Assignment Project Exam Help COMP9318 Tutorial 2: Classification

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Consider the following training dataset and the original decision tree induction algorithm (ID3).

Risk is the class label attribute. The Height values have been already discretized into disjoint ranges.

SS to mation gair Other is thosen axthetis attribute 1p 2. Calculate the information gain if Height is chosen as the test attribute.

- 3. Draw the final decision tree (without any pruning) for the training dataset.
- 5. Draw the final decision tree (without any pruning) for the training dataset



Solution to Q1 I

1. The original entropy is $I_{Risk} = I(Low, Medium, High) = I(4, 8, 3) = 1.4566$. Consider *Gender*.

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The expected entropy is $\frac{9}{15} \cdot I(3,6,0) + \frac{6}{15} \cdot I(1,2,3) = 1.1346$. The information gain is 1/4566 - 1.1346 = 0.32202. Contain 19 St. / DOWCOGET.COM

Add We (1.5, 1.6] I(2, 0, 0) I(0, 0, 0, 0) I(0, 0, 0, 0)

The expected entropy is $\frac{2}{15} \cdot I(2,0,0) + \frac{2}{15} \cdot I(2,0,0) + \frac{3}{15} \cdot I(0,3,0) + \frac{4}{15} \cdot I(0,4,0) + \frac{2}{15} \cdot I(0,1,1) + \frac{2}{15} \cdot I(0,0,2) = 0.1333$. The information gain is 1.4566 - 0.1333 = 1.3233

Solution to Q1 II

- ID3 decision tree:
 - ▶ According to the computation above, we should first choose *Height* to split
 - After split, the only problematic partition is the (1.9, 2.0] one. However, the only remaining attribute Gender cannot divide them. As there is a draw, we have the light project Exam Help

https://powcoder.com The low low medium medium or high or hig

- ▶ **IF** $height \in (1.5, 1.6]$, **THEN** Rish = Low.
- ▶ **IF** $height \in (1.6, 1.7]$, **THEN** Rish = Low.
- ▶ **IF** $height \in (1.7, 1.8]$, **THEN** Rish = Medium.
- ▶ **IF** $height \in (1.8, 1.9]$, **THEN** Rish = Medium.
- ▶ **IF** $height \in (1.9, 2.0]$, **THEN** Rish = Medium (or High).
- ▶ **IF** $height \in (2.0, \infty]$, **THEN** Rish = High.

Consider applying the SPRINT algorithm on the following training dataset

Age

				J	
	23	family	High]	
Assignme	nt F	roie	High High	xam	Help
0	68	family	Low		1
	32	truck	Low		
1	, 20	family	→ High		
Answe The Downg	uest D.C)WCO	der.	com	

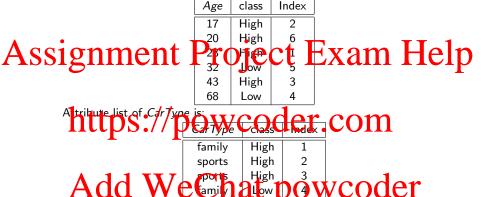
CarType

Risk

- 1. Write down the attribute lists for attribute Age and CarType, respectively.
- 2. Assume the first split criterion is Age < 27.5. Write down the attribute list for the left hid node (i.e. corresponding to the partition whose Age (c) (s)
- 3. Assume that the two attribute lists for the root node are stored in relational tables name AL_Age and AL_CarType, respectively. We can in fact generate the attribute lists for the child nodes using standard SQL statements. Write down the SQL statements which will generate the attribute lists for the left child node for the split criterion Age < 27.5.</p>
- 4. Write down the final decision tree constructed by the SPRINT algorithm.

Solution to Q2 I

► Attribute list of *Age* is:



truck

family

Attribute list of Age is:

Age	class	Index
17	High	2
20	High	6
23	High	1

I ow-

High

Solution to Q2 II

Attribute list of *CarType* is:

 CarType
 class
 Index

 family
 High
 1

 sports
 High
 2

 family
 High
 4

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FROM AL_Age

Specification of the Select C. CarType C. Class, C. Index

FROM AL_Age A, AL_CarType C

WHERE A.Age < 27.5

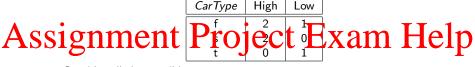
each of them have gini index value as:

0				
Age	above	below	gini _{split}	
17 – 20	(1, 0)	(3, 2)	0.40	
20 - 23	(2, 0)	(2, 2)	0.33	
23 - 32	(3, 0)	(1, 2)	0.22	
32 - 43	(3, 1)	(1, 1)	0.42	
43 – 68	(4, 1)	(0, 1)	0.27	

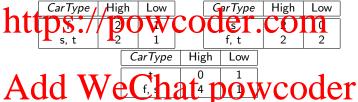
Solution to Q2 III

therefore, the best split should be Age > 27.5.

Consider the attribute list of CarType:



Consider all the possible cuts:



Each of them have gini index value as: 0.44, 0.33, 0.27, respectively. Therefore, the best split is CarType in ('truck').

Obviously, splitting on Age is better. Therefore, we shall split by Age > 27.5.

The attribute lists for each of the child node have already been computed. Since the tuples in the partition for Age < 27.5 are all "high", we only need to look at the partition for $Age \ge 27.5$.

Solution to Q2 IV

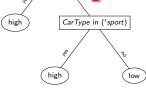
Age	class	Index
32	Low	5
43	High	3
68	Low	4

Assignment Project Land Help family Low truck I ow

> It is deficus that Car Trop in (sports) can immediately sut this partition into two pure partitions and thus will have as the girl index value. So we can skip a lot of calculations.

The final tree is:

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Consider a (simplified) email classification example. Assume the training dataset contains 1000 emails in total, 100 of which are spams.

A Salculate the class prior probability distribution. How would you classify a Salculate the class prior Project Exam Help 2. A Griend of you suggests that whether the email contains a \$ char is a

good feature to detect spam emails. You look into the training dataset and obtain the following statistics (\$ means emails containing a \$ and \$ are those not containing any \$}

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SPAM

Described (naive) Byes Classification phospilly no or precto

"evidence". How would this classifier predict the class label for a new incoming email that contains a \$ character?

3. Another friend of you suggest looking into the feature of whether the email's length is longer than a fixed threshold (e.g., 500 bytes). You obtain the following results (this feature denoted as $L(\bar{L})$).

60

https://powcoder.com How would a naive Bayes classifier predict the class label for a new incoming email that contains a \$ character and is shorter than the threshold?

SPAM

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$$P(SPAM) = \frac{100}{1000} = 0.10$$

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In order to build a (naïve) bayes classifier, we need to calculate (and store) the likelyhood of the feature for each class.

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Solution to Q3 II

To classify the new object, we calculate the posterior probability for both classes as:

Assignment
$$P(SPAM \mid X) = \frac{1}{P(X)} \cdot P(X \mid SPAM) \cdot P(SPAM)$$

$$= \frac{1}{P(X)} \cdot 0.91 \cdot 0.10 = \frac{1}{P(X)} \cdot 0.091$$

$$\text{https://powcoderm.comm}$$

$$= \frac{1}{P(X)} \cdot P(\$ \mid NOSPAM) \cdot P(NOSPAM)$$

$$= \frac{1}{P(X)} \cdot P(\$ \mid NOSPAM) \cdot P(NOSPAM)$$
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So the prediction will be SPAM.

3. The likelyhood of the new feature for each class is:

$\begin{array}{c} P(L \mid \text{SPAM}) & \frac{40}{100} \\ P(L \mid \text{NOSPAM}) & \frac{400}{900} \end{array}$	$\frac{1}{5} = 0.40$ $\frac{1}{5} = 0.44$
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Solution to Q3 III

(Note: we can easily obtain probabilities, e.g.,

 $P(\bar{L} \mid \mathtt{SPAM}) = 1 - P(\bar{L} \mid \mathtt{SPAM}) = 0.60)$

To classify the new object, we calculate the posterior probability for both classes as:

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$$= \frac{1}{P(X)} \cdot P(\$, \bar{L} \mid \text{SPAM}) \cdot P(\text{SPAM})$$

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$$=\frac{1}{P(X)} \cdot 0.60 \cdot 0.91 \cdot 0.10 = \frac{1}{P(X)} \cdot 0.055$$

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$$=\frac{1}{P(X)}\cdot P(\$, \bar{L}\mid \texttt{NOSPAM})\cdot P(\texttt{NOSPAM})$$

$$= \frac{1}{P(X)} \cdot P(\$ \mid \texttt{NOSPAM}) \cdot P(\bar{L} \mid \texttt{NOSPAM}) \cdot P(\texttt{NOSPAM})$$

$$= \frac{1}{P(X)} \cdot 0.56 \cdot 0.07 \cdot 0.90 = \frac{1}{P(X)} \cdot 0.035$$

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Based on the data in the following table,

1. estimate a Bernoulli Naive Bayes classifer (using the add-one smoothing)

3. estimate a multinomial Naive Bayes classifier (using the add-one smoothing)

4. apply the classifier to the test document

You do the sestimate the document.

docID words in decument			class = China?
training et	1	Vaiper Vaiwa Coll DOWC) (Car
	2	Macao Taiwan Shanghai	Yes
	3	Japan Sapporo	No
	4	Sapporo Osaka Taiwan	No
test set	5	Taiwan Taiwan Sapporo Bangkok	?

Solution to Q3 I

We use the following abbreviations to denote the words, i.e., TP = Taipei, TW = Taiwan, MC = Macao, SH = Shanghai, JP = Japan, SP = Sapporo, OS = Star Cherotabulary 10 1 CCT EX am Help 1. (Bernoulli NB) We take each word in the vocabulary as a

feature/attribute, and hence can obtain the following "rational" training

docID TF	P TW	МС	SH	JP	SP	os	class
5 0) 1	0	0	0	1	0	?

Solution to Q3 II

By looking at the test data, we calculate the *necessary* probabilities for the 'Y' class as (note that there are 2 possible values for each variable)

Assignment Project Exam Help $P(TP = 0|Y) = \frac{1+1}{2+2}$

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Add We $\bigcap_{P=0|Y}^{P(SH=0|Y)} \underbrace{p_{Q_1}^{1+1}}_{2+2}$ wcoder

$$P(SP = 1|Y) = \frac{0+1}{2+2}$$
$$P(OS = 0|Y) = \frac{2+1}{2+2}$$

```
P(Y|X) \propto P(Y) \cdot P(TP = 0|Y) \cdot P(TW = 1|Y) \cdot P(MC = 0|Y) \cdot P(SH = 0|Y)
= \frac{1}{2} \frac{1}{2} \frac{3}{4} \frac{1}{2} \frac{1}{2} \frac{3}{4} \frac{1}{4} \frac{3}{4} = \frac{27}{4096} \approx 0.0066
```

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We calculate the *necessary* probabilities for the 'N' class as

Assignment $\underset{P(TP)}{\text{Projec}} = \underbrace{\overset{2}{t}}_{N} = \underbrace{xam}$ Help

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$$P(SH = 0|N) = \frac{2+1}{2+2}$$

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$$P(SP = 1|N) = \frac{2+1}{2+2}$$
$$P(OS = 0|N) = \frac{1+1}{2+2}$$

Solution to Q3 V

Finally,

$$\begin{array}{c} Assignment(N) \sim P(N) \cdot P(TP = 0|N) \cdot P(TW = 1|N) \cdot P(MC = 0|N) \cdot P(SH = 0|N) \\ = \frac{1}{2} \frac{3}{4} \frac{1}{2} \frac{3}{4} \frac{1}{4} \frac{3}{2} \frac{1}{4} \frac{1}{2} = \frac{81}{4096} \approx 0.020 \end{array}$$

Therefore, doc 5 should belong to the 'No class, (Mallindaral NB) Work the meg Oceanienes

	Doc	class
A 11 TTT	TP TW MC TW SH	Y
Add W	ersphortwn	wcoder vocabulary (OOV) words
The testing document	is (ignoring the out-of-	-vocabulary (OOV) words

Bangkok):

Doc	class
TW TW TW SP	?

By looking at the test data, we calculate the necessary probabilities for the Assignment Project Exam Help

$$P(w_i = TW|Y) = \frac{2+1}{5+7}$$

 $https://powed = \frac{2+1}{5+7}$

FinAlly, dd We Chat poweder
$$P(w_{i} = TW|Y) \cdot P(w_{i} = TW|Y) \cdot P(w_{i} = TW|Y)$$

$$P(w_{i} = TW|Y) \cdot P(w_{i} = SP|Y)$$

$$= \frac{1}{2} \frac{1}{4} \frac{1}{4} \frac{1}{4} \frac{1}{12} = \frac{1}{1536} \approx 0.000651$$

We calculate the *necessary* probabilities for the 'Y' class as

Assignment $\Pr_{P(w_i = T_w|N) = \frac{2}{5+7}} \stackrel{?}{E} \times \text{xam Help}$

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Finally,

Add We C
$$\frac{1}{2}$$
 $\frac{1}{6}$ $\frac{1}{6}$ $\frac{1}{6}$ $\frac{1}{4}$ $\frac{1}{1728}$ ≈ 0.000579

Therefore, doc 5 should belong to the 'Yes' class.

- 1. First, we randomly obtained 47 training examples among which we have 22 negative instances (denoted as "-"), and 25 positive instances (denoted as "-"), and 25 positive instances (denoted as "-") that is purestimate of the probability that a novel test instance belongs to the positive class?
- 2. We then identify a feature x, and rearrange the 47 training examples based on their x wives the identities shown in the table below er

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	
Assignment Project E	xam Help
3 + 6	
https://powcoder.	com

count

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For each of the group of training examples with the same x value, compute its probability p_i and $logit(p) := log \frac{p}{1-p}$.

- 3. What is your estimate of the probability that a novel test instance belongs to the positive class if its x value is 1?
- 4. We can run a linear regression on the (x, logit) pairs from each group. Will this be the same as what Logistic Regression does?

	X	cnt(y=0)	cnt(y=1)	p	logit(p)
	1	6	2	0.250000	-1.098612
h ++	2	g • /5/	XX 200	1.285714	-0.916291
IIU	3	5.// DC)W ² CO	161538	0114151
	4	3 👢	7	0.700000	0.847298
	5	1	8	0.888889	2.079442

- 3. Praid We Chat powcoder
 4. Not the same. The main reason is that Ligistic regression will maximi
- 4. Not the same. The main reason is that Logistic regression will maximize the likelihood of the data, and this is in generally different from minimizing the SSE as in Linear Regression.

- ▶ Represent the vectors in the non-orthogonal bases $\mathcal{B} = \begin{pmatrix} 1 & 2 \\ 0 & -2 \end{pmatrix}$.
- Let Z_p be a vector Z represented in the polar coordinate: (p, θ) . What if white C_p ? Vii Z let P same as C_p ?
- Can you construct a matrix M such that its impact on vectors represented in polar coordinates exhibit "linearality"? i.e., M(x+y) = Mx + My? Add WeCnat powcoder

Assignment Project Exam Help $\binom{2}{3} = \mathcal{B}\mathbf{A}' \Rightarrow \mathbf{A}' = \binom{5}{1.5}$

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Obviously, we still have $\mathbf{C}' = \mathbf{A}' + \mathbf{B}'$.

- (Obivously) No.

$$\mathbf{X}_{n\times d} = \begin{pmatrix} \mathbf{o}_1 \\ \mathbf{o}_2 \\ \vdots \\ \mathbf{o}_m \end{pmatrix}$$
. Now we consider a linear projection $\mathbf{A}_{d\times m}$ of all the points to a m -dimersional space (m) which is projection $\mathbf{A}_{d\times m}$ of all the points to $\pi(o_i) = \mathbf{A}^{\top} \mathbf{o}_i$.

 $\begin{array}{c} \text{Computer } \mathit{r} \coloneqq \frac{\|\pi(o_i)\|^2}{\|o_i\|^2}. \text{ Can you guess what will be the maximum and} \\ \text{Minimum values of } e \text{Chat powcoder} \\ \end{array}$

Since

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Therefore
$$p_r = \frac{\|\pi(\mathbf{o})\|^2}{\|\mathbf{o}\|^2} = \frac{\mathbf{o} \cdot (\mathbf{A} \mathbf{A}^{\top})}{\mathbf{o}^{\top} \mathbf{o}}$$

Commert: The above is the haveleigh Quotient (c.f., its Wikipedia page) when \mathbf{A}^{TV} the maximum and minimum eigenvalues of M, respectively. This property is also used in the technical proof of the spectral clustering too (not required).