School of Computing and Information Systems COMP30026 Models of Computation Tutorial Week 9

30 September to 2 October 2020

The exercises

- 73. Give regular expressions for the following languages over the alphabet $\Sigma = \{0, 1\}$.
 - (a) $\{w \mid w \text{ begins with a 1 and ends with a 0}\}$
 - (b) $\{w \mid w \text{ contains the substring 0101}\}\ (\text{so } w = x0101y \text{ for some strings } x \text{ and } y)$
 - (c) {w | w has lengthat tents and point conter.com
 - (d) $\{w \mid \text{the length of } w \text{ is at most } 5\}$
 - (e) $\{w \mid w \text{ is any string except 11 and 111}\}$
 - $\begin{array}{l} \text{ (f) } \{\textit{w} \mid \text{ every schedipesition of we is at 1}\} \\ \text{ (g) } \{\textit{w} \mid \textit{w} \text{ contains pleast two 0s and at most one C}\} \end{array} \\ \mathbf{Exam} \ Help$

 - (h) $\{\epsilon, 0\}$
 - (i) The empty set (j) AASSI STITUTE THE BANGO HOLD
- 74. String s is a suffix of string t iff there exists some string u (possibly empty) such that t = us. For any language L we can define the set of suffixes of strings in L: $\frac{L}{\text{Normal power}} = \{x \mid x \text{ is a suffix of some } y \in L\}$

Let A be any regular language. Show that suffix(A) is a regular language. Hint: Think about how a DFA for Alar petral vorced to reachisp of the OCET

75. In general it is difficult, given a regular expression, to find a regular expression for its complement. However, it can be done, and you have been given all the necessary tricks and algorithms. This question asks you to go through the required steps for a particular example.

Consider the regular language $(ba^*a)^*$. Assuming the alphabet is $\Sigma = \{a, b\}$, we want to find a regular expression for its complement, that is, for

$$L = \{ w \in \{ \mathtt{a}, \mathtt{b} \}^* \mid w \text{ is not in } (\mathtt{ba}^*\mathtt{a})^* \}$$

To complete this task, go through the following steps.

- (a) Construct an NFA for (ba*a)*. Two states suffice.
- (b) Turn the NFA into a DFA using the subset construction method.
- (c) Do the "complement trick" to get a DFA D for L.
- (d) Reflect on the result: Wouldn't it have been better/easier to apply the "complement trick" directly to the NFA?
- (e) Turn DFA D into a regular expression for L using the NFA-to-regular-expression translation shown in the lecture on regular expressions (not examinable).
- 76. A palindrome is a string that reads the same forwards and backwards. Use the pumping lemma for regular languages and/or closure results to prove that the following languages are not regular:
 - (a) $A = \{0^n 1^n 2^n \mid n \ge 0\}$
 - (b) $B = \{a^iba^j \mid i > i > 0\}$

- (c) $C = \{w \in \{a, b\}^* \mid w \text{ is not a palindrome}\}$
- 77. Give context-free grammars for the following languages. Assume the alphabet is $\Sigma = \{0, 1\}$.
 - (a) $\{w \mid w \text{ starts and ends with the same symbol}\}$
 - (b) $\{w \mid \text{the length of } w \text{ is odd}\}$
 - (c) $\{w \mid \text{the length of } w \text{ is odd and its middle symbol is 0}\}$
 - (d) $\{w \mid w \text{ is a palindrome}\}$
- 78. Construct a context-free grammar for the language $\{a^iba^j \mid i > j \ge 0\}$.
- 79. Show that the class of context-free/languages is closed under the regular operations: union, concatenation, and Klacht that Him Down words of the Carabbar for A and B can be manipulated to produce context-free grammars for $A \cup B$, AB, and A^* . Careful: The variables used in the grammars for A and in B could overlap.
- 80. If we consider its Sill with the Indoor "(opticles) of Kalsh vera Ga pointext-free grammar to try to capture certain classes of sentences and phrases. For example, we can consider articles (A), nouns (N), adjectives (Q), intransitive verbs (IV), transitive verbs (TV), noun phrases (AP) well in the second sentences (AP) well in the second sentences (AP) well in the second sentences (AP) and sentences (AP) sentences generated by the sentences (AP) and sentences (AP) sentences generated by the sentences (AP) and sentences (AP) sentences generated by the sentences (AP) and sentences (AP) sentences generated by the sentences (AP) and (AP) sentences (AP) and (AP) sentences (AP) and (AP) sentences (AP)

Are they all meaningful? Discuss "well-formed" versus "meaningful".

- 81. How would you change the grammar from the previous question so that "adverbial modifiers" such as "angrily" or "happily" can be used? For example, we would like to be able to generate sentences like "the dog barks constantly" and "the black cat sleeps quietly".
- 82. Consider this context-free grammar G with start symbol S:

Draw an NFA which recognises L(G). Hint: The grammar is a regular grammar; you may want to use the labels S, A, and B for three of the NFA's states.

83. Consider the context-free grammar G with rules

$$S \rightarrow \mathtt{ab} \mid \mathtt{a} \, S \, \mathtt{b} \mid S \, S$$

Use structural induction to show that no string $w \in L(G)$ starts with abb.

84. (Drill.) Consider the context-free grammar $(\{S\}, \{a, b\}, R, S)$ with rules R:

$$S \rightarrow \mathbf{a} \mid \mathbf{b} \mid S S$$

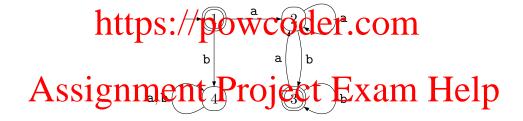
Show that the grammar is ambiguous; then find an equivalent unambiguous grammar.

85. (Drill.) Consider the context-free grammar $(\{A, B, T\}, \{a, b\}, R, T)$ with rules R:

$$\begin{array}{ccc} T & \rightarrow & A \mid B \\ A & \rightarrow & \mathtt{a} \, \mathtt{b} \mid \mathtt{a} \, A \, \mathtt{b} \\ B & \rightarrow & \epsilon \mid \mathtt{a} \, \mathtt{b} \, B \end{array}$$

Show that the grammar is ambiguous; then find an equivalent unambiguous grammar.

86. (Drill.) Give a context-free grammar for the language recognised by this DFA:



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