COMP3400 Assignment 2 Written

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Tail Recursion

Consider a function that takes the average of a list of numbers:

average Assignment Project Exam Help

average [1, 2, 3]

2.0

https://powcoder.com
This will be a partial function because average [] = undefined. Let us use a default value to avoid this and define

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Doing so makes this problem easier (though it will irritate the statisticians).

Question 1. [3 MARKS]

Define a *primitive recursive* of average:

p_average :: (Fractional a) => [a] -> a

Question 2. [3 MARKS]

Define a tail recursive helper function

 $h_average :: (Fractional a) => a -> a -> [a] -> a$

that finds the average of the list.

Question 3. [1 MARK]

Define average via a single call to h_average.

Question 4. [1 MARK]

Define an iteration invariant for h_average that proves the correctness of average.

Question 5. [5 MARKS]

Prove h_average satisfies your iteration invariant.

Question 6. [1 MARK]

State the bound value for h_average.

Question 7. [2 MARKS]

Prove your bound value is always non-negative and decreasing.

Question 8. [2 MARKS]

Define *two* distinct quick-checks for average that *both* use lists from Arbitrary [Float].

In particular, your quick-checks should be for lists of arbitrary length.

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Higher Order Functions NUPS://powcoder.com

Consider the higher-order function foo

Question 9. [3 MARKS]

Define takeWhile by equating it to a single invocation of foo.

Question 10. [3 MARKS]

Define map by equating it to a single invocation of foo.

Question 11. [3 MARKS]

Define iterate by equating it to a single invocation of foo.

Induction

Question 12. [8 MARKS]

Consider the following definitions for implementing addition on natural numbers.

```
data Nat = Zero | Succ Nat deriving Show

plus :: Nat -> Nat -> Nat

plus m Zero = m

plus m (Succ(n)) = plus (Succ m) n
```

Further consider this *embedding* which maps each Nat to a unique integer.

```
emb :: Nat -> Integer
emb Zero = 0
emb (Succ n) = 1 + emb n
```

Using ind Atiss rigenment Project Exam Help

```
emb $ plus m n = emb m + emb n
```

where + is the additt pried power oder.com

When justifying your steps use the line numbers on this page.

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Hint: Do induction over n while letting m be free.