

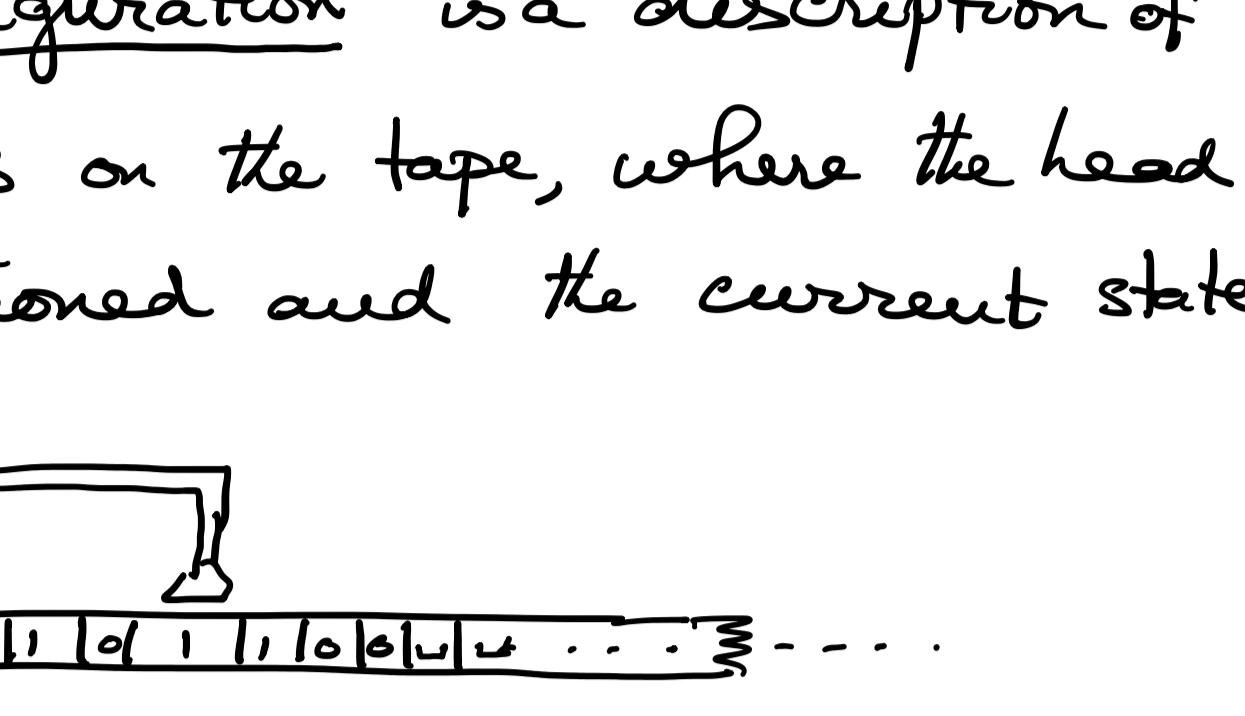
TURING MACHINE:

At each step there is a finite amount of "information processing".
q-tuple

$$M = (Q, \Sigma, \Gamma, \delta, s, a, r)$$

Q : finite set of states

A TM has a tape divided into cells



$\Sigma \rightarrow$ input alphabet

$\Gamma \rightarrow$ tape alphabet $\Sigma \subset \Gamma$

$\sqcup \rightarrow$ blank $\in \Gamma \setminus \Sigma$

$\vdash \rightarrow$ turnstile left end marker

$$\delta : Q \times \Gamma \rightarrow Q \times \Gamma \times \{L, R\}$$

$$\text{e.g. } \delta(q, a) = (q', b, L)$$

means read "a" in the tape cell where the head is positioned,

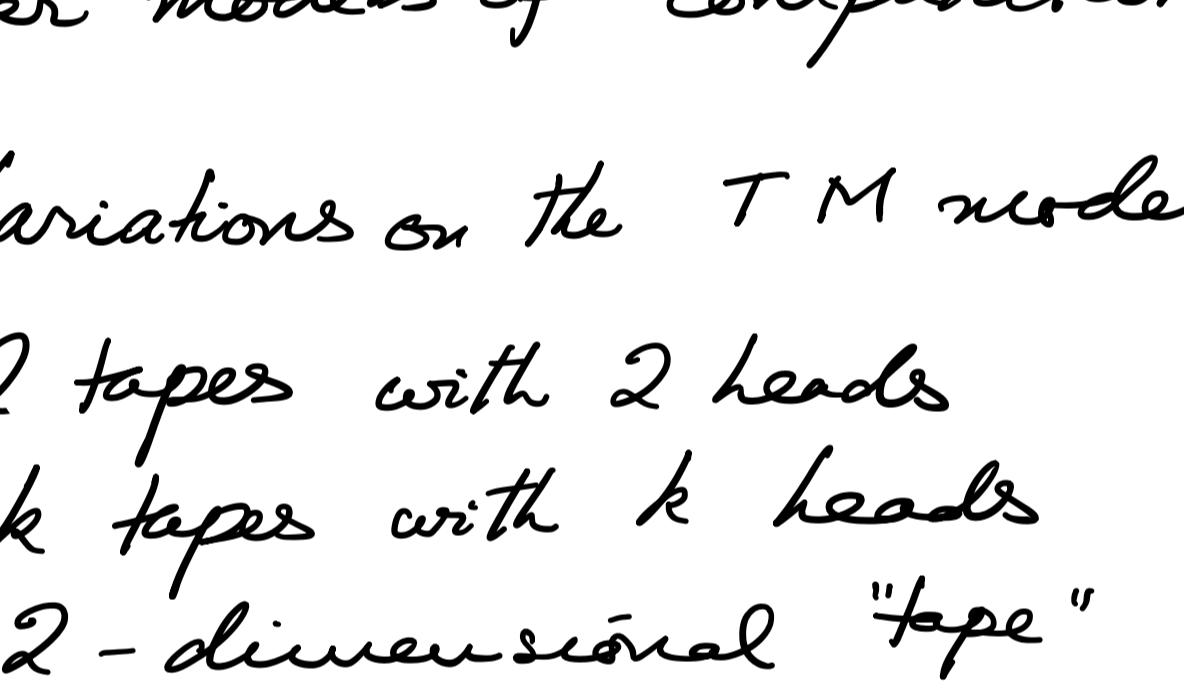
change state from q to q' , erase a and write b, then move one step to the left.

$s \in Q$ start state

$a \in Q$ accept state

$r \in Q$ reject state

A configuration is a description of what is on the tape, where the head is positioned and the current state.



This says it is looking at the symbol to its right.
Start : $s|1101100$

- always looks like this, obviously with different words.
- (1) it can reach ^{the} accept state and stop
 - (2) it can reach ^{the} reject state and stop
 - (3) it can loop forever.

M accepts w if there is a finite sequence of configurations C_1, C_2, \dots, C_k s.t.

1. C_1 is $s|w$
2. Each C_i yields C_{i+1}
3. C_k is an accept config $u|a|v \quad u, v \in \Gamma^*$

NEW PHENOMENON :

looping forever

$$L(M) = \{w \in \Sigma^* \mid M \text{ accepts } w\}$$

L is Turing recognizable if

\exists TM M such that

$$L = L(M)$$

If $w \notin L(M)$: it may be rejected or it may loop forever.

L is Turing decidable if \exists TM M s.t. $L(M) = L$

and $\forall w \in \Sigma^*$ M halts on w .

We say L is computably enumerable (CE) if $L = L(M)$

We say L is computable or decidable if $L = L(M)$ for some TM M and M always halts on every word.

KNOWN $P \not\subseteq \text{EXPTIME}$

KNOWN $PSPACE = NPSPACE$

RANDOM ACCESS MACHINE : RAM = TM (ASSEMBLY LANGUAGE)

WHILE PROGRAMS:

$x, y, z \dots$ variables
integer constants

arithmetic expressions $a_1 + a_2, a_1 \cdot a_2 \dots$

boolean expression

skip / if a then c_1 else c_2 / $x := a$ /

$c_1; c_2$ / while a do c

TURING COMPLETE:

Can simulate TM and can be simulated by TM

λ -CALCULUS = TM

\hookrightarrow core of functional programming

= POST PRODUCTION SYSTEMS

= PHRASE-STRUCTURE GRAMMARS

= MARKOV ALGORITHMS

= COMBINATORY LOGIC

= 2 STACK PDA

= 2 COUNTER MACHINES

DFA + 2 updatable integer vars.