Lecture 1 Introduction

Thursday, January 7, 2021 11:12 AM

Equivalence relations

A binary relation on a set X is a subset of XXX : eit is a set of pairs

[NOTATION: (a,b) ER as a Rb]

R must satisfy:

- (i) Reflexivity YXEX x Rx
- (ii) Mosignment Project Exam Help
- (iii) Transituity /x yze x x ky Ly kz > x kz https://powcoder.com

Eg n = mddhild Enat powcoder means remainder after dividing n by 7 and m by 7 is the same.

Partial order

"Thick bese than or aqual to"

A binary relation R is a partial order or X if:

(i) tx EX x Rx JANTISYMMETRY

xky 4y Kx ⇒ ~ - J (ii) /x, yeX

x Ry + y K3 → x Kg (iii) / x, y, z

e.g. numerical inequality

e.g.2 set inclusion

{ a, b, c}

≤ is a partial order {a,b3 ≤ {a,b,c}

{b, c} ≤ {a, b, c}

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It is not necessarily here that I E. g x Ry or y Rx.

If every pair of elements can be compared then we have a total order also called a livear order.

If we have a partial order < we say a < 6 if a & b AND a + 6.

in shirtly less thou b

BASIC FACTS:

Suppose X is a set and R is an equivalence selation $\forall x \in X \text{ we define}$ $[x] = \{y \in X \mid x R y\}$ Ly the againslence class of x.

1. If zky there [x] = [y] (why?)

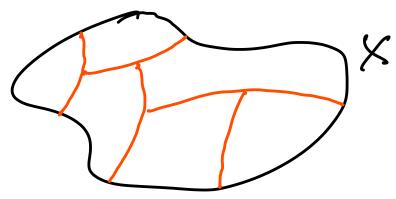
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2. If x, y \(X \) then with \[\infty] = [\infty]

OR https://powcoder.com (why?)

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The aquivalence classes divide

X into <u>disjount</u> "cluys".



THIS IS CALLED
A PARTITION

WELL- FOUNDED ORDERS

A partiel order & on Sis well formeded if every non-empty subset UCS has a minimal element.

Remark We song u & T is minimal if
there is nothing else in u stricty bee

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minimal elements

WHO CARES?

The non-negative integers are a well-formeded order with the usual numerical order

All the integers do not form a

Thue The principle of induction can be used if and only if the order is well founded.

AFTER CLASS QUESTIONS:

Ea,b,c}

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MANGER

AND SANDERS

{ {a,b,c3, {a,b3,{a}} => {a}

 $\{\{a,b\}, \{a,c\}, \{b\}\}\}$ MINIMAL.

 $\{a,b,c\}$ MINIMAL -> MEANINGLESS. $\{a,b,c\}$ \longrightarrow $\{a,b,c\}$ $\{a,b,c\}$ $\{a,b\}$, $\{a\}$, $\{a\}$, $\{a\}$, $\{a\}$ 1/7/2021 OneNote

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