

Week 3 – Data Link Layer

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COMP90007 Internet Technologies
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Error Detection Codes

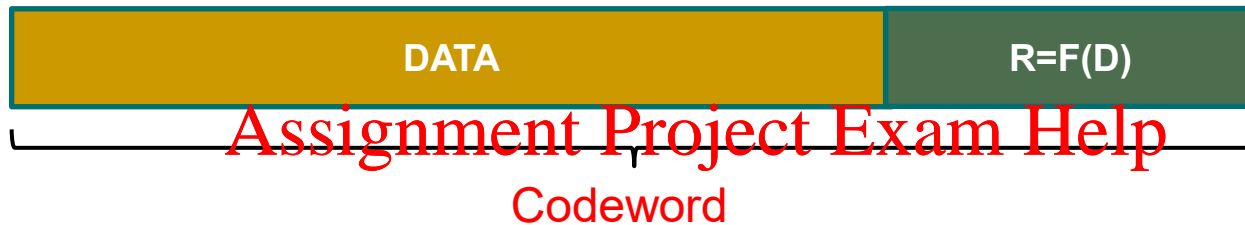
- **Parity Bit** (1 bit): (Hamming distance=2)
- **Internet Checksum** (16 bits): (Hamming distance=2)
- **Cyclic Redundancy Check (CRC)** (Standard 32-bit CRC: Hamming distance=4)

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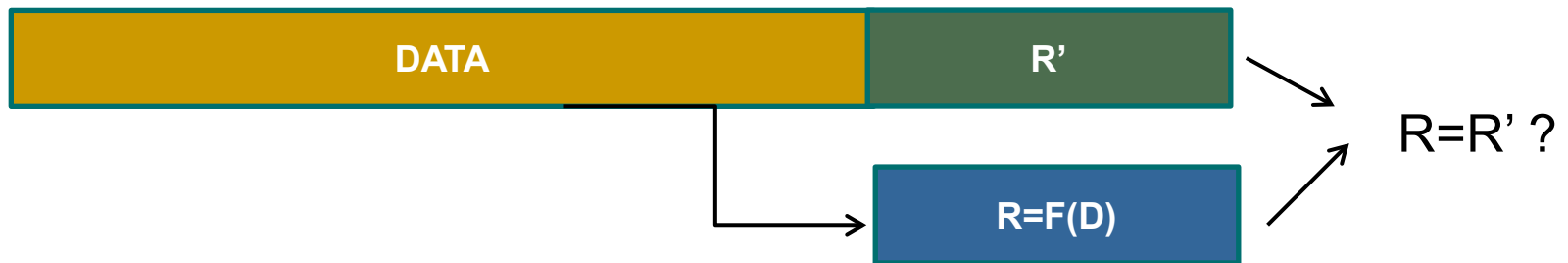
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How it works?

- Sender: calculates R check bits using a function of data bits:



- Receiver: receives the codeword and calculates the same function on the data and match the results with received check bits:



Parity Bit

Given data 10001110, count the number of 1s

Sender: Add parity bit \rightarrow 10001110**0** (for even parity)

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10001110**1** (for odd parity)

Receiver: Check the received data for errors.
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Hamming distance is 2 for Parity Bit...

$2 - 1 = 1$ **error bit can be detected** and

$(2 - 1) / 2 = \frac{1}{2}$ not even 1 bit error can be corrected

Internet Checksum

- There are different variations of checksum
- Internet Checksum (16-bit word):

Sum modulo 2^{16} and add any overflow of high order bits back into low-order bits

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Example of Checksum

Calculate checksum (5-bit word) for data
00110 10001 11001 01011

1
$$\begin{array}{r} 00110 \\ +10001 \\ \hline 10111 \end{array}$$

$$\begin{array}{r} 11001 \\ +10111 \\ \hline 10000 + 1 = 10001 \end{array}$$

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4 The checksum is one's complement of 11100 which is 00011

3
$$\begin{array}{r} 01011 \\ +10001 \\ \hline 11100 \end{array}$$

Data sent: 00110 10001 11001 01011 **00011**

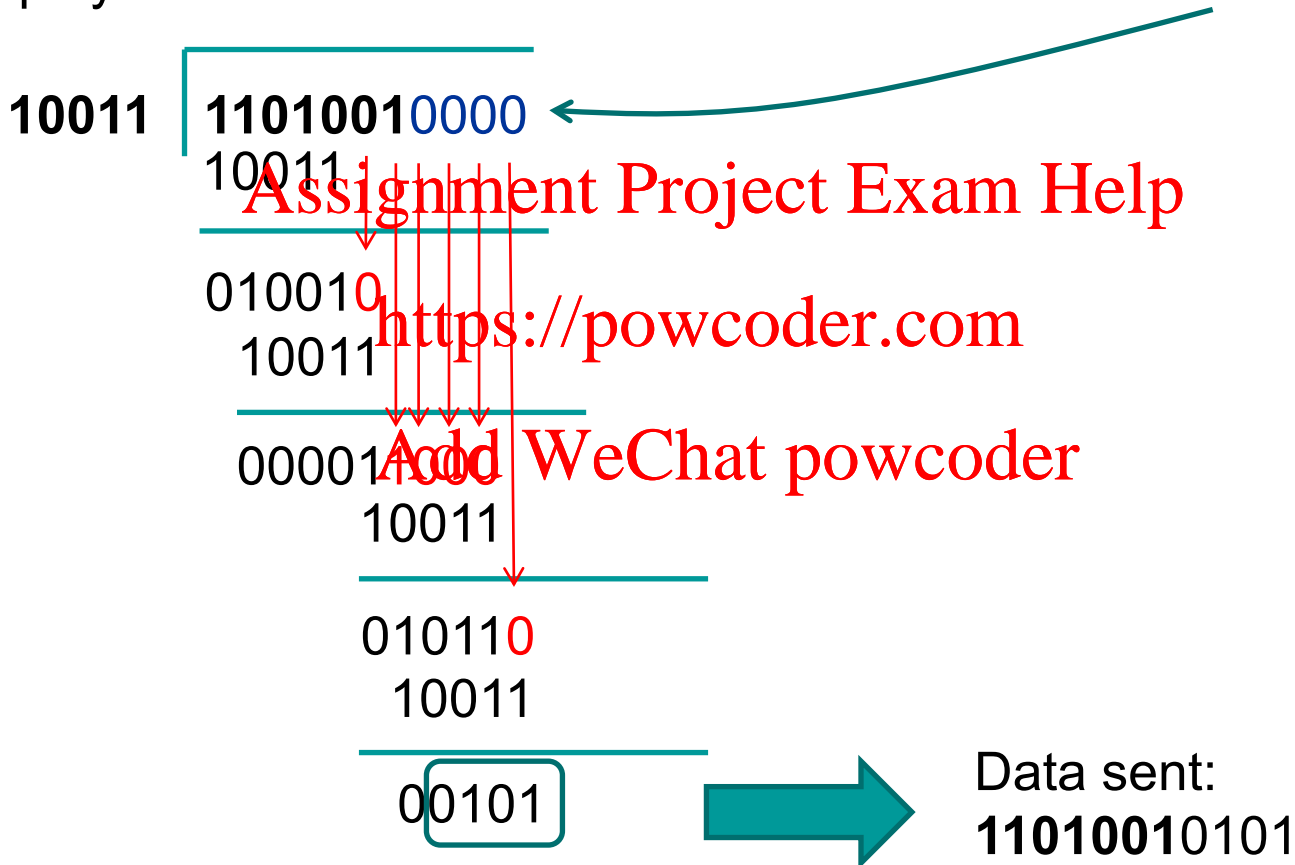
Cyclic Redundancy Check

- Based on a generator polynomial $G(x)$
 - e.g. $G(x) = x^4 + x + 1$ (10011)
 - Steps: **Assignment Project Exam Help**
 - Let r be the degree of $G(x)$ ($r=4$). **Append r zero bits to the low-order end of the frame** so it now contains $m + r$ bits and corresponds to the polynomial $x^r M(x)$.
 - **Divide the bit string corresponding to $G(x)$** into the bit string corresponding to $x^r M(x)$, using modulo 2 division.
 - **Subtract the remainder** (which is always r or fewer bits) from the bit string corresponding to $x^r M(x)$ using modulo 2 subtraction.
 - The result is the checksummed frame to be transmitted. Call its polynomial $T(x)$.

Example

Data: **1101001** and $G(x) = x^4 + x + 1$ (**10011**)

5 bits polynomial add **4** bits as the checksum – so add **0000**



Error Correction: Hamming Code

- $n=2^k-k-1$ (n: number of data, k: check bits)

Example: Data: 0101 - > requires 3 check bits



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- Put check bits in positions p that are power of 2, starting with position 1
- Check bit in position p is parity of positions with a p term in their value

Example

Put check bits in positions p that are power of 2, starting with position 1

■ Data: 0101 → requires 3 check bits

Position	P1	P2	P3	P4	P5	P6	P7
Data	?	?	0	?	1	0	1

111

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1. Calculate the parity bits for P1, P2, P4 (rule: even parity)

$$\begin{aligned} \text{P1} + \text{P3} + \text{P5} + \text{P7} &= ? + 0 + 1 + 1 \text{ (even)} \rightarrow \text{P1} = 0 \\ \text{P2} + \text{P3} + \text{P6} + \text{P7} &= ? + 0 + 0 + 1 \text{ (odd)} \rightarrow \text{P2} = 1 \\ \text{P4} + \text{P5} + \text{P6} + \text{P7} &= ? + 1 + 0 + 1 \text{ (even)} \rightarrow \text{P4} = 0 \end{aligned}$$

Data sent: 0100101

error

error

Example 1: At the receiver: 0100100

$$\begin{aligned} \text{P1} + \text{P3} + \text{P5} + \text{P7} &= 0 + 0 + 1 + 0 = 1 \times \\ \text{P2} + \text{P3} + \text{P6} + \text{P7} &= 1 + 0 + 0 + 0 = 1 \times \\ \text{P4} + \text{P5} + \text{P6} + \text{P7} &= 0 + 1 + 0 + 0 = 1 \times \end{aligned}$$

Error bit: P1, P2, P4 → P(1+2+4)=P7

Example 2: At the receiver: 0000101

$$\begin{aligned} \text{P1} + \text{P3} + \text{P5} + \text{P7} &= 0 + 0 + 1 + 1 = 0 \\ \text{P2} + \text{P3} + \text{P6} + \text{P7} &= 0 + 0 + 0 + 1 = 1 \times \\ \text{P4} + \text{P5} + \text{P6} + \text{P7} &= 0 + 1 + 0 + 1 = 0 \end{aligned}$$

Error bit: P2

Error Control Discussion

- Error Correction: More efficient in noisy transmission media e.g., wireless
- Error Detection: More efficient in the transmission media where low error rates occur, e.g. quality copper
- The error can occur in the check bits
- Require assumption on a specific number of errors occurring in transmission

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