#### Can you use a hashtable to implement skipTo()?

## Better than next()

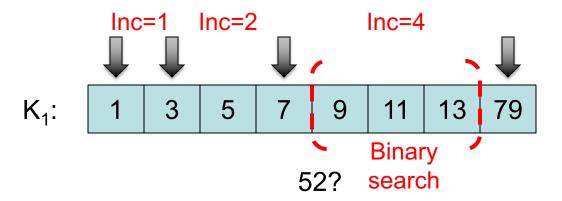
- What's the worst case for sequential merge-based intersection?
- {52, 1} Assignment Project Exam Help
  - To the position whose id is at least 52 → skipTo(52)
  - Essentially, asking the first i, such that K<sub>2</sub>[i] >= 52 (K2's list is sorted).
  - Add WeChat powcoder
     Takes many sequential call of next()
  - Could use binary search in the rest of the list
  - Cost: log<sub>2</sub>(N<sub>remainder</sub>)



K<sub>1</sub>: 52 54 56 58

## skipTo(id)

- Galloping search (gambler's strategy)
  - [Stage 1] Doubling the search range until you overshoot
- [Stage 2] Perform binary search in the last range Assignment Project Exam Help
   Performance analysis (worst case)
- - Let the destilation position dedepositions away.
  - ≈ log<sub>2</sub> n probes in Stage 1 + ≈ log<sub>2</sub> n probes in Stage 2
  - Total = 2 log Add 1 Me Chat powcoder



#### **Total Cost**

- Galloping search (gambler's strategy)
  - Cost of the i-th probe: ≈ 2 log<sub>2</sub>(n<sub>i</sub>)
  - Total costightemopesie 2 Pogan Intelpi)
- $\leq 2\log_2(\frac{((\sum_1^{|K_2|}n_i)/|K_1|)^{|K_1|}}{https://powcoder.com}) \leq 2|K_1|*\log_2(|K_2|/|K_1|)$  Asymptotically, resembles linear merge when
- Asymptotically, resembles linear merge wher |K<sub>2</sub>|/|K<sub>1</sub>| = O(1)| Weselmbles bindary search when |K<sub>1</sub>| = O(1)

# Multiple Term Conjunctive Queries

- K<sub>1</sub> AND K<sub>2</sub> AND ... AND K<sub>n</sub>
- SvS does not perform well if none of the associated thists percentage.
- In addition, attis well addition, attis and attis well as the second attis well as the second attis at the second attis attis at the second attis at the second attis at the second attis at the second attis attis at the second attis at the second attis at the second attis attis at the second attis attis attis at the second attis attis at the second attis attis attis attis attis at the second attis a
- Can you design non-blocking multiple sorted array intersection algorithm?

#### Generalization

- Generalize the 2-way intersection algorithmsignment Project Exam Help
- https://powcoder.com • 2-way:
  - $-\{1, 2\} \rightarrow \text{may exercise}^{K_2:}$
  - skipTo(2)
    - K<sub>3</sub>:
- 3-way:
  - $-\{1, 2, 3\} \rightarrow \text{move } k_1, k_2' \text{s cursor}$
  - -skipTo(3)

eliminator =  $Max_{1 < i < n}(k_i.cursor)$ 

3

4

9

6

27

2

3

### Optimization

- Mismatch found even before accessing K<sub>3</sub>'s cursor Assignment Project Exam Help 1 3
- Choice 1: continue to get correction of the cursors of other list Add WeChat powcoller K<sub>3</sub>:
   Choice 2: settle the
  - dispute within the first two lists → max algorithm [Culpepper & Moffat, 2010]
    - Better locality of access → fewer cache misses
    - Similar to SvS

6

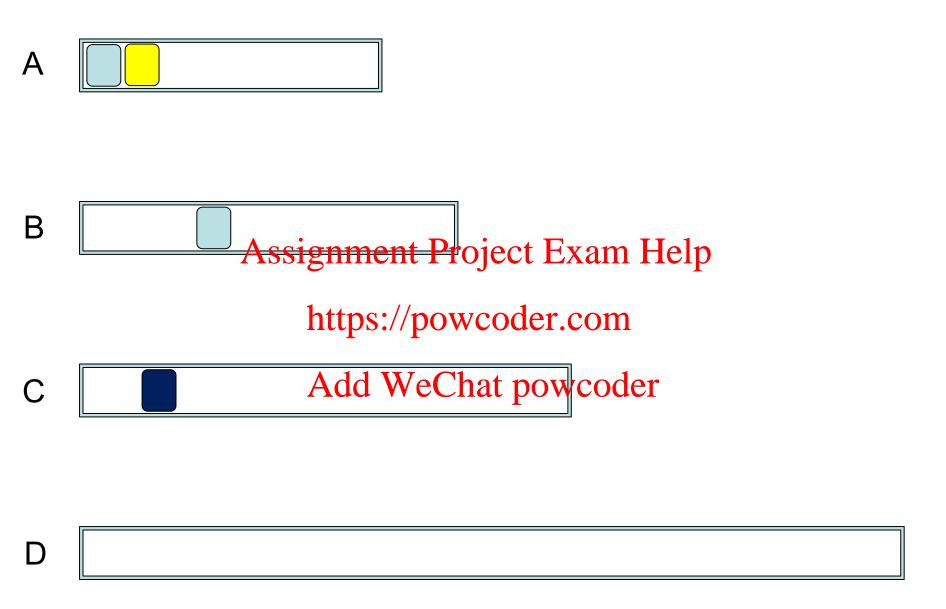
## Pseudo-Code for the Max Algorithm (Wrong)

```
Input: K<sub>1</sub>, K<sub>2</sub>, ..., K<sub>n</sub> in increasing size
       x := K_1[1]; startAt := 2
                                      //x is the eliminator
(1)
(2)
       while x is defined do
            for i = startAt to n do

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y := K<sub>i</sub> skiplo(x)
(3)
(4)
(5)
                      x := K_1.next()
(6)
                                           //restart_1
                                                                   //restart_2
                      if y > xAlbah Wacahat1powycotser startAt := 2 end if
(7)
(8)
                      break
                                        //match in all
                                                             lists
(9)
                 elsif i = n then
                                        //y = x
(10)
                      Output x
(11)
                      x := K_1.next()
(12)
                 end if
            end for
(13)
                                                                                        7
```

end while



The original code has a bug when in restart\_1 cases

#### Pseudo-Code for the Max Algorithm (Fixed)

```
Input: K<sub>1</sub>, K<sub>2</sub>, ..., K<sub>n</sub> in increasing size
                                      x := K_1[1]; startAt := 2
(1)
                                                                                                                                                                                                                                                  (4.1) if i = 1 then
(2)
                                      while x is defined do
                                                                                                                                                                                                                                                 (4.2) if y > x then
                                                             for i = startAt to n do

y := K_i.skipTo(x)
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y := K_i.skipTo(x)
break
(3)
(4)
                                                                                       if y > x then the state of th
(5)
                                                                                                                  x := K_1.next()
(6)
                                                                                                                                                                                                             (4.6) end if
                                                                                                                 if y > Aboth Wacahat1powgodserstartAt := 2 end if
(7)
(8)
                                                                                                                 break
(9)
                                                                                        elsif i = n then
(10)
                                                                                                                  Output x
(11)
                                                                                                                 x := K_1.next()
(12)
                                                                                        end if
(13)
                                                              end for
                                                                                                                                                                                                                                                                                                                                                                                                                                                        9
                                      end while
```

#### References

- J. Shane Culpepper, Alistair Moffat: Efficient set intersection for Projected sindexing. ACM Trans. Inf. Syst. 29(1): 1 (2010) https://powcoder.com
   F.K. Hwang and S. Lin, A simple algorithm for
- F.K. Hwang and S. Lin, A simple algorithm for merging two disjoint intermy offered sets.
   SIAM J. Comput. 1 1 (1972), pp. 31–39.
- Stefan Buettcher, Charles L. A. Clarke, Gordon V. Cormack, Information Retrieval: Implementing and Evaluating Search Engines, 2010 [Chapter 5]