PUSHDOWN a : states

ZE = Zu{E} Zi : input alphabet

17: stack alphabet $\Gamma_{\varepsilon} = \Gamma_{U} \{ \varepsilon \}$

 $\delta: Q \times Z_{\varepsilon} \times \Gamma_{\varepsilon} \to \mathcal{F}(Q \times \Gamma_{\varepsilon})$ transition function

90 € Q start state

FSQ accept states

Here Pr means finite powerset

Start in to, stack is surpty, looking at the first inject significal

(1)

at each step the automaton may

(i) look at input symbol & top of stock and then

"Assignment Project Exam Helpe to next symbol

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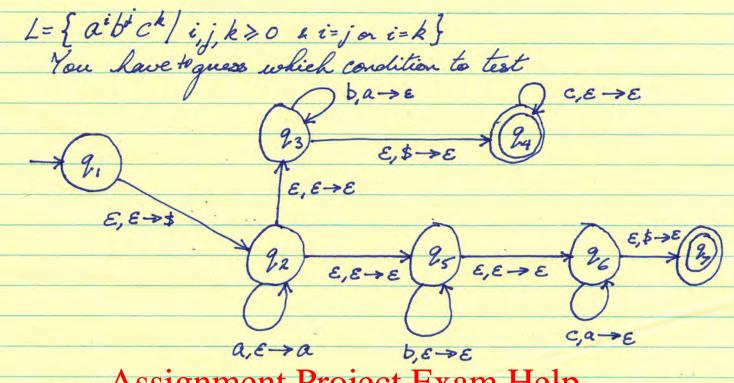
you see b on top of the stack & replace it with a Add WeChatpowcoderput

b may be &: just push c'onto stack

C may be E: just pop the stack

{0"1" /n> 0}

What happens if you see an unexpected symbol? The machine jame, this counts as reject. This happens for example if there are more 1's than O's. This machine is deterministic.



Informal stescription: puch is on the stack sefere your start reading. Then stack all the a's. Guess whether you should the stack of the property whether you should the stack of the property of the matching b's: this happens in 9 s. When all b's have been matched Wie Chat power of est symbol on the stack; jump to 93 and read any C's. These C's are ignored. The bottom branch corresponds to matching a's & C's. In 95 b's are just ignored. In 96 C's & a's are matched.

8 Some important general points:

(x) Acceptance only happens at the end of the simput.

If the PDA is in an accept state with input

Still left to read it cannot say "I will stop

here and accept"; it has to get to the end of the input

in order to accept.

(B) A PDA cannot decide to jane" when it has a possible move to make.

(r)	II I	Here o	sæ.	state	wil	the two	or	more	move	(3)	
	and	one	of t	tem	is	E.E -	3 <	it ca	u cho	ose to	do
	this	at	any	poi	t ee	oen it	one	ofthe	other	move	28
	is	bossi	ble.							* "	
	1								4		

het us look back at the example to explore some possibilities. It should be easy to trace an accepted string through the PDA with choices leading to acceptance. For example aabcc will work as follows:

	INVOT	STATE	STACK	
1	aabcc	2,	ε	
2	aa b.cc	9.2	\$	1
3	Assignmer Assignmen	nt Project E	exam He	elp
4	bcc	92	aa \$	(E, E -> E move)
5	6cchttps:/	/powcoder	.com &	(6,8 72 2000)
6	cc	25		$(\varepsilon, \varepsilon \rightarrow \varepsilon \text{ move})$
7		VeChat pov	vcoder	$(\epsilon, \epsilon \rightarrow \epsilon \text{ move})$
8	C	26	a\$	
9		26	. \$,
10		97		ACCEPT

What if it jumped from 92 to 95 after step 3? In

95 it has an E, E > E move possible lent the

b, E > E move is not possible because the current
input letter is a, not b. So it has to go to 96.

Now it is steck & it rejects. Suppose after line 3

it jumps to 93 & now it james. Suppose after line 2

it jumps to 93. Now input = aabcc, state=93, stack = \$.

The only move it can do takes it to 94 where it will

jum.

FUNDAMENTAL THEOREM

Every CFL is recognized by a PDA. Every language recognized by a PDA is a CFL.

I dea! To show that every CFL is accepted by a PDA

we use the stack to keep teach of partial derivations.

We use nondeterminism to guess which rule to use.

Every time we guess a rule use pop the non terminal

on top of the stack & push the RHS of the rule.

I dea 2 For every pair of States we withodows a new

nonferminal. We design a grammar to keep querate

all the strings that take you from the first state to

the Second State.

FACT The https://powcoder.com/a language & a CFL is always a CFL.

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FACT. In PDA:s nondeterminism cannot always be eliminated.

Deterministic PDA (DPDA): The transition function is

S: $Q \times Z_{\mathcal{E}} \times \Gamma_{\mathcal{E}} \rightarrow (Q \times \Gamma_{\mathcal{E}}) \cdot U \not =$ so we don't have a set of possibilities. Further
For every $q \in Q$, $a \in Z$, $x \in \Gamma$ exactly one of S(q, a, x), $S(q, a, \mathcal{E})$, $S(q, \mathcal{E}, x)$ & $S(q, \mathcal{E}, \mathcal{E})$ is non-empty.
Thus there is never any choice. Every the $\mathcal{E}, \mathcal{E} \rightarrow \mathcal{E}$ moves can only happen because there is no enabled action otherwise. The automaton an page 1 needs some dead states to make it a proper DPDA.

Here is the automator for $\{0^n1^n|n>0\}$ written as a DPDA. There were no transitions coming out of 24 before

(24) (2,4) (2,4) (3) (3) (4) 25 is a new dead state.

2 Assignment Project Exam Help
what happens if we try to process

2011? After matching the first 20's

2 the first https://powcoder.com IN PUT STATE STACK Add WeChat powcoder The only action possible is the E, \$ -> E move to 29 Now it has only I move, to 95 via 1, E > E

15

Here the string is rejected.

The PDA cannot stop in 94 & say "I accept"

A language is a DCFL if it is recognized by a DPDA Every DCFL has an unambiguous grammar best not every language with an unambiguous grammar is a DCFL. Mile can define acceptance by empty stack: if the stack is empty at the end of the input we accept. This is an alternate but equivalent notion of acceptance.

when there is input still to be read.