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Introduction to Information Retrieval

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Lecture 5: Index Compression

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Last lecture – index construction

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- Sort-based indexing
 - Naïve in-memory inversion
 - Blocked Sort-Based Indexing
 - Merge sort is effective for disk-based sorting (avoid seeks!)
- Single-Pass In-Memory Indexing
 - No global dictionary
 - Generate separate dictionary for each block
 - Don't sort postings
 - Accumulate postings in postings lists as they occur
- Distributed indexing using MapReduce
- Dynamic indexing: Multiple indices, logarithmic merge

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Today

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BRUTUS	→	1	2	4	11	31	45	173	174
--------	---	---	---	---	----	----	----	-----	-----

CAESAR	→	1	2	4	5	6	16	57	132	...
--------	---	---	---	---	---	---	----	----	-----	-----

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CALPURNIA	→	2	31	54	101
-----------	---	---	----	----	-----

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- Collection statistics in more detail (with RCV1)
 - How big will the dictionary and postings be?
- Dictionary compression
- Postings compression

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Why compression (in general)?

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- Use less disk space
 - Saves a little money
- Keep more stuff in memory
 - Increases speed
- Increase speed of data transfer from disk to memory
 - [read compressed data | decompress] is faster than [read uncompressed data]
 - Premise: Decompression algorithms are fast
 - True of the decompression algorithms we use

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Why compression for inverted indexes?

- Dictionary
 - Make it small enough to keep in main memory
 - Make it so small that you can keep some postings lists in main memory too
- Postings file(s)
 - Reduce disk space needed
 - Decrease time needed to read postings lists from disk
 - Large search engines keep a significant part of the postings in memory.
 - Compression lets you keep more in memory
- We will devise various IR-specific compression schemes

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Recall Reuters RCV1

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■ symbol	statistic	value
■ N	documents	800,000
■ L	avg. # tokens per doc	200
■ M	terms (= word types)	~400,000
■	avg. # bytes per token (incl. spaces/punct.)	6
■	avg. # bytes per token (without spaces/punct.)	4.5
■	avg. # bytes per term	7.5
■	non-positional postings	100,000,000

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Index parameters vs. what we index

(details IIR Table 5.1, p.80)

size of	word types (terms)			non-positional postings			positional postings		
	dictionary			non-positional index			positional index		
	Size (K)	$\Delta\%$	cumul %	Size (K)	$\Delta\%$	cumul %	Size (K)	$\Delta\%$	cumul %
Unfiltered	484			109,971			197,879		
No numbers	474	-2	-2	100,680	-8	-8	179,158	-9	-9
Case folding	392	-17	-19	96,969	-3	-12	179,158	0	-9
30 stopwords	391	-0	-19	83,390	-14	-24	121,858	-31	-38
150 stopwords	391	-0	-19	67,002	-30	-39	94,517	-47	-52
stemming	322	-17	-33	63,812	-4	-42	94,517	0	-52

Exercise: give intuitions for all the '0' entries. Why do some zero entries correspond to big deltas in other columns?

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Lossless vs. lossy compression

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- Lossless compression: All information is preserved.
 - What we mostly do in IR.
- Lossy compression: Discard some information
- Several of the preprocessing steps can be viewed as lossy compression: case folding, stop words, stemming, number elimination.
- Chap/Lecture 7: Prune postings entries that are unlikely to turn up in the top k list for any query.
 - Almost no loss quality for top k list.

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Vocabulary vs. collection size

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- How big is the term vocabulary?
 - That is, how many distinct words are there?
- Can we assume an upper bound?
 - Not really: At least $70^{20} \sim 10^{37}$ different words of length 20
- In practice, the vocabulary will keep growing with the collection size
 - Especially with Unicode ☺

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Vocabulary vs. collection size

- Heaps' law: $M = kT^b$
- M is the size of the vocabulary, T is the number of tokens in the collection
- Typical values: $30 \leq k \leq 100$ and $b \approx 0.5$
- In a log-log plot of vocabulary size M vs. T , Heaps' law predicts a line with slope about $\frac{1}{2}$
 - It is the simplest possible relationship between the two in log-log space
 - An empirical finding ("empirical law")

Heaps' Law

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Fig 5.1 p81
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For RCV1, the dashed line

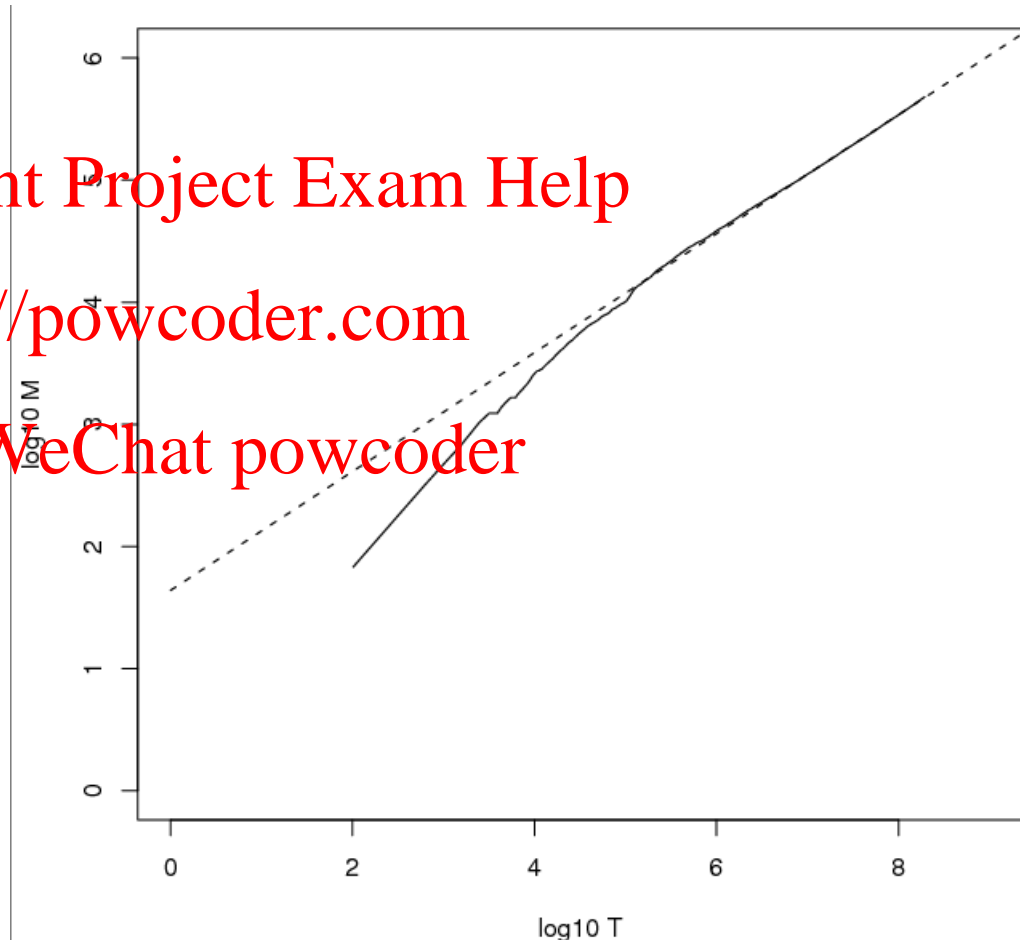
$$\log_{10} M = 0.49 \log_{10} T + 1.64$$

is the best least squares fit.

Thus, $M = 10^{1.64} T^{0.49}$ so $k = 10^{1.64} \approx 44$ and $b = 0.49$.

Good empirical fit for Reuters RCV1 !

For first 1,000,020 tokens,
law predicts 38,323 terms;
actually, 38,365 terms



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- What is the effect of including spelling errors, vs. automatically correcting spelling errors on Heaps' law?

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- Compute the vocabulary size M for this scenario:
 - Looking at a collection of web pages, you find that there are 3000 different terms in the first 10,000 tokens and 30,000 different terms in the first 1,000,000 tokens.
 - Assume a search engine indexes a total of 20,000,000,000 (2×10^{10}) pages, containing 200 tokens on average
 - What is the size of the vocabulary of the indexed collection as predicted by Heaps' law?

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Zipf's law

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- Heaps' law gives the vocabulary size in collections.
- We also study the relative frequencies of terms.
- In natural language, there are a few very frequent terms and very many very rare terms.
- Zipf's law: The i th most frequent term has frequency proportional to $1/i$.
- $cf_i \propto 1/i = K/i$ where K is a normalizing constant
- cf_i is collection frequency: the number of occurrences of the term t_i in the collection.

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Zipf consequences

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- If the most frequent term (*the*) occurs cf_1 times
 - then the second most frequent term (*of*) occurs $cf_1/2$ times
 - the third most frequent term (*and*) occurs $cf_1/3$ times ...
- Equivalent: $cf_i = K/i$ where K is a normalizing factor, so
 - $\log cf_i = \log K - \log i$
 - Linear relationship between $\log cf_i$ and $\log i$
- Another power law relationship

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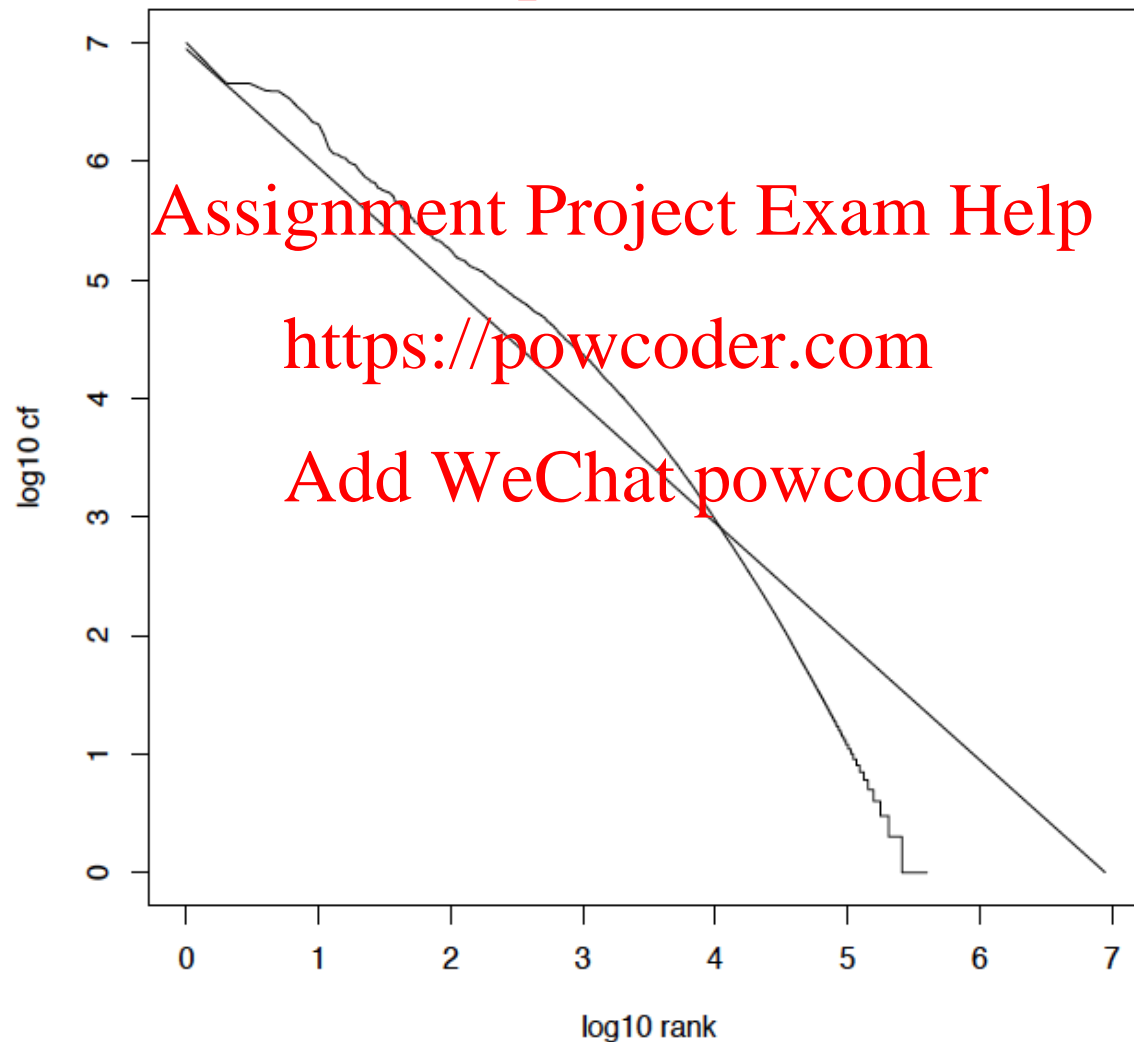
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Zipf's law for Reuters RCV1

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Assignment Project Exam Help Compression

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- Now, we will consider compressing the space for the dictionary and postings

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- Basic Boolean index only
- No study of positional indexes, etc.
- We will consider compression schemes

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DICTIONARY COMPRESSION

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Why compress the dictionary?

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- Search begins with the dictionary
- We want to keep it in memory
- Memory footprint competition with other applications <https://powcoder.com>
- Embedded/mobile devices may have very little memory
- Even if the dictionary isn't in memory, we want it to be small for a fast search startup time
- So, compressing the dictionary is important

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Dictionary storage - first cut

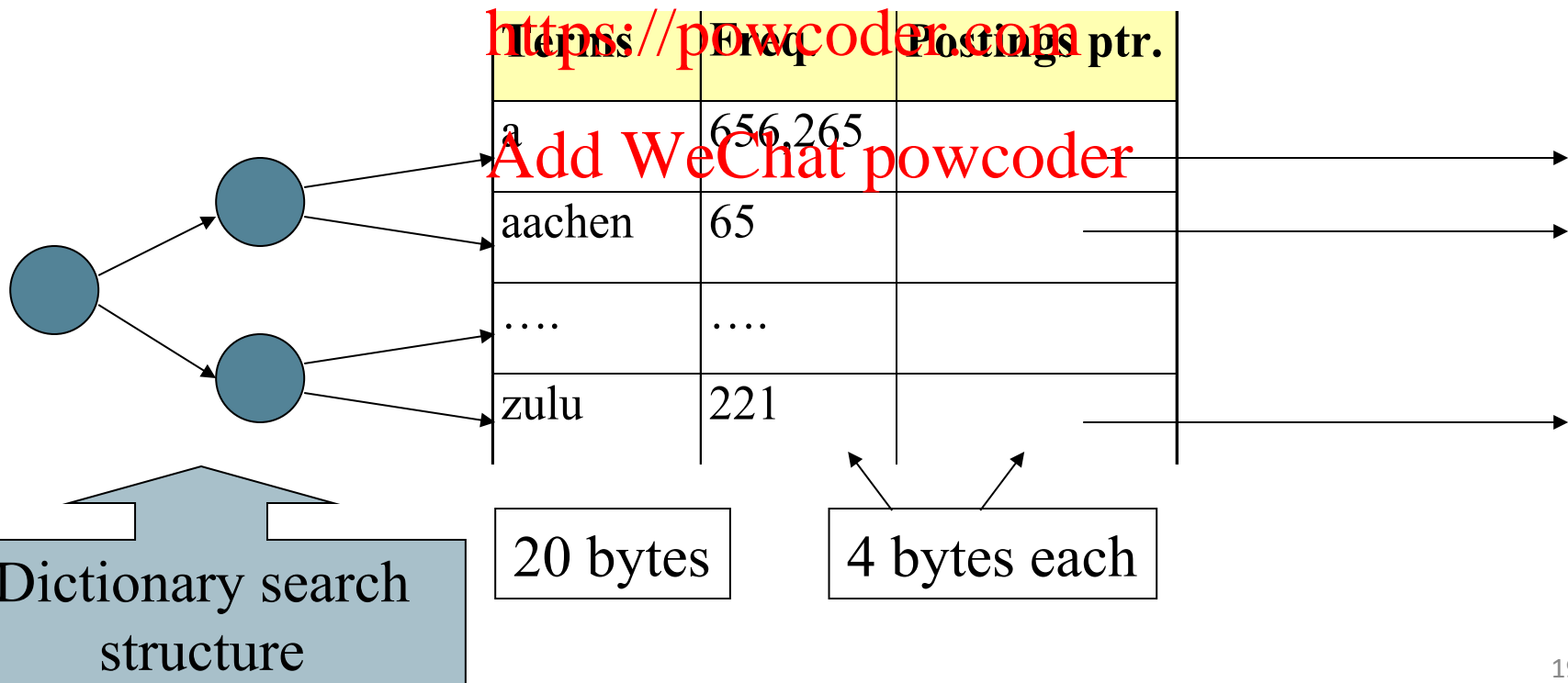
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- Array of fixed-width entries
 - ~400,000 terms; 28 bytes/term = 11.2 MB.

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Fixed-width terms are wasteful

- Most of the bytes in the **Term** column are wasted – we allot 20 bytes for 1 letter terms.
 - And we still can't handle *superfragilisticexpalidocious* or *hydrochlorofluorocarbons*.
- Written English averages ~4.5 characters/word.
 - Exercise: Why isn't this the number to use for estimating the dictionary size?
- Ave. dictionary word in English: ~8 characters
 - How do we use ~8 characters per dictionary term?
- Short words dominate token counts but not type average.

Compressing the term list:

Dictionary-as-a-String

- Store dictionary as a (long) string of characters:
 - Pointer to next word shows end of current word
 - Hope to save up to 60% of dictionary space.

....systilesyzygeticsyzygialsyzygyszaibelyiteszczecinszomo....

Freq.	Postings ptr.	Term ptr.
33		
29		
44		
126		

Total string length =
400K x 8B = 3.2MB

Pointers resolve 3.2M
positions: $\log_2 3.2M =$
22bits = 3bytes

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Assignment Project Exam Help Space for dictionary as a string

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- 4 bytes per term for Freq.
 - 4 bytes per term for pointer to Postings.
 - 3 bytes per term pointer
- Now avg. 11 bytes/term, not 20.
- Avg. 8 bytes per term in term string
 - 400K terms x 19 → 7.6MB (against 11.2MB for fixed width)

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Blocking

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- Store pointers to every k th term string.
 - Example below: $k=4$.
- Need to store term lengths (1 extra byte)

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....7systile9syzygetic8syzygial6syzygy11szaibelyite8szczecin9szomo....

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Freq.	Postings ptr.	Term ptr.
33		
29		
44		
126		
7		

Save 9 bytes
on 3
pointers.

Lose 4 bytes on
term lengths.

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- Example for block size $k = 4$
- Where we used 3 bytes/pointer without blocking
 - $3 \times 4 = 12$ bytes,

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now we use $3 + 4 = 7$ bytes.

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Shaved another ~ 0.5 MB. This reduces the size of the dictionary from 7.6 MB to 7.1 MB.

We can save more with larger k .

Why not go with larger k ?

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Exercise

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- Estimate the space usage (and savings compared to 7.6 MB) with blocking, for block sizes of $k = 4, 8$ and 16.

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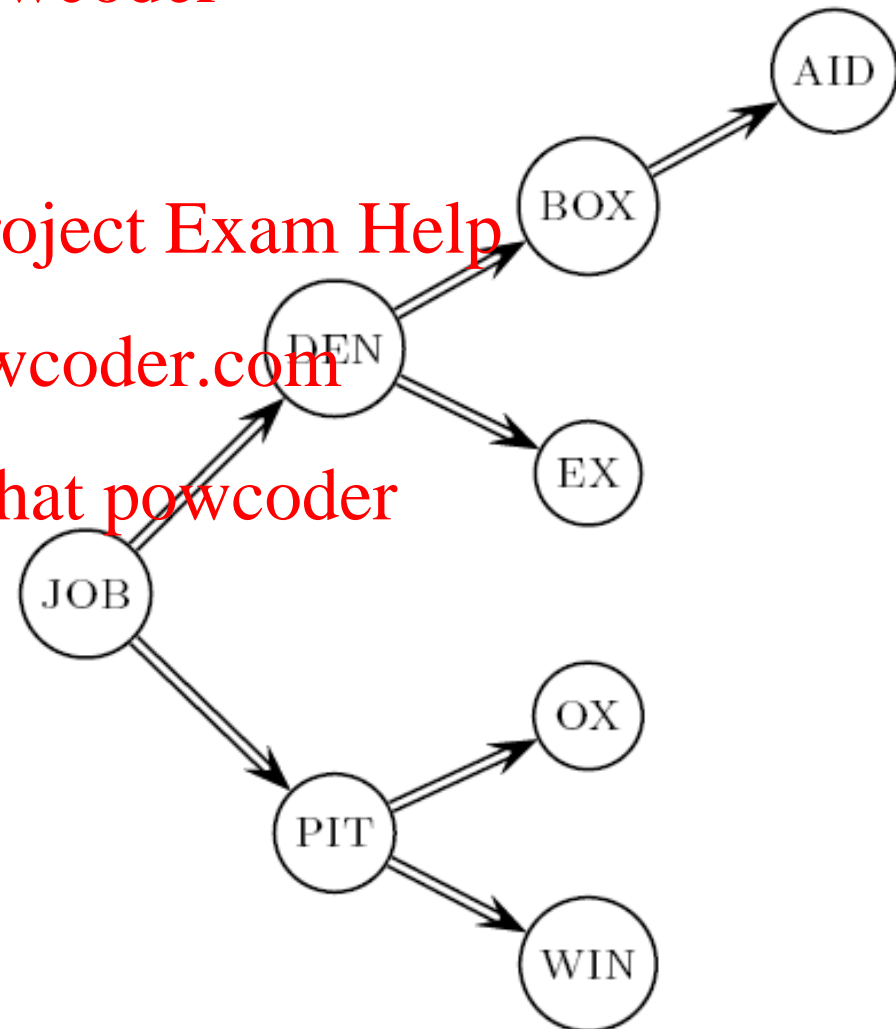
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Dictionary search without blocking

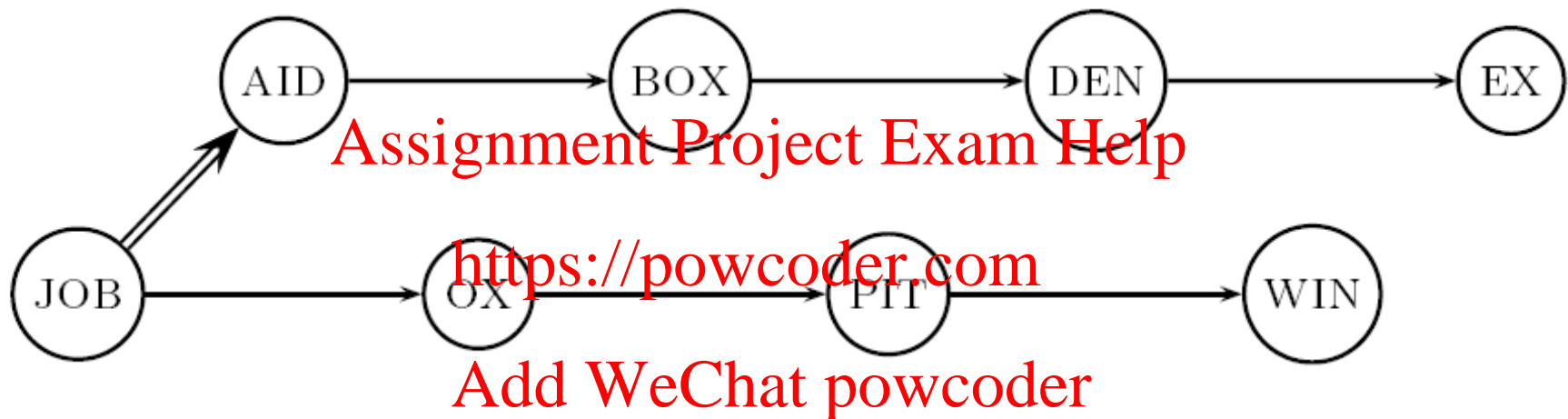
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- Assuming each dictionary term equally likely in query (not really so in practice!), average number of comparisons = $(1+2 \cdot 2+4 \cdot 3+4)/8 \sim 2.6$

Exercise: what if the frequencies of query terms were non-uniform but known, how would you structure the dictionary search tree?



Dictionary search with blocking



- Binary search down to 4-term block;
 - Then linear search through terms in block.
- Blocks of 4 (binary tree), avg. =
 $(1+2 \cdot 2+2 \cdot 3+2 \cdot 4+5)/8 = 3$ compares

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Exercise

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- Estimate the impact on search performance (and slowdown compared to $k=1$) with blocking, for block sizes of $k = 4, 8$ and 16 .

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Front coding

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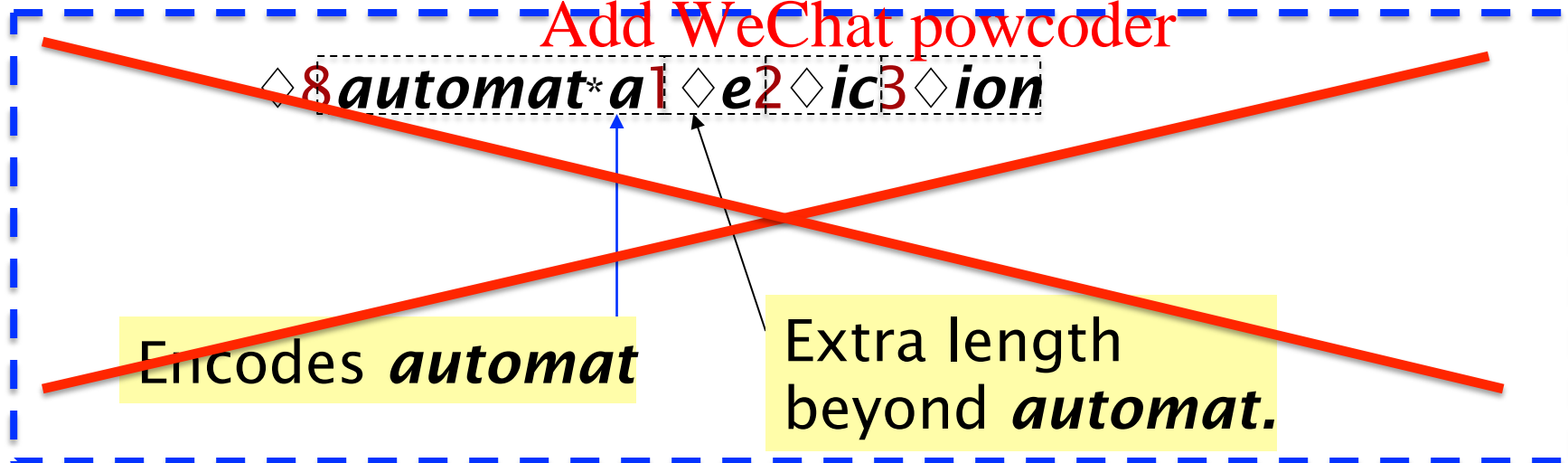
- Front-coding:
 - Sorted words commonly have long common prefix – store differences only
 - (for last $k-1$ in a block of k)

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8automata8automate9automatic10automation

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Begins to resemble general string compression. 29

Front Encoding [Witten, Moffat, Bell]

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- Complete front encoding
 - (prefix-len, suffix-len, suffix)
- Partial 3-in-4 front encoding
 - No encoding/compression for the first string in a block
 - Enables binary search

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Assume
previous
string is
“auto”



String	Complete Front Encoding	Partial 3-in-4 Front Encoding
8, automata	4, 4, mata	, 8, automata
8, automate	7, 1, e	7, 1, e
9, automatic	7, 2, ic	7, 2, ic
10, automation	8, 2, on	8, , on

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RCV1 dictionary compression summary

Technique	Size in MB
Fixed width	11.2
Dictionary-as-String with pointers to every term	7.6
Also, blocking $k = 4$	7.1
Also, Blocking + front coding	5.9

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POSTINGS COMPRESSION

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- The postings file is much larger than the dictionary, factor of at least 10.
- Key desideratum: store each posting compactly.
- A posting for our purposes is a docID.
- For Reuters (800,000 documents), we would use 32 bits per docID when using 4-byte integers.
- Alternatively, we can use $\log_2 800,000 \approx 20$ bits per docID.
- Our goal: use a lot less than 20 bits per docID.

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Postings: two conflicting forces

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- A term like **arachnocentric** occurs in maybe one doc out of a million – we would like to store this posting using $\log_2 1M \approx 20$ bits.
- A term like **the** occurs in virtually every doc, so 20 bits/posting is too expensive.
 - Prefer 0/1 bitmap vector in this case

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Assignment Project Exam Help Postings file entry

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- We store the list of docs containing a term in increasing order of docID.
 - **computer**: 33,47,154,159,202 ...
- Consequence: it suffices to store gaps.
 - 33,14,107,5,43 ...
- Hope: most gaps can be encoded/stored with far fewer than 20 bits.

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Three postings entries

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	encoding	posting list					
THE	docIDs	...	283042	283043	283044	283045	...
	gaps		1	1	1		...
COMPUTER	docIDs	...	283047	283154	283159	283202	...
	gaps		107	5	43		...
ARACHNOCENTRIC	docIDs	252000	500100				
	gaps	252000	248100				

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Variable length encoding

- Aim:
 - For *arachnocentric*, we will use ~ 20 bits/gap entry.
 - For *the*, we will use ~ 1 bit/gap entry.
- If the average gap for a term is G , we want to use $\sim \log_2 G$ bits/gap entry.
- Key challenge: encode every integer (gap) with about as few bits as needed for that integer.
- This requires a *variable length encoding*
- Variable length codes achieve this by using short codes for small numbers

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Variable Byte (VB) codes

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- For a gap value G , we want to use close to the fewest bytes needed to hold $\log_2 G$ bits
- Begin with one byte to store G and dedicate 1 bit in it to be a continuation bit
- If $G \leq 127$, binary-encode it in the 7 available bits and set $c = 1$
- Else encode G 's lower-order 7 bits and then use additional bytes to encode the higher order bits using the same algorithm
- At the end set the continuation bit of the last byte to 1 ($c = 1$) – and for the other bytes $c = 0$.

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Hex(824)=0x0338

Hex(214577)=0x00034631

Example

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docIDs	824	829	215406
gaps		5	214577
VB code	00001101 10111000	00001101	00001101 00001100 10110001

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Postings stored as the byte concatenation

000001101011100010000101000011010000110010110001

Key property: VB-encoded postings are uniquely prefix-decodable.

For a small gap (5), VB uses a whole byte.

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Other variable unit codes

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- Instead of bytes, we can also use a different “unit of alignment”: 32 bits (words), 16 bits, 4 bits (nibbles).
- Variable byte alignment wastes space if you have many small gaps – nibbles do better in such cases.
- Variable byte codes:
 - Used by many commercial/research systems
 - Good low-tech blend of variable-length coding and sensitivity to computer memory alignment matches (vs. bit-level codes, which we look at next).
- There is also recent work on word-aligned codes that pack a variable number of gaps into one word (e.g., simple9)

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Simple9

- Encodes as many gaps as possible in one DWORD
- 4 bit selector + 28 bit data bits
 - Encodes 9 possible ways to “use” the data bits

Selector	# of gaps encoded	Len of each gap encoded	Wasted bits
0000	28	1	0
0001	14	2	0
0010	9	3	1
0011	7	4	0
0100	5	5	3
0101	4	7	0
0110	3	9	1
0111	2	14	0
1000	1	28	0

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Unary code

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- Represent n as n 1s with a final 0.
- Unary code for 3 is 1110.

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- Unary code for 40 is

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- Unary code for 80 is: **Add W**

or Add WeChat powcoder

111

110

- This doesn't look promising, but....

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Bit-Aligned Codes

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- Breaks between encoded numbers can occur after any bit position
- *Unary code*
 - Encode k by k 1s followed by 0
 - 0 at end makes code unambiguous

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Number	Code
0	0
1	10
2	110
3	1110
4	11110
5	111110

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Unary and Binary Codes

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- Unary is very efficient for small numbers such as 0 and 1, but quickly becomes very expensive
 - 1023 can be represented in 10 binary bits, but requires 1024 bits in unary
- Binary is more efficient for large numbers, but it may be ambiguous

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Elias-γ Code

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- To encode a number k , compute

- $k_d = \lfloor \log_2 k \rfloor$ unary

- $k_r = k - 2^{\lfloor \log_2 k \rfloor}$ binary

- k_d is number of binary digits, encoded in unary

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Number (k)	k_d	k_r	Code
1	0	0	0
2	1	0	10 0
3	1	1	10 1
6	2	2	110 10
15	3	7	1110 111
16	4	0	11110 0000
255	7	127	11111110 1111111
1023	9	511	1111111110 111111111

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Elias- δ Code

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- Elias- γ code uses no more bits than unary, many fewer for $k > 2$
 - 1023 takes 19 bits instead of 1024 bits using unary
- In general, takes $2\lfloor \log_2 k \rfloor + 1$ bits
- To improve coding of large numbers, use Elias- δ code
 - Instead of encoding k_d in unary, we encode $k_d + 1$ using Elias- γ
 - Takes approximately $2 \log_2 \log_2 k + \log_2 k$ bits

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Elias-δ Code

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- Split $(k_d + 1)$ into:

$$k_{dd} = \lfloor \log_2(k_d + 1) \rfloor$$

$$k_{dr} = (k_d + 1) - 2^{\lfloor \log_2(k_d + 1) \rfloor}$$

- encode k_{dd} in unary, k_r in binary, and k_r in binary

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Number (k)	k_d	k_r	k_{dd}	k_{dr}	Code
1	0	0	0	0	0
2	1	0	1	0	10 0 0
3	1	1	1	0	10 0 1
6	2	2	1	1	10 1 10
15	3	7	2	0	110 00 111
16	4	0	2	1	110 01 0000
255	7	127	3	0	1110 000 1111111
1023	9	511	3	2	1110 010 111111111

```
#
# Generating Elias-gamma and Elias-delta codes in Python
#
```

```
import math
```

```
def unary_encode(n):
    return "1" * n + "0"
```

```
def binary_encode(n, width):
    r = ""
    for i in range(0,width):
        if ((1<<i) & n) > 0:
            r = "1" + r
        else:
            r = "0" + r
    return r
```

```
def gamma_encode(n):
    logn = int(math.log(n,2))
    return unary_encode( logn ) + " " + binary_encode(n, logn)
```

```
def delta_encode(n):
    logn = int(math.log(n,2))
    if n == 1:
        return "0"
    else:
        loglog = int(math.log(logn+1,2))
        residual = logn+1 - int(math.pow(2, loglog))
        return unary_encode( loglog ) + " " + binary_encode( residual, loglog ) + " " + binary_encode(n, logn)
```

```
if __name__ == "__main__":
    for n in [1,2,3, 6, 15,16,255,1023]:
        logn = int(math.log(n,2))
        loglogn = int(math.log(logn+1,2))
        print n, "d_r", logn
        print n, "d_dd", loglogn
        print n, "d_dr", logn + 1 - int(math.pow(2,loglogn))
        print n, "delta", delta_encode(n)
        #print n, "gamma", gamma_encode(n)
        #print n, "binary", binary_encode(n)
```

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Assignment Project Exam Help Gamma code properties

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- G is encoded using $2 \lfloor \log G \rfloor + 1$ bits
 - Length of offset is $\lfloor \log G \rfloor$ bits
 - Length of length is $\lfloor \log G \rfloor + 1$ bits
- All gamma codes have an odd number of bits
- Almost within a factor of 2 of best possible, $\log_2 G$
- Gamma code is uniquely prefix-decodable, like VB
- Gamma code can be used for any distribution
- Gamma code is parameter-free

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Gamma seldom used in practice

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- Machines have word boundaries – 8, 16, 32, 64 bits
 - Operations that cross word boundaries are slower
- Compressing and manipulating at the granularity of bits can be slow
- Variable byte encoding is aligned and thus potentially more efficient
- Regardless of efficiency, variable byte is conceptually simpler at little additional space cost

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Shannon Limit

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- Is it possible to derive codes that are optimal (under certain assumptions)?
- What is the optimal average code length for a code that encodes each integer (gap lengths) independently?
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- Lower bounds on average code length: Shannon entropy
 - $H(X) = - \sum_{x=1}^n \Pr[X=x] \log \Pr[X=x]$
- Asymptotically optimal codes (finite alphabets): arithmetic coding, Huffman codes

How to design an optimal code for geometric distribution?

Global Bernoulli Model

- Assumption: term occurrence are Bernoulli events
- Notation:
 - n : # of documents, m : # of terms in vocabulary
 - N : total # of (unique) occurrences
- Probability of a term t_i occurring in document d_i : $p = N/nm$
- Each term-document occurrence is an independent event
- Probability of a gap of length x is given by the geometric distribution $\Pr[X = x] = (1 - p)^{x-1} \cdot p$

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It can also be deemed as a generalization of the unary code.

Golomb Code

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- Golomb Code (Golomb 1966): highly efficient way to design optimal Huffman-style code for geometric distribution

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- Parameter b

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- For given $x \geq 1$, compute integer quotient

$$q = \lfloor (x-1)/b \rfloor$$

- and remainder

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$$r = (x-1) - q \cdot b$$

- Assume $b = 2^k$

- Encode q in unary, followed by r coded in binary

- A bit complicated if $b \neq 2^k$. See wikipedia.

- First step: $(q+1)$ bits

- Second step: $\log(b)$ bits

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Golomb Code & Rice Code

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- How to determine optimal b^* ?
- Select minimal b such that

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$$(1-p)^b + (1-p)^{b+1} \leq 1$$

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- Result due to Gallager and Van Voorhis 1975:
generates an optimal prefix code for geometric
distribution

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- Small p approximation:

$$b^* \approx \ln 2 / p = 0.69 \cdot \text{avg_val}$$

- Rice code: only allow $b = 2^k$

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Local Bernoulli Model

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- If length of posting lists is known, then a Bernoulli model on each individual inverted list can be used
- Frequent words are coded with smaller b , infrequent words with larger b
- Term frequency need to be encoded (use gamma-code)
- Local Bernoulli outperforms global Bernoulli model in practice (method of practice!)

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RCV1 compression

Data structure	Size in MB
dictionary, fixed-width	11.2
dictionary, term pointers into string	7.6
with blocking, $k = 4$	7.1
with blocking & front coding	5.9
collection (text, xml markup etc)	3,600.0
collection (text)	960.0
Term-doc incidence matrix	40,000.0
postings, uncompressed (32-bit words)	400.0
postings, uncompressed (20 bits)	250.0
postings, variable byte encoded	116.0
postings, g-encoded	101.0

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Google's Indexing Choice

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- Index shards partition by doc, multiple replicates
- Disk-resident index
 - Use outer parts of the disk
 - Use different compression methods for different fields: Rice_k (a special kind of Golomb code) for gaps, and Gamma for positions.
- In-memory index
 - All positions; No docid
 - Keep track of document boundaries
 - Group-variant encoding
 - Fast to decode

Source: [Jeff Dean's WSDM 2009 Keynote](#)

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Assignment Project Exam Help Other details

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- $\text{Gap} = \text{docid}_n - \text{docid}_{n-1} - 1$

- $\text{Freq} = \text{freq} - 1$

- $\text{Pos_Gap} = \text{pos}_n - \text{pos}_{n-1} - 1$

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- C.f., Jiangong Zhang, Xiaohui Long and Torsten Suel:
Performance of Compressed Inverted List Caching in
Search Engines. WWW 2008.

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Assignment Project Exam Help Index compression summary

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- We can now create an index for highly efficient Boolean retrieval that is very space efficient
- Only 4% of the total size of the collection
- Only 10-15% of the total size of the text in the collection
- However, we've ignored positional information
- Hence, space savings are less for indexes used in practice
 - But techniques substantially the same.

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Resources for today's lecture

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- IIR 5
- MG 3.3, 3.4.
- F. Scholer, H.E. Williams and J. Zobel. 2002. Compression of Inverted Indexes For Fast Query Evaluation. *Proc. ACM-SIGIR 2002*.
 - Variable byte codes
- V. N. Anh and A. Moffat. 2005. Inverted Index Compression Using Word-Aligned Binary Codes. *Information Retrieval* 8: 151–166.
 - Word aligned codes