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https://wei Wang @ CSE, UNSW Powcoder.com

Quadratic Form

- Let **A** be some $n \times n$ matrix.

What is Ax? What's the type of the output? What may x Assignment Project Exam Help

- E.g., what if $x_i \in \{0,1\}$? $x_i \in [0,1]$? $x_i \in \Re$?
- What is $\mathbf{x}^{\top} \mathbf{A} \mathbf{x}$? What's the type of the output? Why it is the type of the output? Why it is

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- What is $\mathbf{x}^{\top} \mathbf{A} \mathbf{x}$?, What's the type of the output? Why it is $\mathbf{x}^{\top} \mathbf{A} \mathbf{x} = \sum_{i,j} A_{ij} \cdot (x_i x_j)$

Unnormalized Graph Laplacian

 Let A is the adjacency matrix of a "normal" (unweighted) undirected graph G. $\mathbb V$ are the vertices of G and $\mathbb E$ are the

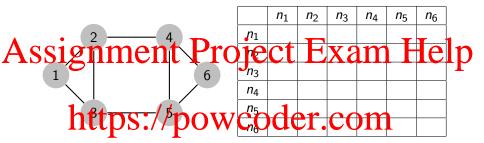
Assignment Project Exam, Help $A_{ii} = A_{ii} = 1$.

- \bullet $A_{ii} = ?$
- What about \mathbf{x}^{\top} bowcoder. com where $\mathbf{D} = \mathrm{Diag}(d_1, d_2, \dots, d_n)$ and
- $d_i = deg(v_i)$?
- Mat dout XX Chat powcoder

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• ℓ_2 differences between assignments on the two ends of an entropy of the coder.com

Example



- 1 is the one vector.
 Add Wie Chat powcoder 1
- $\mathbf{a} \mathbf{x}^{\mathsf{T}} \mathbf{I} \mathbf{x} =$

Binary \mathbf{x} induces a Clustering /1

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- x =
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Binary x induces a Clustering /2

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Min Cut vs. Normalized Cut

- Min cuts are not always desirable.
 - Biased towards cutting small sets of isolated nodes.

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- : And the week hat powcoder
 - $ncut(A, B) = \frac{cut(A, B)}{vol(A)} + \frac{cut(A, B)}{vol(B)},$

where
$$vol(A) = \sum_{v_i \in A} d_i) = \sum_{v_i \in A, v_j \in \mathbb{V}} w_{i,j}$$
.

Connection to L

$$ncut(A, B) = cut(A, B) \left(\frac{1}{vol(A)} + \frac{1}{vol(B)} \right)$$

Let $x_i = \frac{1}{vol(A)}$ if $v_i \in A$, and $= \frac{-1}{vol(B)}$ otherwise. Assignment Project Exam Help

• $\mathbf{x}^{\top} \mathbf{D} \mathbf{x} = (\mathbf{x}^{\top} D) \mathbf{x} = \sum_{F} d_{i} x_{i}^{2} =$ https://powcoder.com

 $Add \ \, \ \, \ \, \begin{matrix} \textit{ncut}(A,B) = \frac{\textbf{x}^{\top}\textbf{L}\textbf{x}}{\textbf{x}^{\top}\textbf{D}\textbf{x}} \\ \textit{Add WeChat powcoder} \end{matrix}$

Relaxation and Optimization

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- NP-hard to optimize under the discrete constraint.
- Relaxations grow the frasible region expand for the minimum value within the enlarged region.
 - allow **x** to be a real vector?
 - Yes, but too large.

 This live the constraint a plant of the property of the result of the property of the pro
- Solution: the second smallest eigenvector of the generalized eigen value problem $\mathbf{L}\mathbf{x} = \lambda \mathbf{D}\mathbf{x}$.
- Normalized Laplacian:

$$L' = D^{-\frac{1}{2}}(D - W)D^{-\frac{1}{2}} = I - D^{-\frac{1}{2}}WD^{-\frac{1}{2}}$$

Spectral Clustering Algorithm Framework

- Algorithm SC_recursive_bin_cut(data, k)
 - ullet Construct the weighted graph G
- ASSIGNATIVE the the special graph laplacian For Games Help new representation of vertices in a new 1-dimensional space (i.e., embedding).
 - Gluster the vertices in the embedding space according to the the function WCOGET.COM
 - For each cluster, recursively call the algorithm if more clusters are needed.

Spectral Clustering Algorithm Framework

- Algorithm SC_k_way_cut(data, k)
 - ullet Construct the weighted graph G
- ASSIGNATIVE the the special graph laplacian For Camphille power representation of vertices in a new t-dimensional space (i.e., embedding).
 - Cluster the vertices in the embedding space using another little of algorithm W. G. m. of COM

Notes on the Algorithms

 How to construct the weighted graph if only n objects are given?

Assignment, with the polarity or distance mong objects. Help of object o. One can also induce a sparse graph if one caps the raw weights by a threshold.

- Which believe we we we derive the state of the state of
 - Normalized graph laplacian $\mathbf{L} = \mathbf{D}^{-\frac{1}{2}}(\mathbf{D} \mathbf{W})\mathbf{D}^{-\frac{1}{2}}$.

Comments on Spectral Clustering

- Pros:
 - Usually better quality than other methods.

Assignment Project Exam Help Freedom to construct a (sparse) G to preserve local

- Freedom to construct a (sparse) G to preserve local similarity/connectivity.
- Only requires/some similarity measure.

 Could be inore dice wilding to the for high inersional sparse vectors (esp. if k-means is not fully optimized for such case).
- · Added Weer Surchat powcoder
 - Assumes clusters are of similar sizes.
 - Does not scale well with large datasets; but more scalable variants exist.
 - One of the relaxation of the original NP-hard problem may not be the tightest relaxation.