

Software System Design and Implementation

https://powcoder.com

Add Wei Curtis Millar De Wooder

Data Types

Product Types

Assignment Project Exam Help deriving (Show, Eq)

data Vector https://powcoder.com deriving (Show, Eq)

```
movePoint :: Acidd Weel That powcoder
  = Point (x + dx) (y + dy)
```

Data Types

•0000000000000

Records

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```
https://powcoder.com
, opacityC :: Int

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```

Data Types

Sum Types

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```
https://powcoder.com
```

Addin Section powcoder

Data Types

Constructors

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Data Types

Custom Constructors

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data Point = Point Float Float

driving (Shdw Fo) WCOder.COM

data Vector = Vector Float Float

deriving (Show, Eq)

Here, Point an Acctor ar Wetconstness. powcoder

Data Types

Algebraic Data Types

```
Just as the Point constructor took two Float arguments, constructors for sum types
                 nent Project ExampHelp
data PictureObject
   = Path
             [Point]
                         Colour LineStyle
     Ellipse Point Float Float Float
            Colour LineStyle FillStyle Powcoder
```

```
type Picture = [PictureObject]
```

Here, type creates a *type alias* which provides only an alternate name that refers to an existing type.

Data Types

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- Patterns are used to deconstruct an value of 1 particular type
 A pattern can be a binding to a hole (_), a name, of a constructor of the type.
- When defining a function, each argument is bound using a separate pattern.

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Data Types

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```
if' :: Bool https://powcoder.com
if' False _ else' = else'
```

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Data Types

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```
factorial :: https://powcoder.com
factorial n = n * factorial (n - 1)
```

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Data Types

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```
isVowel :: Char -> Bool
isVowel 'o' = True
isVowel 'u' And WeChat powcoder
```

Data Types

Records and Accessors

```
data Assignment Project Examt Help
```

-- Is equivahttps://powcoder.com

```
data Color = Color Int Int Int
```

```
redC (CoAdd WeChat powcoder greenC (Color _ g _ _) = g blueC (Color _ b _) = b opacityC (Color _ _ o) = o
```

Data Types

Patterns in Expressions

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```
factorial :: Int -> Int factorial x https://powcoder.com

case x of

0 -> 1

n -> n * factorial (n - 1) Chat powcoder

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```

Data Types

Newtype

new types significant telephone in the property of the propert

```
newtype Kilometers = Kilometers Float newtype Milentups Float powcoder.com
```

```
kilometersToMiles :: Kilometers -> Miles
kilometersToMiles (Kilometers kms) = Miles $ kms / 1.60934

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```

milesToKilometers :: Miles -> Kilometers

milesToKilometers (Miles miles) = Kilometers \$ miles * 1.60934

Data Types

Natural Numbers

data Assignment Project Exam Help

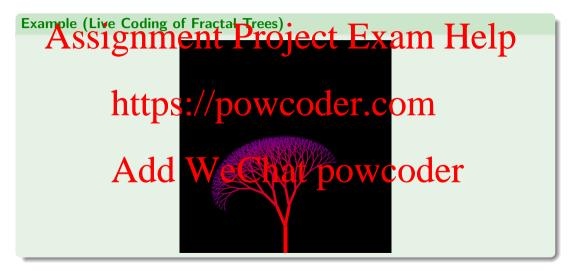
```
add :: Nat -> Nat -> Nat add Zero https://powcoder.com
```

```
zero = Zero
one = Succ ZAdd WeChat powcoder
two = add one one
```

- 1 Nat is recursive as it has the (Succ) constructor which takes a Nat.
- 2 Nat has the Zero constructor which does not recurse and acts like a base case.

Data Types

More Cool Graphics



Type Classes

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- 2 Type classes describe a set of behaviours that can be implemented for any type.
- A function or type class instance can operate on a type variable constrained by a type class instance COVIN COCET. COM
- 4 A type class is similar to an OOP interface.
- When creating an instance of a type class with laws, you must ensure the laws are held manually they carried be checked to the completion of the checked to the checked the completion of the checked to the checked the completion of the checked the completion of the checked the completion of the checked the
- When using a type class with *laws* you can assume that all laws hold for all instances of the type class.

Show

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Show simply allows us to take a type and represent it as a string.

```
Haskell Definitettps://powcoder.com
```

show :: a -> [Char]

This is implemented all whee lit-intats sport to the char

Read

Effectives signmenta Projecte Exame Help value and decode it.

You can think threat possessing the following definition but it is instually somewhat more complex.

Definition

class Read a Archarl We Chat powcoder

This is implemented for all of the built-in types such as Int, Bool, and Char

Ord

ord Assignment Project ExaminHelp

Haskell Definition

class Ord a here (<=) https://powcoder.com

- **1** Tranisitivity: $x \le y \land y \le z \rightarrow x \le z$

- **1 Totality** (total order): $x < y \lor y < x$

Eq

Eq alassipementes roject e wxeamed Help

Haskell Definition

class Eq a where

(==)https://powcoder.com

- **1** Reflexivity: x = x
- Symmetry: X DY WeChat powcoder

 Transitivity DY WeChat powcoder
- **10 Negation** (equality): $x \neq y \rightarrow \neg(x = y)$
- **Substitutivity** (equality): $x = y \rightarrow f x = f y$

Derived Instances

When defining a new type we can have the compiler generate instance of Show Read, Ord, on Eq. with the der twing statement at the end of the deviation. The order is the compiler of the deviation.

```
Haskell Example

data Colour https://greenow.coder.com
, blueC :: Int
Add Wreing Stat. powcoder
```

Derived instances of Ord will be total orders and will order by fields in the order they appear in a product type and will order constructors in the same order they are defined. Derived instances of Eq will be strict equalities.

Kinds of Types

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- ① Just as values and functions in the *runtime language* of Haskell have *types*, types in the *type language* of Haskell have *kinds*.
- The kind https://powcoder.com
- Just as functions exist over values (with the type a -> b), type constructors exist for types.
- * -> * is a type constitution at taken at compressive compressive concrete type.

Maybe

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Haskell Definition

```
-- Maybe :: * -> *
data Maybe ahthps://powcoder.com
```

- Maybe is a type constructor that takes a type and produces a type that may or may not hotal active. We chat powcoder
- 2 Maybe Int is a concrete type that may or may not hold an Int.

List

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-- *List* :: * -> * data List a = Cons a (List a)

https://powcoder.com

- List a is recursive as it has the (Cons) constructor which takes a List a.
- 2 List a has the Nil constructor which does not recurse and acts like a base case.
- List is a type Coloruc of text at the proposition of a value.
- 4 List Int is a concrete type that zero or more values of type Int.

Haskell List

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```
Definition
```

```
data [a] = ahttps://powcoder.com
```

- [a, b, c] is syntactic sugar for the constructor (a : (b : (c : []))).
 "abc" is syntactic sugar for the constructor (DOWCOOOCC).
- Both can also be used as patterns.

Tree

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data Tree a hode a (Tree a) (Tree a) (Tree a) (Tree a) (Tree a)

- ① Tree a is recursive in the same manner as List a.
- Tree is a type constructive takes a type and produces a type that holds zero or more of a value in a tree.
- Tree Int is a concrete type that holds zero or more values of type Int in a tree.

Semigroup

A serAges is grantone of the Project: Example the peration is associative

Haskell Definition

class Semigrant phere//powcoder.com

• Associativity: $(a \bullet (b \bullet c)) = ((a \bullet b) \bullet c)$ Example Add WeChat powcoder

Example

Data Types

instance Semigroup [a] where (<>) = (++)

Monoid

A mAissignmentaProjectciEmann-Help

Haskell Definition

```
class (Semigroup a) => Monoid a where mempty: https://powcoder.com
```

1 Identity: $(mempty \bullet x) = x = (x \bullet mempty)$

Example Add WeChat powcoder

```
instance Monoid [a] where
  mempty = []
```

Inductive Proofs

Supple SSAP 19 17 CAT to properly to find the set of natural numbers N can be defined as follows:

Definition of Natural Numbers

- 0 is a natural trips://powcoder.com
- 2 For any natural number n, n+1 is also a natural number.

- Therefore, to show P(n) for all n, it suffices to show:

 P(0) (the **backs**), and **e** Chat **powcoder**
 - 2 assuming P(k) (the *inductive hypothesis*), $\Rightarrow P(k+1)$ (the *inductive case*).

Natural Numbers Example

data Assignment Project Exam Help

```
add :: Nat -> Nat -> Nat add Zero https://powcoder.com
```

```
one = Succ Zero de WeChat powcoder
```

```
Example (1 + 1 = 2)
Prove one 'add' one = two (done in editor)
```

Induction on Lists

Hast Assignment Projects Exam Help

Definition of Haskell Lists

For any list xs, xx, xs is also hist tor any list xs, xx is also hist tor any list xs, xx is also hist tor any list xs.

This means, if we want to prove that a property P(1s) holds for all lists 1s, it suffices to show: Add WeChat powcoder

P([]) (the base case) to show:

- P(x:xs) for all items x, assuming the inductive hypothesis P(xs).

List Monoid Example

(++) Assignment Project Exam Help

(++) (x:xs) ys = x : xs ++ ys -- 2

Example (Molattps://powcoder.com

Prove for all xs, ys, zs: ((xs ++ ys) ++ zs) = (xs ++ (ys ++ zs))

Additionally Prove

- o for all xs: Add WeChat powcoder
- ② for all xs: xs ++ [] == xs

(done in editor)

List Reverse Example

```
\underset{(++)}{\overset{(++)}{\text{A:Signment}}} \underset{(s:xs)}{\overset{\text{[a]}}{\text{ys}}} \underset{=}{\overset{\text{[a]}}{\text{ment}}} \underset{ys}{\overset{\text{[a]}}{\text{Project}}} \underset{=}{\text{Exam Help}}
```

```
reverse :: https://powcoder.com
reverse (x:xs) = reverse xs ++ [x] -- B
```

```
To Prove for all Is: reverse (reverse Is) powcoder
```

(done in editor)

First Prove for all vs: reverse (vs.

First Prove for all ys: reverse (ys ++ [x]) = x:reverse ys
(done in editor)

Graphics and Artwork

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- = Path [Point] Colour LineStyle
- | Circle Point Float, Colour LineStyle FillStyle | Polygon Pt DS:// DOW COLOT FiCOM
- | Ellipse Point Float Float Float Colour LineStyle FillStyle

And deriving And ded We Chat powcoder

type Picture = [PictureObject]

Homework

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- Last week's quiz is due before on Friday. Make sure you submit your answers.
 Do the first blog and ing/exp is which first blog and ingred in first blog and in

$\begin{array}{c} \text{This week's quiz is also up, it's due next Friday (in 9 days).} \\ & Add \ WeChat \ powcoder \end{array}$