PROGRAMMING IN HASKELL

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Chapter 10 - Declaring Types and Classes

Type Declarations

In Haskell, a new name for an existing type can be defined using a type declaration.

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type String = [Add We Chat powcoder

String is a synonym for the type [Char].

Type declarations can be used to make other types easier to read. For example, given

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```
origin :: Pos
origin = (0,0)
left :: Pos \rightarrow Pos
left (x,y) = (x-1,y)
```

Like function definitions, type declarations can also have <u>parameters</u>. For example, given

type Pair
$$a = (a,a)$$

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```
mult :: Pair Int \rightarrow Int mult (m,n) = m*n

copy :: a \rightarrow Pair a copy x = (x,x)
```

Type declarations can be nested:

type Pos = (Int,Int)



type Trans Assignment Project Exam Help

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However, they cannot be recursive:

type Tree = (Int,[Tree])



Data Declarations

A completely new type can be defined by specifying its values using a <u>data declaration</u>.

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data Bool = False Flat powcoder

Bool is a new type, with two new values False and True.

Note:

- The two values False and True are called the constructors for the type Bool.
- Type and constructor names must begin with an upper-case letter.
- 2 Data declarations are similar to context free grammars? The former specifies the values of a type, the latter the sentences of a language.

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Values of new types can be used in the same ways as those of built in types. For example, given

data Answer = Yes | No | Unknown

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```
answers :: [AddsWeSh]at powcoder
answers = [Yes,No,Unknown]

flip :: Answer → Answer

flip Yes = No

flip No = Yes

flip Unknown = Unknown
```

The constructors in a data declaration can also have parameters. For example, given

data Shape = Circle Float I Rect Float Float

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```
square :: Float → Shape square n = Rect n n

area :: Shape → Float area (Circle r) = pi * r^2 area (Rect x y) = x * y
```

Note:

- Shape has values of the form Circle r where r is a float, and Rect x y where x and y are floats.
- Circle and Rect can be viewed as <u>functions</u> that construct values of type Shape: Assignment Project Exam Help

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Circle :: Float → Shape

Rect :: Float → Float → Shape

Not surprisingly, data declarations themselves can also have parameters. For example, given

data Maybe a = Nothing I Just a

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```
safediv :: Int -AdthWeChMapphoodder
safediv _ 0 = ?
safediv m n = ?

safehead :: [a] → Maybe a
safehead [] = ?
safehead xs = ?
```

Recursive Types

In Haskell, new types can be declared in terms of themselves. That is, types can be <u>recursive</u>.

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data Nat = Zero | WeChat powcoder

Nat is a new type, with constructors Zero :: Nat and Succ :: Nat \rightarrow Nat.

Note:

A value of type Nat is either Zero, or of the form Succ n where n :: Nat. That is, Nat contains the following infinite sequence of values:

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Zero

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Succ Zero

Succ (Succ Zero)

•

•

- We can think of values of type Nat as <u>natural numbers</u>, where Zero represents 0, and Succ represents the successor function 1+.
- For example, the value

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Succ (Succ (AddcWeChatp)) wcoder

represents the natural number

$$1 + (1 + (1 + 0))$$

Using recursion, it is easy to define functions that convert between values of type Nat and Int:

Two naturals can be added by converting them to integers, adding, and then converting back:

add :: Nat → Nat → Nat add m n = int2nats(gnat2introject mat2introject mat2introject

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However, using recursion the function add can be defined without the need for conversions:

add Zero n = nadd (Succ m) n = Succ (add m n) Two naturals can be added by converting them to integers, adding, and then converting back:

add :: Nat → Nat → Nat add m n = int2nats(gnat2intropect mat2intro)

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However, using recursion the function add can be defined without the need for conversions:

add m n = ?

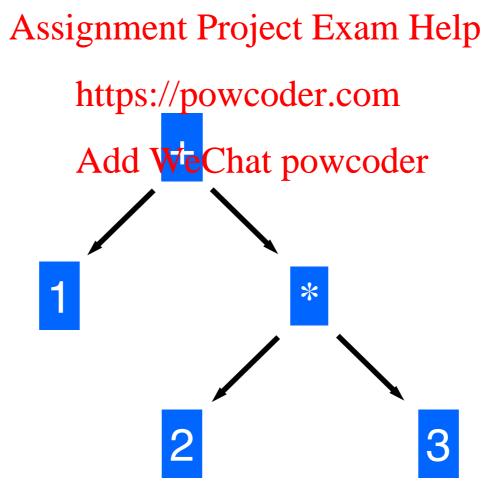
For example:

Note:

The recursive definition for add corresponds to the laws 0+n = n and (1+m)+n = 1+(m+n).

Arithmetic Expressions

Consider a simple form of <u>expressions</u> built up from integers using addition and multiplication.



Using recursion, a suitable new type to represent such expressions can be declared by:

```
data Expr = Val Int

I Add Expr Expr
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I Mul Expr Expr
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```

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For example, the expression on the previous slide would be represented as follows:

Add (Val 1) (Mul (Val 2) (Val 3))

Using recursion, it is now easy to define functions that process expressions. For example:

```
size :: Expr → Int
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size = ?

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eval :: Expr → Int
eval = ?
```

Note:

The three constructors have types:

Val :: Int → Expr

Add:: Exassignment Project Exam Help

Mul :: Expr _https://powcoder.som

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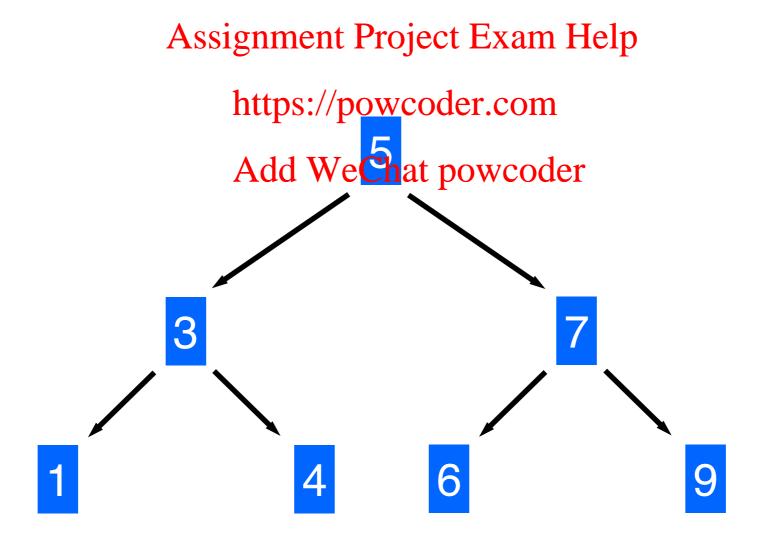
Many functions on expressions can be defined by replacing the constructors by other functions using a suitable <u>fold</u> function. For example:

Exercise: Define fold!

eval = fold id (+) (*)

Binary Trees

In computing, it is often useful to store data in a two-way branching structure or binary tree.



Using recursion, a suitable new type to represent such binary trees can be declared by:

data Tree a = Leaf a

I Node (Tree a) a (Tree a)

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For example, the tree on the previous slide would be represented as follows:

t :: Tree Int t = Node (Node (Leaf 1) 3 (Leaf 4)) 5 (Node (Leaf 6) 7 (Leaf 9)) We can now define a function that decides if a given value occurs in a binary tree:

occurs :: Ord a =\Assignmenteroject\Examplelp
occurs x t = ? https://powcoder.com

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But... in the worst case, when the value does not occur, this function traverses the entire tree.

Now consider the function <u>flatten</u> that returns the list of all the values contained in a tree:

```
flatten

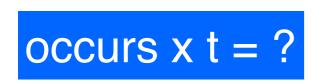
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```

A tree is a <u>search tree</u> if it flattens to a list that is ordered. Our example tree is a search tree, as it flattens to the ordered list [1,3,4,5,6,7,9].

Search trees have the important property that when trying to find a value in a tree we can always decide which of the two sub-trees it may occur in:



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This new definition is more <u>efficient</u>, because it only traverses one path down the tree.

Exercises

Using recursion and the function add, define a function that <u>multiplies</u> two natural numbers.

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Define a suitable function fold for expressions, and give a few examples of its use.

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A binary tree is <u>complete</u> if the two sub-trees of every node are of equal size. Define a function that decides if a binary tree is complete.