

COMP 330 Winter 2021

Mid-term Examination Solutions

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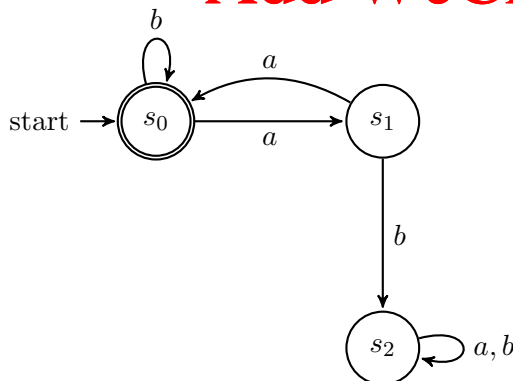
Question 1[40 points] In this question the alphabet is fixed as $\{a, b\}$.

- Write a regular expression for the language of strings containing a 's only when they occur as part of a block of consecutive a 's of *even length*. Thus the legal strings cannot contain an a by itself or a substring of 3 or 5 or 7... consecutive a 's. Thus $baabbb$ is accepted, so is $aabaabaaaabbaabbaa$ and so is $bbbbbbb$ which has no consecutive pair of a 's. However $baaab$ is not allowed as this has three consecutive a 's nor is $bababaab$ or $baaaab$.

Solution: $b^*(aa)^n b^*$. The a 's have to appear in pairs, but there can be any number (including 0) of b 's before the pair of a 's. This pattern can be repeated any number of times. Finally there could be a block of b 's at the end. There are other correct answers as well.

- Design a DFA (not an NFA) for this language. A picture is preferred. **You must show the dead state if there is one.** For full credit your machine must have 3 states including the dead state (if there is one).

Solution:



Question 2[40 points] Show, using the pumping lemma, that the following language is not regular. The alphabet is $\Sigma = \{a, b\}$. I prefer answers formatted as a game against the demon.

$$L = \{a^r b^t \mid r - t = 2, r, t > 0\}.$$

Solution:

The demon chooses some pumping length p . The angel chooses $a^{p+2}b^p$ as the string w . The demon has to choose x, y, z in such a way that the length of xy is less than p . This means that the string y has to be part of the initial block of a 's. The demon has no choice. So we have $y = a^k$ where $0 < k \leq p$. The angel chooses $i = 2$ so the new string is $xyyz = a^{p+2+k}b^p$. But the difference is now $p + 2 + k - p = 2 + k \neq 2$, so the pumped string is not in the language and so, the language cannot be regular.

Question 3[20 points]

Are the following statements true or false? No explanations are required. We have some fixed alphabet that we are working with.

1. If L is a non-regular language and R is a regular language then $L \cap R$ must be regular. **FALSE**
2. If L is a non-regular language and R is a regular language then $L \cap R$ cannot be regular. **FALSE**
3. For every regular language there is a unique minimal NFA. **FALSE**
4. When we run the minimization algorithm on a DFA we cannot be sure that it will always terminate. **FALSE**
5. If L_1 is an infinite regular language and L_2 is a finite language then the DFA to recognize L_1 must have more states than the DFA to recognize L_2 . **FALSE**

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