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## Lecture 5

Thursday, January 21, 2021 11:17 AM

The algebra of regular expressions

LAWS of regular expression:

1. 
$$R + \phi = \phi + R = R$$

2. 
$$R + S = S + R$$

3. 
$$R + (S+T) = (R+S) + T$$

$$\mathcal{L} \quad \mathcal{R} \cdot \mathcal{E} = \mathcal{E} \cdot \mathcal{R} = \mathcal{R}$$

7. 
$$R \cdot (sh T + s \cdot /p \circ w) \cdot T \cdot T$$
  
8.  $R \cdot (s+T) = R \cdot s + R \cdot T$ 

R. R. 
$$(S+T) = R \cdot S + R \cdot T$$

BASIC PROOF PATTERN X=Y(=) X SY and Y SX.

then w = w, w = with w, e R & w 2 6 p. But there is no elevent of of so such a decomposition cannot exist & hence There is no word in R. & i.e R. \$=\$.

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(9)  $\omega \in R \cdot (S+T)$ i.e.  $\omega = \omega_1 \omega_2$  where  $\omega_1 \in R + \omega_2 \in S+T$ if  $\omega_2 \in S+T$  we have Z cases (a)  $\omega_2 \in S$  so then  $\omega_1 \omega_2 \in R \cdot S$ (b)  $\omega_2 \in T$  so then  $\omega_1 \omega_2 \in R \cdot T$ i.e.  $\omega_1 \omega_2 \in R \cdot S+R \cdot T$ never se similarly

other valid equations:

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w = ω, ··· Add We Chat powcoder what does it mean to say ω; e R\*?

 $\omega_i = \omega_i^{(i)} \omega_i^{(2)} \cdots \omega_i^{(k_i)}$  for some  $k_i \in \mathbb{N}$ .

where  $\omega_i^{(j)} \in \mathbb{R}$ 

 $\omega = \omega_1^{(1)} \cdots \omega_n^{(k_1)} \omega_2^{(1)} \cdots \omega_2^{(k_n)} \cdots \omega_n^{(k_n)}$ 

But this is just a sequence of words from Rice WER\*.

$$R^{**} \subseteq R^{*}$$

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elearly R= C'R so r self-ket exercise: Show  $(R^*S)^*R^* = (R+S)^*$ 

The point of algebra: to solve aquations! x = Sx + T

x: unknown S,T segular expressions.

We want to solve this for x.

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Then the sheeps://paweoder.com/ in fact
this is MACHENECSHAREDOWCODER

 $Sx + T = S(S^*T) + T$   $= SS^*T + \varepsilon \cdot T = (SS^* + \varepsilon) \cdot T$   $= S^*T = x$ 

 $5x+2=17 \Rightarrow x=3$   $5x+3=17 \Rightarrow x=?$  14/5=2%  $2x+7=3 \Rightarrow x=?-2$ regative neurobers. > ?? fractions (rational numbers) t/q

 $\alpha \times \beta = \gamma$   $\alpha, \beta, \gamma$  tationals

The aquation can be solved and
the solutions are tationals.

 $\alpha x^2 + \beta x + \gamma = 0$ 

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whatde We Chat powcodern example?

To is not rational!

You have to expand the concept of

neuber.

Algebraic numbers

Cubic equation: Tantaglia, Cardano, Scipia...
They solved cubic & biquadratic agus.
They came across /-/ !!

One has to expand the concept of number again! COMPLEX neurbers. How to solve the quintic (5th order)? NORWAY (died at age 26) Abel FRANCE ( died et age 22) Galois Fundamentel Kerren of nent Project Exam Help any polynomial aquation GARSS algobia of order n'withowcoder comefficients has Add Weetiat powcoder numbers

CLOSURE PROPERTIES of
REGULAR LANGUAGES

Suppose L,, L2 are regular languages:

(1) L; is also regular

(2) L; L2 is also regular

(3) L; UL2 is also regular

I will formalize the proof of 12) in forms of automate. Fix E as the alphabet  $M_1 = (S_1, S_1, S_1, S_1, F_1)$   $L(M_1) = L_1$   $M_2 = (S_1, S_2, S_2, F_2)$   $L(M_2) = L_2$  I want to define an NFA+E modes N S t  $L(N) = L_1 \cdot L_2$ .

 $N = (Q, Q, \Delta, F)$ Assignment Project Exam Help  $Q = S_1 \cup S_2 \cup S_1 \cap S_2 \cup F$ https://powcoder.com

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L is a regular language so is L. why?

LINL2 is also regular since L, ML2 = (L, UL2) But I want to show a direct Assignment Project Exam Help

M, = (S, s, E, F, ) L (M, ) = L, My = (https://powcoder.com) = L2 New Add We Chat powcoder )  $S = S_1 \times S_2 = \{(s,t) | se S_1 te S_2\}$ 8. 2 (81, 82) F = Fix F2  $\mathcal{E}((s,t),a) = (\mathcal{E}_1(s,a),\mathcal{E}_2(t,a))$ This mic keeps track of both sets of transitions.

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