3/23/2021 OneNote

Reductions — I

Tuesday, March 23, 2021 11:18 AM

P, Q are problems

P seduces to Q

= If I can solve Q then
I can solve P

= Q is "harder than" P

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a is attps//petwardercomes P

→ If I cand/we chat powcoder I

know P is undecidable them. Q must be undecidable.

If I know Dis decidable then P

is also decidable

When proving PSQ I do

NOT have to explain how I propose

to solve Q: P < Q is a

KECALL: (M, w) means encoding of a TM Manda word w.

HTM = { (M, w) | M halts on wif

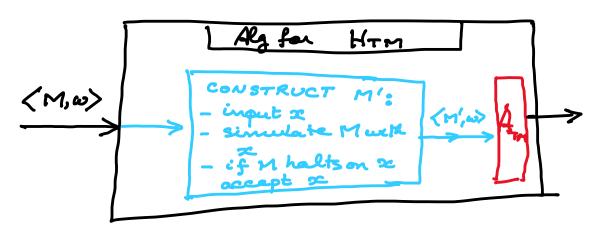
We showed membership in HTM is undecidable.

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Very https://powcoder.com also

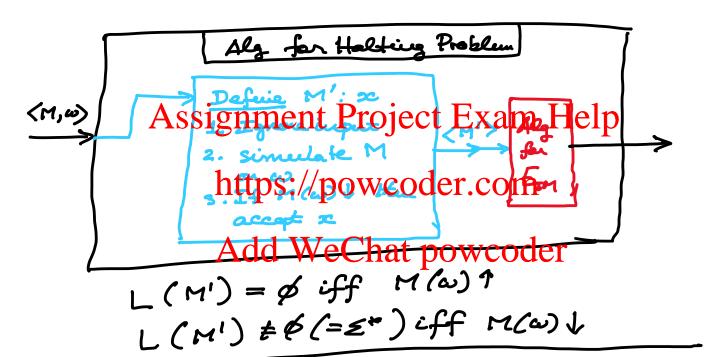
waste Weethat powcoder

We will prove Home ATM



If M(w) halts then M'(w) halts and accepts and muy Hetical algorithme for deciding ATM will be able to declect this. So we will know if M(w) halts or not.

Halting Problem \leq Emptiness Problem $E_{TM} = \{ \langle M \rangle | L(M) = \emptyset \}$



Is L (M) a regular language?

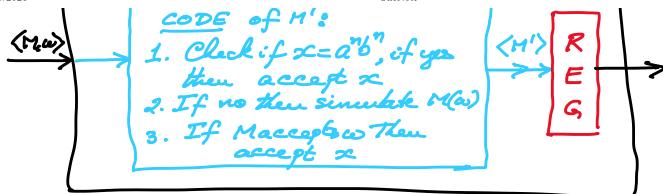
UN DECIDABLE PROBLEM

REG = { (M) | L (M) is regular}

ATM < REG

Alg for ATM

CONSTRUCT M', input &



$$L(M') = \sum_{i=1}^{n} if Maccept \omega$$

$$L(M') = \{a^{n}b^{n}/n \ge 0\} \text{ if M does}$$

$$not accept \omega$$

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 $EQ_{+n} = \{\langle M_1, M_2 \rangle | L(M_1) - L(M_2) \}$ https://powcoder.com

ETM = EMPTYTM & EQTM Add WeChat powcoder

ALG for ETM

1 Define M': on input = reject

2. -> < M, M'> > EQTM

if L(M)=& then L(M)=L(N')
if L(M) + b then L(M) + L(M')

The shiff in BLUE is always computable.

EXERCISES:

1 (M) - 1 (M) . of M- O. malalte

1. LUNG-LUNG Dave " and "

2. L(M) is context free

 $3. \left(L(M) \right) < \infty$

4. L(M) = 5*

MAPPING REDUCTION:

Suppose L1, L2 5 25"

 $L_1 \leq_m L_2$

if there is a TOTAL, COMPUTABLE

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such theteps://powcoder.com

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f is called a mapping reduction

NOTE (1) LI Sm L2 Thew I, Sm Is

(2) ≤ m has a définite direction

it is NOT the sauce as me.

The function of has a direction: from

L, 10 -2.

1. If $P \leq_m Q$ and P is undecidable

There is a surreum -

- 2. If P Sm Q and Q is decidable then P is decidable
- 3. If P SmQ and Dis CE Hen Pis CF
 - 4. If P Sm Q and Pis NOT CE Hun Q is not CE
- 5. If $P \leq_m Q$ and P is not coCEthen Q cannot be coCE.

 Assignment Project Exam Help CE: Lis CE if there is an algebrack

can https://powcoder.com= * and if
we can be with the bound of the continuate and
say "yes". But if w \$1, the alg

may never give au auswer.

coCE: Lie coCE if there is an alg.

which can be sun on every we E. .

If w & L the alg will eventually

krainak and say "no" but if wel

the alg may never give an answer.

ATM, Horm are co CE

LiacoCE (CE ATM S EMPTYTH BUT NOT ATM EMPTYTM

if there were such a reduction Sm EMPTYTH Hen Assignment Project Exam Help https://powcoder.com

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