School of Computing and Information Systems COMP90038 Algorithms and Complexity Tutorial Week 11

8-12 October 2018

Plan

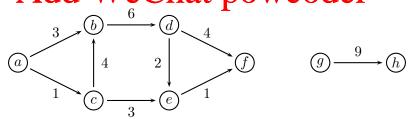
The exam is not far away, so keep up with tutorials; as always, try tackling the problems before the tute.

The exercises

- 74. Use the dynamic-programming algorithm developed in Lecture 18 to solve this instance of the coin-row problem: 20, 50, 20, 5, 10, 20, 5.
- 75. In Week 12 we will meet the concept of *problem reduction*. This question prepares you for that. First, when we talk about the length of a path in an un-weighted directed acyclic graph (DAG), we mean the number of edges in the path. (You could also consider the un-weighted graph weighted, with all edges having weight 1)

Show how to reduce the coin-row problem to the problem of finding a longest path in a DAG. That is give an algorithm that transforms any coin-row instance into a longest path-in-DAG instance in such a way that a solution to the latter provides a solution to the former. Hint: If there are n coins, use n+1 nodes; let an edge with weight i correspond to picking a coin with value i.

76. Consider the predent principal freelength of Congest Cathin a weighted, not necessarily connected, DAG. We assume that all weights are positive, and that a "longest" path is a path whose edge weights add up to the maximal possible value. For example, for the following graph, the longes path is of weight 5: hat powcoder



Use a dynamic programming approach to the problem of finding longest path in a weighted dag.

- 77. Design a dynamic programming algorithm for the version of the knapsack problem in which there are unlimited numbers of copies of each item. That is, we are given items I_1, \ldots, I_n that have values v_1, \ldots, v_n and weights w_1, \ldots, w_n as usual, but each item I_i can be selected several times. Hint: This actually makes the knapsack problem a bit easier, as there is only one parameter (namely the remaining capacity w) in the recurrence relation.
- 78. Work through Warshall's algorithm to find the transitive closure of the binary relation given by this table (or directed graph):

