PROGRAMMING IN HASKELL

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Chapter 3 - Types and Classes (Original slides by Graham Hutton)

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What is a Type?

A <u>type</u> is a name for a collection of related values. For example, in Haskell the basic type

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contains the two logical values:





Type Errors

Applying a function to one or more arguments of the wrong type is called a <u>type error</u>.

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> 1 + False https://powcoder.com

> 1 + False Error Add WeChat powcoder

1 is a number and False is a logical value, but + requires two numbers.

Types in Haskell

If evaluating an expression e would produce a value of type t, then e <u>has type</u> t, written

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Every well formed expression has a type, which can be automatically calculated at compile time using a process called <u>type inference</u>.

- All type errors are found at compile time, which makes programs <u>safer and faster</u> by removing the need for type checks at run time.
- In GHCi, the <u>type</u> command calculates the type of an expression, without evaluating it:

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> not False True

> :type not False not False :: Bool

Basic Types

Haskell has a number of basic types, including:



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- fixed-precision integers



- arbitrary-precision integers



- floating-point numbers

List Types

A <u>list</u> is sequence of values of the <u>same</u> type:

```
[False, True, False] :: [Bool]

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['a','b','c','d'] :: [Char]
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```

In general:

[t] is the type of lists with elements of type t.

Note:

The type of a list says nothing about its length:

[FalseATssighment[Project Exam Help [False, True, Palse P.: [False, True, False P.: [False, True] [F

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The type of the elements is unrestricted. For example, we can have lists of lists:

[['a'],['b','c']] :: [[Char]]

Note:

Strings in Haskell are just lists of characters!

Assignment Project Exam Help [['a'],['b', c'] :: [[Char]]

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is equivalent to:

["a","bc"] :: [String]

Tuple Types

A <u>tuple</u> is a sequence of values of <u>different</u> types:

```
(False, True) :: (Bool, Bool) Exam Help

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(False, 'a', True) :: (Bool, Char, Bool)
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```

In general:

(t1,t2,...,tn) is the type of n-tuples whose ith components have type ti for any i in 1...n.

Note:

The type of a tuple encodes its size:

```
(False, Taus) gnmen Profess Exam Help (False, True, https://powse,descape)
```

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The type of the components is unrestricted:

```
('a',(False,'b')) :: (Char,(Bool,Char))
(True,['a','b']) :: (Bool,[Char])
```

Function Types

A <u>function</u> is a mapping from values of one type to values of another type:

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not :: Bool → Bool

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isDigit :: Charadd Bwe Chat powcoder

In general:

 $t1 \rightarrow t2$ is the type of functions that map values of type t1 to values to type t2.

Note:

- ? The arrow \rightarrow is typed at the keyboard as ->.
- The argument and result types are unrestricted. For example, Furletions With Pieutiple and United to the example are possible using lists or tuples:

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```
add :: (Int,Int) \rightarrow Int add (x,y) = x+y

zeroto :: Int \rightarrow [Int] zeroto n = [0..n]
```

Curried Functions

Functions with multiple arguments are also possible by returning <u>functions as results</u>:

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```
add' :: Inhttps!//powdoder.com
add' x y = x+y
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```

add' takes an integer x and returns a function $\underline{add' x}$. In turn, this function takes an integer y and returns the result x+y.

Note:

add and add' produce the same final result, but add takes its two arguments at the same time, whereas add' takes them one at a time:

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```
add :: (Inthttps://powcoder.com

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add' :: Int → (Int → Int)
```

Functions that take their arguments one at a time are called <u>curried</u> functions, celebrating the work of Haskell Curry on such functions. Process of the second of th

```
mult :: Int \rightarrow (Int \rightarrow (Int \rightarrow Int))
Assignment Project Exam Help
mult x y z = x*y*z
```

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mult takes an integer x and returns a function $\underline{\text{mult } x}$, which in turn takes an integer y and returns a function $\underline{\text{mult } x}$ y, which finally takes an integer z and returns the result x^*y^*z .

Why is Currying Useful?

Curried functions are more flexible than functions on tuples, because useful functions can often be made by partially applying anomied for the partially applying anomied for the partial part

For example: https://powcoder.com

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```
add' 1 :: Int → Int

take 5 :: [Int] → [Int]

drop 5 :: [Int] → [Int]
```

Currying Conventions

To avoid excess parentheses when using curried functions, two simple conventions are adopted:

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? The arrow - https://piakes.terthenright.

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Int \rightarrow Int \rightarrow Int

Means Int
$$\rightarrow$$
 (Int \rightarrow (Int \rightarrow Int)).

As a consequence, it is then natural for function application to associate to the <u>left</u>.

mult x y z Assignment Project Exam Help

https://powcoder.com

Means ((mult x) y) z. Powcoder

Unless tupling is explicitly required, all functions in Haskell are normally defined in curried form.

Polymorphic Functions

A function is called <u>polymorphic</u> ("of many forms") if its type contains one or more type variables.

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length :: [ahttps://powcoder.com

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for any type a, length takes a list of values of type a and returns an integer.

Note:

Type variables can be instantiated to different types in different circumstances:

```
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> length [False,True]

2 https://powcoder.com

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> length [1,2,3,4]

a = Int
```

Type variables must begin with a lower-case letter, and are usually named a, b, c, etc. Many of the functions defined in the standard prelude are polymorphic. For example:

```
fst :: (a,b) → a
head :: [ahttps://powcoder.com
take :: Int Add We Chat powcoder
zip :: [a] \rightarrow [b] \rightarrow [(a,b)]
id :: a → a
```

What's the type of sum?

What should be the type of sum (the function that sums a list of numbers)?

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sum :: [a] -https://powcoder.com

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We should be able to use sum with various types of numbers:

sum [1,2,3] —> 6 sum [1.5,2.3] —> 3.8

Overloaded Functions

A polymorphic function is called <u>overloaded</u> if its type contains one or more class constraints.

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sum :: Num a powcoder.com

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for any numeric type a, sum takes a list of values of type a and returns a value of type a.

Note:

Constrained type variables can be instantiated to any types that satisfy the constraints:

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```
> sum [1,2,3]
6

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> sum [1.1,2.2,3.3]
6.6

> sum ['a','b','c']
ERROR

a = Int

Char is not a numeric type
```

Haskell has a number of type classes, including:

- Num Numeric types
- Assignment Project Exam Help
- Ord Ordered types owcoder.com
- ? For example: Add WeChat powcoder
 - (+) :: Num $a \Rightarrow a \rightarrow a \rightarrow a$
 - $(==) :: Eq a \Rightarrow a \rightarrow a \rightarrow Bool$
 - (<) :: Ord $a \Rightarrow a \rightarrow a \rightarrow Bool$

Hints and Tips

- When defining a new function in Haskell, it is useful to begin by writing down its type; Assignment Project Exam Help
- Within a scriptipit is good practice to state the type of every new function defined;

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- When stating the types of polymorphic functions that use numbers, equality or orderings, take care to include the necessary class constraints.

Exercises

(1) What are the types of the following values?

```
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        https://powcoder.com
('a','b','c')
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[(False, '0'), (True, '1')]
([False,True],['0','1'])
[tail,init,reverse]
```

(2) What are the types of the following functions?

```
second xs = head (tail xs)
swap (x,y) = (y,x)
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pair x y = (x,y)
https://powcoder.com
double x = x*2
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palindrome xs = reverse xs == xs
twice f x = f (f x)
```

(3) Check your answers using GHCi.

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Chapter 4 - Defining Functions

Conditional Expressions

As in most programming languages, functions can be defined using <u>conditional expressions</u>.

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```
abs :: Int \rightarrow Int

abs n = if n \triangleddh\forallreChatepowcoder
```

abs takes an integer n and returns n if it is non-negative and -n otherwise.

Conditional expressions can be nested:

```
signum :: Int → Int

signum Assignment Project Exam

if n == 0 then 0 else 1

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```

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Note:

In Haskell, conditional expressions must <u>always</u> have an else branch, which avoids any possible ambiguity problems with nested conditionals.

Guarded Equations

As an alternative to conditionals, functions can also be defined using guarded equations.

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```
https://powcoder.com

abs n | n ≥ 0 = n

| otherwise We Chat powcoder
```

As previously, but using guarded equations.

Guarded equations can be used to make definitions involving multiple conditions easier to read:

Assignment Project Exam Help signum n = ?

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Note:

The catch all condition <u>otherwise</u> is defined in the prelude by otherwise = True.

Pattern Matching

Many functions have a particularly clear definition using pattern matching on their arguments.

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```
not :: Bobttps: powcoder.com

not False = \textstyle WeChat powcoder

not True = False
```

not maps False to True, and True to False.

Functions can often be defined in many different ways using pattern matching. For example

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can be defined more compactly by



However, the following definition is more efficient, because it avoids evaluating the second argument if the first argument is False:

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True && b = b
False && _https://powcoder.com

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Note:

The underscore symbol _ is a <u>wildcard</u> pattern that matches any argument value.

Patterns are matched in order. For example, the following definition always returns False:

https://powcoder.com

Patterns may not repeat batiables of example, the following definition gives an error:

List Patterns

Internally, every non-empty list is constructed by repeated use of an operator (:) called "cons" that adds an element to the estatement for the estatement to the estatement t

https://powcoder.com

[1,2,3,4] Add WeChat powcoder

Means 1:(2:(3:(4:[]))).

Functions on lists can be defined using x:xs patterns.

```
head :: [a] → a
head(ssignment Project Exam Help

tail :: [a] → [a]

tail = ? Add WeChat powcoder.
```

head and tail map any non-empty list to its first and remaining elements.

Note:

x:xs patterns only match non-empty lists:

> heasignment Project Exam Help Error https://powcoder.com

2 x:xs patterns must be <u>parenthesised</u>, because application has priority over (:). For example, the following definition gives an error:

head x:_ = x

Lambda Expressions

Functions can be constructed without naming the functions by using <u>lambda expressions</u>.

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https://powcoder.com $\lambda x \rightarrow x+x$ Add WeChat powcoder

the nameless function that takes a number x and returns the result x+x.

Note:

The symbol λ is the Greek letter <u>lambda</u>, and is typed at the keyboard as a backslash \.

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ln mathematics, nameless functions are usually denoted using the প্রাণ্ডি প্রকর্মনার প্রাণ্ডি বিশ্ব প্রাণ্ডি প্রাণ্ডি বিশ্ব বিশ্ব প্রাণ্ডি বিশ্ব বিশ্র বিশ্ব ব

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In Haskell, the use of the λ symbol for nameless functions comes from the <u>lambda calculus</u>, the theory of functions on which Haskell is based.

Why Are Lambda's Useful?

Lambda expressions can be used to give a formal meaning to functions defined using <u>currying</u>.

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For example:

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add
$$x y = X + Y$$
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means

add =
$$\lambda x \rightarrow (\lambda y \rightarrow x+y)$$

Lambda expressions are also useful when defining functions that return <u>functions as results</u>.

For example:

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is more naturally defined by

const ::
$$a \rightarrow (b \rightarrow a)$$

const $x = \lambda_{-} \rightarrow x$

Lambda expressions can be used to avoid naming functions that are only <u>referenced once</u>.

For example:

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odds n = map f [0, n-1]
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where
f x Adt2WeChat powcoder

can be simplified to

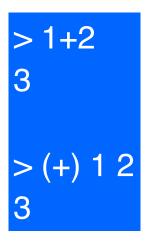
odds n = map $(\lambda x \to x^2 + 1) [0..n-1]$

Sections

An operator written <u>between</u> its two arguments can be converted into a curried function written <u>before</u> its two arguments by assign parentheixest. Exam Help

For example: https://powcoder.com

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This convention also allows one of the arguments of the operator to be included in the parentheses.

For example:



In general, if \oplus is an operator then functions of the form (\oplus) , $(x\oplus)$ and $(\oplus y)$ are called <u>sections</u>.

Why Are Sections Useful?

Useful functions can sometimes be constructed in a simple way using sections. For example:

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- (1+) https://powcoder.com
- Add WeChat powcoder
 reciprocation function
- (*2) doubling function
- (/2) halving function

Exercises

- (1) Consider a function <u>safetail</u> that behaves in the same way as tail, except that safetail maps the empty list to the empty list, whereas tail gives an error in this case. Define safetail using:
 - (a) a conditional expression, Project Exam Help
 - (b)guarded equations;
 - (c) pattern matching.ps://powcoder.com

Hint: the library function wile That proventer used to test if a list is empty.

Give three possible definitions for the logical or operator (||) using pattern matching.

Redefine the following version of (&&) using conditionals rather than patterns:

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(4) Do the same for the following version: