Tree-Structured Indexes

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Introduction

As for any index, 3 alternatives for data entries **k***:

- Data record with key value k
- <k, rid of data record with search key value k>
 <k, list of rids of data records with search key k>
- Choice is ofthogonal to the chnique used to locate data anties koder
- Tree-structured indexing techniques support both range searches and equality searches.
- ISAM: static structure; B+ tree: dynamic, adjusts gracefully under inserts and deletes.

Range Searches

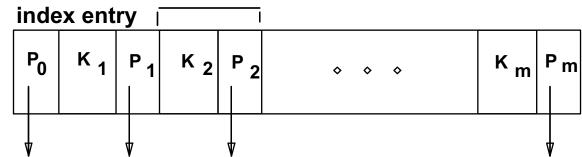
- "Find all students with gpa > 3.0"
 - If data is in sorted file, do binary search to find first such student, then scan to find others.
 - Cost of bisharyest areniestn Exemplified Prigh.

Simple idea: https://eowroodeamfile.

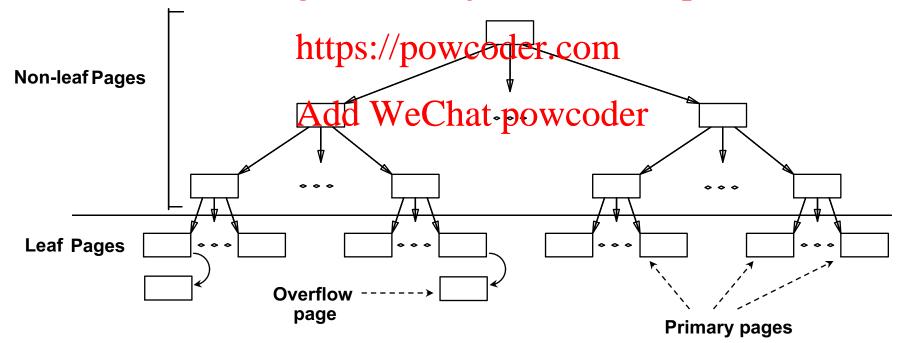


► Can do binary search on (smaller) index file!

ISAM (Indexed Sequential Access Method)



Index file may still be quite large. But we can apply the idea repeatedly! Assignment Project Exam Help



Leaf pages contain data entries.

Comments on ISAM

- File creation: Leaf (data) pages allocated sequentially, sorted by each key; then index pages allocated, then space for overflow pages.
- Index entries: <search key value, page id>; they 'direct' search spigmment Projection xam Help pages.
- Search: Start at root, use key comparisons to go to leaf. Cost = log F N Add WeChat powcoder
 F = # entries/index pg, N = # leaf pgs
- Insert: Find leaf data entry belongs to, and put it there.
- Delete: Find and remove from leaf; if empty overflow page, de-allocate.

► Static tree structure: *inserts/deletes affect only leaf pages*.

Data Pages

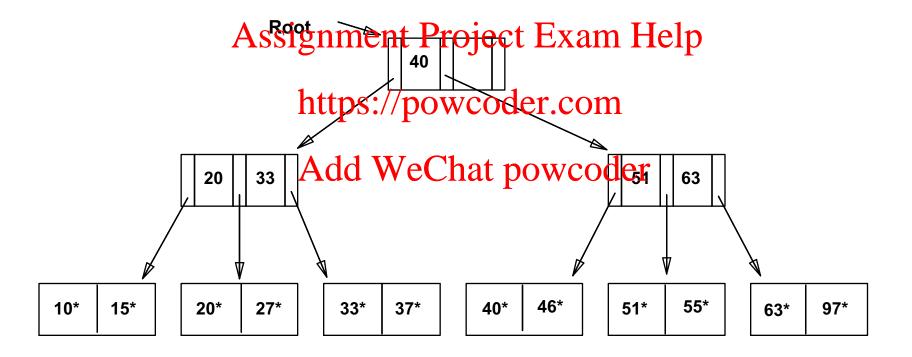
Index Pages

Overflow pages

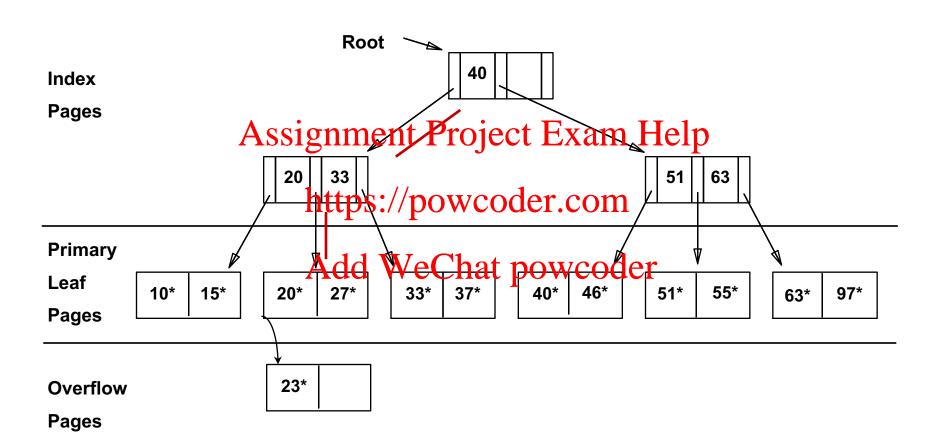
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Example ISAM Tree

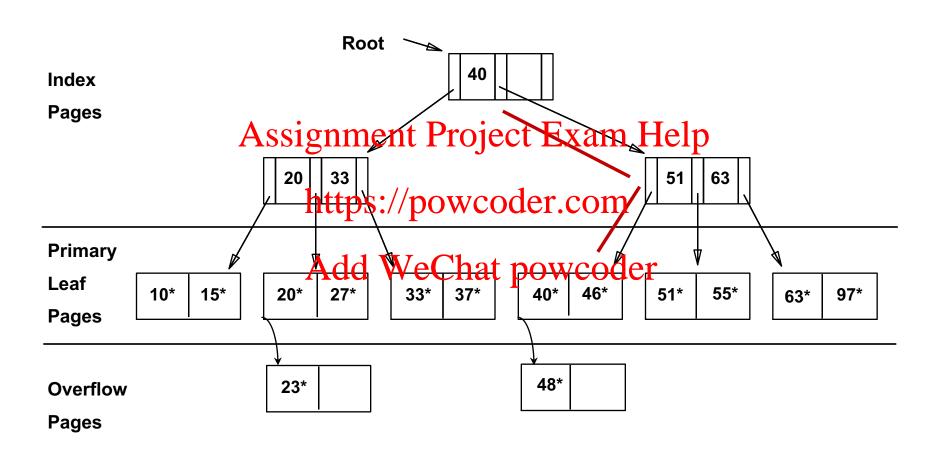
Each node can hold 2 entries; no need for `next-leaf-page' pointers. (Why?)



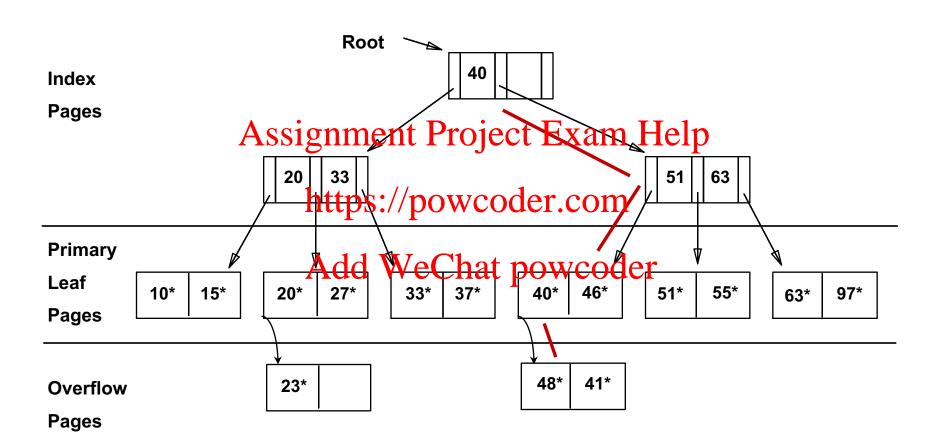
Inserting 23*



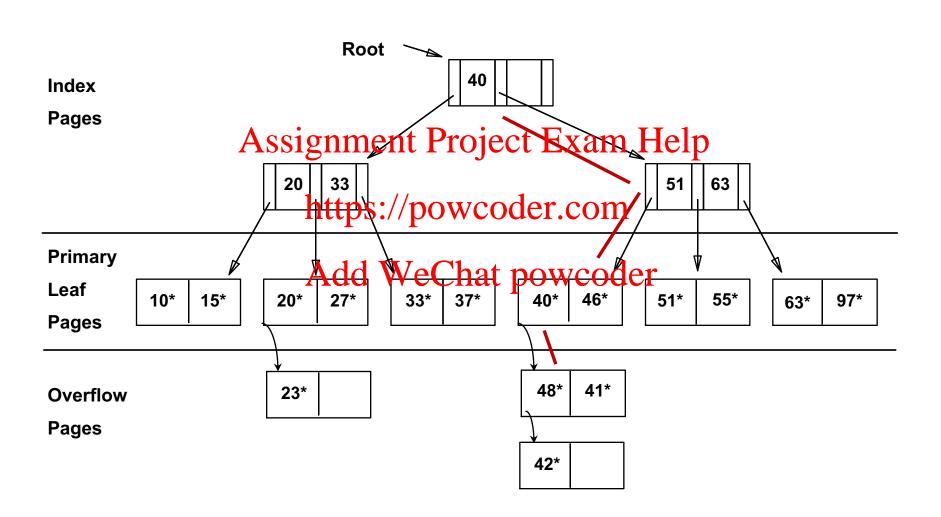
Inserting 48*



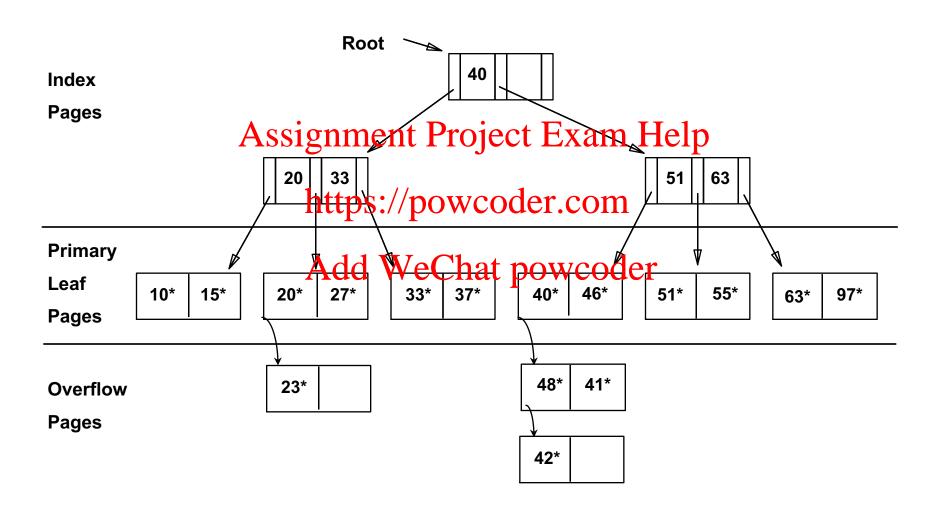
Inserting 41*



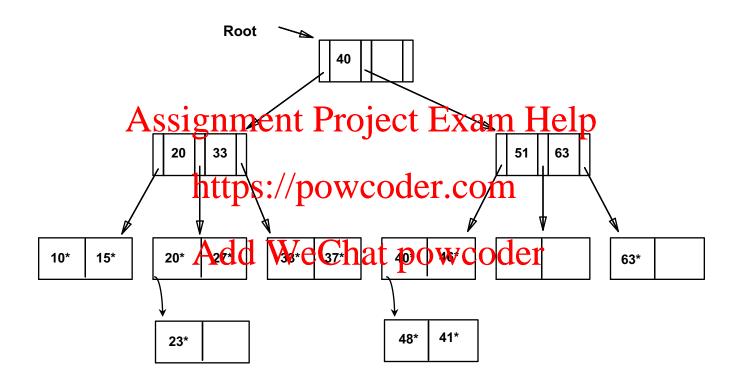
Inserting 42*



Then Deleting 42*, 51*, 97*,55*



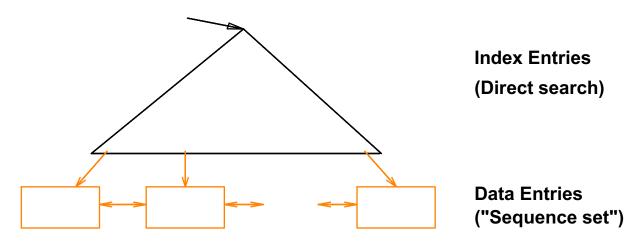
... After Deleting 42*, 51*, 97*, 55*



► Note that 51* appears in index levels, but not in leaf!

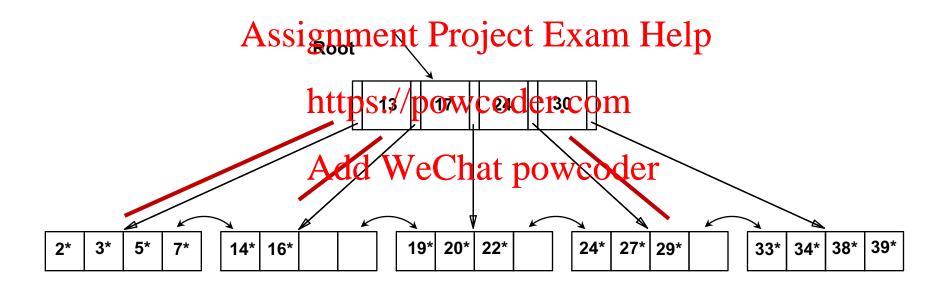
B+ Tree: Most Widely Used Index

- Insert/delete at log F N cost; keep tree height-balanced. (F = fanout, N = # leaf pages)
- Minimum 50% occupancy (except for root). Each node contaigs when the project 2 de mother
- The parameter d. is called the order of the tree.
- Supports equality and range-searches efficiently.
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Example B+ Tree

Search begins at root, and key comparisons direct it to a leaf. Search for 5^* , 15^* , all data entries $\ge 24^*$...



 \blacksquare Based on the search for 15*, we know it is not in the tree!

B+ Trees in Practice

Typical order: 100. Typical fill-factor: 67%.

– average fanout = 133

Typical capacities:

- Height 4: 1334 = 312,900,700 records
- Height 3: 1336ps://p2,952,637cettords

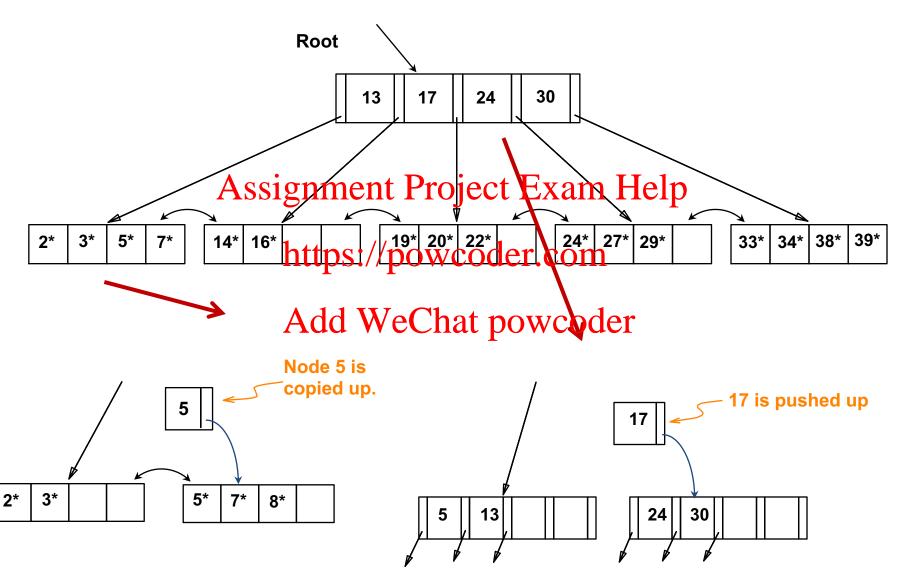
Can often hold top Wevellatin down the repool:

- Level 1 = 1 page = 8 Kbytes
- Level 2 = 133 pages = 1 Mbyte
- Level 3 = 17,689 pages = 133 MBytes

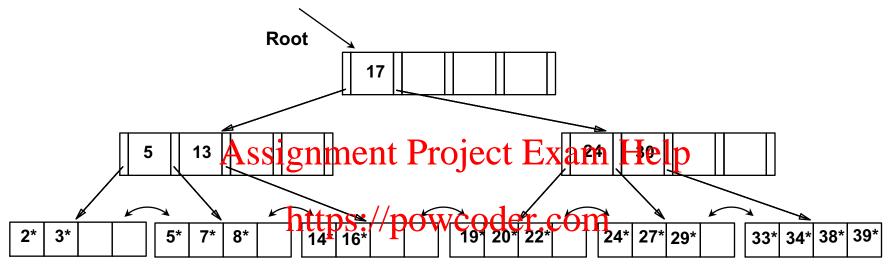
Inserting a Data Entry into a B+ Tree

- Find correct leaf *L*.
- Put data entry onto *L*.
 - If L has enough space, done!
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 Else, must split L (into L and a new node L2)
 - - Redistributetensi i peventy depoconmiddle key.
- Insert index entry pointing to L2 into parent of L.
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 This can happen recursively
 - To split index node, redistribute entries evenly, but push up middle key. (Contrast with leaf splits.)
- Splits "grow" tree; root split increases height.
 - Tree growth: gets <u>wider</u> or <u>one level taller at top.</u>

Inserting 8*



After Inserting 8*



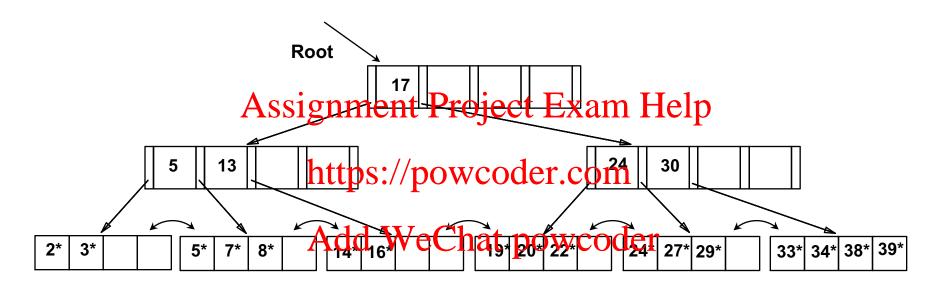
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- ❖ In this example, we can avoid split by re-distributing entries; however, this is usually not done in practice.
 - Redistributing I/O costs is not smaller than those of splitting.
 - It has a chance that redistributing does not work;
 thus costs for exploring redistribution are wasted.

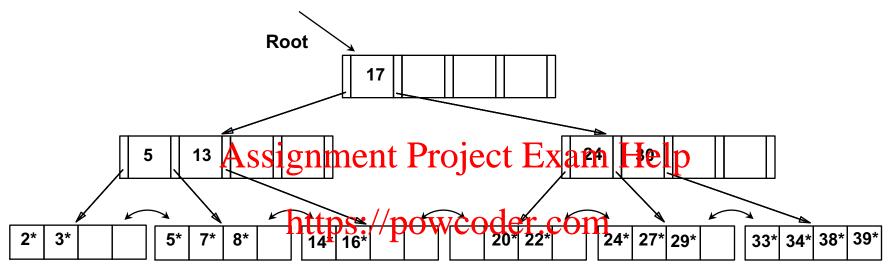
Deleting a Data Entry from a B+ Tree

- Start at root, find leaf L where entry belongs.
- Remove the entry.
 - If L is at leastigalf-full project Exam Help
 - If L has only **d-1** entries,
 - Try to re-distribute, borrowing from sibling (adjacent node with same parent as L).
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 If re-distribution fails, merge L and sibling.
- If merge occurred, must delete entry (pointing to L or sibling) from parent of L.
- Merge could propagate to root, decreasing height.

Deleting 19*

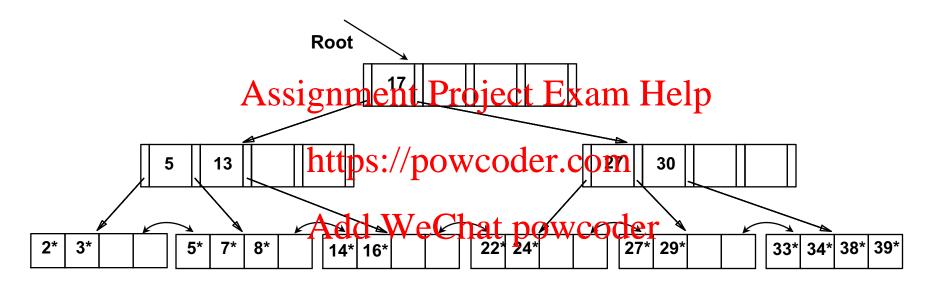


Deleting 20*



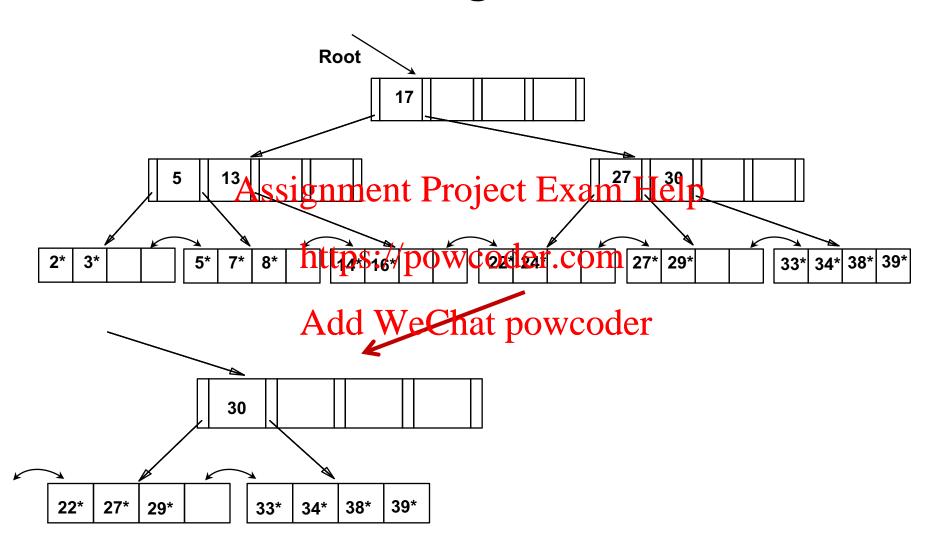
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After Deleting 20* ...

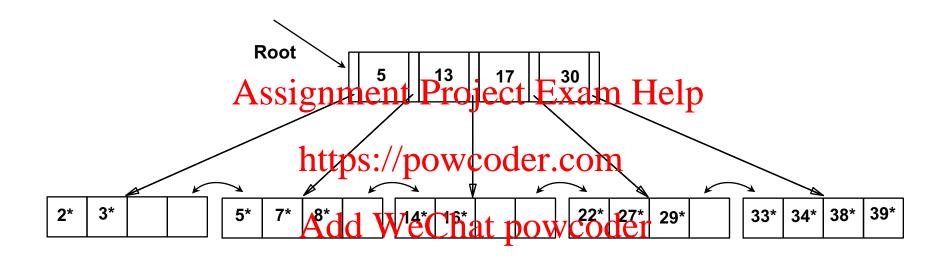


Deleting 20* is done with re-distribution. Notice how middle key is *copied up*.

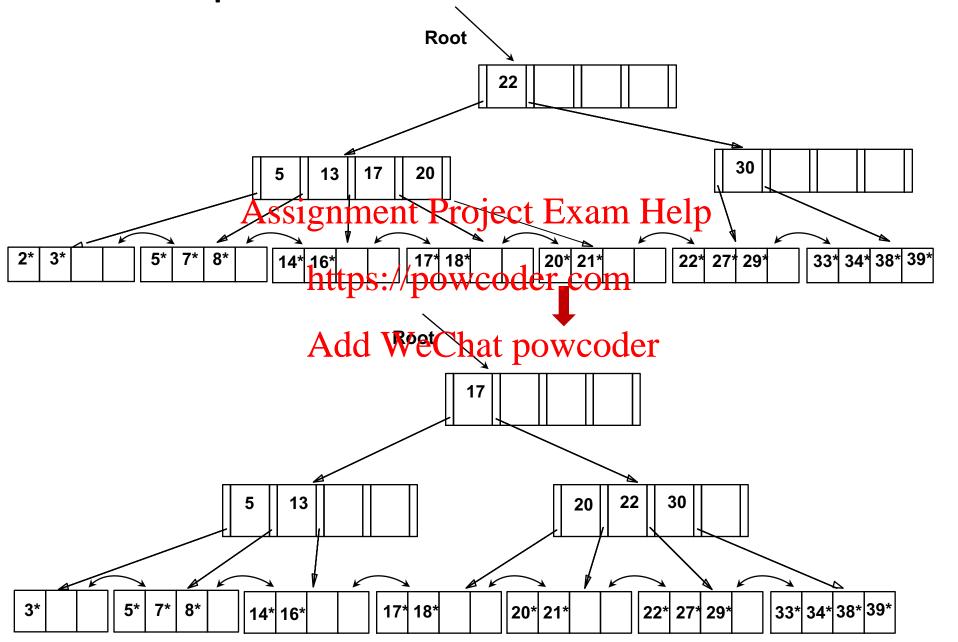
Deleting 24* ...



After Deleting 24*



Example of Non-leaf Re-distribution

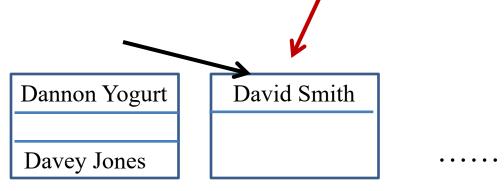


Prefix Key Compression

- Important to increase fan-out. (Why?)
- Key values in index entries only 'direct traffic'; can often compress them.
 - E.g., If we have adjacent index entries with search key values Dannon Yogurt; Bayid Smith to Dav. (The other keys can be compressed toohttps://powcoder.com

 Is this correct? Not quite! What if there is a data entry *Davey Jones*?
 - (Can only compress David Smith to Davi)
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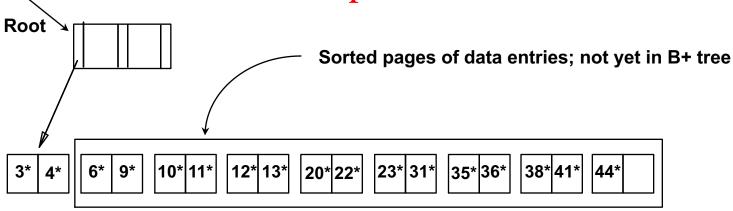
 In general, while compressing, must leave each index entry greater
 - than every key value (in any subtree) to its left.
- Insert/delete must be suitably modified.



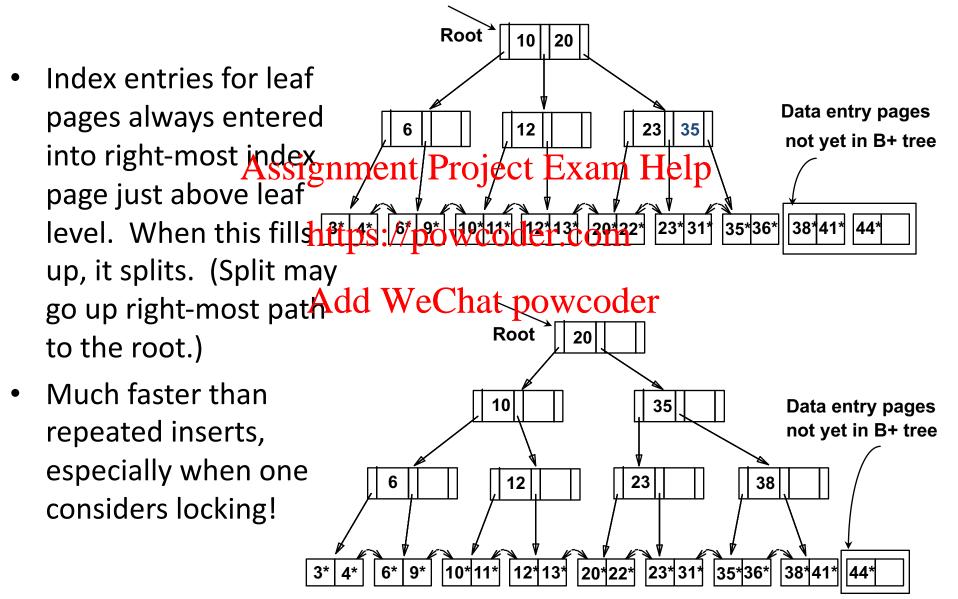
Bulk Loading of a B+ Tree

- If we have a large collection of records, and we want to create a B+ tree on some field, doing so by repeatedly inserting records is very slow.
- Bulk Loading can be done much more efficiently.
- Initialization: Sort all data entries, insert pointer to first (leaf) page in a new (root) page.

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Bulk Loading (Contd.)



Summary of Bulk Loading

Option 1: multiple inserts.

- Slow.
- Does not give sequential storage of leaves.
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 Option 2: <u>Bulk Loading</u>

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 Has advantages for concurrency control.
- Fewer I/Os addny buttet powcoder
- Leaves will be stored sequentially (and linked, of course).
- Can control "fill factor" on pages.

A Note on 'Order'

Order (d) concept replaced by physical space criterion in practice (`at least half-full').

- Index pagesigamteptchtojbotdmany holpe entries than leaf pages.
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 Variable sized records and search keys mean differnt nodes will contain wiffen the trum to the contain with the contai
- Even with fixed length fields, multiple records with the same search key value (*duplicates*) can lead to variable-sized data entries (if we use Alternative (3)).

Summary

Tree-structured indexes are ideal for range-searches, also good for equality searches.

ISAM is a static structure ject Exam Help

- Only leaf pages modified; overflow pages needed.
- Overflow chains can degrade performance unless size of data set and data distribution stay constant.

B+ tree is a dynamic structure.

- Inserts/deletes leave tree height-balanced; log F N cost.
- High fanout (F) means depth rarely more than 3 or 4.
- Almost always better than maintaining a sorted file.

Summary (Contd.)

- Typically, 67% occupancy on average.
- Usually preferable to ISAM, modulo locking consideration and the consideration of the consider
- If data entries are data records, splits can change rids!
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 Key compression increases fanout, reduces height.
- Bulk loading can be thuch faster than repeated inserts for creating a B+ tree on a large data set.
- Most widely used index in database management systems because of its versatility. One of the most optimized components of a DBMS.