

FACULTY OF SCIENCE McGill University FINAL EXAMINATION for Winter 2021

COMPUTER SCIENCE COMP 330

Theory of Computing

Assignment Project Exam Help

Instructions: https://powcoder.com

This exam has 5 questions. Please answer all questions. The first 4 questions are each worth 15 points and the the last question is worth 40 points. This last question consists of 10 multiple choice questions. This is an **exam note**, yet also the the last questions are each worth 15 points and the last question consists of 10 multiple choice questions. This is an **exam note**, yet also the last question consists of 10 multiple choice questions. This is an **exam note**, yet also the cover pages and the questions appear starting on page 1 over 4 numbered pages. This title page and the cover pages before this one are not numbered.

Question 1 [15 points]

Classify the following language as either

- 1. regular or
- 2. context-free but not regular or
- 3. decidable but not context-free

You must prove your answer as explained below.

L consists of even length non-empty strings 1 over the alphabet $\{a,b\}$, so every word in L can be written as w_1w_2 with $|w_1| = |w_2|$ (i.e. w_1 and w_2 have the same length); we require that w_1 starts with a and w_2 starts with b. Here are some examples of words in L: aaabaa, abbb, aababbaa, ab.

If you think it is regular it is sufficient to give an NFA². If you think that it is context-free but not regular you have to give a PDA or CFG and a pumping lemma proof that it is not regular; you do not have to prove that your CFG or PDA is correct but the description should be clear. For the last case you need to give a pumping lemma proof that it is not context-free as well as an algorithm for Algorithm for Algorithm for the Project of Exam Help

Question 2 [15 points]

https://powcoder.com Suppose that I am given two regular languages R_1 and R_2 from the same fixed two-letter alphabet. Describe in outline how you would algorithmically test whether $R_1 \subseteq R_2$. You can assume that you are given explicit descriptions of DFA's to recognize the languages. You have to describe in outline the steps you gold take to answer the original Thy algorithm that to work without any special assumptions about the languages beyond the fact that they are regular. Your description should be high-level: for example, if you are going to say as some stage that you are testing whether an accept state is reachable from the start state you can just say that, you do **not** have to give the details of an algorithm to test reachability. Similarly if you want to say that you want to test something about R^* you need not give an explicit description of how you construct a DFA to recognize R^* . I am not suggesting that either of these steps is part of the required answer; they are just examples.

Question 3 [15 points]

One of the following sets is CE and the other is co-CE.

- 1. $\{M: |L(M)| < 330\},\$
- 2. $\{M: |L(M)| \ge 330\},\$

where M is a Turing machine description, L(M) means the language recognized by M and |L(M)|is the size of this language. Identify which set is CE and which is co-CE and qive proofs for both.

¹Anyone who asks whether ε is in the language will not be answered.

²I will not answer if you ask me whether a DFA is OK.

There is no credit for guessing, you must give the proofs. You can take it for granted that neither set is decidable.

Question 4 [15 points]

One of the following questions is decidable, the other is undecidable. For the decidable question give an outline of an algorithm to solve it. For the undecidable question give a short proof of undecidability by showing that it is equivalent to a question that we know to be undecidable. Here R is a regular language and L is a context-free language specified however you prefer and the question in each case is whether the indicated inclusion holds.

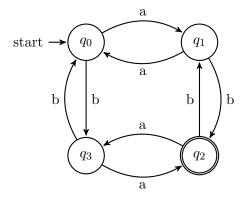
- \bullet $R \subseteq L$
- \bullet $L \subseteq R$

Question 5 [40 points]

Here are 10 multiple-choice questions; each question has 4 choices. In every case, exactly one statement is correct. You must indicate the correct answer. You are not required to give any reasons for your answer. Each question is worth 4 points. Please just write the letter corresponding to your choice safeguestion content place explanations an

- 1. The size of the smallest DFA to recognize a regular language R

 - (a) depends on the number of words in R.
 (b) depends on whether the employering conference of the composition of the number of words in R.
 - (c) depends on whether the language is infinite or not.
 - (d) None of the Ardd WeChat powcoder
- 2. Consider the DFA shown below.



This DFA accepts the language in which there are

- (a) an even number of a's and an odd number of b's
- (b) an odd number of a's an even number of b's
- (c) an odd number of a's and an odd number of b's

- (d) an even number of a's and an even number of b's
- 3. The regular expression for the language accepted by the automaton above is
 - (a) $((aa)^*(bb)^*)^*$.
 - (b) $(abba)^*(ba^*b)^*a^*$.
 - (c) it is not possible to write a regular expression for this language.
 - (d) It is possible to write a regular expression but our angelic professor would never make us do such an awful problem on the final. None of the answers given in (a), (b) or (c) are correct.
- 4. The intersection of two deterministic context-free languages
 - (a) can fail to be context free.
 - (b) must be context free but not necessarily deterministic.
 - (c) must be regular.
 - (d) can never be context free.

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- (a) must contain an infinite regular subset.
- (b) need not control power der.com
- (c) must never contain an infinite regular subset.
- (d) None of the above.

 6. If L_1 and L_2 are languages over the same appliable then C
 - (a) it is possible that $L_1 \cap L_2$ is context-free even though neither L_1 nor L_2 are context free.
 - (b) if $L_1 \cap L_2$ is context-free then at least one of them must be context free.
 - (c) if $L_1 \cap L_2$ is context-free then at least one of them must be regular and the other has to be context-free.
 - (d) if $L_1 \cap L_2$ is context-free then both L_1 and L_2 must be context free.
- 7. We are interested in the question of whether two Turing machines (TM for short) accept any words in common. In symbols: given TM descriptions $\langle M_1 \rangle$ and $\langle M_2 \rangle$ we want to answer the question $L(M_1) \cap L(M_2) = \emptyset$? This question is
 - (a) decidable (computable).
 - (b) undecidable but computably enumerable (CE).
 - (c) undecidable but **co**CE.
 - (d) neither CE nor coCE.

- 8. Consider the set $FOO = \{\langle M \rangle || L(M)| < \infty \}$. Here we are using our standard notation, $\langle M \rangle$ means the encoding of a Turing machine. The language FOO defines
 - (a) the set of Turing machine descriptions that accept only finitely many inputs
 - (b) the set of Turing machine decriptions that accept all their inputs.
 - (c) the set of Turing machine descriptions that accept infinitely many different inputs.
 - (d) the set of Turing machines that accept only their own description as input.
- 9. The validity problem for first-order logic (FOL) is the following: given a formula ϕ of FOL we want to know if this formula is true in all interpretations. This problem is
 - (a) decidable since we can always negate the formula and decide either ϕ or $\neg \phi$.
 - (b) undecidable but computably enumerable since we can search through all proofs for a proof of ϕ .
 - (c) not decidable or CE but it is co-CE since we can search for an interpretation that shows that it is not valid.
- $\underset{10.\ \text{The halting problem can be solved by}}{\text{ASSIgnment Project Exam Help}} Project = \sum_{i=1}^{(d)} Project = \sum_{i=1}^{$
- - (a) asking the Internet, which has the answer to all questions.
 - (b) guessing at http Sow Apo W Gode Fit Coladity greater than zero.
 - (c) using deep learning.
 - (d) There is no Agorttan two we held time problem coder