

COMP302: Programming Languages and Paradigms

Assignment Project Exam Help

Prof. Brigitte Pientka (Sec 01)

bpientka@cs.mcgill.ca

Francisco Ferreira (Sec 02)

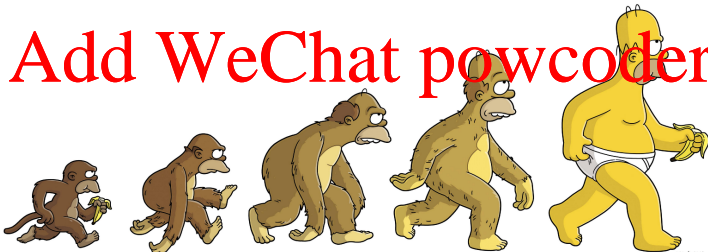
fferre8@cs.mcgill.ca

<https://powcoder.com>

School of Computer Science
McGill University

Week 4-1, Fall 2017

Add WeChat powcoder



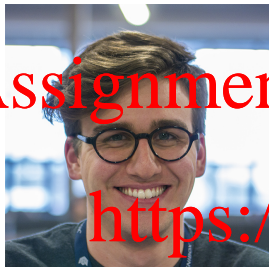
MACHINE

ASSEMBLY

PROCEDURAL

OBJECT ORIENTED

FUNCTIONAL



“Higher-order functions; relatively simple once mastered yet very powerful and they make you look awesome!”

Jeremie Poisson (TA for COMP 302)

Office Hours: Wed 12:00pm - 2:00pm

Add WeChat powcoder



“Higher order functions are super cool!”

Eric Zhang (TA for COMP 302)

Office Hours: Wed 2:00pm - 4:00pm

Functions are first-class values!

Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder

Functions are first-class values!

Assignment Project Exam Help

- Pass functions as arguments (Continued)
- Return them as results (Today)

<https://powcoder.com>

Add WeChat powcoder



Functions are first-class values!

Assignment Project Exam Help

- Pass functions as arguments (Continued)
- Return them as results (Today)

<https://powcoder.com>

Add WeChat powcoder



Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder

Common Higher-Order Functions (Built-In)

- `List.map: ('a -> 'b) -> 'a list -> 'b list`

- `List.filter: ('a -> bool) -> 'a list -> 'a list`

- `List.fold_right: ('a -> 'b -> 'b) -> 'a list -> 'b -> 'b`

- `List.fold_left: ('a -> 'b -> 'a) -> 'a -> 'b list -> 'a`

- `List.for_all: ('a -> bool) -> 'a list -> bool`

- `List.exists: ('a -> bool) -> 'a list -> bool`

Check the OCaml `List` library for more built-in higher-order functions! They make great practice questions!

Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder

Functions are first-class values!

Assignment Project Exam Help

- Pass functions as arguments (Continued)
- Return them as results (Today)

<https://powcoder.com>

Add WeChat powcoder



What does it mean to return a function?

Assignment Project Exam Help

Let's go back to the beginning... from the 1 week

```
1 (* We can also bind variable to functions. *)  
2 let area : float -> float = function r -> pi *. r *. r  
3  
4 (* or more conveniently, we write usually *)  
5 let area (r:float) = pi *. r *. r  
6
```

Add WeChat powcoder

- The variable name `area` is bound to the *value* `function r -> pi *. r *. r` which OCaml prints simply as `<fun>`.
- The type of the variable `area` is `float -> float`.

Assignment Project Exam Help

Write a function `curry` that

- takes as input a function $f:('a * 'b) \rightarrow 'c$
- returns as a result a function $'a \rightarrow 'b \rightarrow 'c$.

<https://powcoder.com>



Haskell B. Curry

Add WeChat powcoder

Assignment Project Exam Help

Write a function `curry` that

- takes as input a function `f:('a * 'b) -> 'c`
- returns as a result a function `'a -> 'b -> 'c`.

<https://powcoder.com>



Haskell B. Curry

```
1 (* curry : ('a * 'b) -> 'c -> 'a -> 'b -> 'c *)
2 (* Note : Arrows are right-associative *)
3 let curry f = (fun x y -> f (x,y))
```

Add WeChat powcoder

Assignment Project Exam Help

Write a function `curry` that

- takes as input a function `f:('a * 'b) -> 'c`
- returns as a result a function `'a -> 'b -> 'c`.

<https://powcoder.com>



Haskell B. Curry

```
1 (* curry: ('a * 'b) -> 'c -> 'a -> 'b -> 'c *)
2 (* Note: Arrows are right-associative *)
3 let curry f = (fun x y -> f (x,y))
4
5 let curry_version2 f x y = f (x,y)
6
7 let curry_version3 = fun f -> fun x -> fun y -> f (x,y)
```

Assignment Project Exam Help

Write a function `curry` that

- takes as input a function `f:('a * 'b) -> 'c`
- returns as a result a function `'a -> 'b -> 'c`.

<https://powcoder.com>



Haskell B. Curry

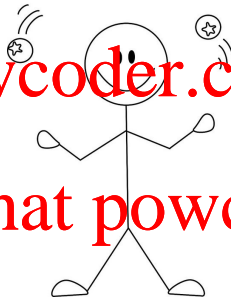
```
1 (* curry: ('a * 'b) -> 'c -> 'a -> 'b -> 'c *)
2 (* Note: Arrows are right-associative *)
3 let curry f = (fun x y -> f (x,y))
4
5 let curry_version2 f x y = f (x,y)
6
7 let curry_version3 = fun f -> fun x -> fun y -> f (x,y)
```

Assignment Project Exam Help

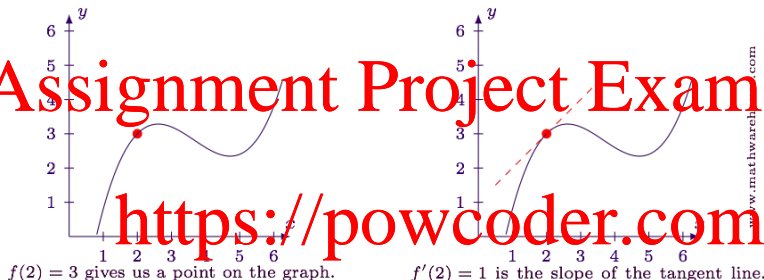
<https://powcoder.com>

Add WeChat powcoder

Let's play!



Bonus: Approximating the Derivative

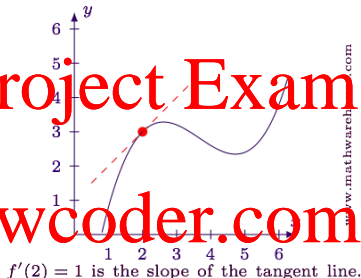
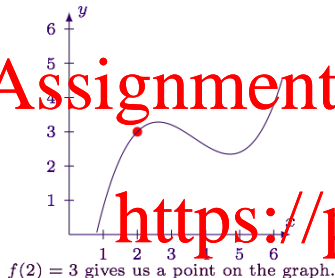


<https://powcoder.com>

Add WeChat powcoder

$$f'(x) = \frac{df}{dx} = \lim_{\epsilon \rightarrow 0} \frac{f(x + \epsilon) - f(x)}{\epsilon}$$

Bonus: Approximating the Derivative



$f'(x) = \frac{df}{dx} = \lim_{\epsilon \rightarrow 0} \frac{f(x + \epsilon) - f(x)}{\epsilon}$

Add WeChat powcoder

Implement a function `deriv : (float -> float) * float -> float -> float` which

- given a function `f:float -> float` and an epsilon `dx:float`
- returns a function `float -> float` describing the derivative of `f`.

Bonus: Approximating the Derivative

$$f'(x) = \frac{df}{dx} = \lim_{\epsilon \rightarrow 0} \frac{f(x + \epsilon) - f(x)}{\epsilon}$$

Assignment Project Exam Help

Implement a function `deriv : (float -> float) * float -> float -> float` which

- given a function `f:float -> float` and an epsilon `dx:float`
- returns a function `float -> float` describing the derivative of `f`.

<https://powcoder.com>

Add WeChat powcoder

Bonus: Approximating the Derivative

$$f'(x) = \frac{df}{dx} = \lim_{\epsilon \rightarrow 0} \frac{f(x + \epsilon) - f(x)}{\epsilon}$$

Assignment Project Exam Help

Implement a function `deriv : (float -> float) * float -> float -> float` which

- given a function `f:float -> float` and an epsilon `dx:float`
- returns a function `float -> float` describing the derivative of `f`.

<https://powcoder.com>

Add WeChat powcoder

```
1 let deriv (f, dx) = fun x -> (f (x +. dx) -. f x) /. dx
```

Higher-order functions are super cool!

Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder



Higher-order functions are super cool!

Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder



Question: Do you know what the functions in the picture mean?



- Logician and Mathematician
- June 14, 1903 – August 11, 1995
- Most known for the **Lambda-Calculus**.
 - a simple language consisting of variables, functions (written as $\lambda x.t$) and function application
 - we can define all computable functions in the Lambda-Calculus!

Add WeChat **powcoder**

Church Encoding of Booleans:

$$\mathbf{T} = \lambda x. \lambda y. x$$

$$\mathbf{F} = \lambda x. \lambda y. y$$