PROGRAMMING IN HASKELL

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Chapter 11 - The Countdown Problem

What Is Countdown?

- ? A popular <u>quiz programme</u> on British television that has been running since 1982.

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- Based upon https//gipa/penchwersion called "Des Chiffres et Des Lettres" coder
- Includes a numbers game that we shall refer to as the <u>countdown problem</u>.

Example

Using the numbers

```
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```

and the arithmetiq operators powcoder



construct an expression whose value is 765

Rules

- All the numbers, including intermediate results, must be positive naturals (1,2,3,...).

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- Each of the source mumbers can be used at most once when constructing the expression.
- We <u>abstract</u> from other rules that are adopted on television for pragmatic reasons.

For our example, one possible solution is

$$(25-10)*(50+1)$$
 = 765

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Notes:

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- There are 780 solutions for this example.
- Changing the target number to 831 gives an example that has no solutions.

Evaluating Expressions

Operators:

```
data Op = Assignment Broject Exam Help
```

https://powcoder.com Apply an operator:

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```
apply :: Op \rightarrow Int \rightarrow Int \rightarrow Int apply Add x y = x + y apply Sub x y = x - y apply Mul x y = x * y apply Div x y = x `div` y
```

Decide if the result of applying an operator to two positive natural numbers is another such:

```
valid :: Op \rightarrow Int \rightarrow Int \rightarrow Bool valid Add _Assignment Project Exam Help valid Sub x y = x > y valid Mul _ = Thftps://powcoder.com valid Div x y = x `mod` y == 0

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```

Expressions:

data Expr = Val Int | App Op Expr Expr

Return the overall value of an expression, provided that it is a positive natural number:

```
eval (Val n) Assignment Project Exam Help eval (App o I r) = [apply o x y | x — eval I https://powcoder.com//y eval r
```

Either succeeds and returns a singleton list, or fails and returns the empty list.

Formalising The Problem

Return a list of all possible ways of choosing zero or more elements from a list:

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choices :: [a] htt[3]]/powcoder.com

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For example:

> choices [1,2] [[],[1],[2],[1,2],[2,1]]

Return a list of all the values in an expression:

```
values :: Expr → [Int]
values (Val n) = [n]
values (App _ | r) = values | ++ values r
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```

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Decide if an expression is a solution for a given list of source numbers and a target number:

```
solution :: Expr \rightarrow [Int] \rightarrow Int \rightarrow Bool solution e ns n = elem (values e) (choices ns) && eval e == [n]
```

Brute Force Solution

Return a list of all possible ways of splitting a list into two non-empty parts:

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split :: [a] \rightarrow [([a],[*])) ps://powcoder.com

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For example:

```
> split [1,2,3,4]
[([1],[2,3,4]),([1,2],[3,4]),([1,2,3],[4])]
```

Return a list of all possible expressions whose values are precisely a given list of numbers:

```
exprs :: [Int] → [Expr]
exprs [] = [] Assignment Project Exam Help
exprs [n] = [Val n]
exprs ns = [e | (ls,rhttpsp/itps wcoder.com

, | ← exprs ls

, r ← Axdrd rWeChat powcoder

, e ← combine | r]
```

The key function in this lecture.

Combine two expressions using each operator:

```
combine :: Expr → Expr → [Expr]
combine | r =
  [App o | r | o ← [Add,Sub,Mul,Div]]
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```

Return a list of all possible expressions that solve an instance of the countdown problemer

```
solutions :: [Int] \rightarrow Int \rightarrow [Expr]
solutions ns n = [e | ns' \leftarrow choices ns
, e \leftarrow exprs ns'
, eval e == [n]]
```

How Fast Is It?

System: 2.8GHz Core 2 Duo, 4GB RAM

Compiler: Assignment Project Exam Help GHC version 7.10.2

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Example: Asolutions [1,3,7,10,25,50] 765

One solution: 0.108 seconds

All solutions: 12.224 seconds

Can We Do Better?

- Many of the expressions that are considered will typically be invalid fail to evaluate.

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- For our example, only around 5 million of the 33 million possible vexpressions are valid.
- Combining generation with evaluation would allow <u>earlier rejection</u> of invalid expressions.

Fusing Two Functions

Valid expressions and their values:

```
Assignment Project Exam Help type Result = (Expr,Int)

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```

We seek to define twoction that fuses together the generation and evaluation of expressions:

```
results :: [Int] \rightarrow [Result]
results ns = [(e,n) | e \leftarrow exprs ns
, n \leftarrow eval e]
```

This behaviour is achieved by defining

where

```
combine' :: Result → Result → [Result]
```

Combining results:

New function that solves countdown problems: Add WeChat powcoder

```
solutions' :: [Int] \rightarrow Int \rightarrow [Expr] solutions' ns n =

[e | ns' \leftarrow choices ns

, (e,m) \leftarrow results ns'

, m == n]
```

How Fast Is It Now?

Example: solutions' [1,3,7,10,25,50] 765

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One solution: 0.014 seconds Powcoder

Around 10 times faster in both cases.

All solutions: 1.312 seconds

Can We Do Better?

Many expressions will be <u>essentially the same</u> using simple arithmetic properties, such as:

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Exploiting such properties would considerably reduce the search and solution spaces.

Exploiting Properties

Strengthening the valid predicate to take account of commutativity and identity properties:

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How Fast Is It Now?

Example: solutions" [1,3,7,10,25,50] 765

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Valid: 250,000 expressions Add Wechat powcoder

Around 20 times less.

Solutions: 49 expressions

Around 16 times less.

One solution: 0.007 seconds Around 2 times faster.

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All solutions: Out 19/percender.com times faster

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More generally, our program usually returns all solutions in a fraction of a second, and is around 100 times faster that the original version.