

# Assignment Project Exam Help



Software System Design and Implementation

<https://powcoder.com>

Induction, Data Types and Type Classes

Dr. Liam O'Connor

University of Edinburgh, IFCS (and UNSW)

Term 2, 2020

Add WeChat powcoder

## Recap: Induction

# Assignment Project Exam Help

Suppose we want to prove that a property  $P(n)$  holds for **all** natural numbers  $n$ . Remember that the set of natural numbers  $\mathbb{N}$  can be defined as follows:

### Definition of Natural Numbers

- 1 0 is a natural number.
- 2 For any natural number  $n$ ,  $n + 1$  is also a natural number.

<https://powcoder.com>  
Add WeChat powcoder

## Recap: Induction

Therefore, to show  $P(n)$  for all  $n$ , it suffices to show:

- 1  $P(0)$  (the *base case*), and
- 2 assuming  $P(k)$  (the *inductive hypothesis*),  
 $\Rightarrow P(k+1)$  (the *inductive case*).

### Example

Show that  $f(n) = n^2$  for all  $n \in \mathbb{N}$ , where:

$$f(n) = \begin{cases} 0 & \text{if } n = 0 \\ 2n - 1 + f(n - 1) & \text{if } n > 0 \end{cases}$$

(done on iPad)

## Induction on Lists

Haskell Lists can be defined similarly to natural numbers

### Definition of Haskell Lists

- 1 `[]` is a list
- 2 For any list `xs`, `x:xs` is also a list (for any item `x`).

<https://powcoder.com>

Add WeChat powcoder

## Induction on Lists

Haskell lists can be defined similarly to natural numbers

### Definition of Haskell Lists

- 1 `[]` is a list
- 2 For any list `xs`, `x:xs` is also a list (for any item `x`).

This means, if we want to prove that a property  $P(ls)$  holds for all lists `ls`, it suffices to show:

- 1  $P([])$  (the base case)
- 2  $P(x:xs)$  for all items `x`, assuming the inductive hypothesis  $P(xs)$ .

<https://powcoder.com>

Add WeChat powcoder

## Induction on Lists: Example

```
sum :: [Int] -> Int
sum [] = 0 -- 1
sum (x:xs) = x + sum xs -- 2
```

```
foldr :: (a -> b -> b) -> b -> [a] -> b
foldr f z [] = z -- A
foldr f z (x:xs) = x `f` foldr f z xs -- B
```

### Example

**Prove** for all `ls`:

$$\text{sum } ls == \text{foldr } (+) \ 0 \ ls$$

(done on iPad)

Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder

## Custom Data Types

So far, we have seen type synonyms using the `type` keyword. For a graphics library, we might define:

```
type Point    = (Float, Float)
type Vector   = (Float, Float)
type Line     = (Point, Point)
type Colour   = (Int, Int, Int, Int) -- RGBA
```

```
movePoint :: Point -> Vector -> Point
movePoint (x,y) (dx,dy) = (x + dx, y + dy)
```

But these definitions allow Points and Vectors to be used interchangeably, increasing the **likelihood of errors**.

## Product Types

We can define our own compound types using the data keyword:



```
data Point = Point Float Float  
           deriving (Show, Eq)
```

```
data Vector = Vector Float Float  
            deriving (Show, Eq)
```

```
movePoint :: Point -> Vector -> Point  
movePoint (Point x y) (Vector dx dy)  
    = Point (x + dx) (y + dy)
```

<https://powcoder.com>

Add WeChat powcoder



## Records

We could define Colour similarly:

```
data Colour = Colour Int Int Int Int
```

But this has so many parameters, it's hard to tell which is which.

<https://powcoder.com>

Add WeChat powcoder

Assignment Project Exam Help

## Records

We could define `Colour` similarly:

```
data Colour = Colour Int Int Int Int
```

But this has so many parameters, it's hard to tell which is which.

Haskell lets us declare these types as *records*, which is identical to the declaration style on the previous slide, but also gives us projection functions and record syntax:

```
data Colour = Colour { redC      :: Int
                      , greenC   :: Int
                      , blueC    :: Int
                      , opacityC :: Int
                      } deriving (Show, Eq)
```

Here, the code `redC (Colour 255 128 0 255)` gives 255.

## Enumeration Types

Assignment Project Exam Help

Similar to enums in C and Java, we can define types to have one of a set of predefined values:

```
data LineStyle = Solid
               | Dashed
               | Dotted
               deriving (Show, Eq)
```

```
data FillStyle = SolidFill | NoFill
               deriving (Show, Eq)
```

Types with more than one constructor are called *sum types*.

<https://powcoder.com>

Add WeChat powcoder

## Algebraic Data Types

Just as the `Point` constructor took two `Float` arguments, constructors for sum types can take parameters too, allowing us to model different kinds of shape:

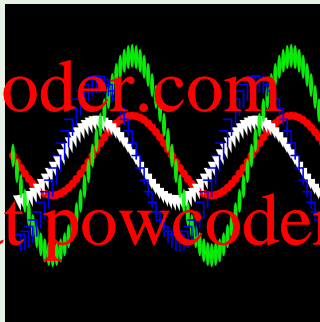
```
data PictureObject
  = Path    [Point]      Colour LineStyle
  | Circle Point Float   Colour LineStyle FillStyle
  | Polygon [Point]      Colour LineStyle FillStyle
  | Ellipse Point Float Float Float
              Colour LineStyle FillStyle
deriving (Show, Eq)
```

```
type Picture = [PictureObject]
```

## Live Coding: Cool Graphics

# Assignment Project Exam Help

Example (Ellipses and Curves)



<https://powcoder.com>  
Add WeChat powcoder

## Recursive and Parametric Types

# Assignment Project Exam Help

Data types can also be defined with **parameters**, such as the well known Maybe type, defined in the standard library:

```
data Maybe a = Just a | Nothing
```

<https://powcoder.com>

Add WeChat powcoder

## Recursive and Parametric Types

# Assignment Project Exam Help

Data types can also be defined with **parameters**, such as the well known Maybe type, defined in the standard library:

```
data Maybe a = Just a | Nothing
```

Types can also be **recursive**. If lists weren't already defined in the standard library, we could define them ourselves:

```
data List a = Nil | Cons a (List a)
```

# Add WeChat powcoder

## Recursive and Parametric Types

# Assignment Project Exam Help

Data types can also be defined with **parameters**, such as the well known Maybe type, defined in the standard library:

```
data Maybe a = Just a | Nothing
```

Types can also be **recursive**. If lists weren't already defined in the standard library, we could define them ourselves:

```
data List a = Nil | Cons a (List a)
```

We can even define natural numbers, where 2 is encoded as Succ (Succ Zero):

```
data Natural = Zero | Succ Natural
```

<https://powcoder.com>

Add WeChat powcoder



## Types in Design

### Sage Advice

An old adage due to Yaron Minsky (of Jane Street) is:

*Make illegal states **unrepresentable**.*

Choose types that *constrain* your implementation as much as possible. Then failure scenarios are eliminated automatically.

Add WeChat powcoder

Assignment Project Exam Help

<https://powcoder.com>

## Types in Design

### Sage Advice

An old adage due to Yaron Minsky (of Jane Street) is:

*Make illegal states **unrepresentable**.*

Choose types that *constrain* your implementation as much as possible. Then failure scenarios are eliminated automatically.

### Example (Contact Details)

```
data Contact = C Name (Maybe Address) (Maybe Email)
```

is changed to:

```
data ContactDetails = EmailOnly Email | PostOnly Address  
                  | Both Address Email  
data Contact = C Name ContactDetails
```

What failure state is eliminated here? Liam: also talk about other famous screwups

## Partial Functions

Failure to follow Yaron's excellent advice leads to **partial functions**.

### Definition

A **partial function** is a function not defined for all possible inputs.

Examples: head, tail, (!!), division

Partial functions are to be avoided, because they cause your program to crash if undefined cases are encountered.

<https://powcoder.com>

Add WeChat powcoder

## Partial Functions

Failure to follow Yaron's excellent advice leads to **partial functions**.

### Definition

A **partial function** is a function not defined for all possible inputs.

Examples: head, tail, (!!), division

Partial functions are to be avoided, because they cause your program to crash if undefined cases are encountered.

To eliminate partiality, we must either:

- enlarge the code man, usually with a Maybe type:

```
safeHead :: [a] -> Maybe a -- Q: How is this safer?  
safeHead (x:xs) = Just x  
safeHead []     = Nothing
```

## Partial Functions

Failure to follow Yaron's excellent advice leads to **partial functions**.

### Definition

A **partial function** is a function not defined for all possible inputs.

Examples: head, tail, (!!), division

Partial functions are to be avoided, because they cause your program to crash if undefined cases are encountered.

To eliminate partiality, we must either:

- enlarge the codomain, usually with a Maybe type:

```
safeHead :: [a] -> Maybe a -- Q: How is this safer?  
safeHead (x:xs) = Just x  
safeHead []      = Nothing
```

- Or we must **constrain** the domain to be more specific:

```
safeHead' :: NonEmpty a -> a -- Q: How to define?
```

## Type Classes

You have already seen functions such as:

- compare
- (==)
- (+)
- show

that work on **multiple types**, and their corresponding constraints on type variables Ord, Eq, Num and Show

<https://powcoder.com>

Add WeChat powcoder

## Type Classes

You have already seen functions such as:

- compare
- (==)
- (+)
- show

<https://powcoder.com>

that work on **multiple types**, and their corresponding constraints on type variables Ord, Eq, Num and Show.

Add WeChat powcoder

These constraints are called *type classes*, and can be thought of as a **set of types** for which certain operations are implemented.

## Show

The Show type class is a set of types that can be converted to strings. It is defined like:

`class Show a where` *nothing to do with DP*  
`show :: a -> String`

# Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder



## Show

The Show type class is a set of types that can be converted to strings. It is defined like:

```
class Show a where -- nothing to do with DF  
  show :: a -> String
```

Types are added to the type class as an *instance* like so:

```
instance Show Bool where  
  show True  = "True"  
  show False = "False"
```

<https://powcoder.com>

Add WeChat powcoder

## Show

The Show type class is a set of types that can be converted to strings. It is defined like:

```
class Show a where
  show :: a -> String
```

Types are added to the type class as an *instance* like so:

```
instance Show Bool where
  show True  = "True"
  show False = "False"
```

We can also define instances that depend on other instances:

```
instance Show a => Show (Maybe a) where
  show (Just x) = "Just " ++ show x
  show Nothing  = "Nothing"
```

Fortunately for us, Haskell supports automatically deriving instances for some classes, including Show.

## Read

# Assignment Project Exam Help

Type classes can also overload based on the type **returned**, unlike similar features like Java's interfaces:

```
class Read a where
  read :: String -> a
```

Some examples:

- `read "34" :: Int`

<https://powcoder.com>  
Add WeChat powcoder

## Read

# Assignment Project Exam Help

Type classes can also overload based on the type **returned**, unlike similar features like Java's interfaces:

```
class Read a where  
  read :: String -> a
```

Some examples:

- `read "34" :: Int`
- `read "22" :: Char`

<https://powcoder.com>

Add WeChat powcoder

## Read

# Assignment Project Exam Help

Type classes can also overload based on the type **returned**, unlike similar features like Java's interfaces:

```
class Read a where  
  read :: String -> a
```

Some examples:

- `read "34" :: Int`
- `read "22" :: Char` Runtime error!
- `show (read "34") :: String`

<https://powcoder.com>

Add WeChat powcoder

## Read

# Assignment Project Exam Help

Type classes can also overload based on the type **returned**, unlike similar features like Java's interfaces:

```
class Read a where  
  read :: String -> a
```

Some examples:

- `read "34" :: Int`
- `read "22" :: Char` Runtime error!
- `show (read "34") :: String` Type error!

<https://powcoder.com>

Add WeChat powcoder

## Semigroup

### Semigroups

A *semigroup* is a pair of a set  $S$  and an operation  $\circ : S \rightarrow S \rightarrow S$  where the operation

- is *associative*.

<https://powcoder.com>

Add WeChat powcoder

## Semigroup

### Semigroups

A *semigroup* is a pair of a set  $S$  and an operation  $\bullet : S \rightarrow S \rightarrow S$  where the operation  $\bullet$  is *associative*.

Associativity is defined as, for all  $a, b, c$ :

$$(a \bullet (b \bullet c)) = ((a \bullet b) \bullet c)$$

Haskell has a type class for semigroups! The associativity law is enforced only by programmer discipline:

```
class Semigroup s where
  (<.>) :: s -> s -> s
  -- Law: (<.>) must be associative.
```

What instances can you think of?



## Semigroup

Lets implement additive colour mixing:

```
instance Semigroup Colour where
  Colour r1 g1 b1 a1 <> Colour r2 g2 b2 a2
    = Colour (mix r1 r2)
              (mix g1 g2)
              (mix b1 b2)
              (mix a1 a2)
  where
    mix x1 x2 = min 255 (x1 + x2)
```

Observe that associativity is satisfied.

<https://powcoder.com>

Add WeChat powcoder

## Monoid

### Monoids

A *monoid* is a semigroup  $(S, \bullet)$  equipped with a special *identity element*  $z \in S$  such that  $x \bullet z = x$  and  $z \bullet y = y$  for all  $x, y$ .

<https://powcoder.com>

Add WeChat powcoder

## Monoid

### Monoids

A *monoid* is a semigroup  $(S, \bullet)$  equipped with a special *identity element*  $z \in S$  such that  $x \bullet z = x$  and  $z \bullet y = y$  for all  $x, y$ .

```
class (Semigroup a) => Monoid a where  
  mempty :: a
```

<https://powcoder.com>

Add WeChat powcoder

## Monoid

### Monoids

A *monoid* is a semigroup  $(S, \bullet)$  equipped with a special *identity element*  $z \in S$  such that  $x \bullet z = x$  and  $z \bullet y = y$  for all  $x, y$ .

```
class (Semigroup a) => Monoid a where  
  mempty :: a
```

For colours, the identity element is transparent black:

```
instance Monoid Colour where  
  mempty = Colour 0 0 0 0
```

For each of the semigroups discussed previously:

- Are they monoids?
- If so, what is the identity element?

# Monoid

## Monoids

A *monoid* is a semigroup  $(S, \bullet)$  equipped with a special *identity element*  $z \in S$  such that  $x \bullet z = x$  and  $z \bullet y = y$  for all  $x, y$ .

```
class (Semigroup a) => Monoid a where
```

```
  mempty :: a
```

For colours, the identity element is transparent black:

```
instance Monoid Colour where
```

```
  mempty = Colour 0 0 0 0
```

For each of the semigroups discussed previously:

- Are they monoids?
- If so, what is the identity element?

Are there any semigroups that are *not* monoids?

# Monoid

## Monoids

A *monoid* is a semigroup  $(S, \bullet)$  equipped with a special *identity element*  $z \in S$  such that  $x \bullet z = x$  and  $z \bullet y = y$  for all  $x, y$ .

```
class (Semigroup a) => Monoid a where  
  mempty :: a
```

For colours, the identity element is transparent black:

```
instance Monoid Colour where  
  mempty = Colour 0 0 0 0
```

For each of the semigroups discussed previously:

- Are they monoids?
- If so, what is the identity element?

Are there any semigroups that are *not* monoids?

Non-empty lists, maximum

## Newtypes

Assignment Project Exam Help

There are multiple possible monoid instances for numeric types like Integer:

- The operation (+) is associative, with identity element 0
- The operation (\*) is associative, with identity element 1

<https://powcoder.com>

Add WeChat powcoder

## Newtypes

Assignment Project Exam Help

There are multiple possible monoid instances for numeric types like Integer:

- The operation  $(+)$  is associative, with identity element 0
- The operation  $(*)$  is associative, with identity element 1

<https://powcoder.com>

Haskell doesn't use any of these, because there can be only one instance per type per class in the **entire program** (including all dependencies and libraries used).

A common technique is to define a **separate type** that is represented identically to the original type, but can have its own, different type class instances.

Add WeChat powcoder



## Newtypes

There are multiple possible monoid instances for numeric types like Integer:

- The operation (+) is associative, with identity element 0
- The operation (\*) is associative, with identity element 1

Haskell doesn't use any of these, because there can be only one instance per type per class in the **entire program** (including all dependencies and libraries used).

A common technique is to define a **separate type** that is represented identically to the original type, but can have its own, different type class instances.

In Haskell, this is done with the `newtype` keyword.

## Newtypes

A newtype declaration is much like a data declaration except that there can be only one constructor and it must take exactly one argument:

```
newtype Score = S Integer
```

```
instance Semigroup Score where  
  S x <> S y = S (x + y)
```

```
instance Monoid Score where  
  mempty = S 0
```

Here, `Score` is represented identically to `Integer`, and thus no performance penalty is incurred to convert between them.

In general, newtypes are a great way to prevent mistakes. Use them frequently!

## Ord

Ord is a type class for inequality comparison:

```
class Ord a where  
  (<=) :: a -> a -> Bool
```

What laws should instances satisfy?

<https://powcoder.com>

Add WeChat powcoder

## Ord

Ord is a type class for inequality comparison:

```
class Ord a where  
  (<=) :: a -> a -> Bool
```

What laws should instances satisfy?

For all  $x$ ,  $y$ , and  $z$

① *Reflexivity*:  $x \leq x$ .

Add WeChat powcoder

## Ord

Ord is a type class for inequality comparison:

```
class Ord a where  
  (<=) :: a -> a -> Bool
```

What laws should instances satisfy?

For all  $x$ ,  $y$ , and  $z$

- 1 *Reflexivity*:  $x \leq x$ .
- 2 *Transitivity*: If  $x \leq y$  and  $y \leq z$  then  $x \leq z$ .

Add WeChat powcoder

## Ord

Ord is a type class for inequality comparison:

```
class Ord a where  
  (<=) :: a -> a -> Bool
```

What laws should instances satisfy?

For all  $x$ ,  $y$ , and  $z$ :

- 1 *Reflexivity*:  $x \leq x$ .
- 2 *Transitivity*: If  $x \leq y$  and  $y \leq z$  then  $x \leq z$ .
- 3 *Antisymmetry*: If  $x \leq y$  and  $y \leq x$  then  $x == y$ .

Add WeChat powcoder

<https://powcoder.com>

## Ord

Ord is a type class for inequality comparison:

```
class Ord a where  
  (<=) :: a -> a -> Bool
```

What laws should instances satisfy?

For all  $x$ ,  $y$ , and  $z$

- 1 *Reflexivity*:  $x \leq x$ .
- 2 *Transitivity*: If  $x \leq y$  and  $y \leq z$  then  $x \leq z$ .
- 3 *Antisymmetry*: If  $x \leq y$  and  $y \leq x$  then  $x == y$ .
- 4 *Totality*: Either  $x \leq y$  or  $y \leq x$

## Ord

Ord is a type class for inequality comparison:

```
class Ord a where  
  (<=) :: a -> a -> Bool
```

What laws should instances satisfy?

For all  $x$ ,  $y$ , and  $z$

- 1 *Reflexivity*:  $x \leq x$ .
- 2 *Transitivity*: If  $x \leq y$  and  $y \leq z$  then  $x \leq z$ .
- 3 *Antisymmetry*: If  $x \leq y$  and  $y \leq x$  then  $x == y$ .
- 4 *Totality*: Either  $x \leq y$  or  $y \leq x$

Relations that satisfy these four properties are called *total orders*. Without the fourth (totality), they are called *partial orders*.



## Eq

Eq is a type class for equality or equivalence:

```
class Eq a where  
  (==) :: a -> a -> Bool
```

What laws should instances satisfy?

<https://powcoder.com>

Add WeChat powcoder

## Eq

Eq is a type class for equality or equivalence:

```
class Eq a where
```

```
(==) :: a -> a -> Bool
```

What laws should instances satisfy?

For all x, y, and z:

① *Reflexivity*:  $x == x$ .

Add WeChat powcoder

## Eq

Eq is a type class for equality or equivalence:

```
class Eq a where  
  (==) :: a -> a -> Bool
```

What laws should instances satisfy?

For all x, y, and z:

- 1 *Reflexivity*:  $x == x$ .
- 2 *Transitivity*: If  $x == y$  and  $y == z$  then  $x == z$ .

Add WeChat powcoder

<https://powcoder.com>

## Eq

Eq is a type class for equality or equivalence:

```
class Eq a where
  (==) :: a -> a -> Bool
```

What laws should instances satisfy?

For all x, y, and z:

- ① *Reflexivity*:  $x == x$ .
- ② *Transitivity*: If  $x == y$  and  $y == z$  then  $x == z$ .
- ③ *Symmetry*: If  $x == y$  then  $y == x$ .

Add WeChat powcoder

<https://powcoder.com>

## Eq

Eq is a type class for equality or equivalence:

```
class Eq a where
  (==) :: a -> a -> Bool
```

What laws should instances satisfy?

For all x, y, and z:

- ① *Reflexivity*:  $x == x$ .
- ② *Transitivity*: If  $x == y$  and  $y == z$  then  $x == z$ .
- ③ *Symmetry*: If  $x == y$  then  $y == x$ .

Relations that satisfy these are called *equivalence relations*.

Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder

## Eq

Eq is a type class for equality or equivalence:

```
class Eq a where  
  (==) :: a -> a -> Bool
```

What laws should instances satisfy?

For all x, y, and z:

- 1 *Reflexivity*:  $x == x$ .
- 2 *Transitivity*: If  $x == y$  and  $y == z$  then  $x == z$ .
- 3 *Symmetry*: If  $x == y$  then  $y == x$ .

Relations that satisfy these are called *equivalence relations*.

Some argue that the Eq class should be only for *equality*, requiring stricter laws like:

If  $x == y$  then  $f\ x == f\ y$  for all functions  $f$

But this is debated.

## Types and Values

# Assignment Project Exam Help

Haskell is actually comprised of **two languages**.

- The *value-level* language, consisting of expressions such as `if`, `let`, `3` etc.

<https://powcoder.com>

Add WeChat powcoder

## Types and Values

# Assignment Project Exam Help

Haskell is actually comprised of **two languages**.

- The **value-level** language, consisting of expressions such as `if`, `let`, `3` etc.
- The **type-level** language, consisting of types `Int`, `Bool`, synonyms like `String`, and type **constructors** like `Maybe`, `(->)`, `[ ]` etc.

Add WeChat powcoder

<https://powcoder.com>



## Types and Values

# Assignment Project Exam Help

Haskell is actually comprised of **two languages**.

- The **value-level** language, consisting of expressions such as `if`, `let`, `3` etc.
- The **type-level** language, consisting of types `Int`, `Bool`, synonyms like `String`, and type **constructors** like `Maybe`, `(->)`, `[ ]` etc.

This type level language itself has a type system!

<https://powcoder.com>  
Add WeChat powcoder

## Kinds

# Assignment Project Exam Help

Just as terms in the value level language are given types, terms in the type level language are given *kinds*.

The most basic kind is written as  $*$ .

- Types such as `Int` and `Bool` have kind  $*$ .
- Seeing as `Maybe` is parameterised by one argument, `Maybe` has kind  $* \rightarrow *$ : given a type (e.g. `Int`) it will return a type (`Maybe Int`).

<https://powcoder.com>

Add WeChat powcoder

## Lists

# Assignment Project Exam Help

Suppose we have a function:

```
toString :: Int -> String
```

And we also have a function to give us some numbers:

```
getNumbers :: Seed -> [Int]
```

How can I compose toString with getNumbers to get a function f of type Seed -> [String]?

Add WeChat powcoder

<https://powcoder.com>

## Lists

# Assignment Project Exam Help

Suppose we have a function:

```
toString :: Int -> String
```

And we also have a function to give us some numbers:

```
getNumbers :: Seed -> [Int]
```

How can I compose toString with getNumbers to get a function f of type Seed -> [String]?

**Answer:** we use map:

```
f = map toString . getNumbers
```

<https://powcoder.com>  
Add WeChat powcoder

## Maybe

Suppose we have a function

# Assignment Project Exam Help

```
toString :: Int -> String
```

And we also have a function that may give us a number:

```
tryNumber :: Seed -> Maybe Int
```

# <https://powcoder.com>

How can I compose `toString` with `tryNumber` to get a function `f` of type `Seed -> Maybe String`?

# Add WeChat powcoder

## Maybe

Suppose we have a function

```
toString :: Int -> String
```

And we also have a function that may give us a number:

```
tryNumber :: Seed -> Maybe Int
```

How can I compose `toString` with `tryNumber` to get a function `f` of type `Seed -> Maybe String`?

We want a `map` function but for the `Maybe` type:

```
f = maybeMap toString . tryNumber
```

Let's implement it.

## Functor

All of these functions are in the interface of a single type class, called **Functor**.

```
class Functor f where
```

```
  fmap :: (a -> b) -> f a -> f b
```

Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder

## Functor

All of these functions are in the interface of a single type class, called **Functor**.

```
class Functor f where
```

```
  fmap :: (a -> b) -> f a -> f b
```

Unlike previous type classes we've seen like `Ord` and `Semigroup`, `Functor` is over types of kind `* -> *`

<https://powcoder.com>

Add WeChat powcoder



## Functor

All of these functions are in the interface of a single type class, called `Functor`.

```
class Functor f where
```

```
  fmap :: (a -> b) -> f a -> f b
```

Unlike previous type classes we've seen like `Ord` and `Semigroup`, `Functor` is over types of kind `* -> *`

Instances for:

- Lists
- Maybe
- Tuples (how?)
- Functions (how?)

Demonstrate in live-coding

Assignment Project Exam Help

<https://powcoder.com>

Add WeChat powcoder

## Functor Laws

# Assignment Project Exam Help

The functor type class must obey two laws:

### Functor Laws

- ① `fmap id == id`
- ② `fmap f . fmap g == fmap (f . g)`

<https://powcoder.com>

Add WeChat powcoder

## Functor Laws

# Assignment Project Exam Help

The functor type class must obey two laws:

### Functor Laws

- 1 `fmap id == id`
- 2 `fmap f . fmap g == fmap (f . g)`

In Haskell's type system it's impossible to make a total `fmap` function that satisfies the first law but violates the second.

This is due to *parametricity*, a property we will return to in Week 8 or 9

<https://powcoder.com>  
Add WeChat powcoder

## Homework

# Assignment Project Exam Help

- 1 Do the first programming exercise, and ask us on Piazza if you get stuck. It will be due in ~~exactly 1 week~~ from the start of this lecture.
- 2 Last week's quiz is due this friday. Make sure you submit your answers.
- 3 This week's quiz is also up, due next friday (the friday after this one).

<https://powcoder.com>  
Add WeChat powcoder