Assignment Project Exam Help

Software System Design and Implementation

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Motivation

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We've already the properties properties from programs.

How do we come up with correctness properties in the first place?

Structure of a Module

A Haskell program will usually be made up of many modules, each of which exports one or mostly property in the project Exam Help Typically a module for a data type X will also provide a set of functions, called operations, on X.

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- to query information from the data type: $q:: X \to \cdots$
- to update the data type: $u :: \cdots X \to X$

A lot of software and designed that approveder

Example (Data Types)

A dictionary data type, with empty, insert and lookup.

Data Invariants

One Aussi gramie at Project Exam Help Data Invariants

Data invariants are properties that pertain to a particular data type.

Whenever we up preparious of the other type we mant to the particular data type.

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Example

- That a list Ave s in Westery a Mays pow Goder
- That a binary tree satisfies the search tree properties.
- That a date value will never be invalid (e.g. 31/13/2019).

Properties for Data Invariants

For a given data type X, we define Project Exam Help $\underset{\mathrm{wf} \ :: \ X \rightarrow \ Bool}{\text{For a given data type X, we define }} Project Exam Help$

For a given value x : X, wf x returns true iff our data invariants hold for the value x. $\begin{array}{c} \text{Note of the value } x : X \text{ of the value } x \text{ of the value$

Properties

Data Invariants and ADTs

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For each operation, if all input values of type X satisfy wf, all output values will satisfy wf.

In other words, for each constructor operation c power coder wf $(c \cdots)$, and for each update operation $u :: X \to X$ we must show wf $x \Longrightarrow \text{wf}(u \times X)$

Demo: Dictionary example, sorted order.

Stopping External Tampering

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Even with our sorted dictionary example, there's nothing to stop a malicious or clueless programmer from going in and mucking up our data invariants.

Example https://powcoder.com

The malicious programmer could just add a word directly to the dictionary, unsorted, bypassing our carefully written insert function.

We want to prevent this sort of thing from Happening. WCOGE1

Abstract Data Types

An abstract data type (ADT) is a data type where the implementation details of the type and St. Sals cined be arbles are like eCt EX and Help

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If we don't have access to the implementation of Dict, the we can only access it via the provided operations, which we know preserve our data invariants. Thus, our data invariants cannot be violated if this module is correct.

Abstract Data Types

```
An abstract data type (ADT) is a data type where the implementation details of the type and track called bratishs are little CCT EXAM HELD
```

type Word = String
type Definit https://powcoder.com
emptyDict :: Dick

insertWord :: Word -> Definition -> Dict -> Dict
lookup :: Word -> Dict -> Mewbe Definition

If we don't have access to the implementation of Dict, then we can only access it via the provided operations, which we know preserve our data invariants. Thus, our data invariants cannot be violated if this module is correct.

Demo: In Haskell, we make ADTs with module headers.

Abstract? Data Types

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In general, abstraction is the process of eliminating detail.

The inverse of https://woweoder.com

Abstract data types like the dictionary above are abstract in the sense that their implementation details are hidden, and we no longer have to reason about them on the

level of implemed and WeChat powcoder

Validation

Supple String -- email address Exam Help

-> String -- message

It is possible to mix the two string arguments, and even if we get the order right, it's possible that the given email address is not valid.

Question

Data Invariants and ADTs

Suppose that we wanted to make it impossible to be send marie without first checking that the email address was valid.

How would we accomplish this?

Validation ADTs

We could define a tiny ADT for validated email addresses, where the data invariant is that the contained email address is Picticat Exam Help module Email = Email String

checkEmanttpSing/powender.com
checkEmail str | '0' elem` str = Just (Email str)
| otherwise = Nothing

Validation ADTs

```
We could define a tiny ADT for validated email addresses, where the data invariant is
that the contained email address is Picoject Exam Help module Email, checkEmail, sendEmail)
    newtype Email = Email String
    checkEmanttpsing/powender.com
                     '@' elem str = Just (Email str)
                     otherwise
                                    = Nothing
Then, change the type of sweethat powcoder
```

newtype Email = Email String

Validation ADTs

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```
checkEmanttpsing/powender.com
             '0' elem' str = Just (Email str)
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```

Then, change that powcoder sendEmail :: Email -> String -> IO

The only way (outside of the Email ADT module) to create a value of type Email is to use checkEmail.

Validation ADTs

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  sendEmail :: Email -> String -> IO
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The only way (outside of the EmailADT module) to create a value of type Email is to use checkEmail.

checkEmail is an example of what we call a smart constructor. a constructor that enforces data invariants.

Reasoning about ADTs

Consider the following, more traditional example of an ADT interface, the unbounded Assignment Project Exam Help

```
emptyQueue :: Queue enqueue :: Intpsue//powcoder.com front :: Queue > Int
dequeue :: Queue -> Queue -- partial
We could try to come by with preperties that relies the tree these functions of each other
without reference to their implementation, such as:
```

dequeue (enqueue x emptyQueue) == emptyQueue

However these do not capture functional correctness (usually).

We could imagine a simple implementation for queues, just in terms of lists: Assignment Project Exam Help

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```
We could imagine a simple implementation for queues, just in terms of lists: empty signment Project Exam Help
enqueueL a
frontI.
              = head
dequeueL
              https://powcoder.com
sizeL
```

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```
We could imagine a simple implementation for queues, just in terms of lists:

empty us a gnment Project Exam Help
enqueueL a = (++ [a])

frontL = head

dequeueL
sizeL htaibs://powcoder.com
```

But this implementation is O(n) to enqueue! Unacceptable!

We could imagine a simple implementation for queues, just in terms of lists:

empty signment Project Exam Help enqueueL a frontI. = head dequeueL https://powcoder.com sizeL

But this implementation is $\mathcal{O}(n)$ to enqueue! Unacceptable!

However! Add WeChat powcoder This is a dead simple implementation, and trivial to see that it is correct. If we make a

better queue implementation, it should always give the same results as this simple one. Therefore: This implementation serves as a functional correctness specification for our Queue type!

The typical approach to connect our model queue to our Queue type is to define a relation, called a refinement relation that relates appropriate the same queue conceptually.

```
rel :: Queue -> [Int] -> Bool
```

Data Invariants and ADTs

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Data Invariants and ADTs

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That any query functions for our two types produce equal results for related inputs, such as for size:

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Data Invariants and ADTs

```
Then, we show that the refinement relation holds initially:
```

That any query functions for our two types produce equal results for related inputs. such as for size:

```
prop_size_r AddreWeChate powcoder
```

And that each of the queue operations preserves our refinement relation, for example for enqueue:

```
prop_enq_ref fq lq x =
 rel fg lg ==> rel (enqueue x fg) (enqueueL x lg)
```

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```
emptyQueue https://powcoder.com
```

Assignment Project Exam Help

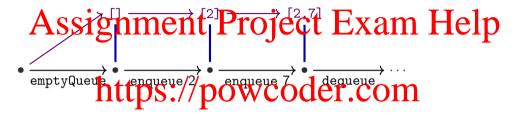
emptyQueue/2/powcoder.com

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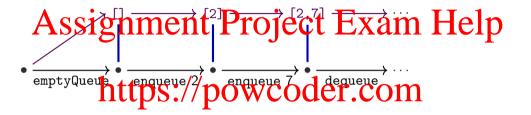
prop_empty_r = rel emptyQueue emptyQueueL

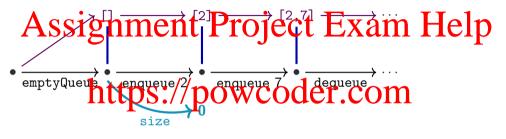
Assignment Project Exam Help emptyQueue https://powcoder.com

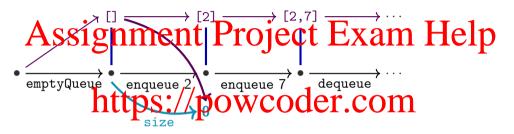
rel fq lq Add (Mucchat powcoder



rel fq lq Add (Mucchat powcoder

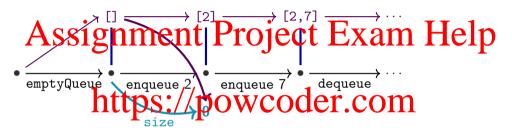






Add WeChat powcoder

prop_size_r fq lq = rel fq lq ==> size fq == sizeL lq



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prop_size_r fq lq = rel fq lq ==> size fq == sizeL lq

Whenever we use a Queue, we can reason as if it were a list!

Abstraction Functions

These entire party diffusions with randomly generated inputs.

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Abstraction Functions

These example partners after the test with the control of the precipitation of the control of th

Abstraction Functions

These entire party diffus to se wit except because liprel fq 1q preconditions are very hard to satisfy with randomly generated inputs. For this example, it's a lot easier if we define an abstraction function that computes the corresponding abstract list from the concrete Queue. $\frac{\text{Powcoder.com}}{\text{toAbstract}} :: \text{Queue} \rightarrow [\text{Int}]$

Conceptually, our refinement relation is then just: $\begin{matrix} Add & We C \\ hat powcoder \end{matrix}$

However, we can re-express our properties in a much more QC-friendly format (Demo)

Fast Queues

operations.

```
data Queue = Q [Int] -- front of the queue
      https://powcoder.com
           Int -- size of the rear
```

We store the rear part of the queue in reverse order, to make enqueueing easier. Add WeChat powcoder

Fast Queues

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```
data Queue = Q [Int] -- front of the queue
      https://powcoder.com
            Int -- size of the rear
```

We store the rear part of the queue in reverse order, to make enqueueing easier.

Thus, converting from Car Queue Comparate progression and the rear:

```
toAbstract :: Queue -> [Int]
toAbstract (O f sf r sr) = f ++ reverse r
```

These kinds of properties establish what is known as a data refinement from the abstrat, sly is in the label to the label

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In general, all functional correctness specifications can be expressed as:

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Refinement and Specifications

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- all data in attps in perwooder.com
- 2 the implementation is a refinement of an abstract correctness model.

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Refinement and Specifications

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Refinement and Specifications

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Warning

Data Invariants and ADTs

While abstraction can simplify proofs, abstraction does not reduce the fundamental complexity of verification, which is provably hard.

In addition to the already-stated refinement properties, we also have some data invarants to the plant of the length of the leng

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- 1 length f == sf
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We will ensure our Arbitrary instance only ever generates values that meet these invariants.

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1 length f == sf

Data Invariants and ADTs

- 0 length r == sr
- important the tear.

We will ensure our Arbitrary instance only ever generates values that meet these invariants.

Thus, our well reduced used need to the late it variants on the outputs of our operations:

```
prop_wf_empty = wellformed (emptyQueue)
prop_wf_enq q = wellformed (enqueue x q)
prop_wf_deq q = size q > 0 ==> wellformed (dequeue q)
```

Implementing the Queue

Assignment Project Exam Help We will generally implement by:

- Dequeue from the front.
- Enqueue thtetps://powcoder.com
- If necessary, re-establish the third data invariant by taking the rear, reversing it, and appending it to the front.

Implementing the Queue

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- Enqueue three s://powcoder.com
- If necessary, re-establish the third data invariant by taking the rear, reversing it, and appending it to the front.

This step is low (C) (n) thursofly lappens to the lappens average case amortised complexity of $\mathcal{O}(1)$ time.

```
enqueue x (Q f sf r sr) = inv3 (Q f sf (x:r) (sr + 1))

Where enqueue x (Q f sf r sr) = inv3 (Q f sf (x:r) (sr + 1))

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       https://powcoder.com
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Whe Assignment Project Exam Help
                 htt\vec{p}\overset{\text{o}}{\underset{0}{\text{in}}}\overset{\text{o}}{\underset{[1,2,3]}{\text{powcod}}}\overset{\text{o}}{\underset{[4]}{\text{er.com}}}
```

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```
enqueue x (Q f sf r sr) = inv3 (Q f sf (x:r) (sr + 1))
When Assignment Project Exam Help
       https://powcoder.com
           \rightarrow Q [1,2,3]
       Add WeChat powcoder
```

```
enqueue x (Q f sf r sr) = inv3 (Q f sf (x:r) (sr + 1))
When Assignment Project Exam Help
       https://powcoder.com

ightarrow Q [1,2,3]
       Add We Chat powcoder
```

Data Invariants and ADTs

Amortised Cost

enqueue x (Q f sf r sr) = inv3 (Q f sf (x:r) (sr + 1))When Assignment Project Exam Help https://powcoder.com d.WeChat;powcoder

Observe that the slow invariant-reestablishing step (*) happens after 1 step, then 2, then 4

Extended out, this averages out to $\mathcal{O}(1)$.

Data Invariants and ADTs

Another Example

```
Consider this ADT interface for a bag of numbers:

data Assignment Project Exam Help
emptyBag :: Bag
addToBag :: Int -> Bag -> Bag

averageBag : had -> Maybe Intwooder.com
```

Another Example

```
Consider this ADT interface for a bag of numbers:

data Assignment Project Exam Help
emptyBag : Bag
addToBag :: Int -> Bag -> Bag
our conceptual abstract model is just a list of numbers: COM
emptyBagA = []
addToBagA x Adds WeChat powcoder
averageBagA [] = Nothing
averageBagA xs = Just (sum xs `div` length xs)
```

But do we need to keep track of all that information in our implementation?

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Consider this ADT interface for a bag of numbers:

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```

But do we need to keep track of all that information in our implementation? No!

Concrete Implementation

```
Our Arges voin which think into recet, the tyta and the lentp data Bag = B { total :: Int , count :: Int }
emptyBag :: Bag
emptyBag = Bhottps://powcoder.com
addToBag :: Int -> Bag -> Bag
addToBag x (B t c) = B (x + t) (c + 1)
                 ld Wechat powcoder
averageBag (B _ 0) = Nothing
averageBag (B t c) = Just (t `div` c)
```

Refinement Functions

Assignment Project Exam Help Normally, writing an abstraction function (as we did for Queue) is a good way to

express our refinement relation in a QC-friendly way. In this case, however, it's hard to

```
write such a function:
toAbstract: net ps. //powcoder.com
toAbstract (B t c) = ?????
```

```
Instead, we will go in the other direction, giving us a refinement function: toConc :: [Ixt Clag VeChat powcoder
```

toConc xs = B (sum xs) (length xs)

prop_ref_empty =

Properties with Refinement Functions

Refirements of the Refirement of the Refirement

```
toConc emhtBaps emprowcoder.com

prop_ref_add x ab =
    toConc (addToBagA x ab) == addToBag x (toConc ab)
    Add WeChat powcoder

prop_ref_avg ab =
    averageBagA ab == averageBag (toConc ab)
```

Assignment 1 and Break

Assignment Project Exam Help

Assignment 1 has been released.

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It is due right before the Wednesday Lecture of Week 5. $\frac{1}{N} \frac{1}{N} \frac{1}$

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Advice from Alumni

The assignments do not involve much coding, but they do involve a lot of thinking.

Start early!

Homework

Assignment Project Exam Help

- Get started on Assignment, 1.
 Next programming Sergise Sur, W.G. Get Got Wed Viet 5.
- 1 Last week's guiz is due this Friday. Make sure you submit your answers.
- This week's quiz is also up, due the following Friday.

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