Preduces to a

= If I can solve Q I can solve P

= Q is "harder Hau" P [P not harder Hau Q]

P & Q

Alg. solving P

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If Pis undecidable then Q must be undecidable.

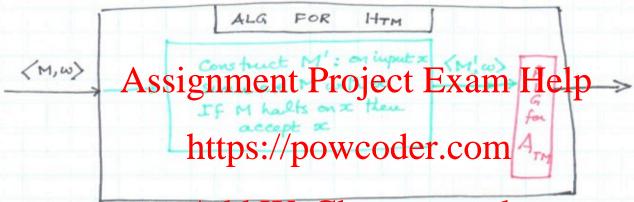
If Q is decidable then P is decidable. When proving P < Q I do not have to explain how to solve Q because it is a conditional statement.

$$H_{TM} = \{ \langle M, \omega \rangle | M \text{ halts on } \omega \}$$

$$A_{TM} = \{ \langle M, \omega \rangle | M \text{ accepts } \omega \}$$

We showed HTM is undecidable

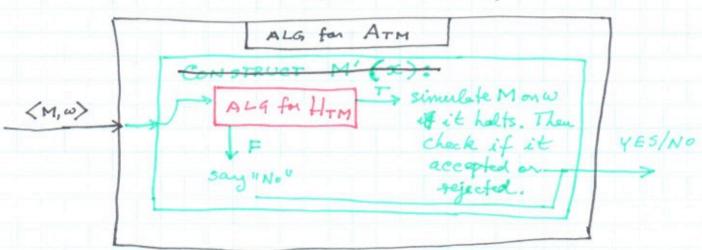
HTM & ATM



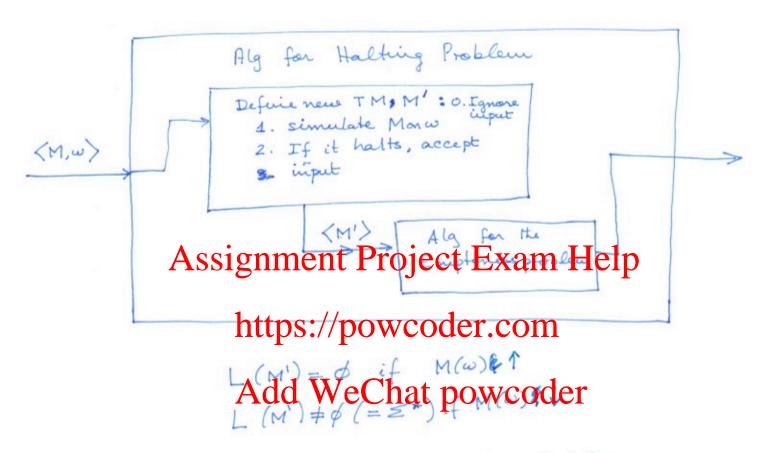
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We could have proved Arm is undecidable directly.

ATM < HTM

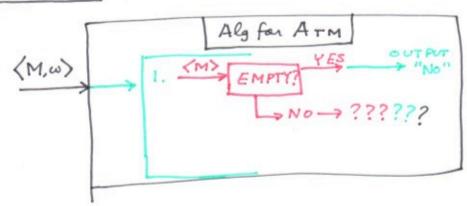


Halting Problem 
$$\leq$$
 Emptimes Problem  $E_{TM} = \{ \langle M \rangle \mid L(M) = \emptyset \}$ 

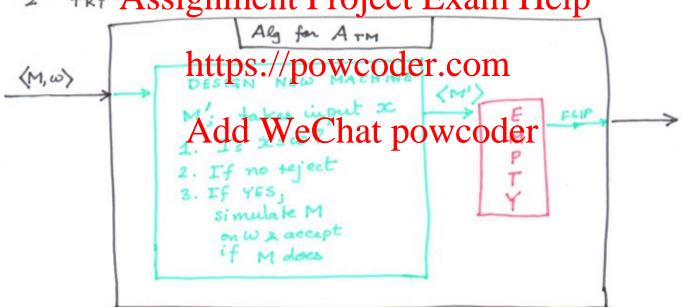


Halting problem is undecidable
Hence Emptiness problem is undecidable

## First TRY



<sup>2</sup> TRY Assignment Project Exam Help



If Macegt 
$$\omega$$
  $L(M) = \{ \omega \}$   
If M does not accept  $\omega$   
then  $L(M') = \emptyset$ 

Is L(M) a regular language?

UN DECIDABLE!

REG?

ATM & REG

(M,w)

ALG for ATM

\*\* Construct a new TM, M'(x)

\*\*Construct a new TM, M'(x)

\*\*

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 $L(M') = Z^*$  if Maccepts  $\omega$   $L(M') = \{a^nb^n | n \ge 0\}$  if M does not accept  $\omega$ 

$$L(M_1) = L(M_2)?$$

$$EQ_{TM} = \left\{ \langle M_1, M_2 \rangle \middle| L(M_1) = L(M_2) \right\}$$

$$EMPTY_{TM} \leq EQ_{TM}$$

ALG for EMPTY<sub>TM</sub>

1. Define TM M': or input x
reject immediately.

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- 1. L(M) = L(M') where M' always halts
- 2. L(M) is context-free
- 3. |L(M) & < 00
- 4. L(M) = 5\*



Sharper notion of reduction MAPPING REDUCTION

Suppose L1, L2 & E\*

L1 &m L2

if there is a TOTAL COMPUTABLE function

 $f: Z^* \longrightarrow Z^*$ 

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f https://poweoder.comeduction

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implies I,  $\leq_m \overline{L}_2$ 

(2)  $\leq m$  has a DIRECTION it is not the same as  $m \geq 1$   $\leq m \leq 1$   $\leq m \leq 1$  does NOT mean  $\leq 1$   $\leq m \leq 1$ 



- 1. If P≤m Q & P is undecidable then Q is undecidable
- 2. If P≤m Q & Q is decidable then
  P is decidable
- 3. If  $P \leq_m Q + Q$  is CE then P := CE
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  Reannot le co CE then

HTM, ATM are both CE lul not co CE.

The reductions we gave were mapping reductions.

CE

ATM is co RE but not CE.

ATM EMPTY

BUT

ATM EMPTYTM

if there were then

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& EMPTYM is CE.

 $\underline{Thm}$   $EQ_{TM}$  is not CE nor COCE  $\underline{PROOF} (1) We show \overline{A_{TM}} \leq_m \overline{EQ_{TM}}$ 

Thus EQTM is not CE so EQTM is not co CE.

(2) We show ATM ≤m EQTM

Thus EQTM is not co CE

80 EQTM is not CE.

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ConstructAdd WeChat powcoder accept

(b)  $M_2(x)$ : ignore input; run  $M(\stackrel{\omega}{\equiv})$  & if it accepts, accept x.  $L(M_1) = \sum^* L(M_2) = \begin{cases} \sum^* \text{ if } Maccepts \ \omega \end{cases}$ 

L(M1) = L(M2) ( Maccepts W

(2) Input (M, w)

M,: ignore input & reject

 $M_2$ : just as above  $L_4(M_1) = \emptyset$  so  $L(M_1) = L(M_2) \iff A$  does not accept  $\omega$ 

Given (M, w) we define a TM M' with input x Assignment Project Exam Help

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(This is OX because we are doing a controlled simulation)

If M does not halt on w then L (M') is infinite else finite so ⟨M,ω⟩∈ HTM ⟨⇒ ⟨M'⟩ ∈ INF