3/11/2021 OneNote

Introduction to computability

Thursday, March 11, 2021 11:16 AM

Diophantire aquation:

- give solutions in whole numbers

- give solutions in tational neumbers

 $x^{2}+y^{2}=1$ $3^{2}+4^{2}=5^{2}$ $5^{2}+12^{2}=13^{2}$

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 $3^2 - 2^3 = 1 \rightarrow \text{only solution}$

MECHANICAL PROCEDURE??
The concept of algorithm was not yet formulated.

Today:
An algorithm is a process for computing something using firite resources, with a precise notion of primitive step; each

step moderes a finite amount of information. SOMETIMES we require that the process halts (terminate).

1928 Hilbert & Ackerman asked for a mechanical procedence to determine if a formula of logic is valid or not.

VALID: True no matter home you interpret the variables.

VALID (Assignment Project Exam Help

ENTSCH(EDUNGSPROBLEME!

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Both these grobbens are impossible!

(USA) ALONZO Welhat pawcoder35 (UK) ALAN TURING 1936

Need a notion of algorithm:

KURT GÖDEL -> TOTAL RECURSIVE FUNCTIONS

ALONZO CHURCH - A-CALCULUS

ALAN TURING - TURING M/c

A.MARKOV, E.POST, S. KLEENE, B. ROSSER ...-

WE HAVE MANY EQUIVALENT SYSTEMS:

(1) Partial recursive f ns (KLEGNE)

(2) FLOW CHARTS

(3) "while " programs

- (4) ASSEMBLY LANGUAGE
- (5) RAM MACHINES
- (6) 2 STACK AUTOMATA
- (7) 2 COUNTER M/C
- (8) QUEVE N/C
- (9) 1000001 PROGRAMMING LANGUAGE
- (10) TURING MACHINES
- (11) \(\lambda CALCULUS\)
- (12) PHRASE STRUCTURG GRAMMAR

CHURCH - TURING THESIS

- (1) Algoritus can be expossed as a sagen of Assignment Project Exam Help
- (2) There is a universal machine.
- (3) There are unsolvable problems.

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ALONZO CHURCH - 1935

BASIC ASSUMPTIONS:

Every algorithm com be coded as a program and represented as a string.

P -> program # P -> source code

P-> program, x-singuts

P(x) - sun P with x as input

 $P(x,y) \rightarrow \cdots x,y,\cdots$

PL has while loops, up hen - esse and ;
What we want: $H(\cdot, \cdot)$ TRUE if P(x) halfs H(#P, x)> FALSE if P(x) loops

> always half.

CLAIM: SUCH AN H CANNOT EXIST! Assence we have such an H. De Assignment Project Exami Help S(#P): https://powcoder.com else halt Add WeChat poweoder S(#S): Does this halt? if H(#S,#\$) then loop else halt. so if S(#3) halts, H referre true, we go to the them branch & loop & if S(#S) loops, It returns false we go to the else branch & halt & such au H cannot exist!

```
EXAMPLE
      COL (n) = if n=1 then seterne 1
   else if nis even col (11/2)
     else col (3n+1)
     COL -> COLL ATZ
  col(11) → col(34) → col(12) → (52)
 → 26 → 13 → 40 → 20 → 10 → 5 → 16 →
  8-74->2->1 HALT
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 As YET UNKNEWN!

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 RECAP Diagonalization
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   The set of infinite sequences of
  positive integers is not counteble
    16 3 39 4 29 13 -- . .
```

The new lists differe in its nthe place from the not element of the nth list.

Hence it cannot be as the list!

The number of pairs of positive integre is countable.

(3,0) (1,28) (1,40) (1,40) (1,40) (2,41) (2,41) (2,41) (3,41) (3,2) (3,3) (3,4) (3,4) (4,1) (4,2) (4,3) (4,4) (4,4) (4,4)

(1,1) (2,1) (1,2) (3,1) (2,2) (1,3)-··
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