The Formal Statement of the Pumping Lemma and its Negation

The pumping lemma states that for any regular language L, there is a positive integer p such that for any string s in the language L with the length of s greater than or equal to p there are three strings x, y, z such that s = xyz with the length of xy less than or equal to p and the length of y strictly positive such that for any natural number i the string xy^iz is in L.

In symbols this is written, for L a regular language

$$\exists p. (p > 0) \land \forall s. (s \in L \land |s| \ge p) \Rightarrow \exists x, y, z. (s = xyz \land |xy| \le p \land |y| > 0 \land \forall i. xy^i z \in L).$$

We negate this in stages as follows:

$$\neg [\exists p. (p Assignment \Rightarrow Pxrojectz Exam, | Help^iz \in L)].$$

which is

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Before we delve any deeper, recall that $P \Rightarrow Q$ is the same as $\neg P \lor Q$ so in the above we can write

Using this conversion to implication gives something more readable, though it may confuse those who expect to see the *ands* become *ors*. Similarly $\neg(P\Rightarrow Q)=\neg(\neg P\vee Q)=P\wedge\neg Q$. Now we can look deeper into the expression and we get

$$\forall p.(p>0) \Rightarrow \exists s.(s \in L) \land (|s| \geq p) \land \neg [\exists x,y,z.(s=xyz \land |xy| \leq p \land |y| > 0) \land \forall i.xy^iz \in L].$$

Then pushing the negation further inside we get

$$\forall p. (p>0) \Rightarrow \exists s. (s \in L) \land (|s| \geq p) \land \forall x, y, z. (s = xyz \land |xy| \leq p \land |y| > 0) \Rightarrow \neg [\forall i. xy^i z \in L].$$

Finally,

$$\forall p.(p>0) \Rightarrow \exists s.(s \in L) \land (|s| \geq p) \land \forall x,y,z.(s=xyz \land |xy| \leq p \land |y|>0) \Rightarrow \exists i.xy^iz \not\in L.$$