Week 9

Assignment Project Exam Help 13: IVIONAUS

https://powcoder.com

University of the Fraser Valley

Dr. Russell Campbell

Russell.Campbell@ufv.ca

COMP 481: Functional and Logic Programming

Overview

- Intro to Monads
- Tightrope Walking Simulation (Pierre)
- Banana on a Wire
- <u>'do' Notation</u>
- Pierre Returns
- Assignment Project Exam Help
- The List Monad nttps://powcoder.com
- MonadPlus` and the `guard` Function
- A Kaight's West hat powcoder
- Monad Laws
 - Left Identity
 - Right Identity
 - Associativity
- More Simplifications

Assignment Project Exam Help

https://pdwddeedsm

Add WeChat powcoder

Bind `>>=`

We have worked with implementing applicatives for various types so that:

A spage movalues represent computations that may end up in failure

• `[ahttques/representalipossible computational results (nondeterministic)

Add WeChat powcoder

• `IO a` values represent computations with side effects

These can be facilitated with the special characters `>>=` as a binary operation between Monad values. This function is called bind.

Monads are a type class with similar behaviour as `Functors` and `Applicatives` to make functions work in context:

Monad

This time, we want: der.com

- Addake and hout value with some tontext 'm a'
- a function that expects no input context `a ->`
- but the function returns a result `m b` with context when applied on the input `m a`

Context of Maybe

Recall how we mapped with functors:

```
Ansignment Project Examples

Just "wisdom!"

https://powcoder.com
ghci> fmap (++"!") Nothing

Nothingld WeChat powcoder
```

 a value of `Nothing` as a result of such a mapping can be interpreted as a failure for some calculation

Context with Applicative

Applicative functors have the added context to the function as well:

```
ghci> Just (+3) <*> Just 3

Just 6
Assignment Project Exam Help

ghci> Nothing <*> Just "greed"
    https://powcoder.com
Nothing

    Add WeChat powcoder
ghci> Just (ord) <*> Nothing
Nothing
```

• if either of the operands is `Nothing` it is propagated to the result

Applicative <\$> and <*>

There was also the applicative style:

Assignment Project Exam Help ghci> max <\$> Just 3 <*> Just 6

Just https://powcoder.com

ghci Add We Chat Bowcoder ghci Max \\$> Just Bowcoder Nothing

Now the implementation of the `Monad` type class:

Monad Implementation

```
Alass Applicative ject Planah methor return :: a -> m a

https://powcoder.com

(>>=) :: m a -> (a -> m b) -> m b

Add WeChat powcoder

(>>) :: m a -> m b -> m b

x >> y = x >>= \_ -> y
```

return

- the `return` function is the same as `pure` as we saw it in the `Applicative` type class
- recently Haskell developers decided it would be a requirement to make any `Monad` also be a subclass of `Applicative`

Assignment Project Exam Help

- just a reminder that `return` is not like in other programming hanguages here it simply wraps a value within the context of `m`
- the A>>> preration has a default implementation that is rarely changed
- there also used to be a `fail` function, but that is no longer required to implement an instance of `Monad`

Maybe as a Monad

The `Maybe` type as an instance of `Monad`:

```
instance Monad Maybe where
    return x = Just x

Assignhingnt Projectorium Help
    Just x >>= f = f x
    https://powcoder.com
```

- if there is wothing input on the left-hand side of `>>=`, the expression evaluates also to `Nothing`
- otherwise, there is a nested value within `Just` and we can apply the function `f` to it
 - note that the result of `f` is in a context with a nested value that at least has the same type as `x`

Example Maybe Monad

Now we give `Maybe` a try as a monad:

```
ghci> return "WHAT" :: Maybe String
Assignment Project Exam Help

ghci> https://powcoder.com
ghci> Just 9 >>= (x -> return (x*10))

Just Add WeChat powcoder

ghci> Nothing >>= \x -> return (x*10)

Nothing
```

Assignment Project Exam Help

— Tightrope/WalkingeSimulation —

Add WeChat powcoder

Using Monads

We will demonstrate one of the advantages of monads:

- Assignment Project Exam Help change the behaviour of calculations in the way we desire
- context of a monad can participate in the computation
- we cannot decihibatthapplicances alone, since they only lift computations into the nested context

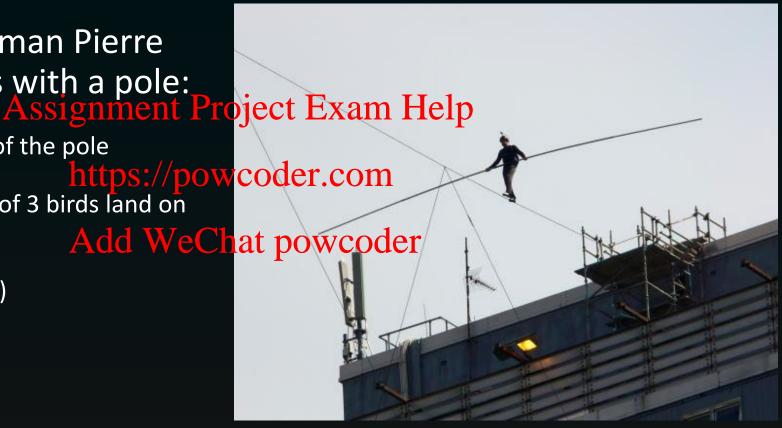
Tightrope Walking

Suppose we have a man Pierre that tightrope walks with a pole:

birds land on either side of the pole

• if more than a difference of 3 birds land on either side, Pierre falls...

(to a safety net, of course)



Photographer: Grant Gibson (CC BY 3.0)

Simulation of Birds

We will first implement a few types to help us keep track of the number of birds:

```
type Birds = Int
type Pole = (Birds, Birds)
```

Assignment Project Exam Help

Next we want functions to simulate birds land into members ideof the pole:

```
landLeftd: Weirdsat>protecod eple
landLeft n (left, right) = (left + n, right)
landRight :: Birds -> Pole -> Pole
landRight n (left, right) = (left, right + n)
```

Without Monads

We try out our functions without monads:

```
ghci> landLeft 2 (0, 0)

Assignment Project Exam Help

ghci landRight 1 (1, 2)

https://powcoder.com

(1,3)

ghci landRight Kat)p(1w2)der

(1,1)
```

just use a negative number to simulate birds flying away

Order of Operations

Chain simulated birds landing by nesting operations:

```
ghci> landLeft 2 (landRight 1 (landLeft 1 (0, 0)))
(3,1)
```

Assignmente a utility function to help us write more concisely:

```
https://powcoder.com
x -: f = f x

Add WeChat powcoder
```

• then we can write the parameter before the function, and rewrite our previous expression:

```
ghci> (0, 0) -: landLeft 1 -: landRight 1 -: landLeft 2
(3,1)
```

Maybe to Manage Failure (1)

So far, this does not check our condition for if Pierre will Adbignment Project Exam Help

• if wetdidsany topsicled tending of birds, then we just get back the ordered pair

Add WeChat powcoder

• instead, we would like to check for Pierre's failure, so we use `Maybe`

Maybe to Manage Failure (2)

Implement new versions of our bird-landing simulation functions:

Simulating Imbalance

- Our implementation will maintain a difference of three for the number of birds on either side of the pole
- if > 3, the result of any `landLeft` or `landRight` will be `Nothing` to indicate imbalance and represent falling
- Assignment Project Exam Help since these versions of our functions:
 - ·https://powgader.com
 - but a `Maybe Pole` for output,
 - Ave will heed to make use of our er
 - to apply successive operations together

```
ghci> return (0, 0) >>= landLeft 1 >>= landRight 1 >>= landLeft 2
Just (3,1)
```

```
return (0, 0) >>= landLeft 1 >>= landRight 1 >>= landLeft 2
```

- note that we had to begin the calculation with the context of a monad, so we used `return`
- the `return` function can be used no matter the specific application

 A of pmonad coptext for a sequence of palculations

Using >>=

https://powcoder.com Finally, iet's see Pierre fall!

Add WeChat powcoder

can you tell at which point the pole became imbalanced?

Know the Monad

Try to make sure you do not conflate the context of the Amongo with the functions are Help

- •hmqnad/ispyaybeandeyOtthefunctions `landLeft` and `landRight`
- the functions have merely been edited to take advantage of Maybe as a monad

Assignment Project Exam Help

https://powerode/Viran

Add WeChat powcoder

Banana Slip

We implement more functions that can combine with the other computations we have designed for simulation:

- suppose a banana on the wire could slip Pierre while walking
- this automatically forces Pierre to fall Assignment Project Exam Help

```
bananatips ?//powcdater.colen
banana _ = Nothing
Add WeChat powcoder
```

It is fairly clear what will happen when we use this function:

```
ghci> return (0, 0) >>= landLeft 1 >>= banana >>= landRight 1
Nothing
```

Changing Default >>

To ignore a monadic value on the *right* and *return the left* value, we can adjust the `>>` operation from its default:

```
(>>) :: (Monad m) => m a -> m b -> m a n >> m = m >>= \_ -> n
```

Assignment Project Exam Help Otherwise, the default is to ignore the left value and return the right value equivalent to the `do` block:

```
n m
```

for monad values n and m, the above returns m.

Carrying Monads Forward

```
ghci> Nothing >> Just 3
Nothing
ghci> Just 3 >> Just 4
Assignment Project Exam Help
ghcihelyst://powebder.com
Nothing
    Add WeChat powcoder
(keep in mind the above demonstrates the default implementation!)
```

Thus, we can omit having to write a 'banana' function,

and just use `>> Nothing` to the same effect.

Assignment Project Exam Help

https://powetatio.com

Add WeChat powcoder

>>= with Lambdas

We can use monad-style expressions with lambdas:

```
ghci> Just 3 >>= (\x -> Just (show x ++ "!"))
Just "3!"
```

- monadic value `Just 3` has its nested `3` passed as input into the lambda on the right side Assignment Project Exam Help
- a monadic value is returned `Just "3!"` https://powcoder.com

The above expression carche cewritten as two nested `>>=` operations:

```
ghci> Just 3 >>= (\x -> Just "!" >>= (\y -> Just (show x ++ y))) Just "3!"
```

Notice >>= "binds" an unwrapped value to the parameter.

Binding and Nesting

The expression can be rewritten as two nested `>>=`:

```
ghci> Just 3 >>= (\x -> Just "!" >>= (\y -> Just (show x ++ y)))
Just "3!"
```

Assignment Project Exam Help

Notice >>= "binds" an unwrapped value to the parameter.

• this ist smilar to the following. m

let Add WeChat powcoder

```
x = 3;

y = "!"

in show x ++ y
```

Helpful But Less Readable

The advantage of the more elaborate version:

- we get monads to help manage context
- at each part of the calculation
- without needing to explicitly write code at each stage to deal with it

```
AbsigNothing() Project Tusta": | Nelf() y -> Just (show x ++ y)))

Nothing

https://powcoder.com
ghci> Just 3 >>= (\x -> Nothing >>= (\y -> Just (show x ++ y)))

Nothingdd WeChat powcoder
ghci> Just 3 >>= (\x -> Just "!" >>= (\y -> Just Nothing))

Just Nothing
```

• at each point, the value could instead be `Nothing`, and the result is dealt with appropriately without error

Organized as a Function

We move toward a nicer syntax available, first, in the form of a function:

Assignment Project Exam Help https://powcoder.com let foo : A Maybe String at powcoder foo = Just 3 >>= (\x -> Just "!" >>= (\y -> Just (show x ++ y)

))

Maybe Context (1)

• there is an alternative cleaner syntax available with the 'do' block Assignment Project Exam Help

Maybe Context (2)

```
foo :: Maybe String
foo = do
    x <- Just 3
    y <- Just "!"
    Just (show x ++ y)</pre>
```

- the `do` block allows a different way to chain

 A sponadic caiculations into one monadic calculation
- if any of the monadic values is a `Nothing` then the result of the 'do' expression will be `Nothing`
- lines that we not manadic value have to be in a `let` expression
- we use `<-` assignment to obtain a nested value (bind)
 - if we have a Just "!" monadic value, the nested value is "!" as a `String` type
 - if we have a `Just 3` monadic value, the nested value is `3` as a numeric type
- the last line of a 'do' block cannot use '<-', since this would not make sense as the result returned for a monadic expression

Typical Do Block

The typical design:

Assignamputermiestignamed Halles

- https://piewethaer.block
- and return them in some combined expression Add WeChat powcoder within the monadic context

Equivalent Examples

One more small example:

```
ghci> Just 9 \Rightarrow (\x -> Just (x > 8))
Just True
Assignment Project Exam Help
let
marystaps://powsoder.com
marySue = do
    Add We Chat powcoder
    Just (x > 8)
ghci> marySue
Just True
```

Review (Simranjit Singh)

```
-- various types of addition
 -- infix (any func that's a special symbol is automatically infix)
1 + 2
-- prefix
Atsignment Project Exam Help
-- fuhttps://powcoder.com
fmap (+1) [1,2,3]
(+1) Add We Chat powcoder
 -- applicative functor
 [(+1)] <*> [1,2,3]
 [(+)] <*> [1] <*> [1,2,3]
 pure (+) <*> [1] <*> [1,2,3]
 (+) <$> [1] <*> [1,2,3]
```

Examples (Simranjit Singh)

```
-- monads
        [1] \rightarrow x \rightarrow x \rightarrow x + 1
        [1,2,3] \rightarrow x \rightarrow return (x+1)
Assignment Projecto Exam Help
       [1,2,3] >>= \xspace 
        -- alterrative cipatipe wcoder
        do
                                               x \leftarrow [1,2]
                                               y \leftarrow [3,4,5]
                                               return $x + y + 1
```

Assignment Project Exam Help

https?//proevRetlernsom

Add WeChat powcoder

Simulation with Do Block

We can rewrite our previous example of Pierre's tightrope walking with a simulation for birds landing on a pole.

We now design it in a 'do' block:

```
routine :: Maybe Pole

routine = do

Assignmente Purpiocto Exam Help

first <- landLeft 2 start

second <- landKight 2 first

landLeft 1 second
Add WeChat powcoder

ghci> routine

Just (3,2)
```

• each line of a 'do' block depends on the success of the previous one

Nested Cases

Without monads, this issue can be seen differently where computation would have to be *nested*:

```
routine :: Maybe Pole
routine = case Just (0, 0) of
Assignthingnt >PNothing Exam Help
    Just start -> case landLeft 2 start of
    https://prevs.odering.m

    Just first -> case landRight 2 first of
    Add WeChat powcoder
    Nothing -> Nothing
    Just second -> landLeft 1 second
```

• the ghci session will issue a warning with the above code, but you should still be able to issue `routine`

Nothing Overwrites Results

Then if we want to throw in a banana peel like we did before:

```
routine :: Maybe Pole

routine = do

Assignment Project Exam Help
first <- landleft 2 start

Nthis / powcoder.com
second <- landRight 2 first
Andleft acan powcoder
```

- the line with `Nothing` does not use `<-`, much like our use of `>>` to ignore a previous monadic value
 - this is nicer than needing to write equivalently `_ <- Nothing`

>>= VS Do

It is up to you whether you want to use `>>=` versus `do` blocks, but in general:

Assignment Project Exam Helpto avoid naming prior results, use `>>=`

- to mix together mutiple previous results, use 'do' blocks

Add WeChat powcoder

Neither is exclusively needed to accomplish the above...

Assignment Project Exam Help

— Patterns Matchingland Failure —

Add WeChat powcoder

Bind with Pattern Matching

Pattern matching can be used on a binding:

```
justH:: Maybe Char

Assignment Project Exam Help

(x:xs) <- Just "hello"

https://powcoder.com
return x
```

- Add WeChat powcoder
 the above grabs the first letter of the string "hello"
- the `justH` function evaluates to `Just h`
 - remember, the left value of a `:` operation is a `Char`, not a singleton

Failing a Pattern Match

When a pattern match fails within a function:

- the next pattern is attempted Assignment Project Exam Help
- if matching falls past all patterns, the function throws an error
 - ·https://powebeler.com

WeChat powcoder With let expressions, an error occurs on failure of matching because there is no falling mechanism for matching further patterns.

Implementing fail Function

When matches fail within a 'do' block:

- the context of the monad often implements a `fail` function
- to deal with the issue in its context
- as we have seen with the `Maybe` type
- this used to be implemented as part of a default `Monad` function
- it is now dealt with as an instance of the `Monad` type with a custom implementation of `fail` per each type Assignment Project Exam Help

For example Pwith Mayre Cara `Monad`, we can implement:

```
fail Adday Wee a hat May be wooder fail _ = Nothing
```

- but `fail` is a default function to throw an error with String message
- then when all patterns fall through unmatched within a `do` block, the function expression will evaluate to `Nothing` instead of crashing

Example of fail

```
wopwop :: Maybe Char
wopwop = do
    (x:xs) <- Just ""

Assignment Project Exam Help

ghcihtopwoppowcoder.com
Nothing
    Add WeChat powcoder</pre>
```

- there is only a failure mitigated within the context of monad `Maybe`
- there is no program-wide failure

Assignment Project Exam Help

https://pbistcManachm

Add WeChat powcoder

Lists as Monads

Recall that we can do nondeterministic calculations with lists using the applicative style:

```
ghci> (*) <$> [1,2,3] <*> [10, 100, 1000]
[10,100,1000,20,2000,30,300,3000]
```

Assignment Project Exam Help

Let us now see the implementation of `Monad` for lists: https://powcoder.com

```
instance Monad [] where

return We Chart powcoder
```

```
xs >>= f = concat (map f xs)
fail _ = []
```

• `return` just puts the input value within minimal list contex, i.e.: a singleton `[x]`

List Context

The function `concat` might seem not to fit the context, but we want to implement nondeterminism.

```
ghci> [3,4,5] >>= (x -> [x,-x]
[3,-3,4,-4,5,-5]
```

Assignment Project Exam Help

• as you can see, all the possible results of `[3,4,5]` fedinto s\x/p> [xo-x2] are shown as one conjoined list

```
The peration can handle []:
```

```
ghci> [] >>= \x -> ["bad", "sad"]
[]
ghci> [1,2,3] >>= \x -> []
[]
```

Chaining

It is possible to chain `>>=` operations to propagate the nondeterminism:

```
ghci> [1,2] \rightarrow (n \rightarrow ['a','b'] \rightarrow (ch \rightarrow return (n, ch))
Assignment Projecta Examblelp
```

- https://powcoder.com notice that the input variable 'n' shows up as part of the final expression after the next `>>=` operation Add WeChat powcoder
 - remember, each next `>>=` operation is nested as part of the previous one
- `return` places each pair within a singleton context
- all the pairs are concatenated together into one flat list

Using Chaining

Describing the propagation of nondeterministic operations:

- "for all" elements in `[1,2]` should be paired
- with every element of `['a', 'b']`.

[(1,'a'),(1,'b'),(2,'a'),(2,'b')]

Chaining in a 'do' Block

Otherwise, in a module, I would use a 'do' block:

```
listOfTuples :: [(Int, Char)]

listOfTuples = do

n <- [1,2]

Assignment Project Exam Help
return (n, ch)

https://powcoder.com

ghci> listOfTuples
[(1, Add(), Chat, pay, 22, der)]
```

- these syntax make the nondeterminism clearer to keep track of
 - `n` takes on every value of `[1,2]`
 - `ch` takes on every value of `['a','b']`

Similar to List Comprehension

Lastly, we had originally learned list comprehension to do essentially the same thing as above:

```
ghci> [ (n, ch) | n <- [1,2], ch <- ['a','b'] ]

Assignment Project Exam Help
```

https://powcoder.com

- the `<-` notation works pretty much the same, to handle the nondeterministic context focus er
- we did not need to use the `return` function because list comprehension takes care of that for us
- documentation typically calls alternatives such as this syntactic sugar for the more formally written expressions

Assignment Project Exam Help

— `MonadPitus: and the deuand` Function —

Add WeChat powcoder

Monad Filtering

List comprehension can apply filtering with a conditional expression:

```
ghci> [ x | x <- [1..50], '7' `elem` show x ]
[7,17,27,37,47]</pre>
```

Assignment Project Exam Help

The MonadPlus`type class is for implementing filtering.

•hitipfor/moracls that can also act as monoids

classAmoriation =>hmanadplus on where

```
mzero :: m a
mplus :: m a -> m a -> m a
```

- `mzero` is synonymous with `mempty` from `Monoid`
- `mplus` corresponds to `mappend`

We know lists are both monads as well as monoids, so:

MonadPlus

Anstantentalingest Therem Help

```
mzero = []
https://powcoder.com
mplus = (++)
```

Add WeChat powcoder

- a failed computation for lists is an empty list
- `mplus` concatenates two nondeterministic computational results

Filtering (1)

There is also a `guard` function that helps perform filters:

```
import Control.Monad

guard :: (MonadPlus m) => Bool -> m ()
guard True = pure ()
Assignment Project Exam Help
guard False = mzero

https://powcoder.com
```

- a Boolean expression is input into "guard" as the test to either create a dummy value or nothing ('mzero')
- empty tuple `pure ()` is used as a dummy and used to then filter
 - input into `>>` operations on the left side, it will either keep or throw away the right-hand side values

Filtering (2)

```
ghci> import Control.Monad
```

```
Absignmen(Project Exturn Hobj" :: [String]
["cool"]
    https://powcoder.com

ghci> guard (1 > 2) >> return "cool" :: [String]
Add WeChat powcoder
[]
```

Using **guard**

There are two ways we can write the use of `guard` in order to filter as in the list comprehension:

- the first is with nested `>>=` expressions
- the second is within a 'do' block

```
ghci> [1..50] >>= (\x -> guard ('7' `elem` show x) >> return x)

Assignment Project Exam Help
```

Examples (David Semke)

```
import Control.Monad
 -- Using list1, create all possible pairs (x, y)
     such that x is always greater than y
list1 = [1, 2, 3, 4, 5]
Aissignment Project Exam Help
   [(x, y) | x \leftarrow list1, y \leftarrow list1, x > y]
      https://powcoder.com
 nestedMethodPairs =
  listice (We)Chai 30 (WCG dard (x > y) >> return (x, y)))
 doMethodPairs = do
    x <- list1
    y <- list1
    guard(x > y)
    return (x, y)
```

Assignment Project Exam Help

http8://pightso@uestm

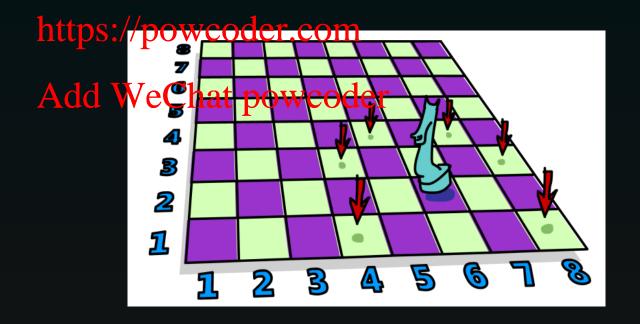
Add WeChat powcoder

Simulating Knights in Chess

We would like to simulate on a chess board, a knight which has a restricted `L` move each turn.

Are they able to reach a square within three turns?

- the image below shows the positions in one turn where a knight piece could choose to move
- it should be symmetrical, and there are two spots missing behind the ASSISHISTION, but the pieces carnot move off the board



Pairs for Positions

We use a pair to keep track of the row and the column

- the first number gives the row
- the second number gives the column

Assignment Project Exam Help

```
type KnightPos = (Int, Int)
https://powcoder.com
```

So, if the knight starts at position `(6, 2)`, can they move to `(6, 1)`?

- we might wonder which is the best move to choose toward the goal
- instead, we just let nondeterminism try all of the moves

moveKnight

```
moveKnight :: KnightPos -> [KnightPos]
 moveKnight(c, r) = do
     (c', r') <- [
             (c+2, r-1), (c+2, r+1), (c-2, r-1), (c-2, r+1),
             (c+1, r-2), (c+1, r+2), (c-1, r-2), (c-1, r+2)
Assignment Project Exam Help [1..8])
     return (c', r')
https://powcoder.com
 ghci> move Knight (6, 2) powcoder
 [(8,1),(8,3),(4,1),(4,3),(7,4),(5,4)]
 ghci> moveKnight (8, 1)
 [(6,2),(7,3)]
```

we can filter the new positions with use of `guard`

`in3` Possibilities Next, we can use this to write a concise function to move three times:

```
in3 :: KnightPos -> [KnightPos]

in3 start = do

Assignstent PovexnighExtant Help

second <- moveKnight first

https://povecoder.com
```

Add WeChat powcoder

Passing in `(6, 2)` generates a fairly long list:

```
ghci> in3 (6, 2) (results omitted for space)
```

Using `in3` Output

We could rewrite the `in3` function using `>>=` notation:

```
in3 start =
  return start >>= moveKnight >>= moveKnight >>= moveKnight
```

Assignment Project Exam Help the return puts start within the context of lists (or nondeterminism) https://powcoder.com

Finally we can test from bether of er2) is an element in the result:

```
ghci> (6, 2) `elem` in3 (6, 1)
True
ghci> (6, 2) `elem` in3 (7, 3)
False
```

Extending Chess Simulation

We could write the previous movement testing as a function and pass in the start and end positions.

- Assignment Project Exam Help (the next chapter shows how to modify the above as a function that can also give back the possible moves to take) https://powcoder.com
- we could also specify how many moves in general as input, not just three moves, specifically er

Assignment Project Exam Help

https://poweddev.scom

Add WeChat powcoder

Monad Laws

Each rule expects two equivalent expressions:

— Left Identity —

- return x >>= f
- f <u>x</u>

Assignment Project Exam Help

https://powced@ightmidentity —

- m >>= return Add WeChat powcoder
- n

Associativity

- (m >>= f) >>= g
- m \Rightarrow (\x -> f x \Rightarrow g)

Left Identity

- return x >>= f
- f x

Remember, that in the situation of monads, the function `f` will result in a value with context.

 note that `return` wraps with that context, and `>>=` removes context to pass the nested value to `f`

Assignment Project Exam Help

```
f :: Num a => a -> Maybe a f x https://pgeogrep.com
```

```
Add WeChat powcoder ghci> return 3 >>= f
```

```
ghci> f 3
Just 100003
```

Right Identity

- m >>= return
- m

Consider right side of first expression:

- function `return` takes a value and wraps it in a minimal context
- Assignment Project Exam Help
 - for lists, minimal context "does not introduce extra nondeterminism" https://powcoder.com

With Aists, Yay (floot feed (O.C.) into `return` with `>>=`:

- first, every element of the list gets wrapped, to get `[[1],[2],[3]]`
- the elements concatenate with `(++)` applied to result in `[1,2,3]`

Associativity

The order that operations executed in a sequence should not matter.

Assignment Project Exam Help

The functions `f` and `g` could be composed first

- but the notation for lambda expression is the legalting composed function,
- instead of something a bit more concise as in mathematics as with $(g \circ f)$ (yes, the order is correct with the above monad law)
- but notice Haskell syntax makes sense for order of execution when we are writing our code

Chaining and Associativity

Recall that we had simulated tightrope walking, and >>=" expressions as with the law of associativity:">chained ">>>=" expressions as with the law of associativity:" the law of associativity:"

```
pure (0, 0) >>= landRight 2 >>= landLeft 2 >>= landRight 2
Just (2,4)
```

Assignment Project Exam Help

- the use of `pure` we have used with `>>=` before
- it reads a bit nicer than using `return` at the start of a block of code

Add WeChat powcoder

The law of associativity allows us to drop parentheses, but with parentheses, we have:

```
((pure (0, 0) >>= landRight 2) >>= landLeft 2) >>= LandRight 2
Just (2,4)
```

But we can also write the expression as:

Multiline

```
:{

pure (0, 0)

AssignmentandRight Exam Help

>>= (\y -> landLeft 2 y

>>= https://pandKighter.com

)))

Add WeChat powcoder
:}

Just (2,4)
```

• each successive function is further nested in parentheses

Flipping with \<=<

At least the law of associativity allows us to be very concise and avoid excessive use of parentheses.

The following operation flips use of `>>=` for nesting functions that work with monads together.

```
Assignment Project Exam Heip-> m b) -> (a -> m c)
```

- https://powcoder.com
 the above is already defined in `Control.Monad`
- Attrelps establish associativity laws for Monads
 - the function `f` takes `b -> m c`
 - the function `g` takes `a -> m b`
- the problem is `g` outputs values of type the same as input for `f`, but monadic
- so `<=<` helps manage their composition

Associativity of `<=<`

Recall that the following are equivalent (associativity we should implement for `>>=`):

• m >>=
$$(\x -> f x >>= g)$$

Assignment Project Exam Help

Then it should also be that the following are equivalent: https://powcoder.com

- (f A dd g) & Chat powcoder
- f <=< (g <=< h)

Then we can also omit parentheses with chaining `<=<`.

But, you have to implement `>>=` properly!

Assignment Project Exam Help

-https://simplifications

More Simplifications

Translating left identity laws:

- `return x >>= f`
- * `f. x` Assignment Project Exam Help

For \there there eates say the following:

• `f <=< return`is the same as just `f` Add WeChat powcoder

So, for right identity, `return <=< f` is also the same as `f`.

Assignment Project Exam Help

— YortpW@ptaveoReneantot —

Helpful Resources

For knowing exactly what thing you are working with and its corresponding documentation (like, which package?):

:info <name_of_thing>

Assignment Project Exam Help

A great way to style your error handling: https://powcoder.com Gabriella Gonzalez (Google Blogger)

https://www.haskelfforalh.com/3021/05/the-trick-to-avoid-deeply-nested-error.html

Working with json style object initialization from files:

- grab the json.zip file from Blackboard
 - you will need to install the yaml package, but there are notes to help with the edits from the article

Names for Binary Operations

```
$
           (none, just as " " [whitespace])
                                                                 (others we have not covered)
           to
                    a -> b: a to b
->
                                                                 *>
                                                                            then
                                                                            (evaluates to right hand functor, unless left mempty)
                      a . b: "b pipe-to a"
           pipe to
                                                                 <$
                                                                            map-replace by 0 <$ f: "f map-replace by 0"
           (f)map
<$>
                                                                             ( e.g.: 3 < [2] evaluates to [3] )
                      (as it is the same as Sontrol Monadap) Project Examalternative expr < | > term: "expr or term"
<*>
           ap(ply)
                                                                            (import Control.Applicative)
           bind
>>=
                     (as it desugars to >>=) https://powcoder.com/(or irrefutable pattern)
           bind
<-
           then
>>
                                          Add WeChat powcoder
                                                                                       (use in signatures)
           index
                                                                                       (causes pattern matching errors even for )
           empty list
           cons
           lambda
                    go II@(I:Is): go II as I cons Is
@
           as
           of type / as
                       f x :: Int: f x of type Int
```

https://stackoverflow.com/questions/7746894/are-there-pronounceable-names-for-common-haskell-operators

Why Did We Learn Haskell?

Assignment Project Exam Help

https://crypto.sttpfo/pedu/dblym/haskell/why.html

Thank You!

Assignment Project Exam Help Questions?

https://powcoder.com%