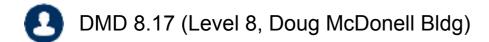


COMP90038 Algorithms and Complexity

Lecture 12: Morat Divider and Conquer Algorithms (with thanks to Harald Søndergaard)

Toby Murray







🦅 @tobycmurray

Divide and Conquer



- In the last lecture we studied the archetypal divideand-conquer sorting algorithms: mergesort and quicksort.
- We also introduced the powerful master theorem, providing solutions to a large class of recurrence https://powcoder.com/relations, for free.

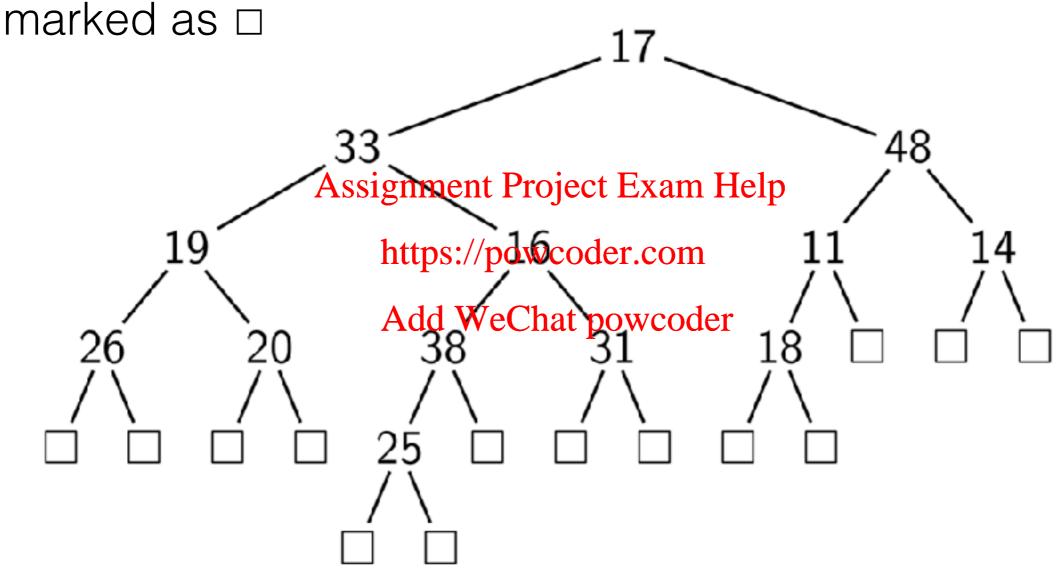
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- allows us to quickly determine the complexity of these divide-and-conquer algorithms
- Now we shall look at tree traversal, and then a final example of divide-and-conquer, giving a better solution to the closest-pair problem.

Binary Trees



An example of a binary tree, with empty subtrees

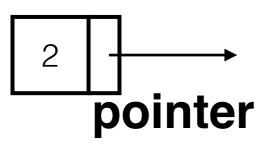


This tree has height 4, the empty tree having height -1

Review of Linked List Terminology



node

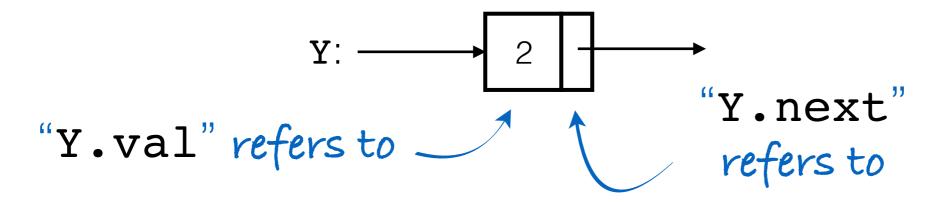


(in Java: "reference")

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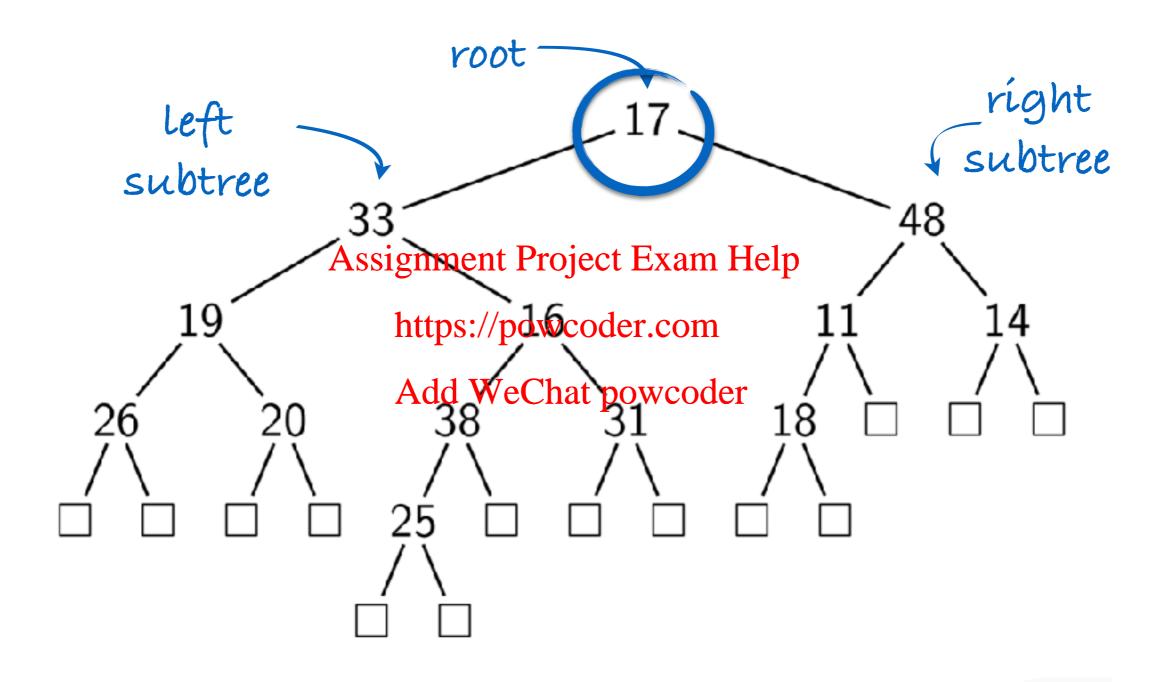


x is (a pointer to) the **head node** of the list



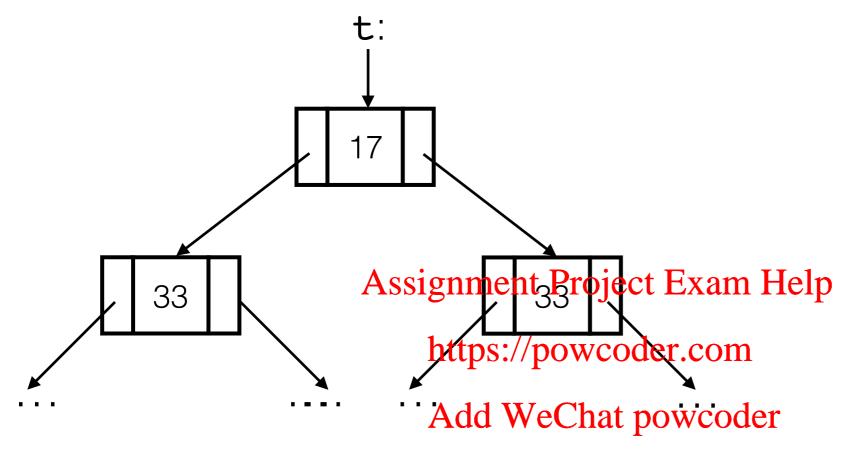
Tree Terminology



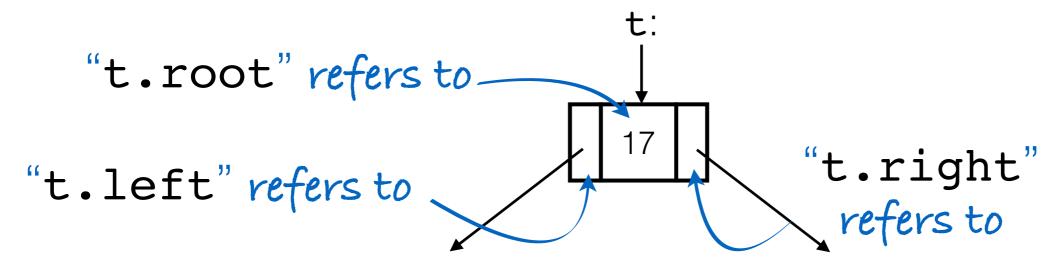


Tree Terminology





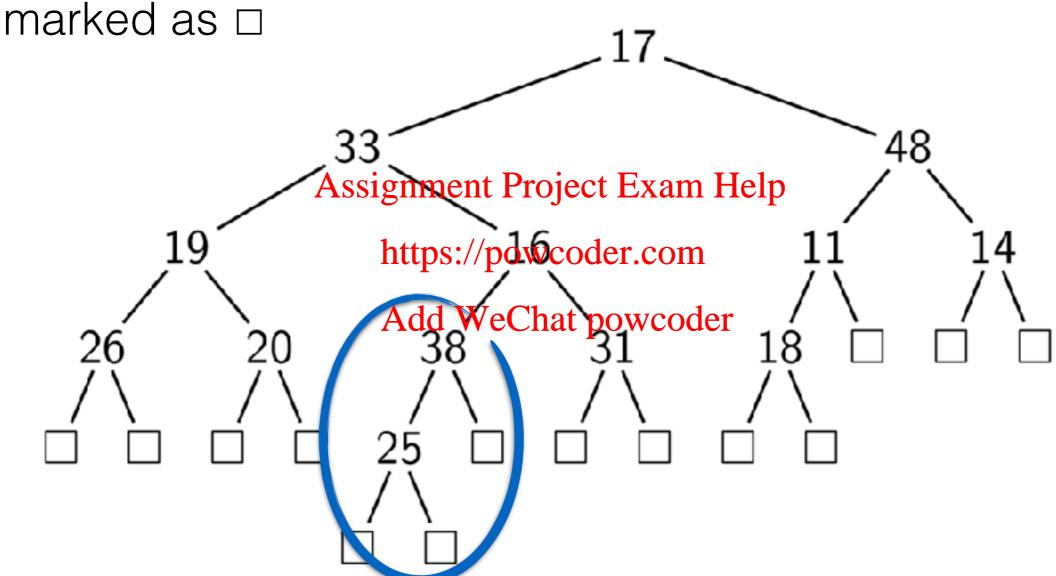
t is (a pointer to) the root node of the tree



Binary Trees



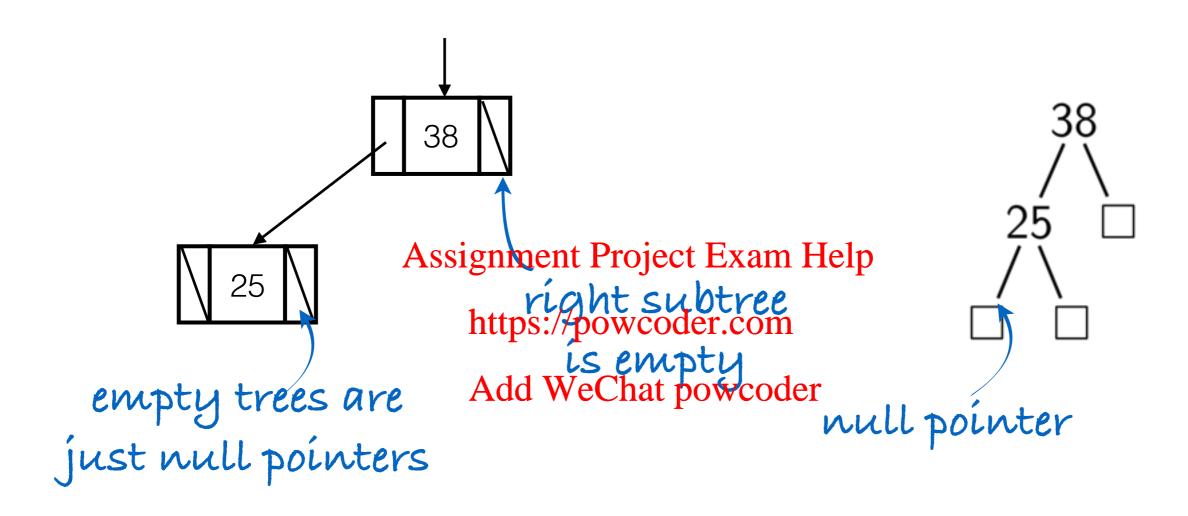
An example of a binary tree, with empty subtrees



This tree has height 4, the empty tree having height -1

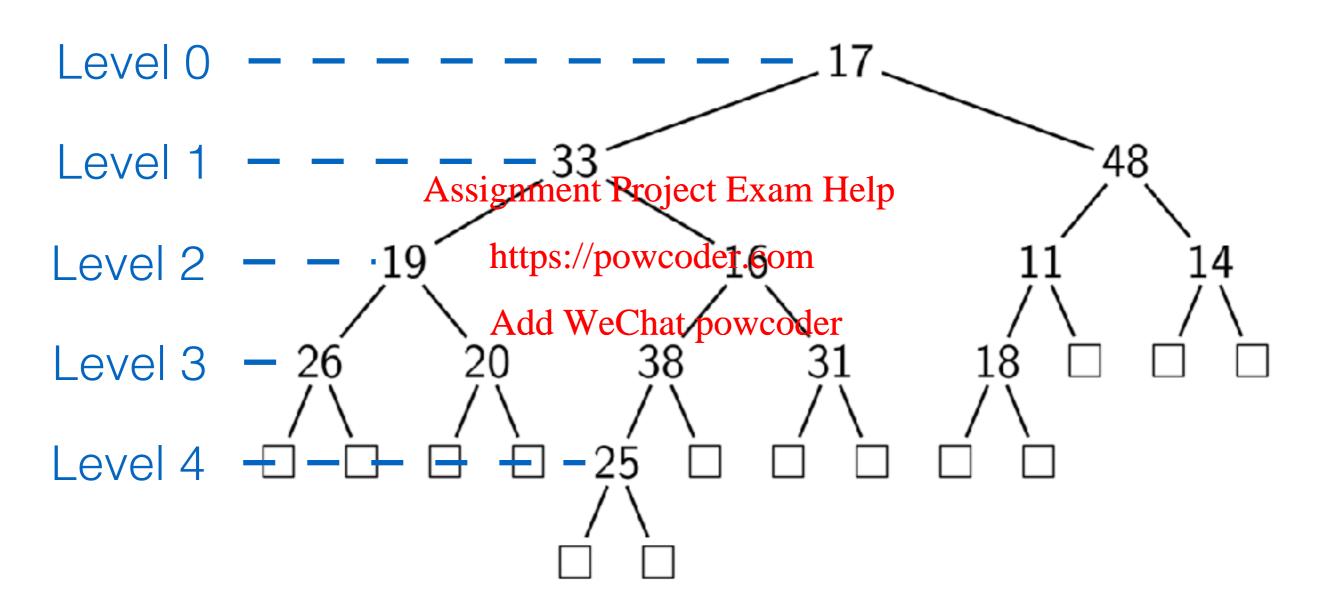
Empty Nodes





Levels and Height



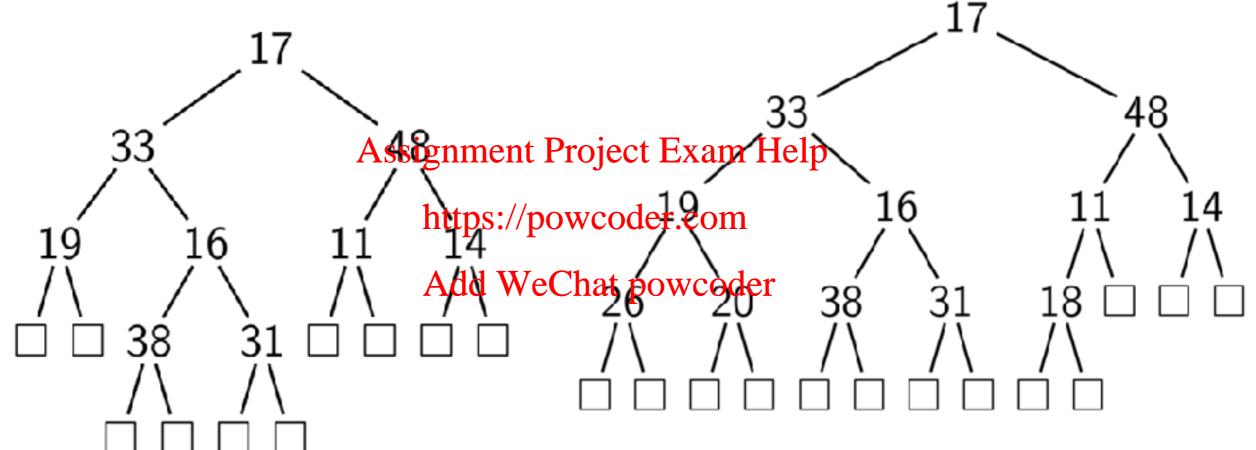


So the tree has **height** 4 (its **maximum level**)

Binary Tree Concepts



Special trees have their **external nodes** □ only at level *h* and *h*+1 for some *h*.



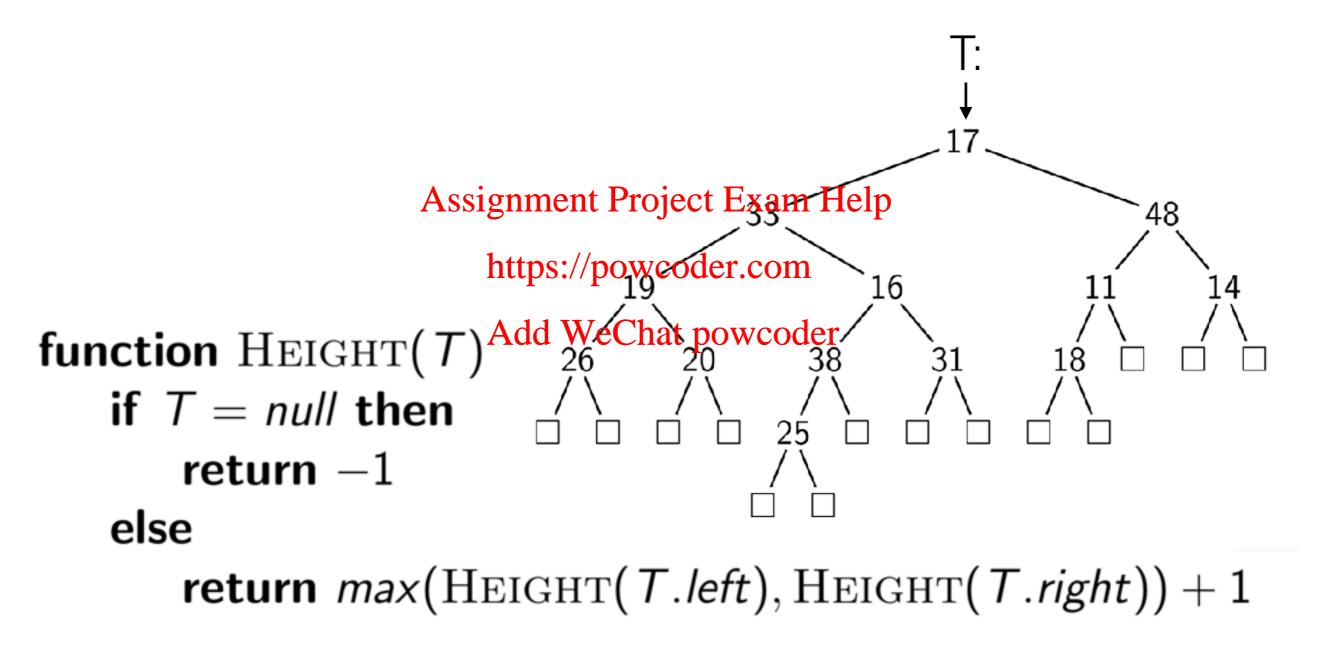
A **full** binary tree: Each node has 0 or 2 (non-empty) children. A **complete** tree: Each level filled left to right.

(Every level except perhaps the last is completely filled.)

Calculating the Height



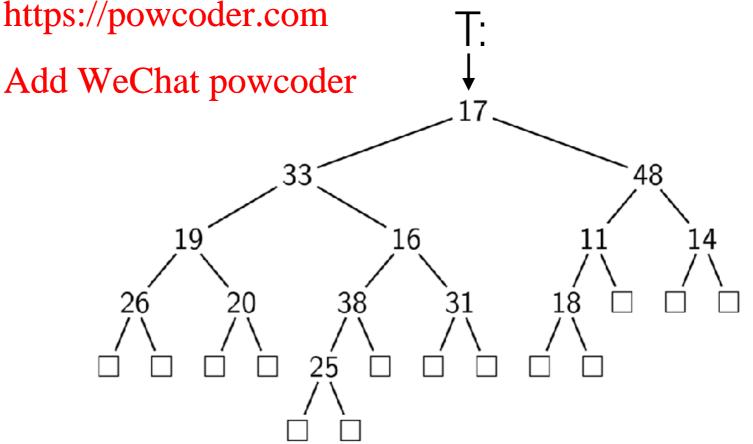
Recursion is the natural way of calculating the height:



Height Complexity



- Input size: number *n* of (internal) nodes (e.g. for T *n* is 13)
- Number of external nodes always n+1 (e.g. for T x is 14)
- The function HEIGHT makes one tree comparison (is T null/ empty?) per nodes (internal raiset External), so altogether 2n + 1 comparisons. https://powcoder.com T.



Binary Tree Traversal



- Preorder traversal visits the root, then the left subtree, and finally the right subtree.
- Inorder traversalivisits the left subtree, then the root, and finally the right subtree.
- **Postorder** traversal visits the left subtree, the right subtree, and finally the root.
- Level-order traversal visits the nodes, level by level, starting from the root.



Visit order:

```
procedure Preorder Traverse(T)

if T ≠ null then

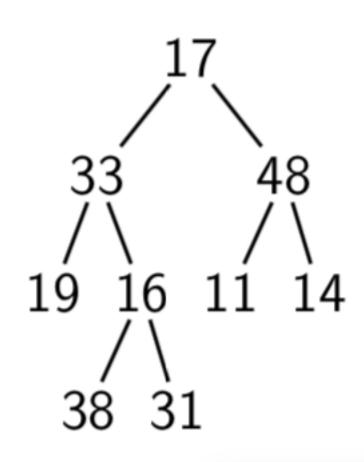
visit T.root

Preorder Traverse(T.left)

Preorder Traverse(T.left)

Preorder Traverse(T.left)

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PreorderTraverse(17)

Call Stack



Visit order: 17

procedure Preorder Traverse(T)

if T ≠ null then

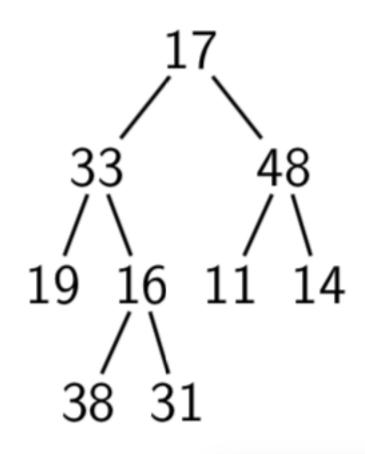
visit T.root

Preorder Traverse(T.left)

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Add WeChat powcoder



PreorderTraverse(17)

Call Stack



Visit order: 17

procedure PreorderTraverse(T)

if T ≠ null then

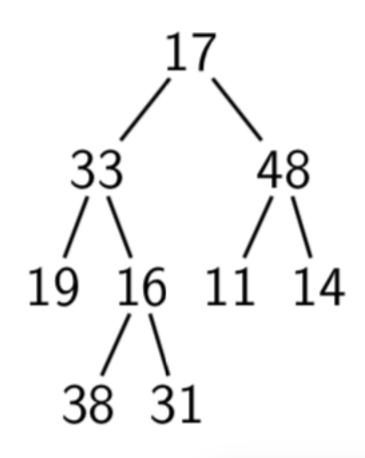
visit T.root

PreorderTraverse(T.left)

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PreorderTraverse(dfr.sight)

Add WeChat powcoder



PreorderTraverse(33)
PreorderTraverse(17)
Call Stack



Visit order: 17 33

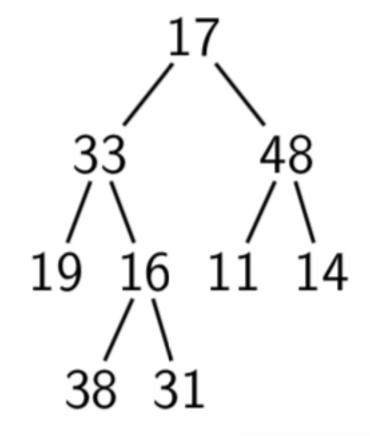
procedure Preorder Traverse(T) if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (T. left)

PREORDER That PRINCE (der. 99 ght)

Add WeChat powcoder



PreorderTraverse(33)

PreorderTraverse(17)



Visit order: 17 33

procedure PREORDERTRAVERSE(T)
if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (T. left)

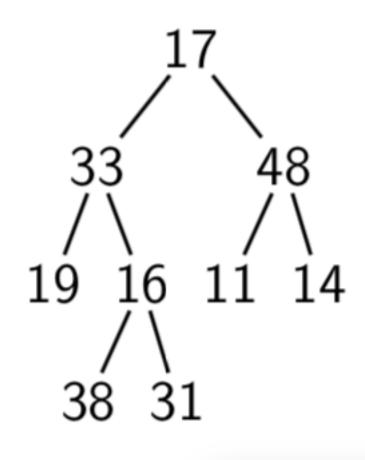
PREORDER That PRINCE (der. 99 ght)

Add WeChat powcoder

PREORDERTRAVERSE(19)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (T. left)

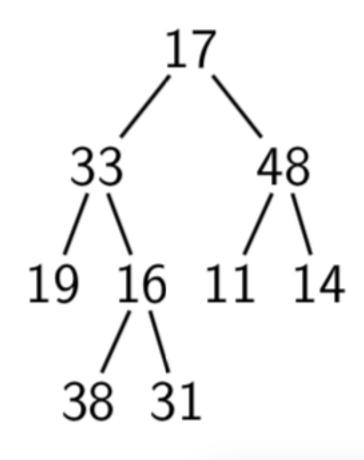
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Add WeChat powcoder

PreorderTraverse(19)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

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PREORDER That PRINCE (der. soght)

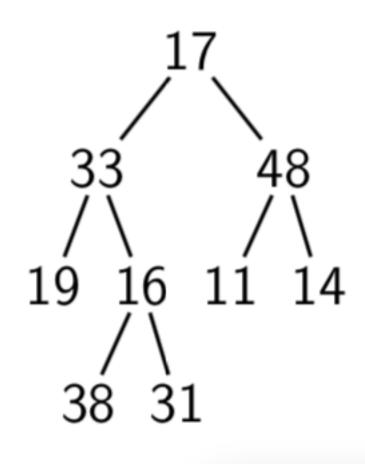
Add WeChat powcoder

PreorderTraverse(null)

PreorderTraverse(19)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19

procedure Preorder Traverse(T)
if $T \neq null$ then

visit *T.root*

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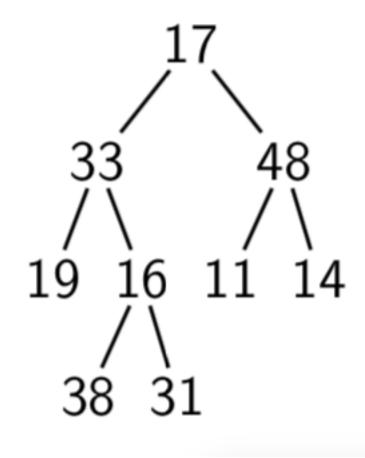
PREORDER That PRINCE (der. 99 ght)

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PreorderTraverse(19)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (7.1811)

PREORDER That PRINCE (der. soght)

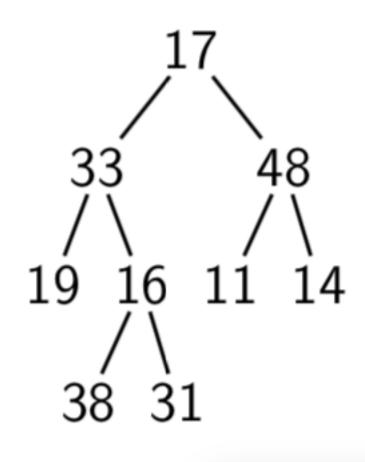
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PreorderTraverse(null)

PreorderTraverse(19)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19

procedure Preorder Traverse(T) if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (T. left)

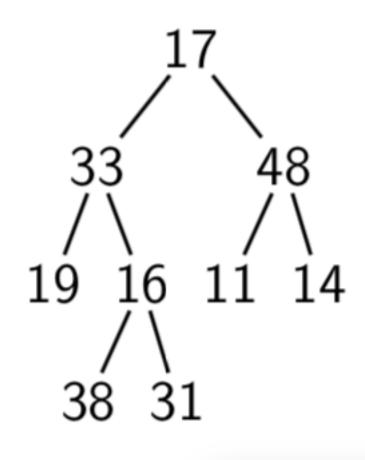
PREORDER That PRINCE (der. 99 ght)

Add WeChat powcoder

PreorderTraverse(19)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19

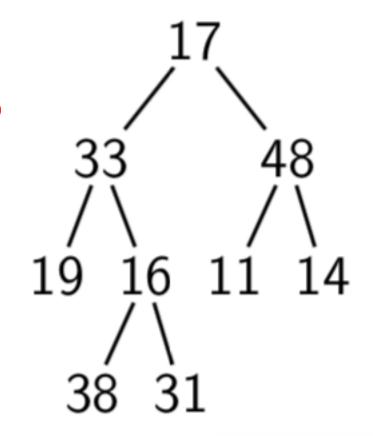
procedure Preorder Traverse (T)if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (7.1811)

PREORDER That ps://presequence.com/presequence/

Add WeChat powcoder



PreorderTraverse(33)

PreorderTraverse(17)



Visit order: 17 33 19

procedure PREORDERTRAVERSE(T) if $T \neq null$ then

visit T.root

PREORDER I RAVERSE (7. left)

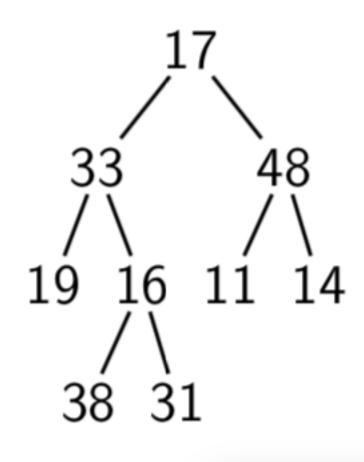
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Add WeChat powcoder

PreorderTraverse(16)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19 16

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (T. left)

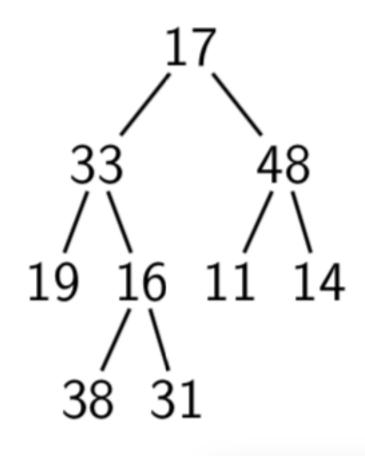
PREORDER That PRINCE (der. 99 ght)

Add WeChat powcoder

PreorderTraverse(16)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19 16

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (7.1811)

PREORDER That PRINCE (der. soght)

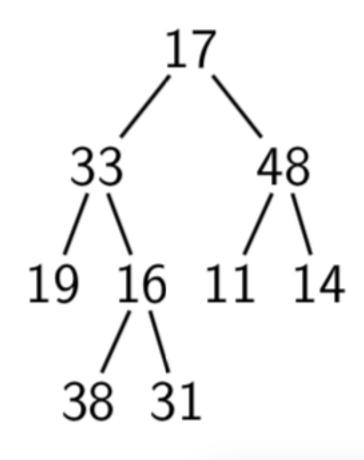
Add WeChat powcoder

PreorderTraverse(38)

PreorderTraverse(16)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19 16 38

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (7.1811)

PREORDER That PRINCE (der. soght)

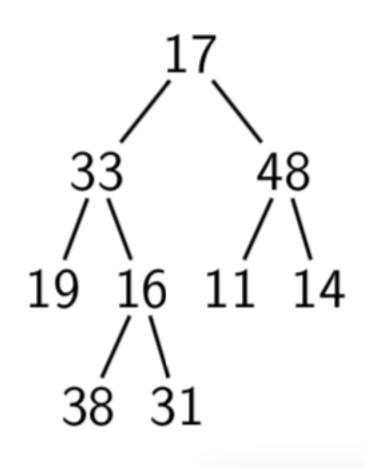
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PreorderTraverse(38)

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Visit order: 17 33 19 16 38

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (T. left)

PREORDER That PRINCE (der. soght)

Add WeChat powcoder

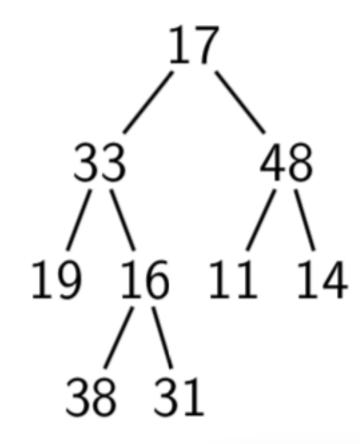
PreorderTraverse(38)

PreorderTraverse(16)

PreorderTraverse(33)

PreorderTraverse(17)

Call Stack



(...skipping the calls to PREORDERTRAVERSE(null)...)



Visit order: 17 33 19 16 38

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (T. left)

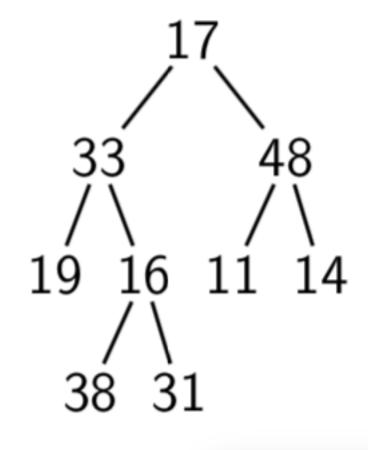
PREORDER Thank PRESENCE (dgr. 99ght)

Add WeChat powcoder

PreorderTraverse(16)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19 16 38

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (7.1811)

PREORDER That PRINCE (der. soght)

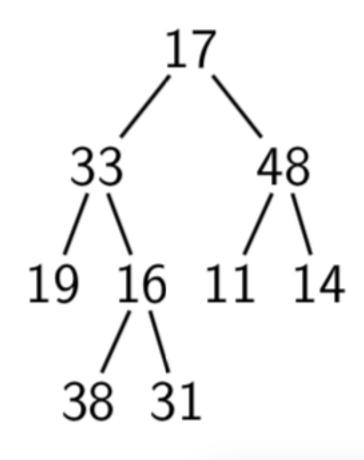
Add WeChat powcoder

PreorderTraverse(31)

PreorderTraverse(16)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19 16 38 31

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (7.1811)

PREORDER That PRINCE (der. soght)

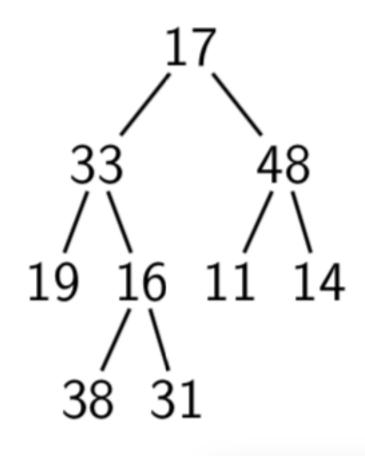
Add WeChat powcoder

PreorderTraverse(31)

PreorderTraverse(16)

PreorderTraverse(33)

PreorderTraverse(17)





Visit order: 17 33 19 16 38 31

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (T. left)

PREORDER That PRINCE (der. soght)

Add WeChat powcoder

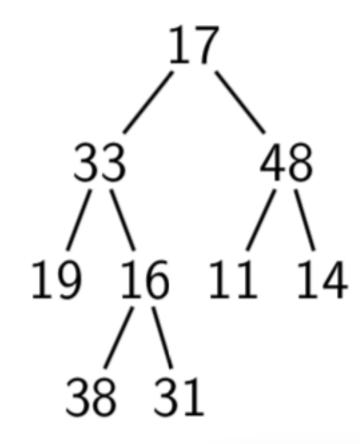
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PreorderTraverse(33)

PreorderTraverse(17)

Call Stack



(...skipping the calls to PREORDERTRAVERSE(null)...)



Visit order: 17 33 19 16 38 31

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (T. left)

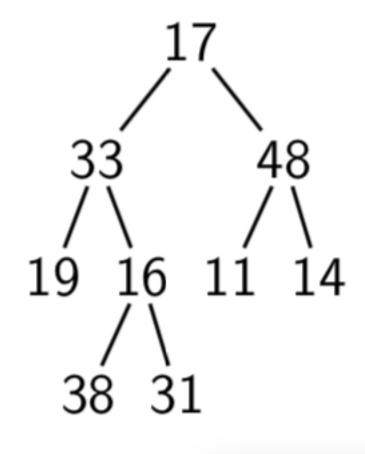
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Add WeChat powcoder

PreorderTraverse(16)

PreorderTraverse(33)

PreorderTraverse(17)





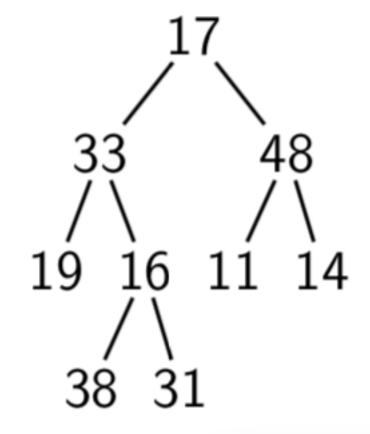
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procedure Preorder Traverse (T)if $T \neq null$ then visit *T.root*

PREORDER TRAVERSE (7.1811)

PREORDER That ps://presequence.com/presequence/

Add WeChat powcoder



PreorderTraverse(33)

PreorderTraverse(17)



Visit order: 17 33 19 16 38 31

procedure Preorder Traverse(T)

if T ≠ null then

visit T.root

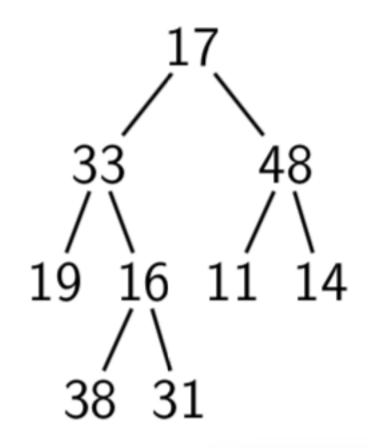
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Preorder Presse(dr.saght)



PreorderTraverse(17)

Call Stack

Add WeChat powcoder



Visit order: 17 33 19 16 38 31

procedure Preorder Traverse(T)

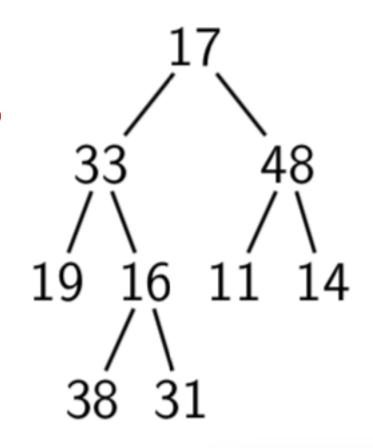
if T ≠ null then

visit T.root

Preorder Project Exam Help

Preorder Traverse(Traverse)

Preorder Traverse(Traverse)



PreorderTraverse(48)
PreorderTraverse(17)
Call Stack

Add WeChat powcoder



Visit order: 17 33 19 16 38 31 48

procedure Preorder Traverse(T)

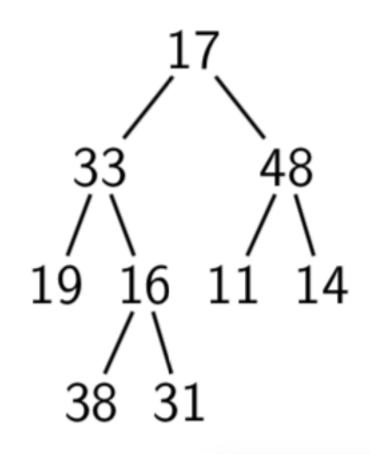
if T ≠ null then

visit T.root

Preorder Project Exam Help

Preorder Traverse(Traverse)

Preorder Traverse(Traverse)



PreorderTraverse(48)
PreorderTraverse(17)
Call Stack

Add WeChat powcoder



Visit order: 17 33 19 16 38 31 48

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (T. left)

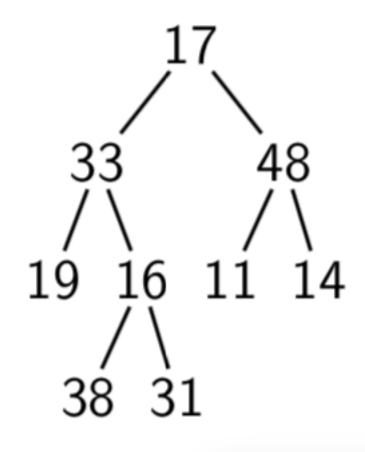
PREORDER That PRINCE (der. 99 ght)

Add WeChat powcoder

PreorderTraverse(11)

PreorderTraverse(48)

PreorderTraverse(17)





Visit order: 17 33 19 16 38 31 48 11

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (T. left)

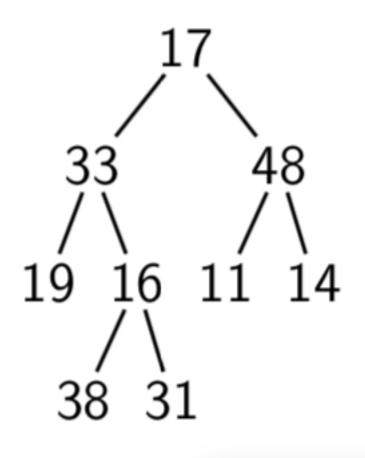
PREORDER That PRINCE (der. 99 ght)

Add WeChat powcoder

PreorderTraverse(11)

PreorderTraverse(48)

PreorderTraverse(17)





Visit order: 17 33 19 16 38 31 48 11

procedure Preorder Traverse(T)

if $T \neq null$ then

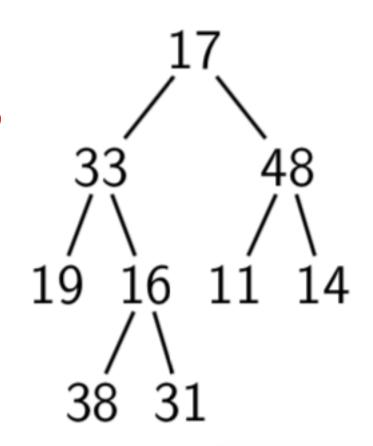
visit *T.root*

PREORDER I RAVERSE (T. left)

PREORDER That PRINCE (der. 99 ght)

Add WeChat powcoder

PreorderTraverse(11)
PreorderTraverse(48)
PreorderTraverse(17)
PreorderTraverse(17)
Call Stack



(...skipping the calls to PREORDERTRAVERSE(null)...)



Visit order: 17 33 19 16 38 31 48 11

procedure Preorder Traverse(T)

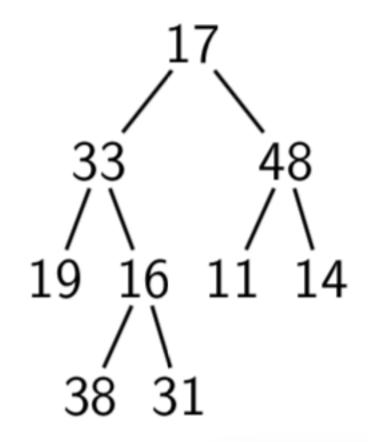
if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (T. left)

PREORDER Thank PRESENCE (dgr. 99ght)

Add WeChat powcoder



PreorderTraverse(48)

PreorderTraverse(17)



Visit order: 17 33 19 16 38 31 48 11

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (T. left)

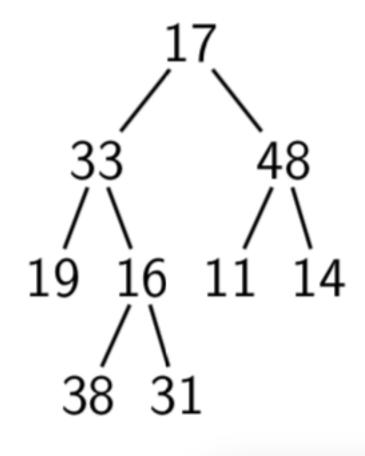
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Add WeChat powcoder

PreorderTraverse(14)

PreorderTraverse(48)

PreorderTraverse(17)





Visit order: 17 33 19 16 38 31 48 11 14

procedure Preorder Traverse(T)

if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (T. left)

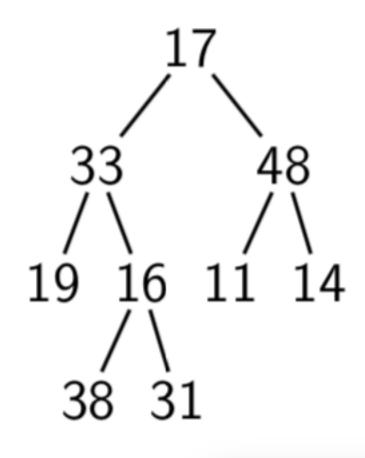
PREORDER That PRINCE (der. soght)

Add WeChat powcoder

PreorderTraverse(14)

PreorderTraverse(48)

PreorderTraverse(17)





Visit order: 17 33 19 16 38 31 48 11 14

procedure Preorder Traverse(T)

if $T \neq null$ then

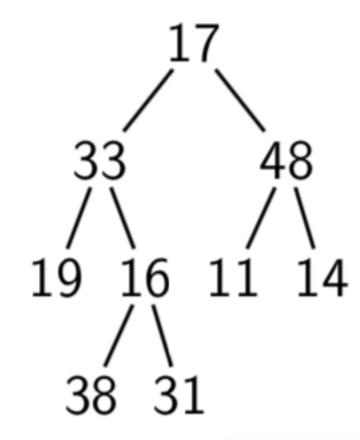
visit *T.root*

PREORDER I RAVERSE (T. left)

PREORDER That PRINCE (der. soght)

Add WeChat powcoder

PreorderTraverse(14)
PreorderTraverse(48)
PreorderTraverse(17)
PreorderTraverse(17)
Call Stack



(...skipping the calls to PREORDERTRAVERSE(null)...)



Visit order: 17 33 19 16 38 31 48 11 14

procedure Preorder Traverse(T)

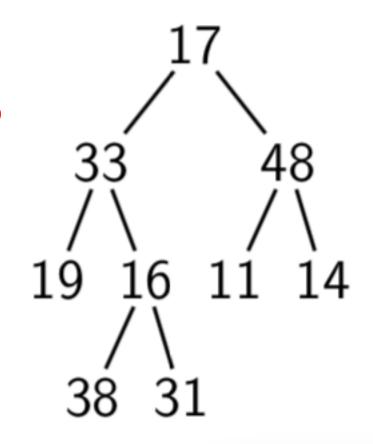
if $T \neq null$ then

visit *T.root*

PREORDER TRAVERSE (T. left)

PREORDER Thank PRESENCE (dgr. 99ght)

Add WeChat powcoder



PreorderTraverse(48)

PreorderTraverse(17)



Visit order: 17 33 19 16 38 31 48 11 14

procedure Preorder Traverse(T)

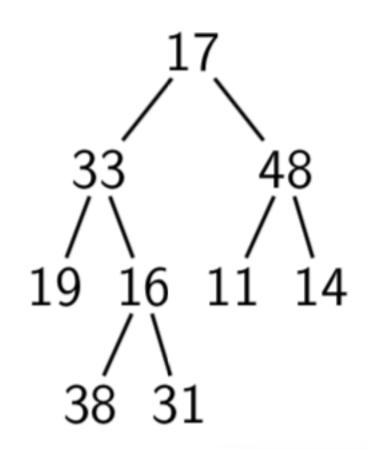
if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (T. left)

PREORDER That PRINCE (der. 99 ght)

Add WeChat powcoder



PreorderTraverse(17)

Call Stack



Visit order: 17 33 19 16 38 31 48 11 14

procedure Preorder Traverse(T)

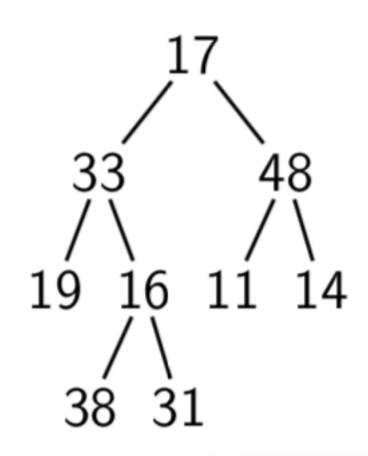
if $T \neq null$ then

visit *T.root*

PREORDER I RAVERSE (7. left)

PREORDER That PRINCE (der. 99 pht)

Add WeChat powcoder





Visit order:

procedure InorderTraverse(T)

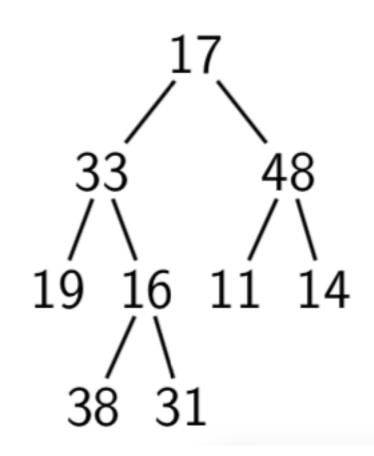
if $T \neq null$ then

InorderTraverse(T.left)

visit T.rootAssignment Project Exam Help

visit T.rootInorderTraverse(T.left)

Add WeChat powcoder



INORDERTRAVERSE(17)

Call Stack



Visit order:

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procedure InorderTraverse(T)

if T \neq null then

InorderTraverse(T.left)

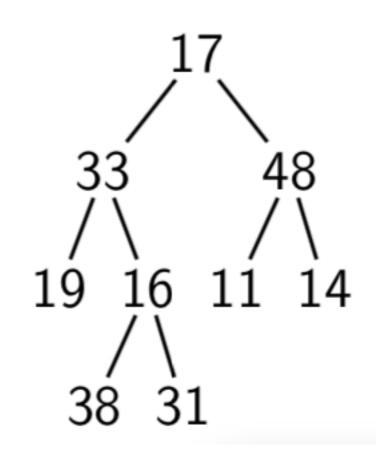
visit T.root

Assignment Project Exam Help

visit T.root

InorderTraverse(T.left)

Add WeChat powcoder
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INORDERTRAVERSE(33)
INORDERTRAVERSE(17)
Call Stack



Visit order:

```
procedure InorderTraverse(T)

if T \neq null then

InorderTraverse(T.left)

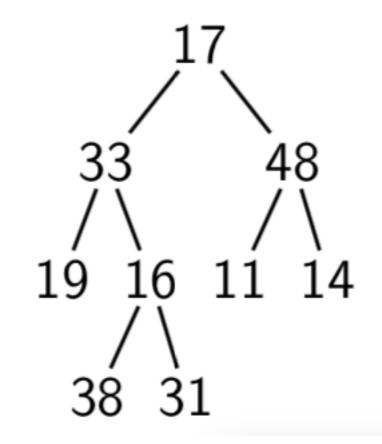
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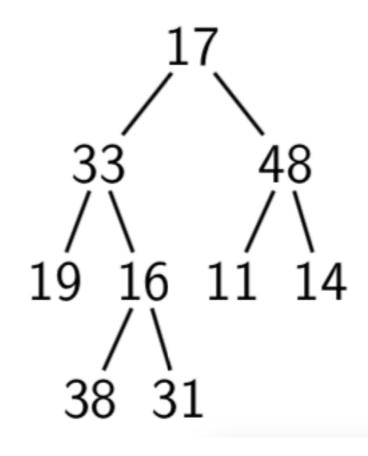
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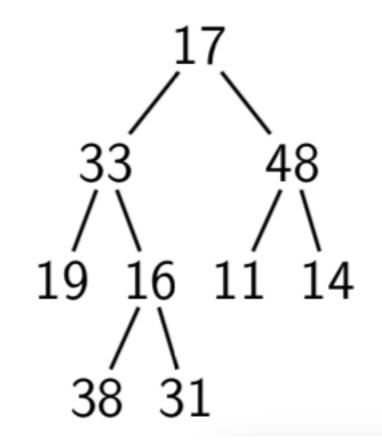
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procedure INORDERTRAVERSE(T)

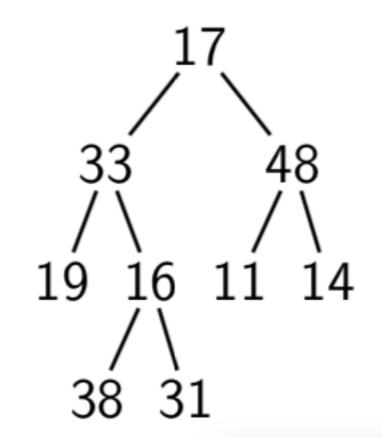
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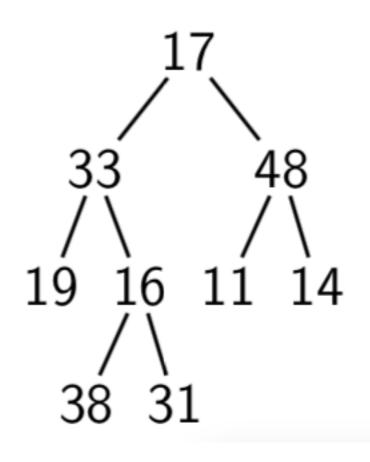
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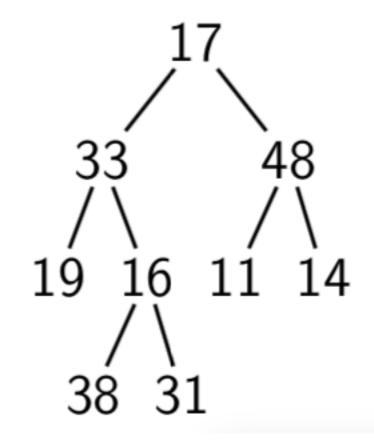
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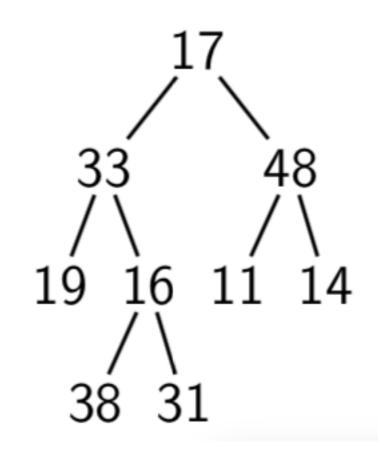
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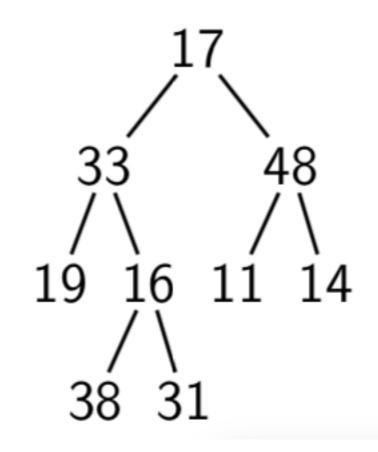
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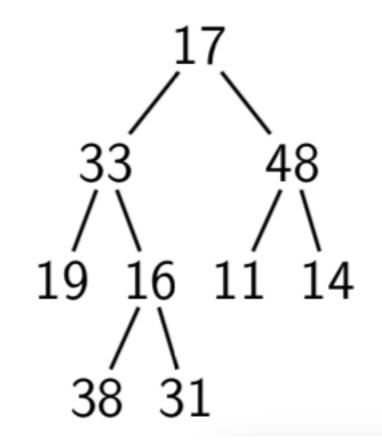
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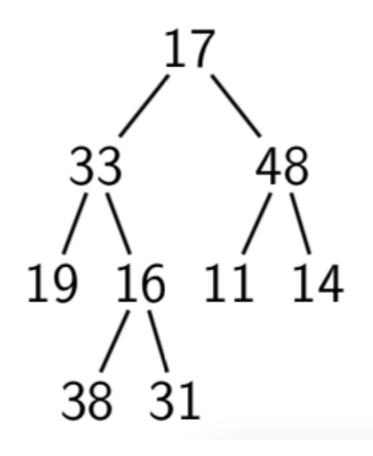
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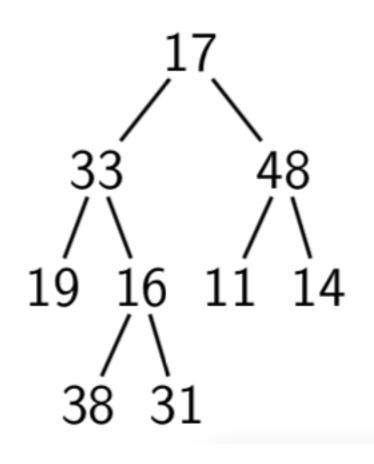
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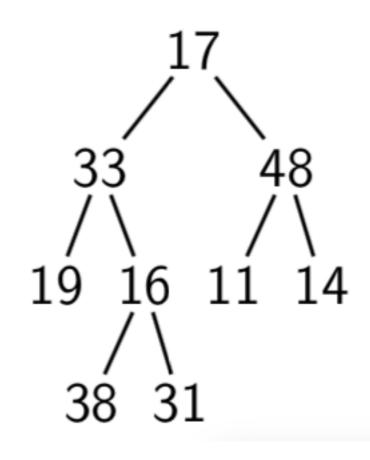
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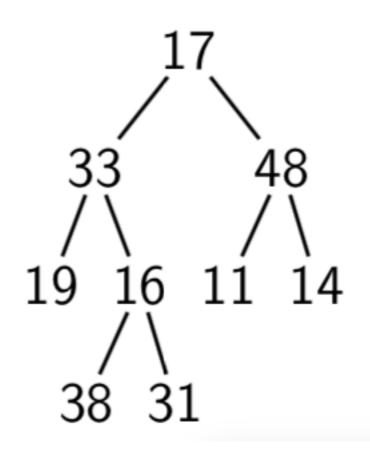
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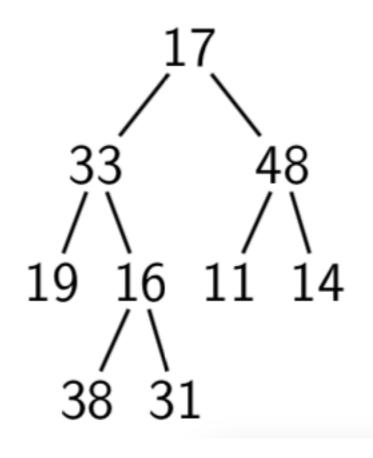
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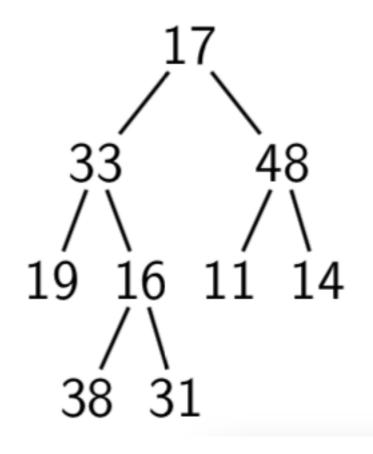
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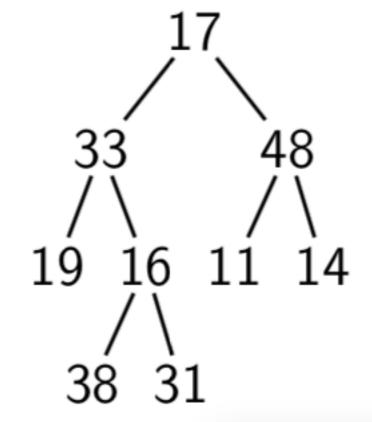
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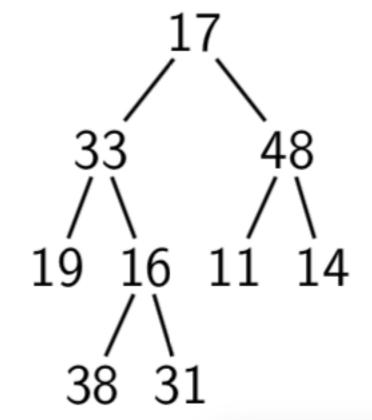
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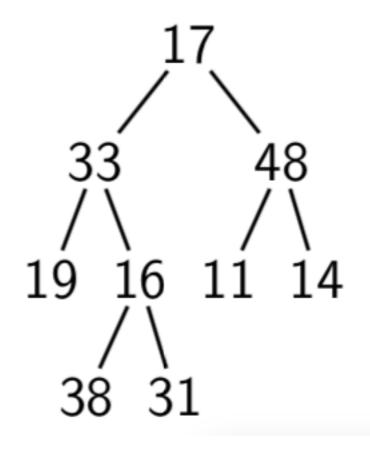
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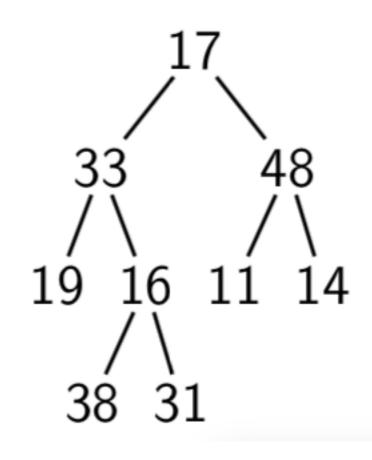
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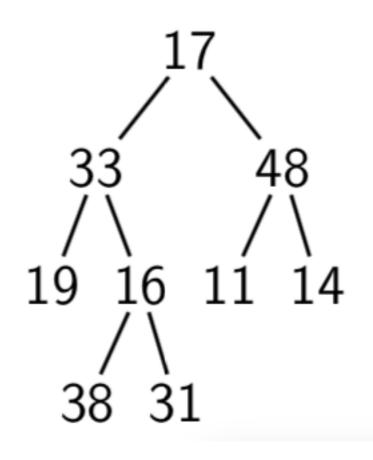
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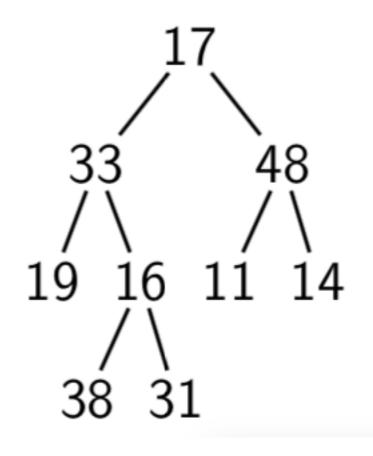
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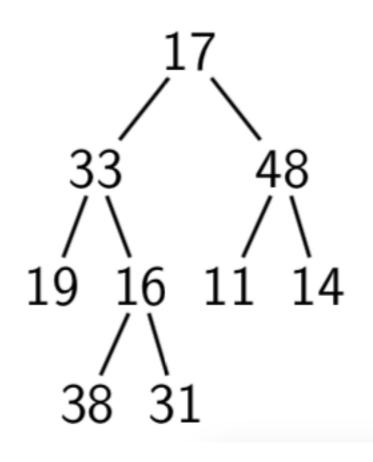
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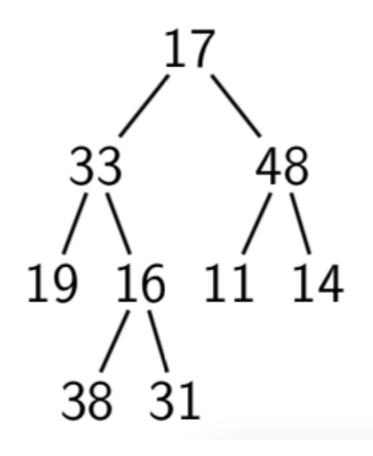
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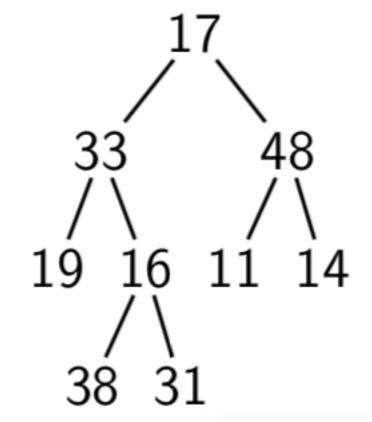
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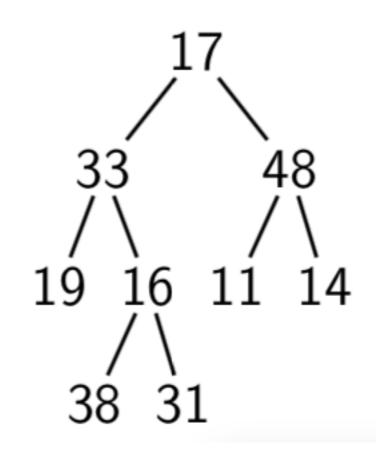
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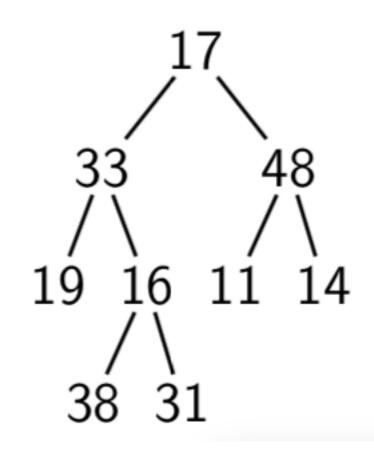
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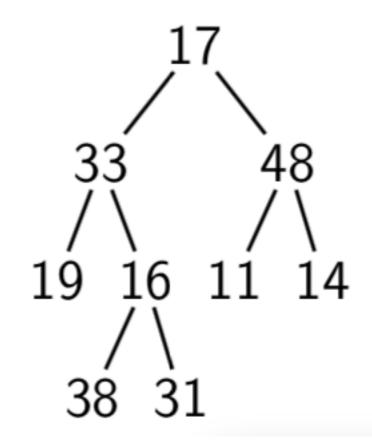
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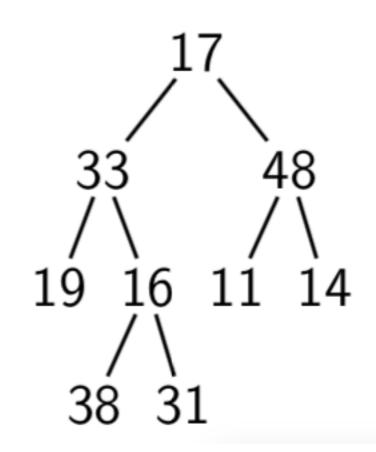
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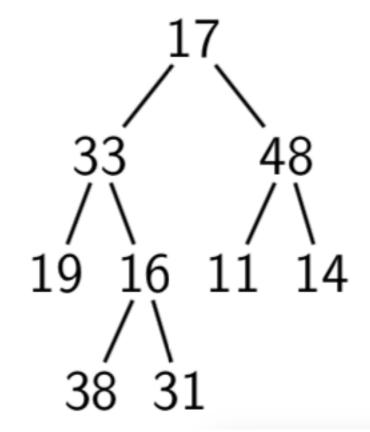
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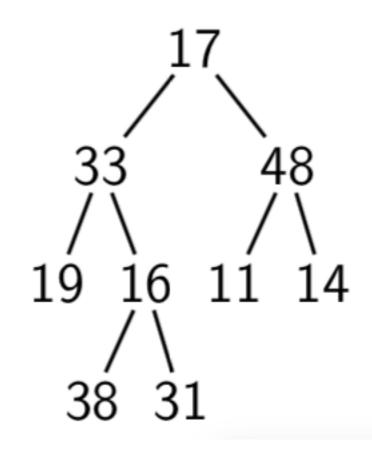
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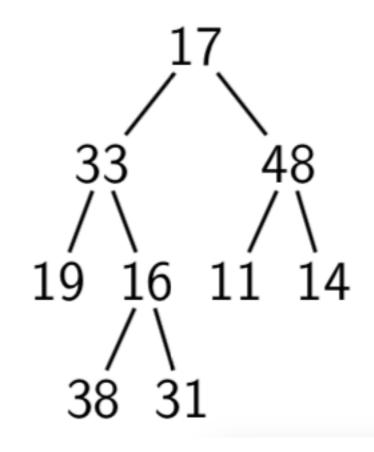
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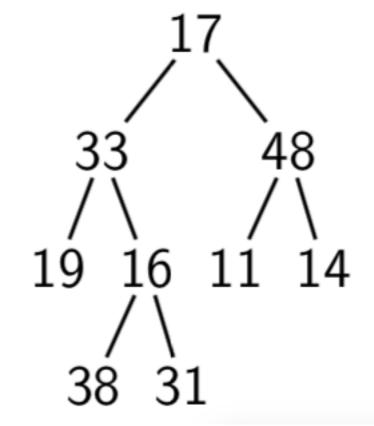
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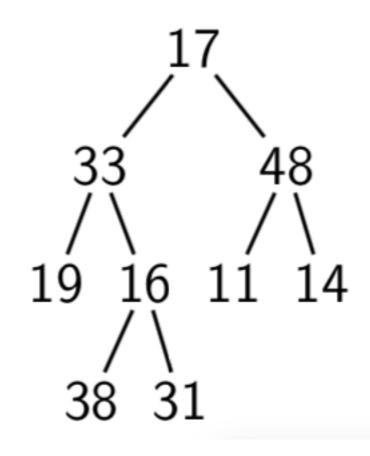
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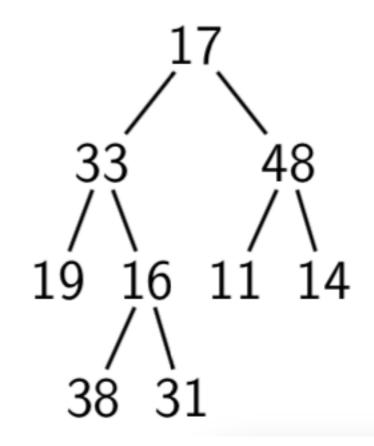
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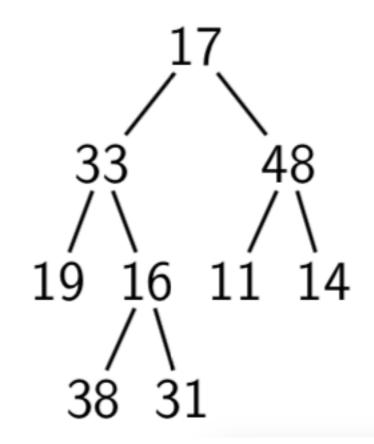
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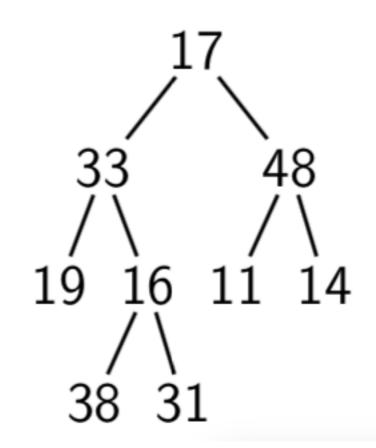
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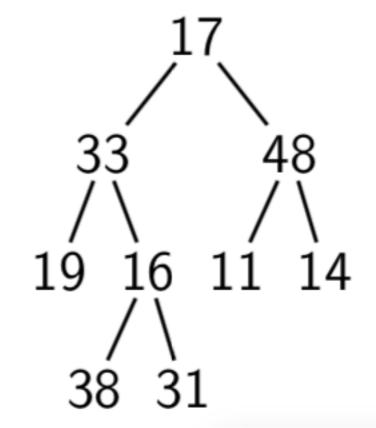
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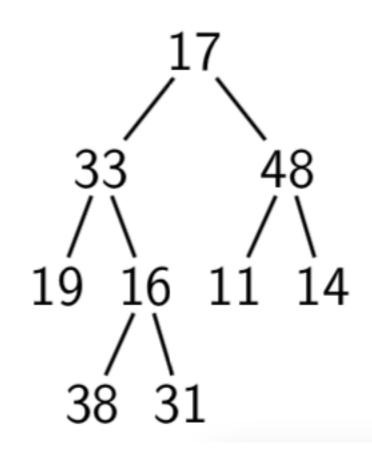
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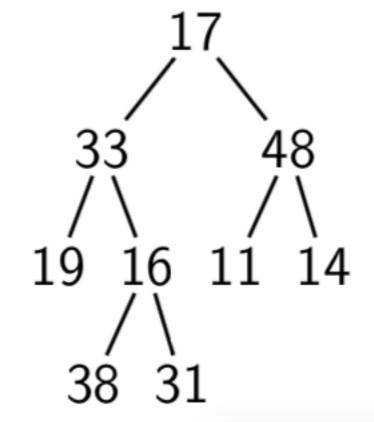
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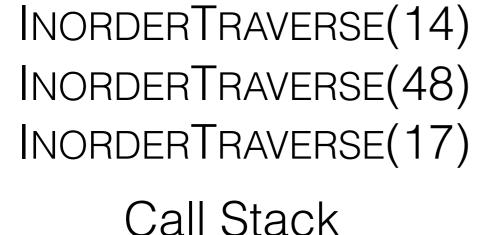
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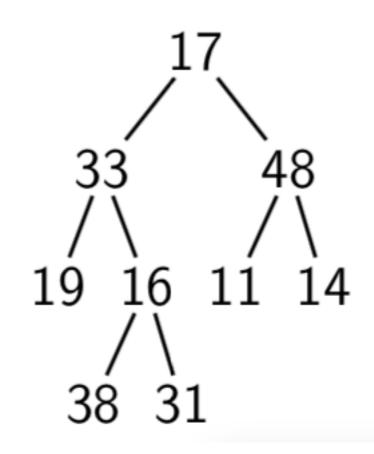
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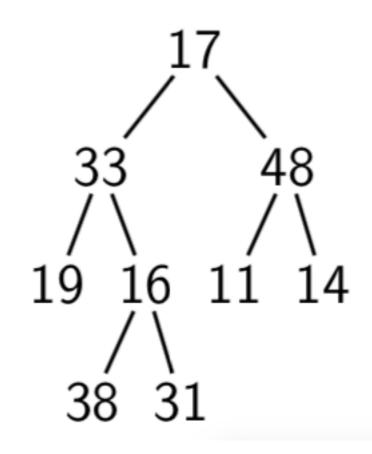
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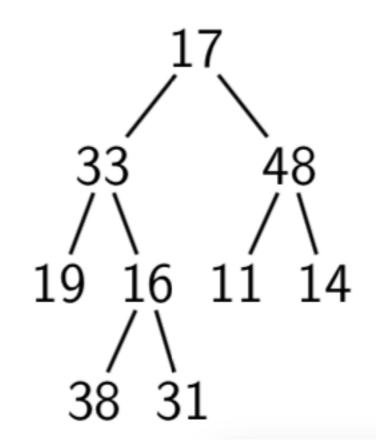
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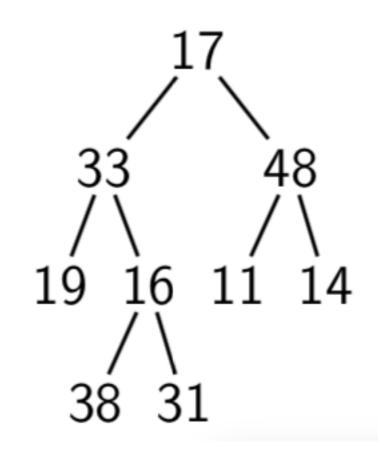
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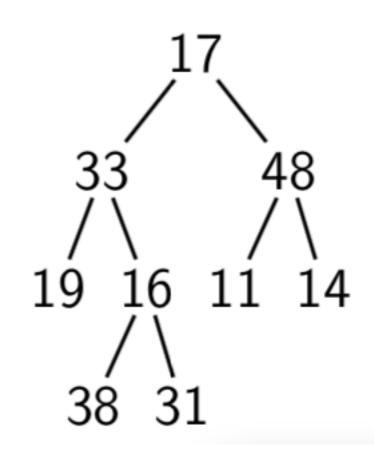
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visit T.root

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Add WeChat powcoder



INORDERTRAVERSE(17)

Call Stack



Visit order: 19 33 38 16 31 17 11 48 14

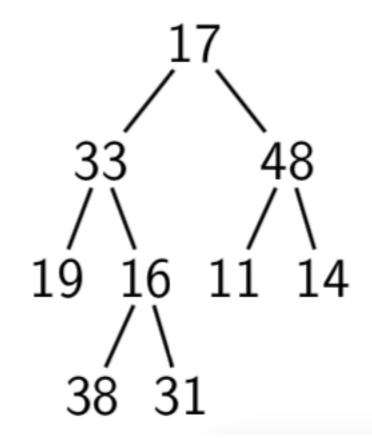
procedure Inorder Traverse (T)

if $T \neq null$ then

INORDERTRAVERSE(*T.left*)
visit *T.root*Assignment Project Exam Help

INORDER TRAVERSE (der.comht)

Add We Chat powcoder





Visit order:

```
procedure PostorderTraverse(T)

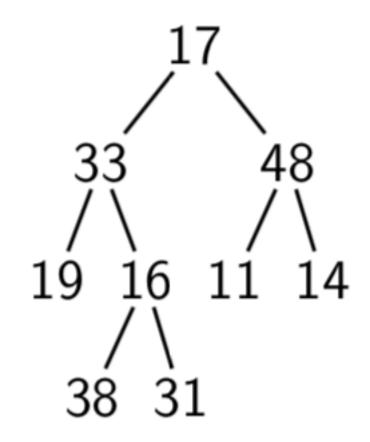
if T \neq null then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.root

Add WeChat powcoder
```



PostorderTraverse(17)

Call Stack



Visit order:

```
procedure PostorderTraverse(T)

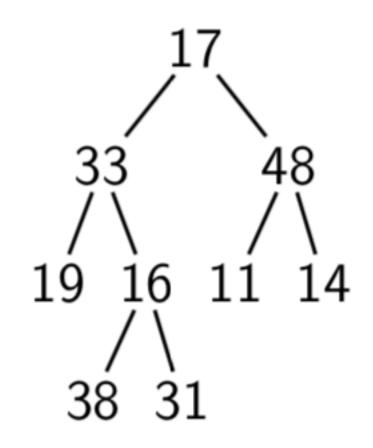
if T \neq null then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.root

Add WeChat powcoder
```



PostorderTraverse(33)
PostorderTraverse(17)
Call Stack



Visit order:

```
procedure Postorder Traverse(T)

if T \neq null then

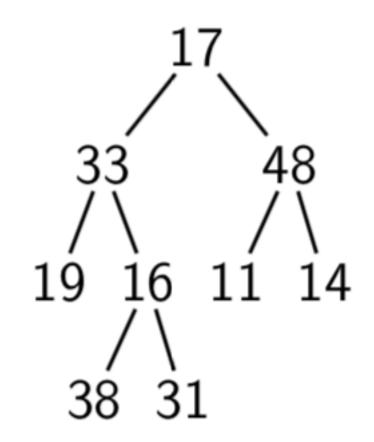
Postorder Traverse(T.left)

Assignment Project Exam Help

Postorder Traverse(T.right)

visit T.root

Add WeChat powcoder
```



PostorderTraverse(19)
PostorderTraverse(33)
PostorderTraverse(17)
Call Stack



Visit order:

```
procedure PostorderTraverse(T)

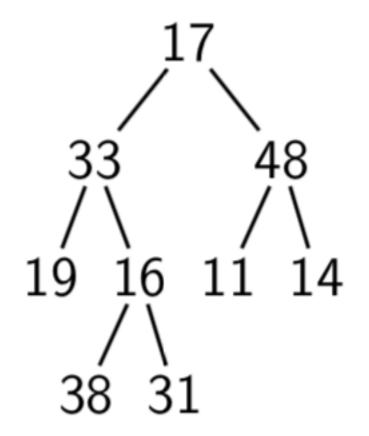
if T \neq null then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.root

Add WeChat powcoder
```



PostorderTraverse(null)

PostorderTraverse(19)

PostorderTraverse(33)

PostorderTraverse(17)



Visit order:

```
procedure PostorderTraverse(T)

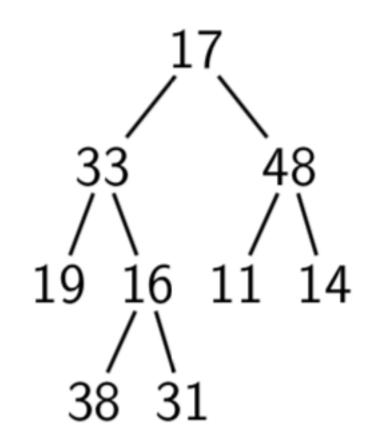
if T \neq null then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.root

Add WeChat powcoder
```



PostorderTraverse(19)
PostorderTraverse(33)
PostorderTraverse(17)



Visit order:

```
procedure Postorder Traverse(T)

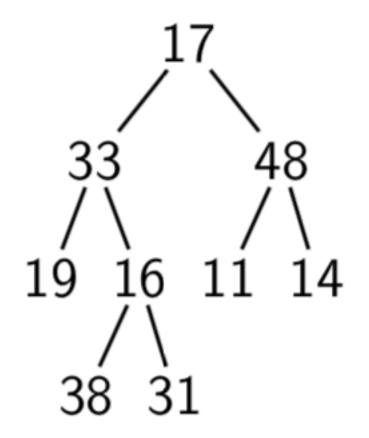
if T \neq null then

Postorder Traverse(T.left)

Assignment Project Exam Help
Postorder Traverse(T.right)

visit T.root

Add WeChat powcoder
```



PostorderTraverse(null)

PostorderTraverse(19)

PostorderTraverse(33)

PostorderTraverse(17)



Visit order:

```
procedure Postorder Traverse(T)

if T \neq null then

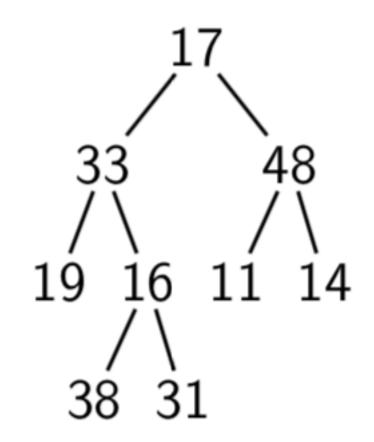
Postorder Traverse(T.left)

Assignment Project Exam Help

Postorder Traverse(T.right)

visit T.root

Add WeChat powcoder
```



PostorderTraverse(19)
PostorderTraverse(33)
PostorderTraverse(17)
Call Stack



Visit order: 19

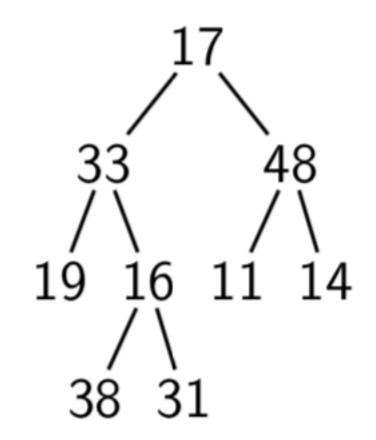
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(19)
PostorderTraverse(33)
PostorderTraverse(17)
Call Stack



Visit order: 19

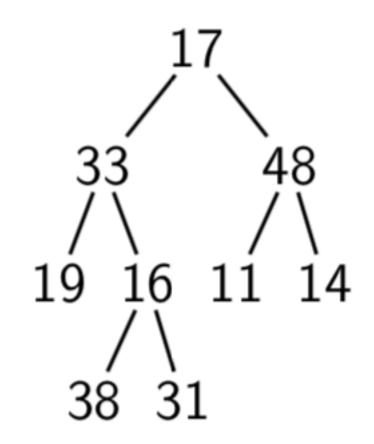
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(33) PostorderTraverse(17)



Visit order: 19

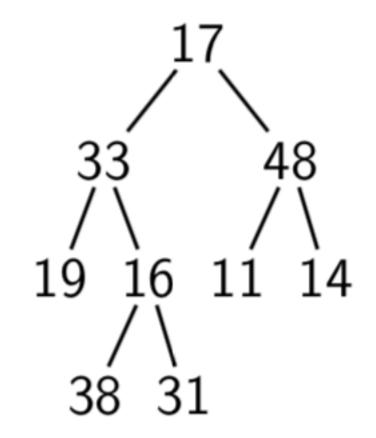
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)
visit T.root

Add WeChat powcoder



PostorderTraverse(16) PostorderTraverse(33) PostorderTraverse(17)



Visit order: 19

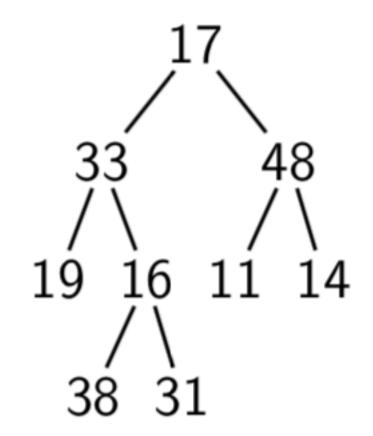
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.root



PostorderTraverse(38)

PostorderTraverse(16)

PostorderTraverse(33)

PostorderTraverse(17)

Call Stack

Add WeChat powcoder



Visit order: 19

procedure Postorder Traverse (T)if $T \neq null$ then Postorder Traverse (T.left)
Assignment Project Exam Help
Postorder Traverse (T.right visit T.roothttps://powcoder.com POSTORDERTRAVERSE (NUII) Add WeChat powcoder

PostorderTraverse(38)

PostorderTraverse(16)

PostorderTraverse(33)

PostorderTraverse(17)



Visit order: 19

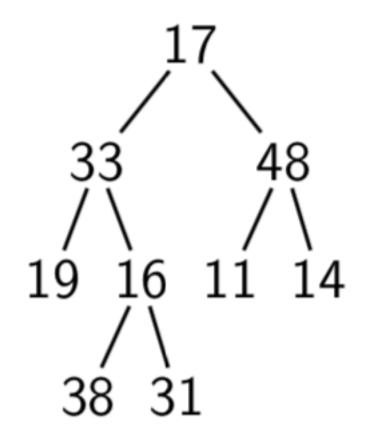
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(38)

PostorderTraverse(16)

PostorderTraverse(33)

PostorderTraverse(17)



Visit order: 19

procedure Postorder Traverse(T)

if $T \neq null$ then

Postorder Traverse(T.left)

Assignment Project Exam Help

Postorder Traverse(T.right

visit T.root

Add WeChat poweder

POSTORDERTRAVERSE (NUII)

Add WeChat powcoder

Door on the powcoder (NO)

PostorderTraverse(38)

PostorderTraverse(16)

PostorderTraverse(33)

PostorderTraverse(17)



Visit order: 19

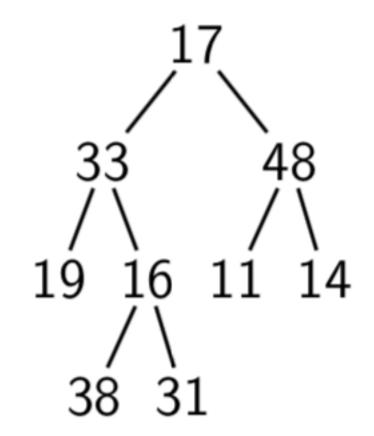
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help,
PostorderTraverse(T.right)

visit T.root



PostorderTraverse(38)

PostorderTraverse(16)

PostorderTraverse(33)

PostorderTraverse(17)

Call Stack

Add WeChat powcoder



Visit order: 19 38

procedure Postorder Traverse (T)

if $T \neq null$ then

Postorder Traverse (T. left)

Assignment Project Exam Help
Postorder Traverse (T. right

visit T.roothttps://powcoder.com

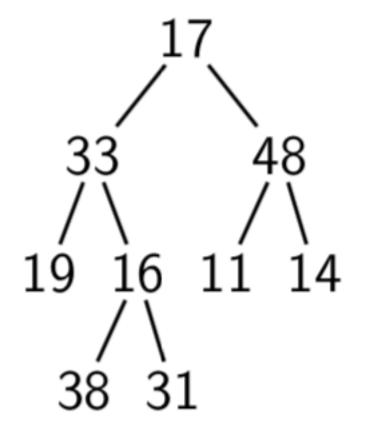
Add WeChat powcoder

PostorderTraverse(38)

PostorderTraverse(16)

PostorderTraverse(33)

PostorderTraverse(17)





Visit order: 19 38

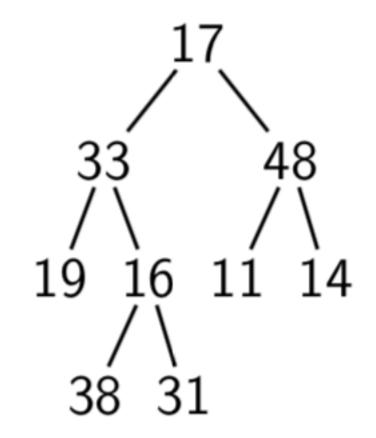
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(16)
PostorderTraverse(33)
PostorderTraverse(17)
Call Stack



Visit order: 19 38

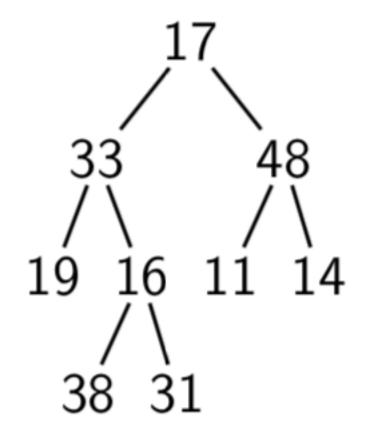
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(31)

PostorderTraverse(16)

PostorderTraverse(33)

PostorderTraverse(17)



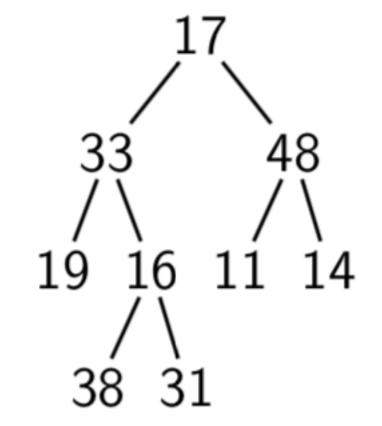
Visit order: 19 38

procedure Postorder Traverse (T) if $T \neq null$ then

Postorder Traverse (T. left)
Assignment Project Exam Help
Postorder Traverse (T. right)
visit T. root

Postorder Traverse (T. right)

Add WeChat powcoder



PostorderTraverse(31)

PostorderTraverse(16)

PostorderTraverse(33)

PostorderTraverse(17)

Call Stack

(...skipping the calls to PostorderTraverse(null)...)



Visit order: 19 38 31

procedure PostorderTraverse(T)
if $T \neq null$ then
PostorderTraverse(T.left)

Postorder Traverse (T.left)
Assignment Project Exam Help
Postorder Traverse (T.right)
https://powcoder.com

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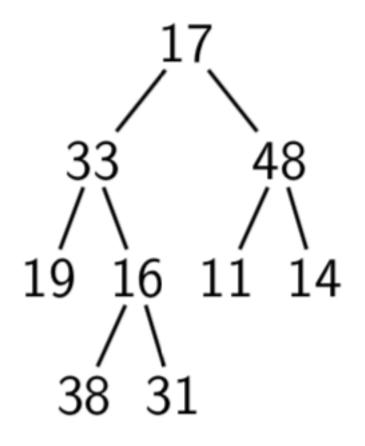
Add WeChat powcoder

PostorderTraverse(31)

PostorderTraverse(16)

PostorderTraverse(33)

PostorderTraverse(17)





Visit order: 19 38 31

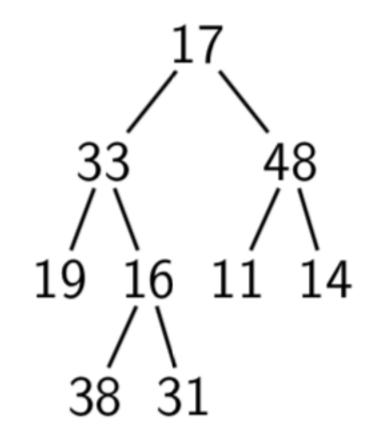
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(16) PostorderTraverse(33) PostorderTraverse(17)



Visit order: 19 38 31 16

procedure PostorderTraverse(T)

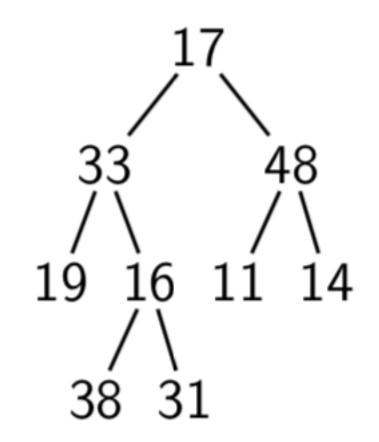
if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.root

Add WeChat powcoder



PostorderTraverse(16)
PostorderTraverse(33)
PostorderTraverse(17)
Call Stack



Visit order: 19 38 31 16

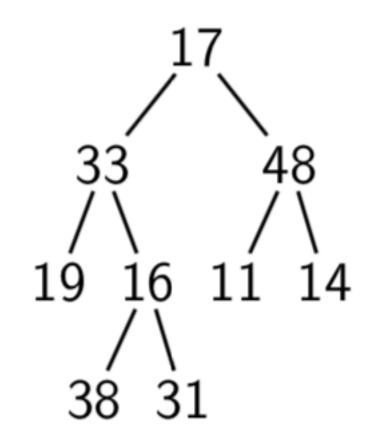
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

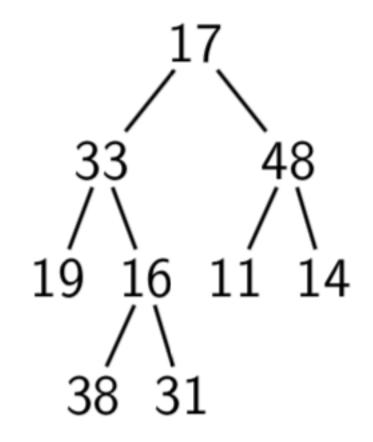
visit T.rootAdd WeChat powcoder



PostorderTraverse(33) PostorderTraverse(17)



Visit order: 19 38 31 16 33



PostorderTraverse(33) PostorderTraverse(17)



Visit order: 19 38 31 16 33

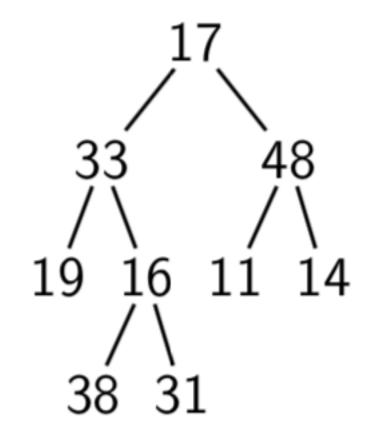
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

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PostorderTraverse(17)

Call Stack



Visit order: 19 38 31 16 33

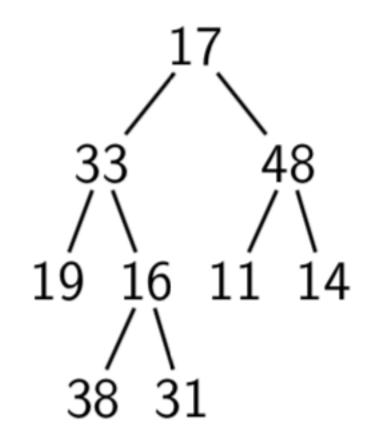
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(48)
PostorderTraverse(17)
Call Stack



Visit order: 19 38 31 16 33

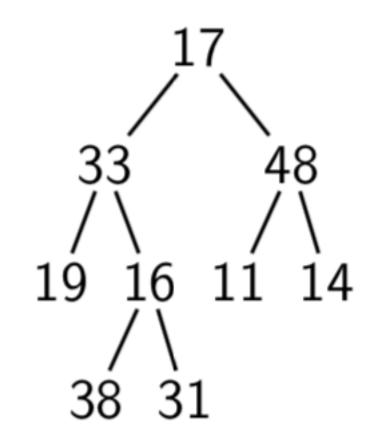
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(11)

PostorderTraverse(48)

PostorderTraverse(17)



Visit order: 19 38 31 16 33

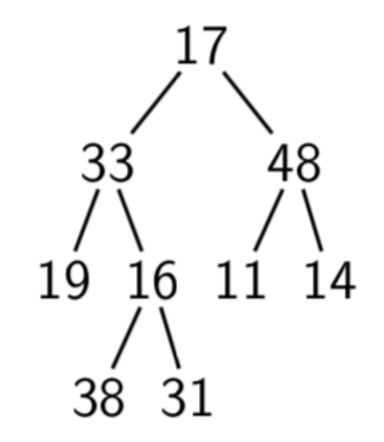
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)
visit T.root

Add WeChat powcoder



PostorderTraverse(11)

PostorderTraverse(48)

PostorderTraverse(17)

Call Stack

(...skipping the calls to PostorderTraverse(null)...)



Visit order: 19 38 31 16 33 11

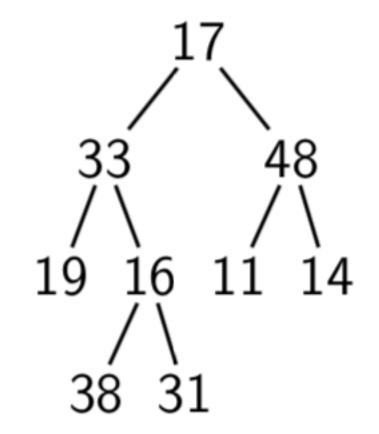
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.root



PostorderTraverse(11)

PostorderTraverse(48)

PostorderTraverse(17)

Call Stack

Add WeChat powcoder



Visit order: 19 38 31 16 33 11

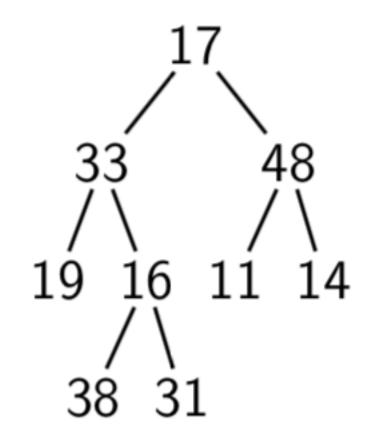
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(48)
PostorderTraverse(17)
Call Stack



Visit order: 19 38 31 16 33 11

procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.root

PostorderTraverse(14)

PostorderTraverse(48)

PostorderTraverse(17)

Call Stack

Add WeChat powcoder



Visit order: 19 38 31 16 33 11

procedure PostorderTraverse(T)

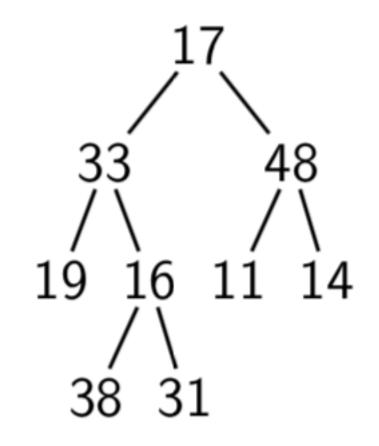
if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

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PostorderTraverse(14)

PostorderTraverse(48)

PostorderTraverse(17)

Call Stack

(...skipping the calls to PostorderTraverse(null)...)



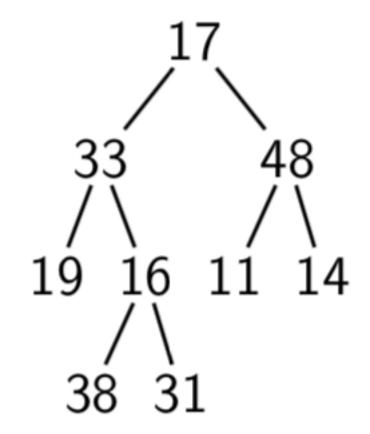
Visit order: 19 38 31 16 33 11 14

procedure PostorderTraverse(T)
if $T \neq null$ then
PostorderTraverse(T.left)

Postorder Traverse (T.left)
Assignment Project Exam Help
Postorder Traverse (T.right)

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PostorderTraverse(14)

PostorderTraverse(48)

PostorderTraverse(17)



Visit order: 19 38 31 16 33 11 14

procedure Postorder Traverse(T)

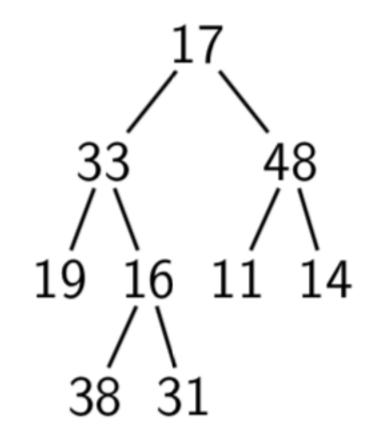
if $T \neq null$ then

Postorder Traverse(T.left)

Assignment Project Exam Help
Postorder Traverse(T.right

visit T.roothttps://powcoder.com

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PostorderTraverse(48)

PostorderTraverse(17)



Visit order: 19 38 31 16 33 11 14 48

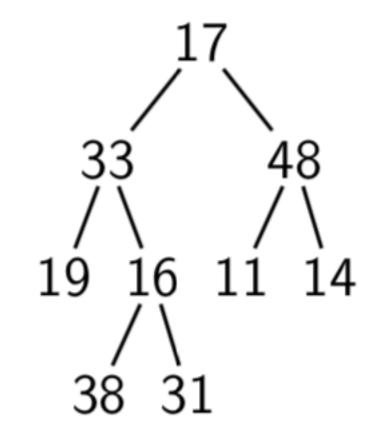
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help,
PostorderTraverse(T.right)

visit T.root



PostorderTraverse(48)
PostorderTraverse(17)
Call Stack

Add WeChat powcoder



Visit order: 19 38 31 16 33 11 14 48

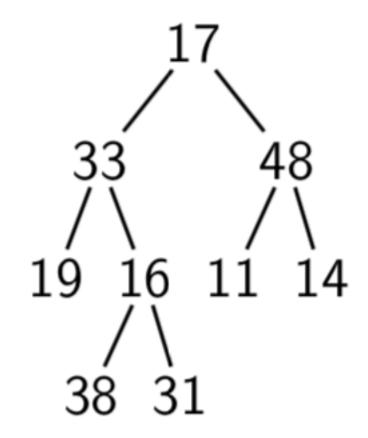
procedure PostorderTraverse(T)

if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.rootAdd WeChat powcoder



PostorderTraverse(17)

Call Stack



Visit order: 19 38 31 16 33 11 14 48 17

procedure PostorderTraverse(T)

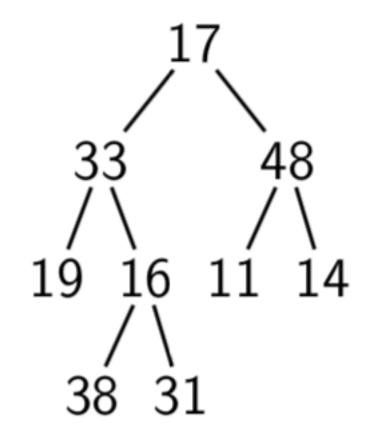
if $T \neq null$ then

PostorderTraverse(T.left)

Assignment Project Exam Help
PostorderTraverse(T.right)

visit T.root

Add WeChat powcoder



PostorderTraverse(17)

Call Stack



Visit order: 19 38 31 16 33 11 14 48 17

procedure PostorderTraverse(T)

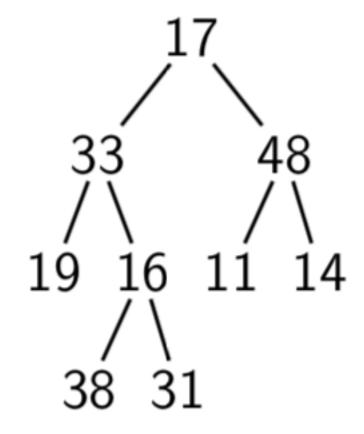
if $T \neq null$ then

PostorderTraverse(T.left)

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PostorderTraverse(T.right)

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Preorder Traversal Using a Stack



Explicitly maintain a stack of nodes

```
push(T)
while the stack is non-empty do

    T ← pop
visit T.root Assignment Project Exam Help
if T.right is non-teps://pyvthoen.com
    push(T.right) dd WeChat powcoder

if T.left is non-empty then
    push(T.left)
```

 In an implementation, the elements placed onto the stack would not be whole trees, but **pointers** to the corresponding internal nodes

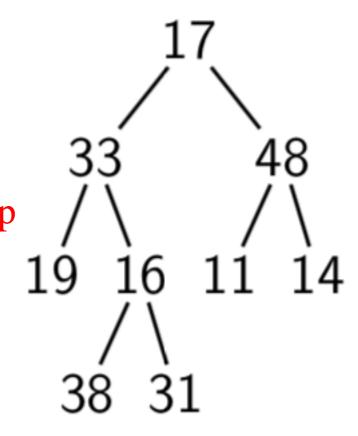


Replace the stack with a queue

```
inject(T)
while the queue is non-empty do

T \leftarrow eject
visit T.root
Assignment Project Exam Help
if T.left is non-empty powcoder.com
    inject(T.left)Add WeChat powcoder

if T.right is non-empty then
    inject(T.right)
```

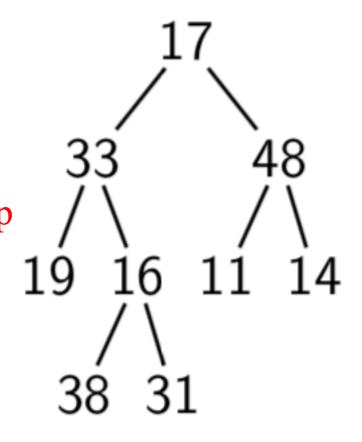


Queue:



Replace the stack with a queue

```
inject(T)
while the queue is non-empty do
    T \leftarrow eject
   visit T.root Assignment Project Exam Help
   if T. left is non-empty powceder.com
       inject( T.left)Add WeChat powcoder
   if T.right is non-empty then
       inject(T.right)
```



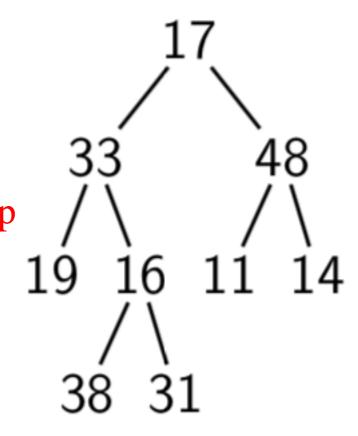
Queue:



Replace the stack with a queue

```
inject(T)
while the queue is non-empty do
    T \leftarrow eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\text{Add WeChat powcoder}

    if T.right is non-empty then
        inject(T.right)
```



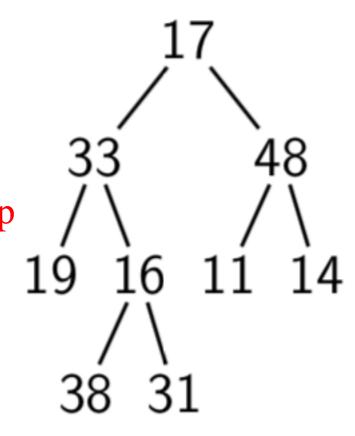
Queue:



Replace the stack with a queue

```
inject(T)
while the queue is non-empty do
    T \leftarrow eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\text{Add WeChat powcoder}

    if T.right is non-empty then
        inject(T.right)
```



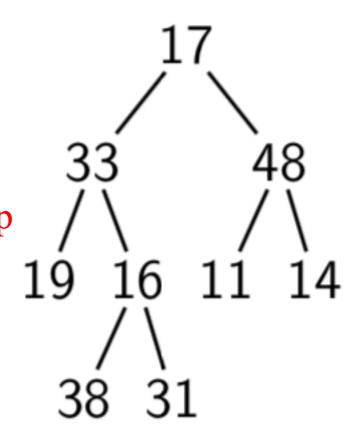
Queue:



Replace the stack with a queue

```
inject(T)
while the queue is non-empty do
    T \leftarrow eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\text{Add WeChat powcoder}

    if T.right is non-empty then
        inject(T.right)
```



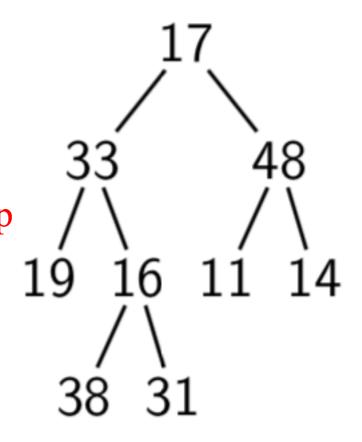
Queue: 33



Replace the stack with a queue

```
inject(T)
while the queue is non-empty do
    T \leftarrow eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty powcoder.com
        inject(T.left)\text{Add WeChat powcoder}

    if T.right is non-empty then
        inject(T.right)
```



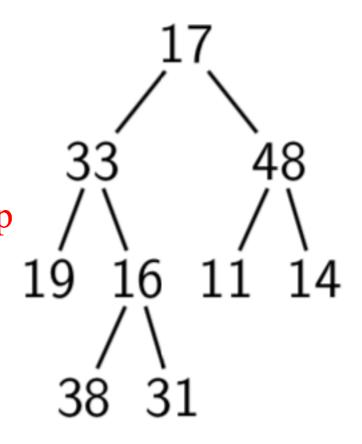
Queue: 33 48



Replace the stack with a queue

```
inject(T)
while the queue is non-empty do
    T \leftarrow eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty Then
        inject(T.left)\dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



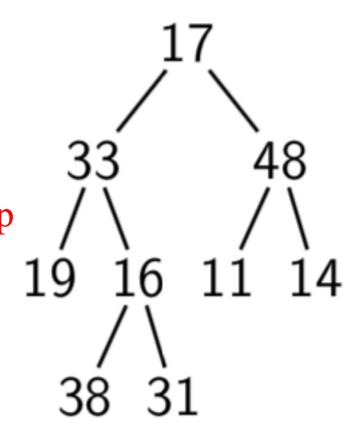
Queue: 48



Replace the stack with a queue

```
inject(T)
while the queue is non-empty do
    T \leftarrow eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty Then
        inject(T.left)\dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



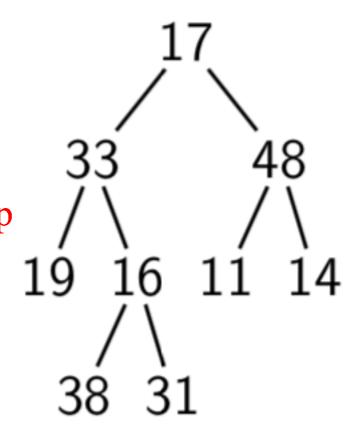
Queue: 48



Replace the stack with a queue

```
inject(T)
while the queue is non-empty do
    T \leftarrow eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty Then
        inject(T.left)\dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



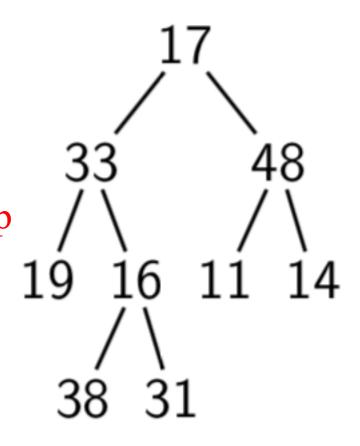
Queue: 48 19



Replace the stack with a queue

```
inject(T)
while the queue is non-empty do
    T \leftarrow eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



Queue: 48 19 16

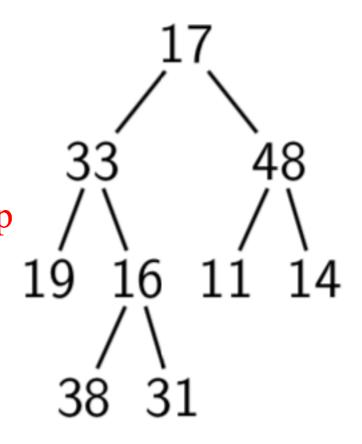


Replace the stack with a queue

```
inject(T)
while the queue is non-empty do

T \leftarrow eject
visit T.root
Assignment Project Exam Help
if T.left is non-empty Then
inject(T.left)\text{Add WeChat powcoder}

if T.right is non-empty then
inject(T.right)
```



Queue: 19 16

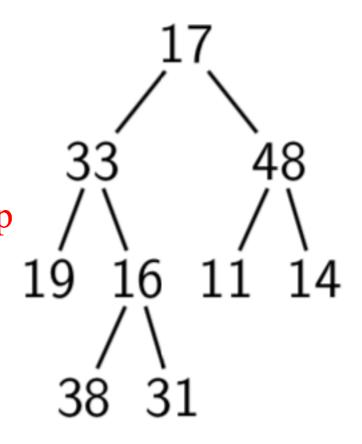


Replace the stack with a queue

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inject(T)
while the queue is non-empty do

    T ← eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left) dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



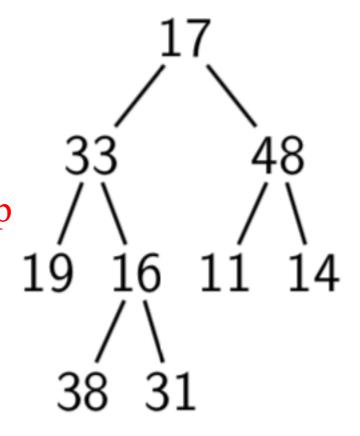
Queue: 19 16



Replace the stack with a queue

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inject(T)
while the queue is non-empty do
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    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\dd WeChat powcoder

if T.right is non-empty then
        inject(T.right)
```



Queue: 19 16 11

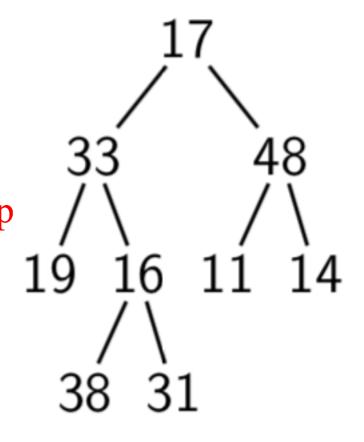


Replace the stack with a queue

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inject(T)
while the queue is non-empty do

    T ← eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\( \) dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



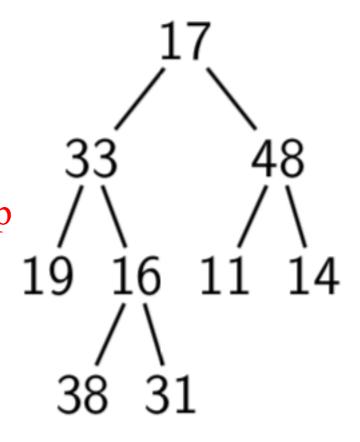
Queue: 19 16 11 14



Replace the stack with a queue

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inject(T)
while the queue is non-empty do
    T \leftarrow eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



Queue: 16 11 14



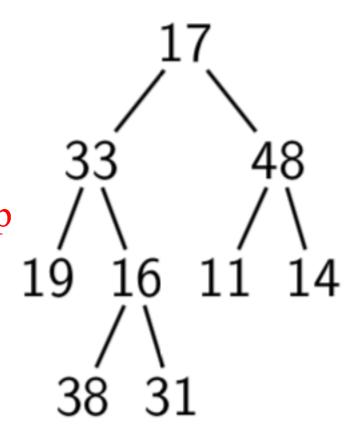
Replace the stack with a queue

```
inject(T)
while the queue is non-empty do

T \leftarrow eject
    visit T.root
    Assignment Project Exam Help

if T.left is non-empty Then
    inject(T.left)\text{Add WeChat powcoder}

if T.right is non-empty then
    inject(T.right)
```



Queue: 16 11 14

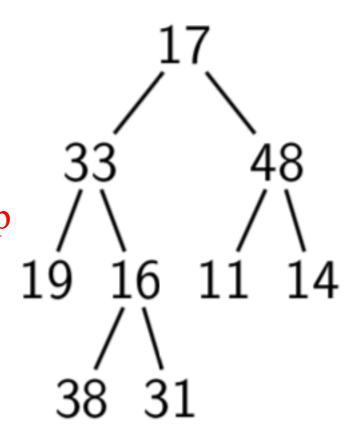


Replace the stack with a queue

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inject(T)
while the queue is non-empty do

    T ← eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\( \) dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



Queue: 11 14



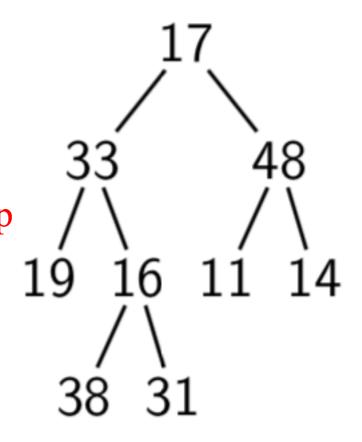
Replace the stack with a queue

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    visit T.root
    Assignment Project Exam Help

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    inject(T.left)\text{Add WeChat powcoder}

if T.right is non-empty then
    inject(T.right)
```



Queue: 11 14

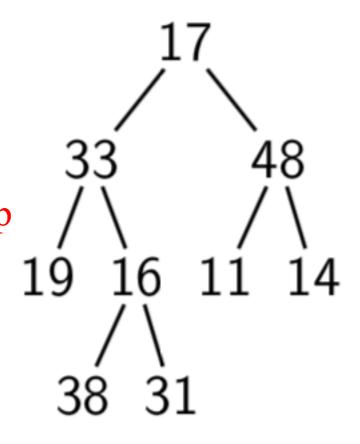


Replace the stack with a queue

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Assignment Project Exam Help
if T.left is non-empty then
inject(T.left) Add WeChat powcoder

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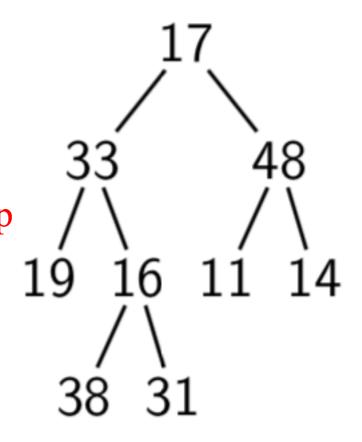
Queue: 11 14 38



Replace the stack with a queue

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    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



Queue: 11 14 38 31

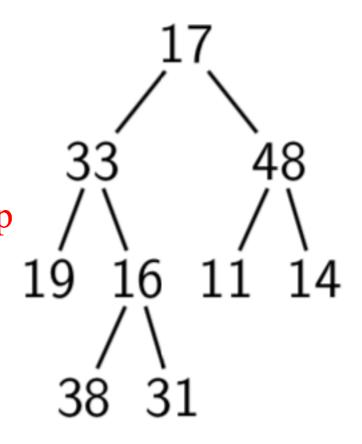


Replace the stack with a queue

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Assignment Project Exam Help
if T.left is non-empty powceder.com
    inject(T.left) Add WeChat powcoder

if T.right is non-empty then
    inject(T.right)
```



Queue: 14 38 31

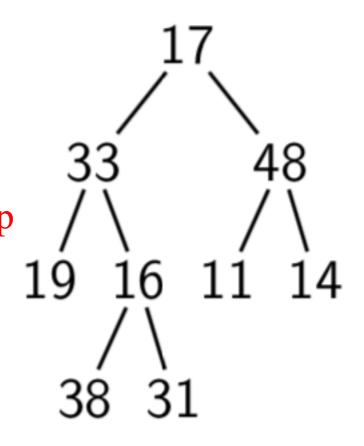


Replace the stack with a queue

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    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\( \) dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



Queue: 14 38 31

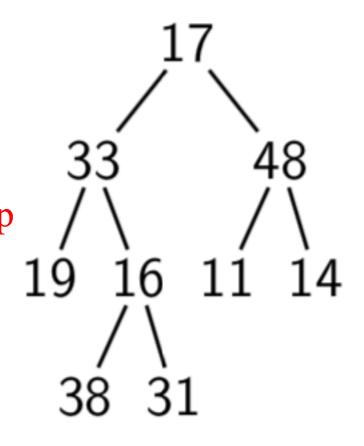


Replace the stack with a queue

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    Assignment Project Exam Help
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        inject(T.left)\( \) dd WeChat powcoder

    if T.right is non-empty then
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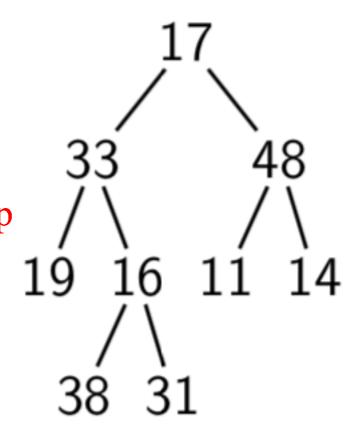
Queue: 38 31



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```



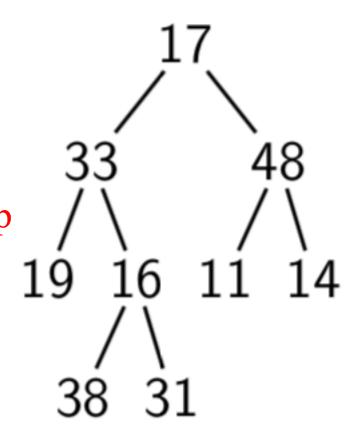
Queue: 38 31



Replace the stack with a queue

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    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\dd WeChat powcoder

if T.right is non-empty then
        inject(T.right)
```



Queue: 31

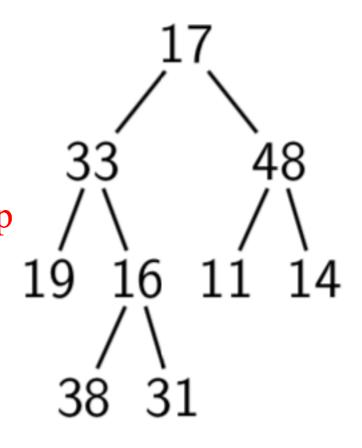


Replace the stack with a queue

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inject(T)
while the queue is non-empty do

    T ← eject
    visit T.root
    Assignment Project Exam Help
    if T.left is non-empty then
        inject(T.left)\( \) dd WeChat powcoder

    if T.right is non-empty then
        inject(T.right)
```



Queue: 31

Traversal order: 17 33 48 19 16 11 14 38

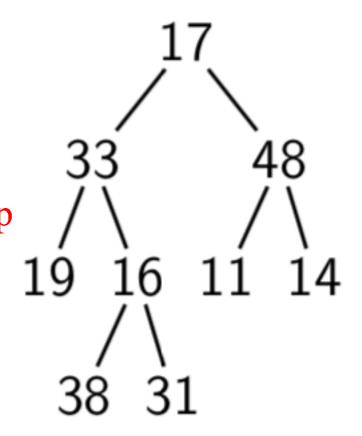


Replace the stack with a queue

```
inject(T)
while the queue is non-empty do

T \leftarrow eject
visit T.root
Assignment Project Exam Help
if T.left is non-empty powcoder.com
    inject(T.left)Add WeChat powcoder

if T.right is non-empty then
    inject(T.right)
```



Queue:

Traversal order: 17 33 48 19 16 11 14 38



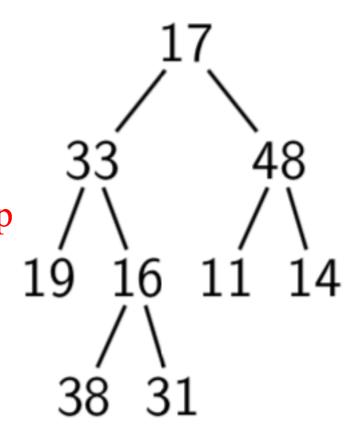
Replace the stack with a queue

```
inject(T)
while the queue is non-empty do

T \leftarrow eject
visit T.root

Assignment Project Exam Help
if T.left is non-empty powereder.com
    inject(T.left)\text{Add WeChat powcoder}

if T.right is non-empty then
    inject(T.right)
```

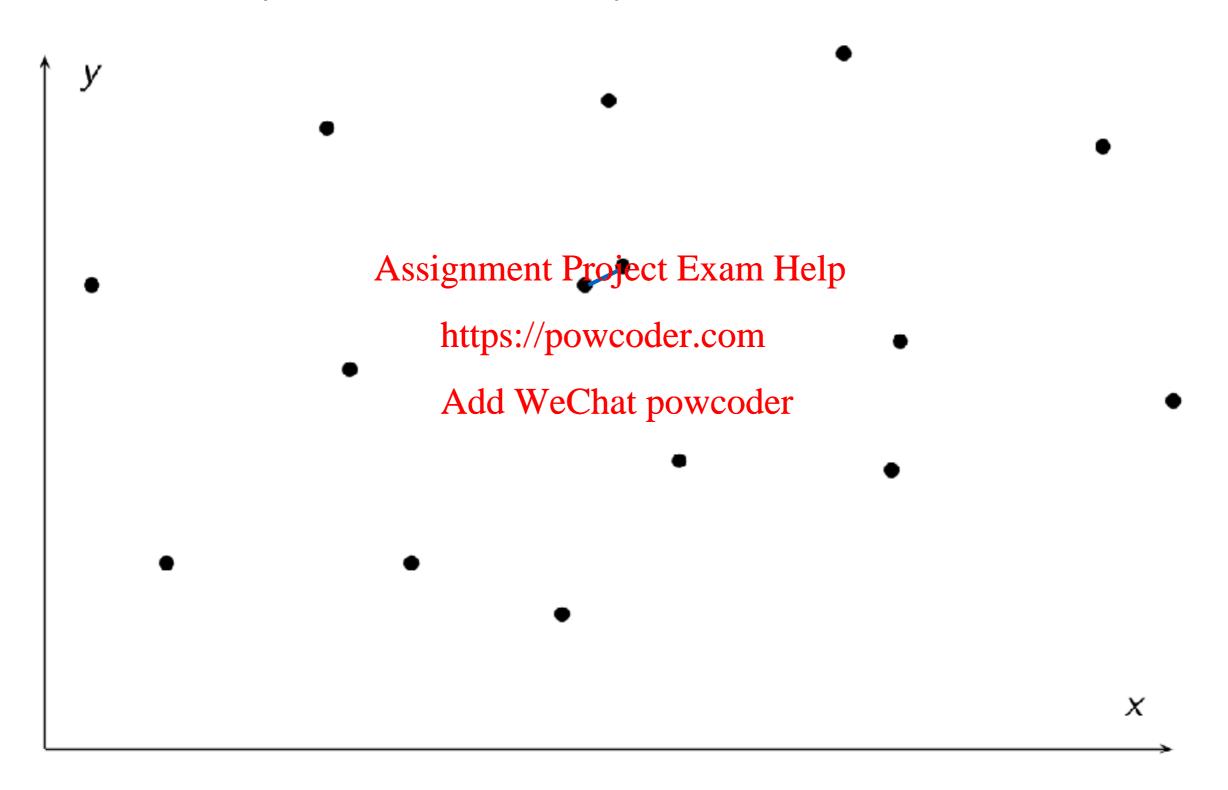


Queue:

Traversal order: 17 33 48 19 16 11 14 38 31

Closest Pair Problem (2D) Revisited (see Lecture 5)

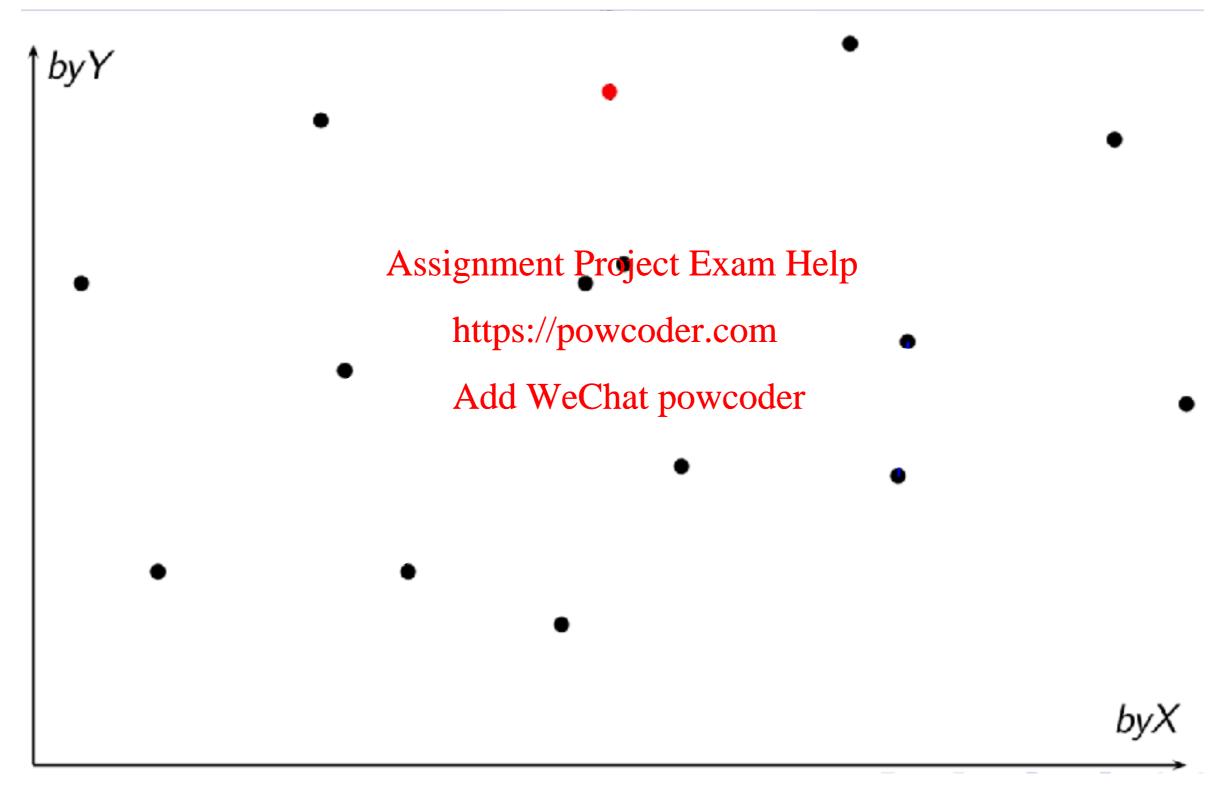




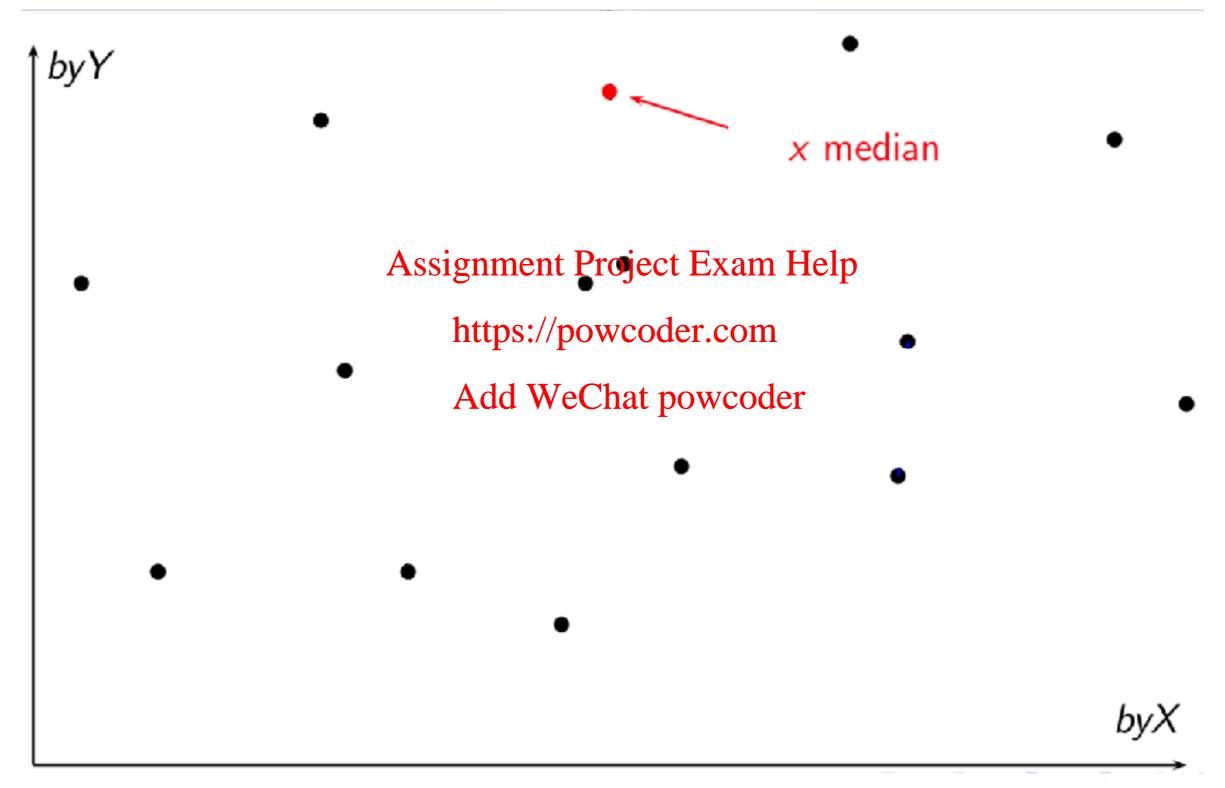


- In Lecture 5 we gave a brute-force algorithm for the closest pair problem: Given n points in the Cartesian plane, find a pair with minimal distance.
- The brute-force method had complexity Θ(n²). We can use divide-and-conquer to do better, namely Θ(n log n). https://powcoder.com
- First, sort the points by wealuepand store the result in array byX. Also sort the points by y value and store the result in array byY.
- Now we can identify the x median, and recursively process the set P_L of points with lower x values, as well as the set P_R with higher x values.

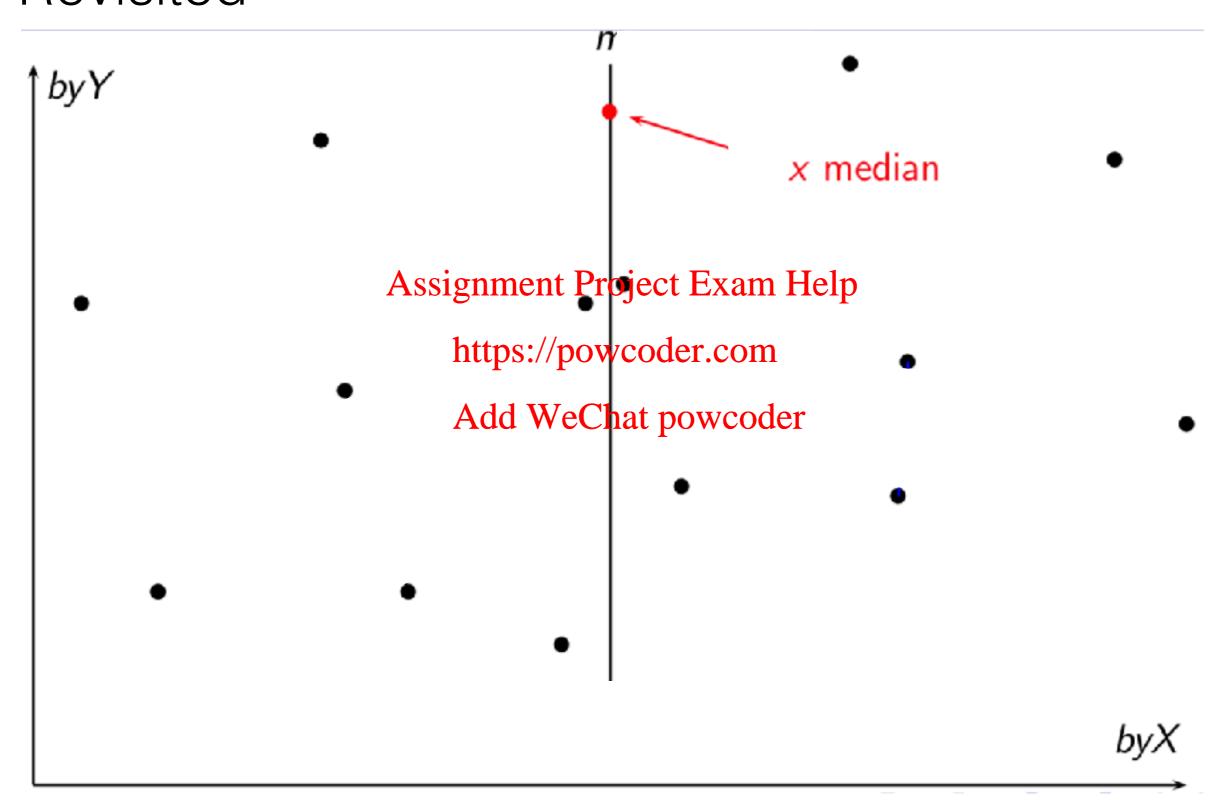




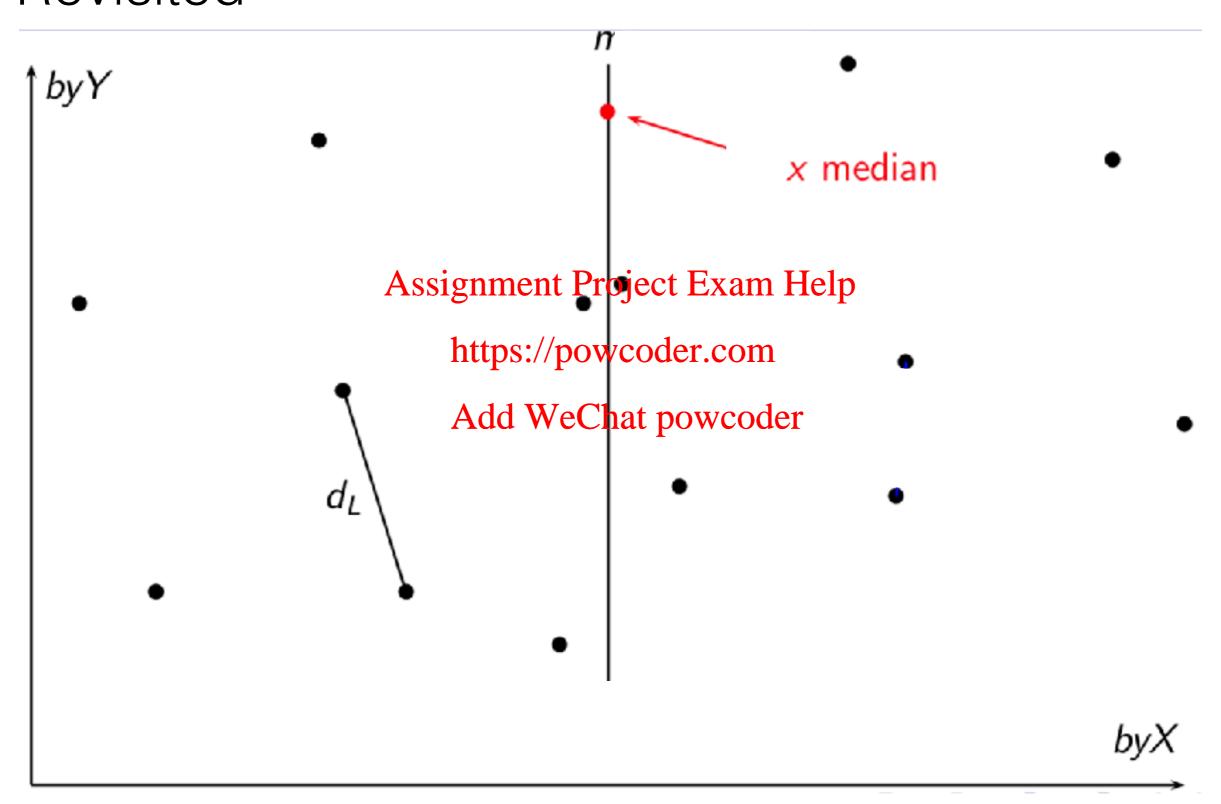




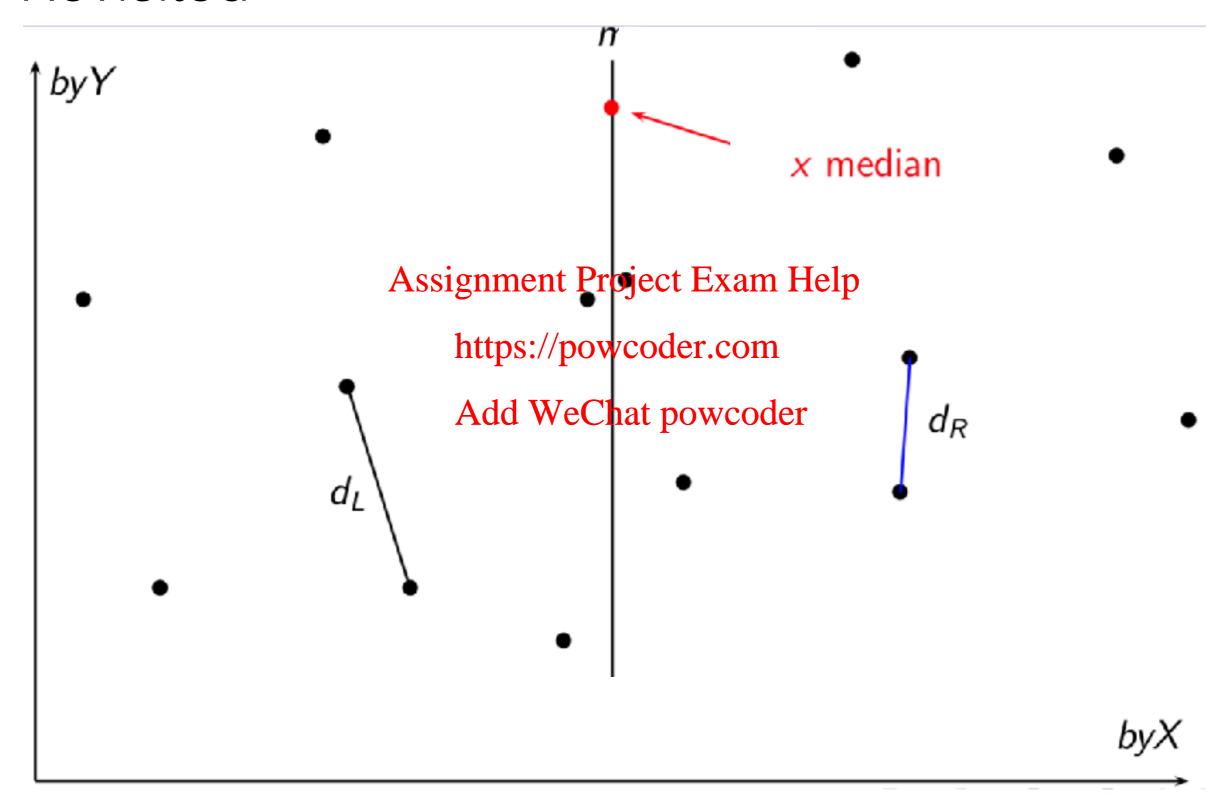




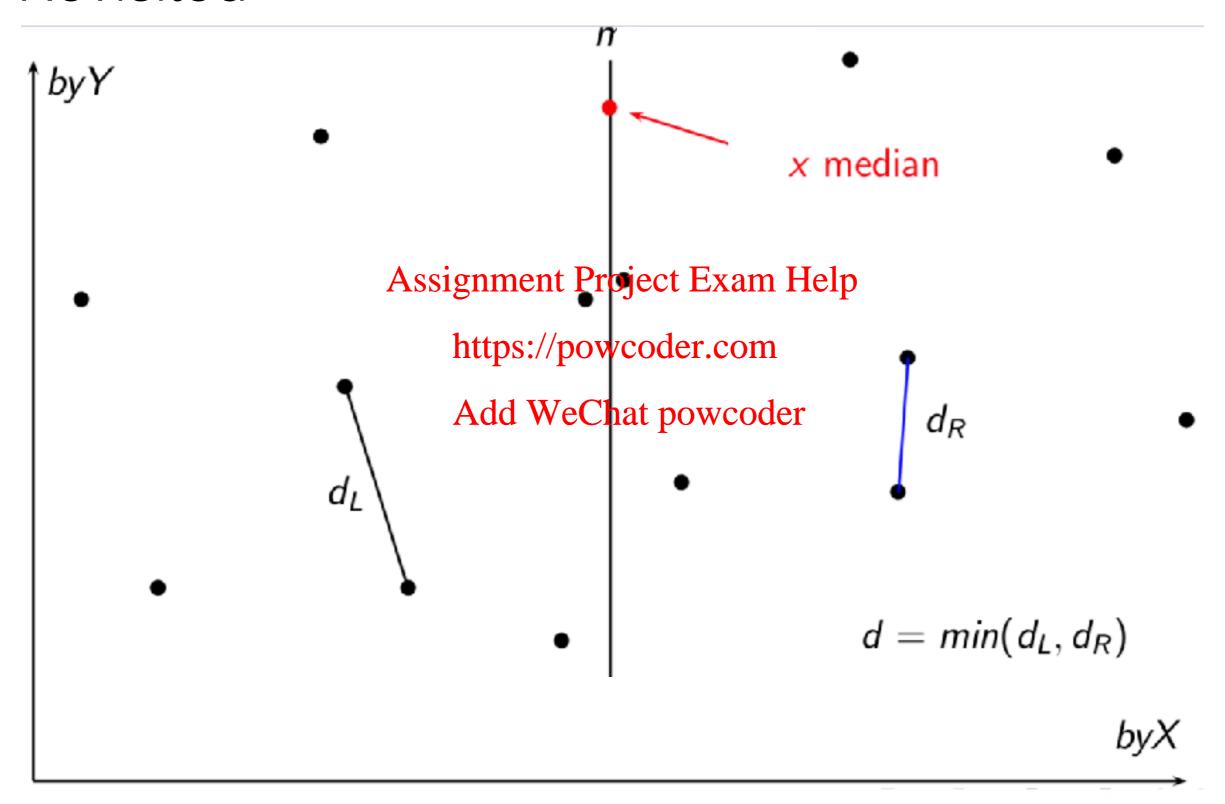




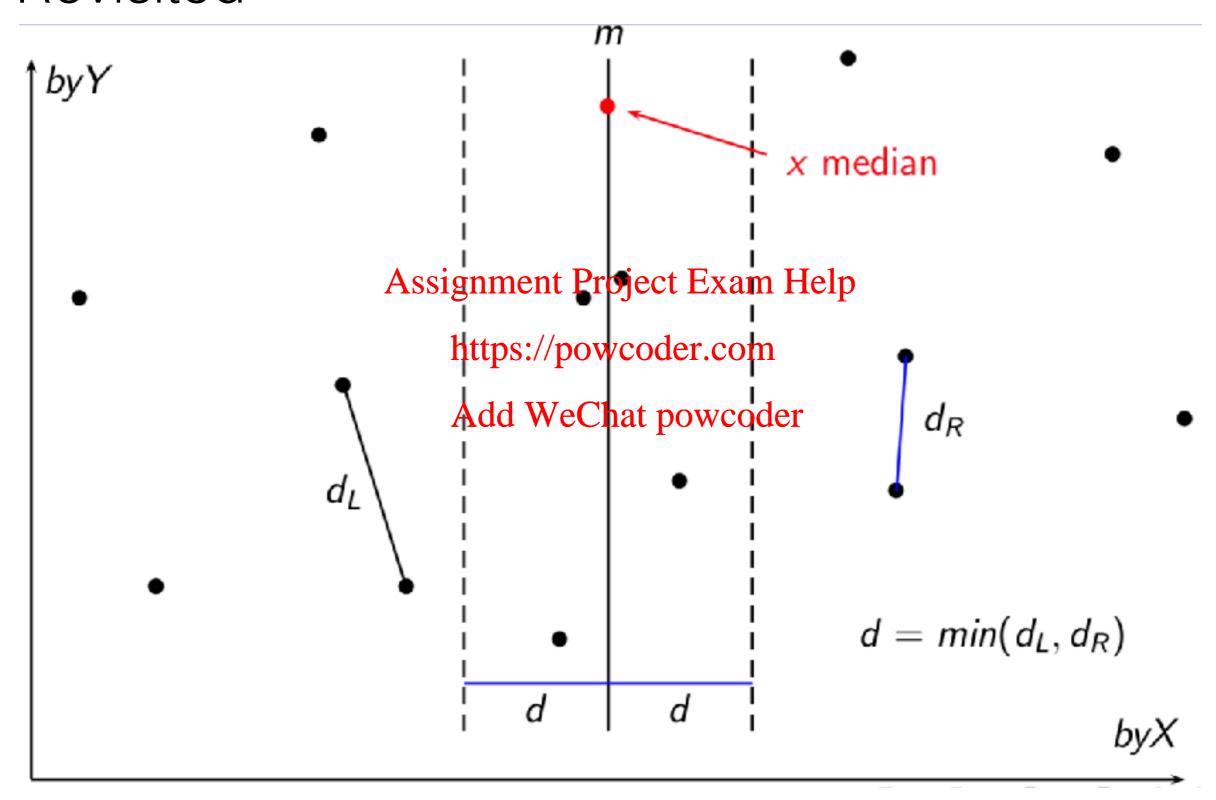














- The recursive calls will identify d_L , the shortest distance for pairs in P_L , and d_R , the shortest distance for pairs in P_R .
- Let m be the x median and let $d = min(d_L, d_R)$. This d is a candidate for the smallest distance.

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• But d may not be the global minimum—there could be some close pair whose points are of the posterior of the median line x = m.

Add WeChat powcoder

- For candidates that may improve on d we only need to look at those in the band $m d \le x \le m + d$.
- So pick out, from array byY, each point p with x-coordinate between m-d and m+d, and keep these in array S.
- For each point in S, consider just its "close" neighbours in S.



- The following calculates the smallest distance and leaves the (square of the) result in *minsq*.
- It can be shown that the while loop can execute **at mosts is times** for Each Helpalue—see diagram. https://powcoder.com

```
minsq \leftarrow d^2 Add WeChat powcoder copy all points of by Y with |x-m| < d to array S k \leftarrow |S| for i \leftarrow 0 to k-2 do j \leftarrow i+1 while j \leq k-1 and (S[j].y-S[i].y)^2 < minsq do minsq \leftarrow min(minsq, (S[j].x-S[i].x)^2 + (S[j].y-S[i].y)^2) j \leftarrow j+1
```

You're Learning Heaps!



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https://powcoder.com
 Next up: Priority queues, heaps and heapsort.
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