Intuitively, a deterministic machine cannot know when the middle of the input hacken rather. Supplet it poissor COCCT

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A deterministic machine won't know when to start popping the stack.