COMP3141

Software System Design and Implementation

Functors, Applicatives, and Monads Practice

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Exercise 4

- Capitalise all characters in the input file.
- Sum all the numbers in the input file.
- Implement a guessing game AI.

State & IO

Week 5 covered State and IO and you've had a few weeks to work with them.
Do you have any questions?

Functors, Applicatives, Monads

- Consider *higher-kinded* types of kind `* -> *` that *contain* or *produce* their argument type.
- *Functor* lets us use a pure function to map between the higher-kinded type applied to different concrete types.
- *Applicative* lets us apply a *n*-ary function in the context of the higher-kinded type.
- *Monad* lets us *sequentially compose* functions that return values in the higher-kinded type.

Functors


```
class Functor f where
  fmap :: (a -> b) -> f a -> f b
```

The functor typeclass must obey two laws:

Functor Laws

1. `fmap id == id`
2. `fmap f . fmap g == fmap (f . g)`

Applicatives


```
class Functor f => Applicative f where
  pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b
```


The functor type class must obey four additional laws:

Applicative Laws

1. `pure id <*> v = v` (Identity)
2. `pure f <*> pure x = pure (f x)` (Homomorphism)
3. `u <*> pure y = pure ($ y) <*> u` (Interchange)
4. `pure (.) <*> u <*> v <*> w = u <*> (v <*> w)` (Composition)

Alternative Applicative

It is possible to express Applicative equivalently as:

```
class Functor f => App f where
  pure :: a -> f a
  tuple :: f a -> f b -> f (a,b)
```


Example (Alternative Applicative)

1. Using `tuple`, `fmap` and `pure`, let's implement `<*>`.
2. And, using `<*>`, `fmap` and `pure`, let's implement `tuple`.

done in Haskell.

Proof exercise: Prove that `tuple` obeys the applicative laws.

Monads


```
class Applicative m => Monad m where
  (>>=) :: m a -> (a -> m b) -> m b
```

We can define a composition operator with (>>=):


```
(<=<) :: (b -> m c) -> (a -> m b) -> (a -> m c)
(f <=< g) x = g x >>= f
```

The monad type class must obey three additional laws:

Monad Laws

1. `f <=< (g <=< x) == (f <=< g) <=< x` (associativity)
2. `pure <=< f == f` (left identity)
3. `f <=< pure == f` (right identity)

Alternative Monad

It is possible to express Monad equivalently as:

```
class Applicative m => Mon m where
  join :: m (m a) -> m a
```


Example (Alternative Monad)

1. Using `join` and `fmap`, let's implement >>=.
2. And, using >>= let's implement `join`.

done in Haskell.

Tree Example


```haskell
data Tree a
  = Leaf
  | Node a (Tree a) (Tree a)
  deriving (Show)
```


Example (Tree Example)

Show that `Tree` is an `Applicative` instance.
done in Haskell!

Note that `Tree` is not a `Monad` instance.

Formulas Example


```
data Formula v = Var v
               | And (Formula v) (Formula v)
               | Or  (Formula v) (Formula v)
               | Not (Formula v)
               | Constant Bool
               deriving (Eq,Show)
```

Example (Formulas Example)

Show that `Formula` is a `Monad` instance.

done in Haskell.

Homework

1. Week 5's quiz is due on Friday. Make sure you submit your answers.
2. The fifth programming exercise is due by the start of my next lecture (in 7 days).
3. This week's quiz is also up, it's due Friday week (in 9 days).

Consultations

- Consultations will be made on request. Ask on piazza or email `cs3141@cse.unsw.edu.au`.
- If there is a consultation it will be announced on Piazza with a link a room number for Hopper.
- Will be in the Thursday lecture slot, 9am to 11am on Blackboard Collaborate.
- Make sure to join the queue on Hopper. Be ready to share your screen with REPL (`ghci` or `stack repl`) and editor set up.