# COMP9318: Data Warehousing

and Data Mining Assignment Project Exam Help

— L2: Data Warehousing and OLAP — https://powcoder.com

Why and What are Data Warehouses?

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# Data Analysis Problems

- The same data found in many different systems
  - Example: customer data across different department Project Exam Help
  - The same concept is defined differently
- Heterogeneous sources
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   Relational DBMS, OnLine Transaction Processing (OLTP)
  - Unstructured data in files (e.g., MS Excel) and documents (e.g., MS Word)

# Data Analysis Problems (Cont'd)

- Data is suited for operational systems
  - Accounting, billing, etc.
  - Do not sepportent lysis across business functions
     https://powcoder.com
- Data quality is bad
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   Missing data, imprecise data, different use of
  - Missing data, imprecise data, different use of systems
- Data are "volatile"
  - Data deleted in operational systems (6months)
  - Data change over time no historical information

#### Solution: Data Warehouse

- Defined in many different ways, but not rigorously.
  - A decision support database that is maintained separately from the organization's operational database Assignment Project Exam Help
  - Support information processing by providing a solid platform of https://powcoder.com consolidated, historical data for analysis.
- "A data warehouse Aschale Limethaten ped violed eated, time-variant, and nonvolatile collection of data in support of management's decision-making process."—W. H. Inmon
- Data warehousing:
  - The process of constructing and using data warehouses

# Data Warehouse—Subject-Oriented

- Organized around major subjects, such as customer, product, sales.
- Focusing on the modeling and analysis of data for decision makers, not on httips of perations decision processing.
- Provide a simple and woncise view around particular subject issues by excluding data that are not useful in the decision support process.

# Data Warehouse—Integrated

- Constructed by integrating multiple, heterogeneous data sources
  - relational databases, flat files on-line transaction records

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- Data cleaning and data integration dechniques are applied.
  - Ensure consistency in naming conventions, encoding structures, attribute measures, etc. among different data sources
    - E.g., Hotel price: currency, tax, breakfast covered, etc.
  - When data is moved to the warehouse, it is converted.

#### Data Warehouse—Time Variant

- The time horizon for the data warehouse is significantly longer than that of operational systems.
  - Operational identification
  - Data warehouse data: provide information from a historical perspective (e.g., past 5-10 years)
- Every key structure in the data warehouse
  - Contains an element of time, explicitly or implicitly
  - But the key of operational data may or may not contain "time element".

#### Data Warehouse—Non-Volatile

- A physically separate store of data transformed from the operational environment.
- 2. Operation Alsupplante of that a clote smooth of the data warehouse environment. The worder of the late of the l
  - Does not require transaction processing, recovery, Add WeChat powcoder and concurrency control mechanisms
  - Requires only two operations in data accessing:
    - initial loading of data and access of data.

#### Data Warehouse Architecture

Extract data from operational data sources

clean, transform Monitoring & Admnistration Bulk load/refresh

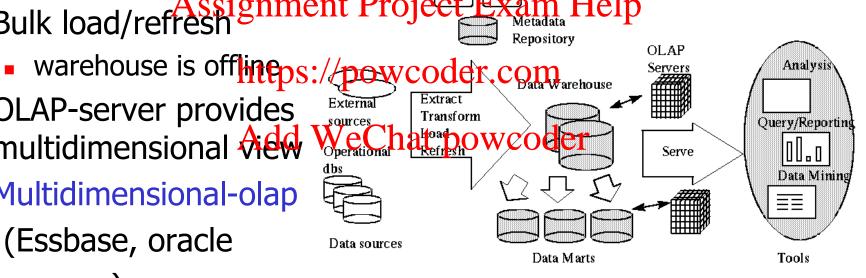
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OLAP-server provides

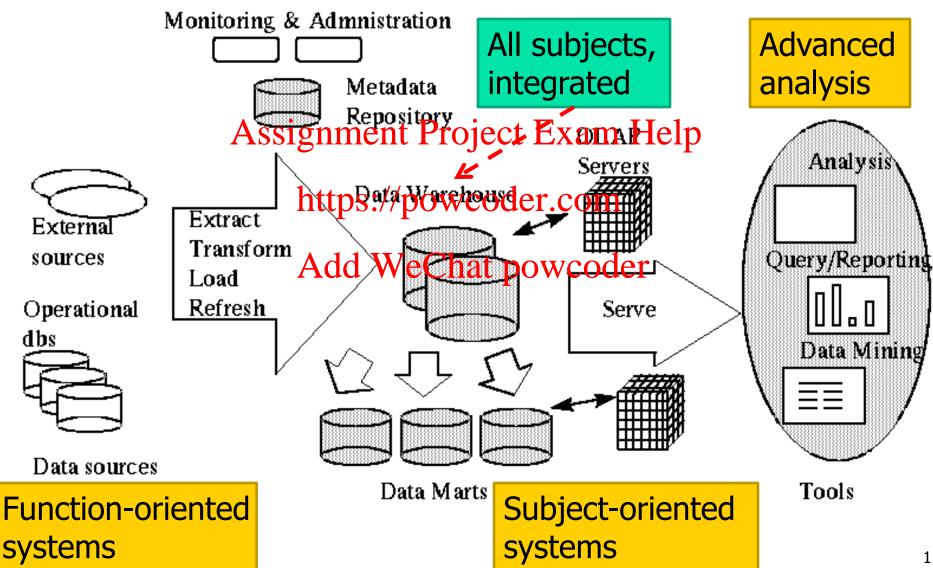
multidimensional & W

Multidimensional-olap (Essbase, oracle express)

Relational-olap (Redbrick, Informix, Sybase, SQL server)



#### Data Warehouse Architecture



# Why Separate Data Warehouse?

- High performance for both systems
  - DBMS— tuned for OLTP: access methods, indexing, concurrency control, recovery Assignment Project Exam Help
  - Warehouse—tuned for OLAP: complex OLAP queries, multidimensionattyew/porsolidation.com
- Different functions and different data:
   Add WeChat powcoder
   missing data: Decision support requires historical data which
  - missing data: Decision support requires historical data which operational DBs do not typically maintain
  - data consolidation: DS requires consolidation (aggregation, summarization) of data from heterogeneous sources
  - data quality: different sources typically use inconsistent data representations, codes and formats which have to be reconciled

#### Why OLAP Servers?

- Different workload:
  - OLTP (on-line transaction processing)
    - Major task of traditional relational DBMS
    - Day-to-days originations: put description of the properties of the prop
  - OLAP (on-line apalytical processing) r.com
    - Major task of data warehouse system
    - Data analysis and decision multipat powcoder
- Queries hard/infeasible for OLTP, e.g.,
  - Which week we have the largest sales?
  - Does the sales of dairy products increase over time?
  - Generate a spread sheet of total sales by state and by year.
- Difficult to represent these queries by using SQL Why?

# OLTP vs. OLAP

	OLTP	OLAP
users	clerk, IT professional	knowledge worker
function	day to day operations	decision support
DB design A	application entempdoject	Expirately
data	current, up-to-date	historical,
	detailed flat relational isolated PS://POWcode	summarized, multidimensional integrated, consolidated
usage	repetitive	ad-hoc
access	read We Chat po	MCG Stark
	index/hash on prim. key	
unit of work	short, simple transaction	complex query
# records accessed	tens	millions
#users	thousands	hundreds
DB size	100MB-GB	100GB-TB
metric	transaction throughput	query throughput, response

# Comparisons

**Databases** 

Purpose	Many purposes; Flexible and general Assignment Project Exa	One purpose: Data analysis  m Help
Conceptual Model	ER	Multidimensional
https://powcoder.com		
	/a.	/5 / / / / / / / / / / / / / / / / / /

**Data Warehouses** 

queries)

Bitmap/Join indexes, Star join,

Materialized data cube

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Logical Model

(Normalized) Relational Model

Add WeChat powcoders cube/cuboids

Physical Model

Relational Tables

ROLAP: Relational tables

MOLAP: Multidimensional arrays

Query Language

SQL (hard for analytical

MDX (easier for analytical

Query Language

SQL (hard for analytical queries)

Query Processing

B+-tree/hash indexes, Multiple join optimization, Materialized

#### The Multidimensional Model

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#### The Multidimensional Model

- A data warehouse is based on a multidimensional data model which views data in the form of a data cube, which is a multidimensional generalization of 2D spread sheet.
- Key conceptssignment Project Exam Help

  - Facts: the subject it models
     Typically transactions in this course; other types includes snapshots, etc. Add WeChat powcoder

    Measures: numbers that can be aggregated

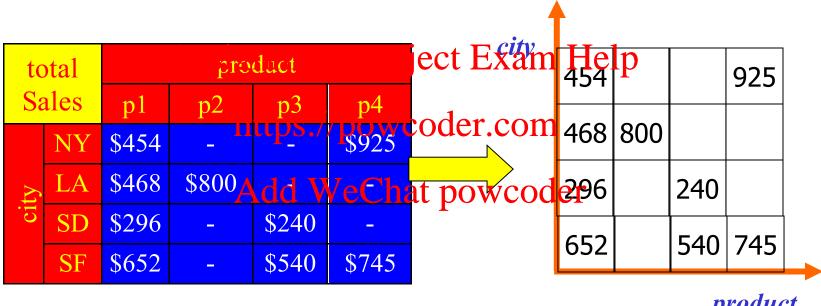
    - Dimensions: context of the measure
  - Hierarchies:
    - Provide contexts of different granularities (aka. grains)
- Goals for dimensional modeling:
  - Surround facts with as much relevant context (dimensions) as possible Why?

# Supermarket Example

- Subject: analyze total sales and profits
- Fact: Each Sales Transaction
  - Measure Pollars Sold Amount Sold Cost
  - Calculated Measure: Profit
- Dimensions: <a href="https://powcoder.com">https://powcoder.com</a>
  - Store Add WeChat powcoder
  - Product
  - Time

# Visualizing the Cubes

A valid instance of the model is a data cube



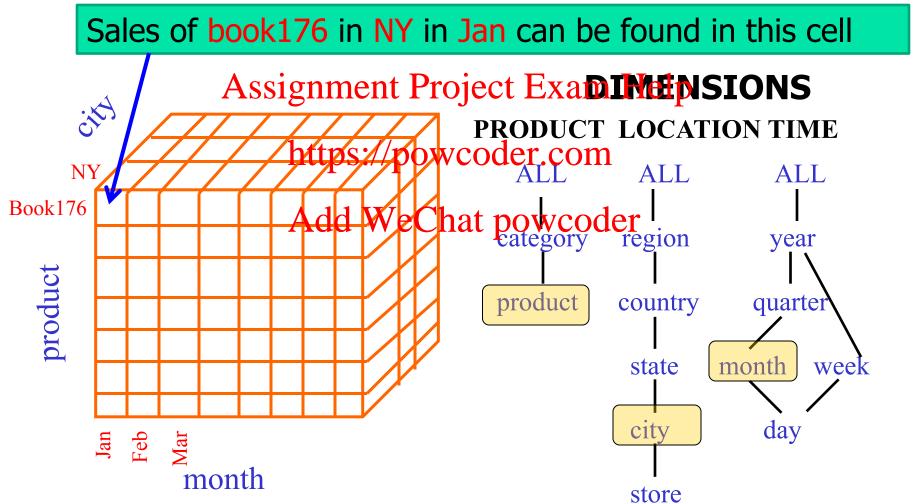
product

**Concepts**: cell, fact (=non-empty cell), measure, dimensions

Q: How to generalize it to 3D?

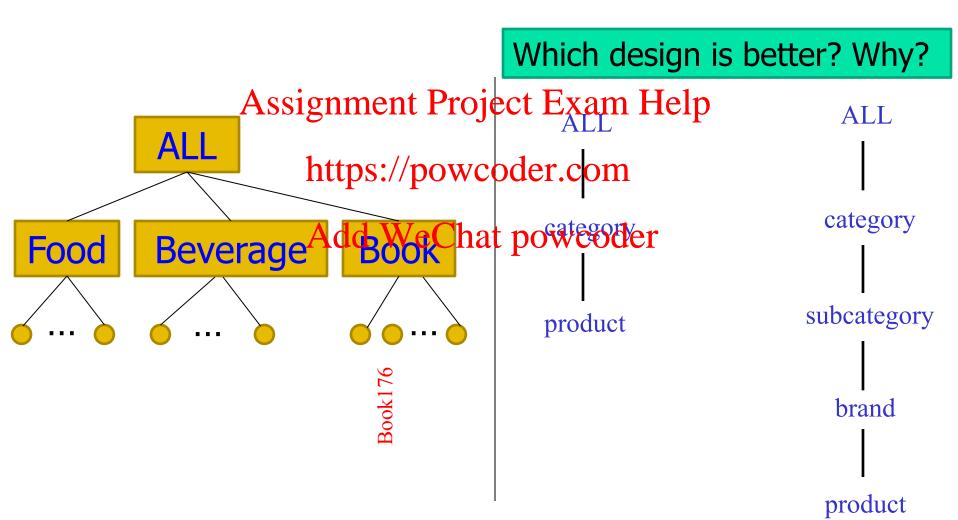
#### 3D Cube and Hierarchies

Concepts: hierarchy (a tree of dimension values), level



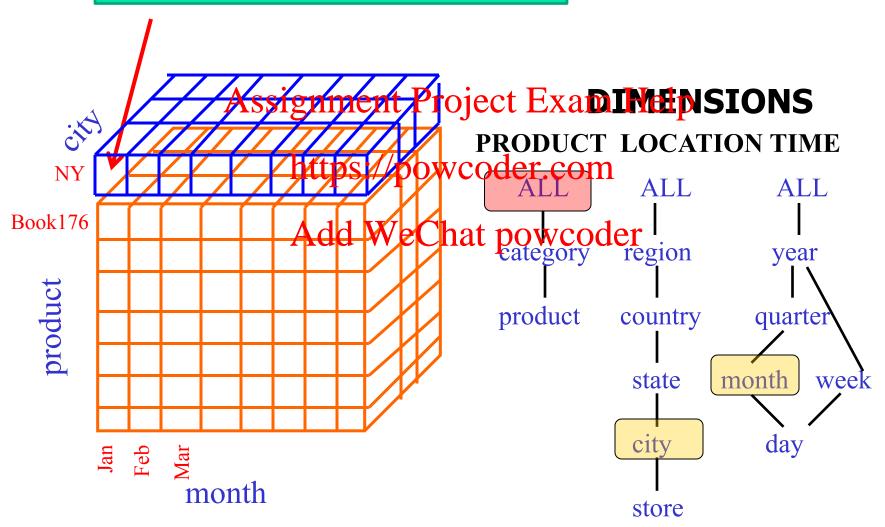
#### **Hierarchies**

Concepts: hierarchy (a tree of dimension values), level



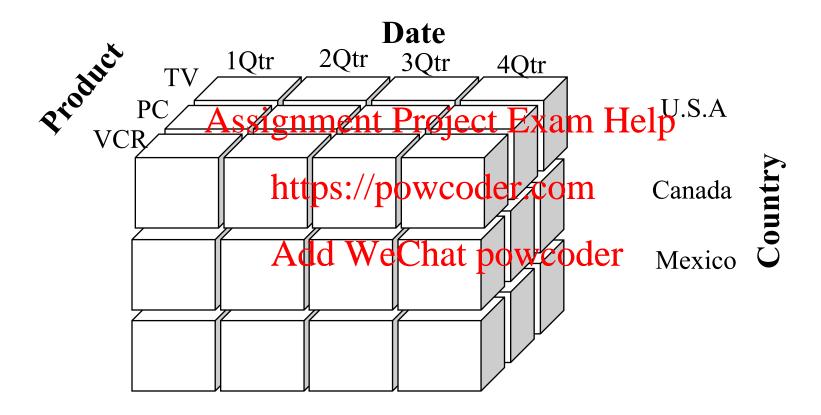
# The (city, moth) Cuboid

Sales of ALL\_PROD in NY in Jan



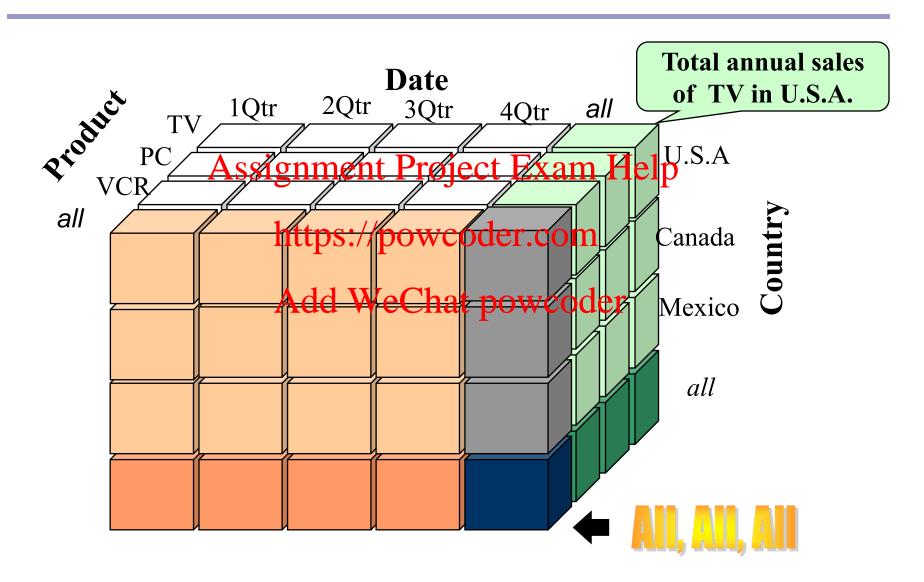
# Assume: no other non-ALL levels on all dimensions.

#### All the Cuboids

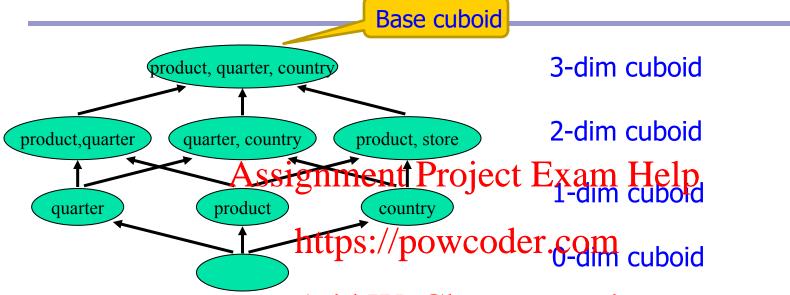


# Assume: no other non-ALL levels on all dimensions.

#### All the Cuboids /2



#### Lattice of the cuboids



- n-dim cube can be Addres Wited ha (Protected), where D<sub>i</sub> is the set of allowed values on the i-th dimension.
  - if D<sub>i</sub> = L<sub>i</sub> (a particular level), then Di = all descendant dimension values of L<sub>i</sub>.
  - ALL can be omitted and hence reduces the effective dimensionality  $\frac{d}{dt}$
- A complete cube of d-dimensions consists of  $\lim_{i=1}^{n} \frac{1}{i} = 1$  cuboids, where  $n_i$  is the number of levels (excluding ALL) on i-th dimension.
  - They collectively form a lattice.

# **Properties of Operations**

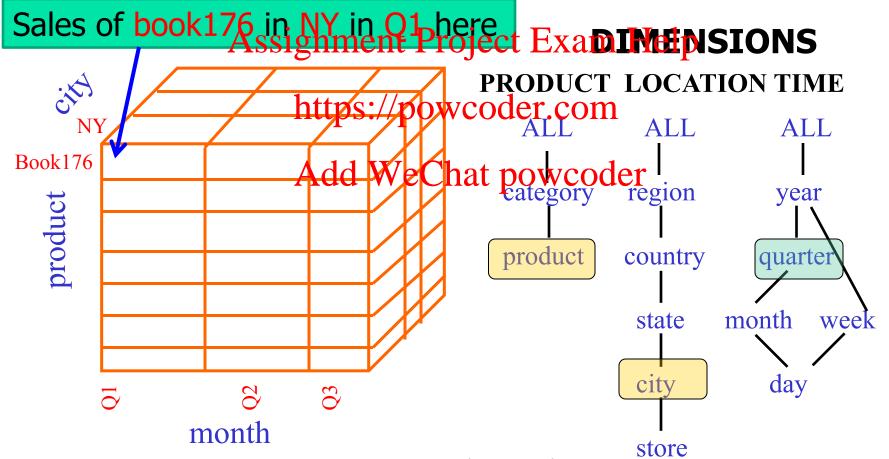
- All operations are closed under the multidimensional model
  - i.e., both signute and route put comand peration is a cube
- So that they can be composed
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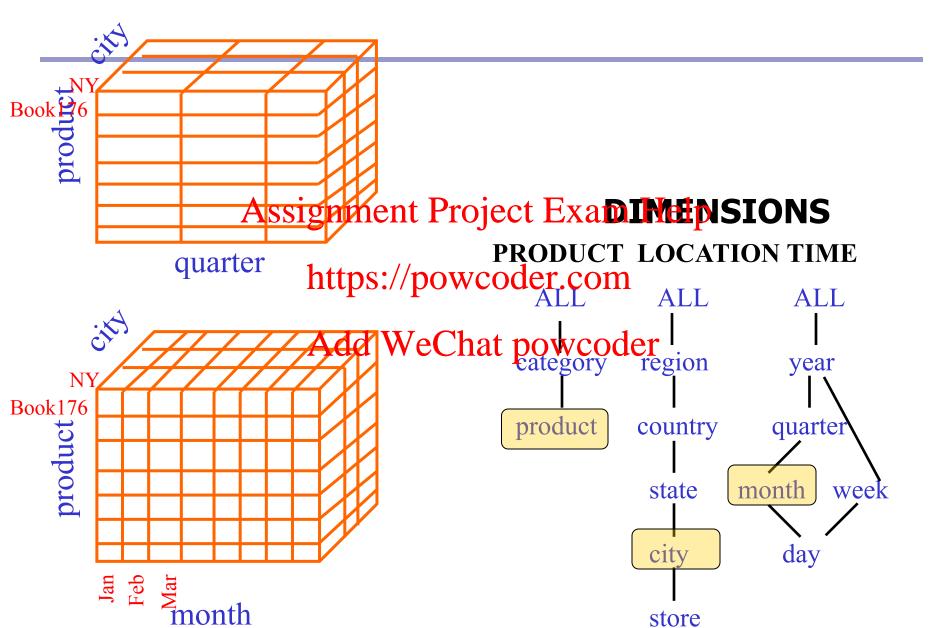
Q: What's the analogy in the Relational Model?

# **Common OLAP Operations**

Roll-up: move up the hierarchy

Q: what should be its value?





# **Common OLAP Operations**

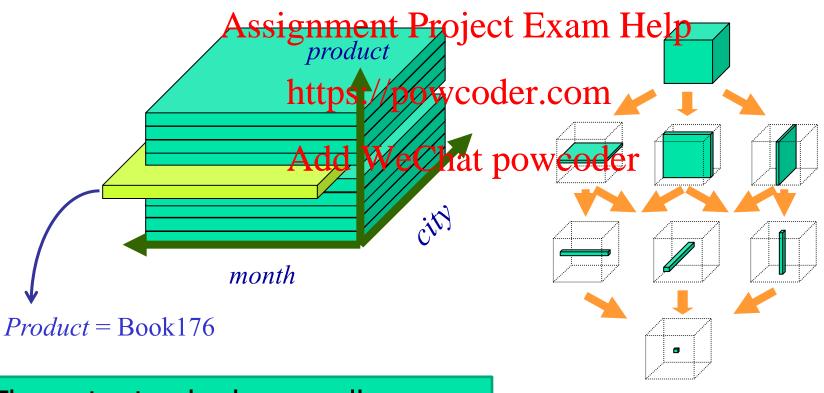
Drill-down: move down
 the hierarchy
 more fine-grained

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more fine-grained in Project Exam Help aggregation https://powcoder.com

# Slice and Dice Queries

 Slice and Dice: select and project on one or more dimension values

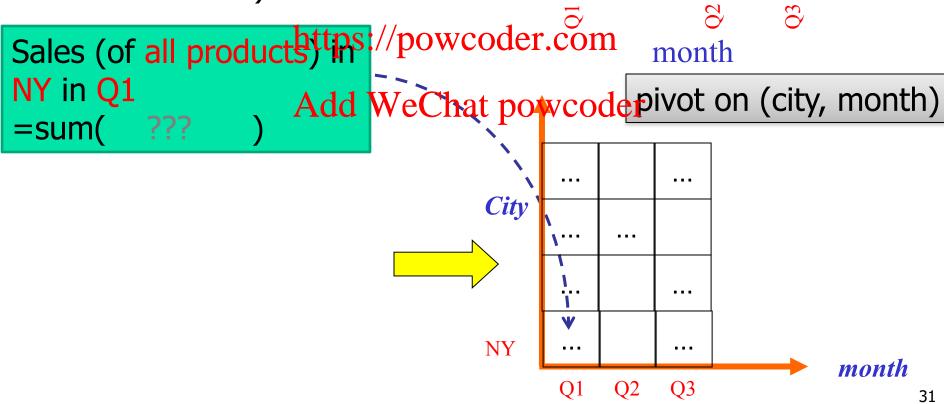


The output cube has smaller dimensionality than the input cube

# **Pivoting**

- Pivoting: aggregate on selected dimensions
  - usually 2 dims (crosstabulation)

    Tabulation
    Project Exam I



Book176

product

#### A Reflective Pause

Let's review the definition of data cubes again.

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- Key message:
  - Disentangle the "object" from its "representation" or "implementation"

# Modeling Exercise 1: Monthly Phone Service Billing



Theme: analyze the income/revenue of Telstra

#### Solution

FACT

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MEASURE <a href="https://powcoder.com">https://powcoder.com</a>

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DIMENSIONS

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#### The Logical Model

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## Logical Models

- Two main approaches:
  - Using relational DB technology:
    - Star scheigan & Moderate Star Scheigen & Star Sch
  - Using multidimensional technology:
    - Just as multidimensional data cube Add WeChat powcoder

### Universal Schema → Star Schema

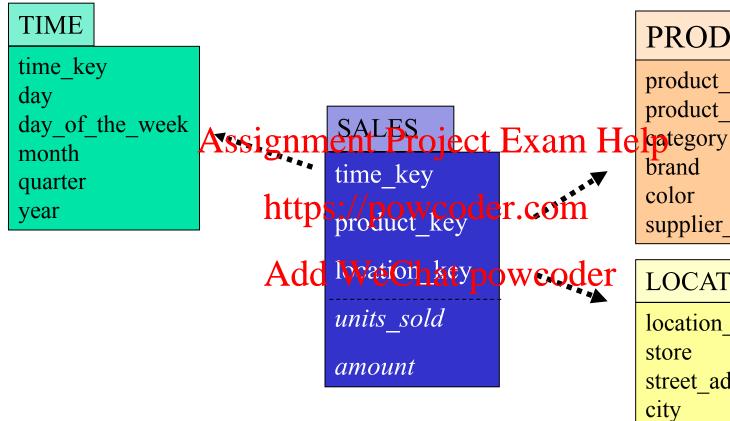
- Many data warehouses adopt a star schema to represent the multidimensional model
- Each dimension is represented by a dimension-table
  - LOCATION (docation key, Ptorjectret addres) pity, state, country, region)
  - dimension tablestapes no provincialided.com
- Transactions are described through a fact-table
   each tuple consists of a pointer to each of the dimension-tables
  - each tuple consists of a pointer to each of the dimension-tables (foreign-key) and a list of measures (e.g. sales \$\$\$)

#### The universal schema for supermarket

Store	City	State	Prod	Brand	Category	\$Sold	#Sold	Cost
S136	Syd	NSW	76Ha	Nestle	Biscuit	40	10	18
S173	Melb	Vic	76Ha	Nestle	Biscuit	20	5	11

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### The Star Schema



#### **PRODUCT**

product key product name supplier\_name

#### LOCATION

location key street address state country region

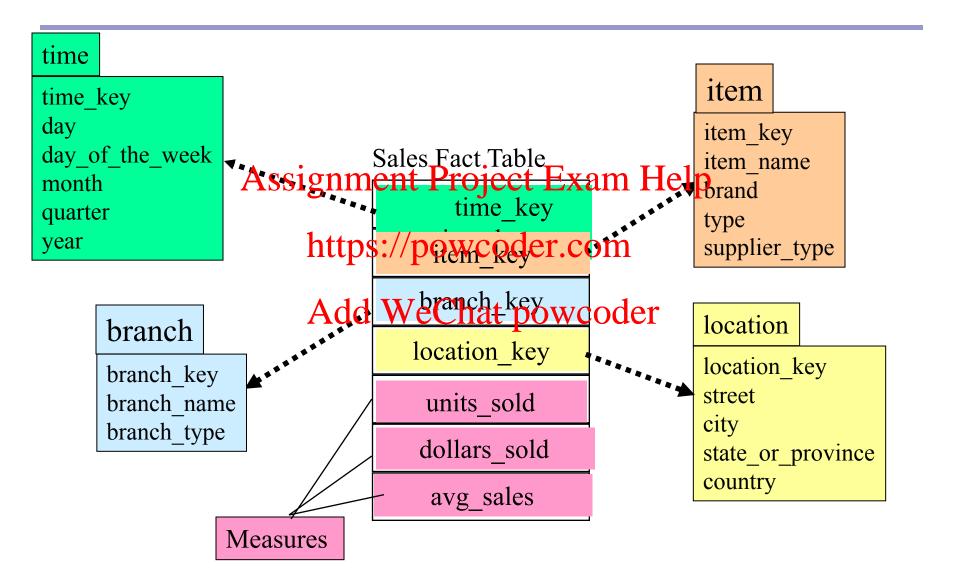
#### Think why:

- (1) Denormalized once from the universal schema
- (2) Controlled redundancy

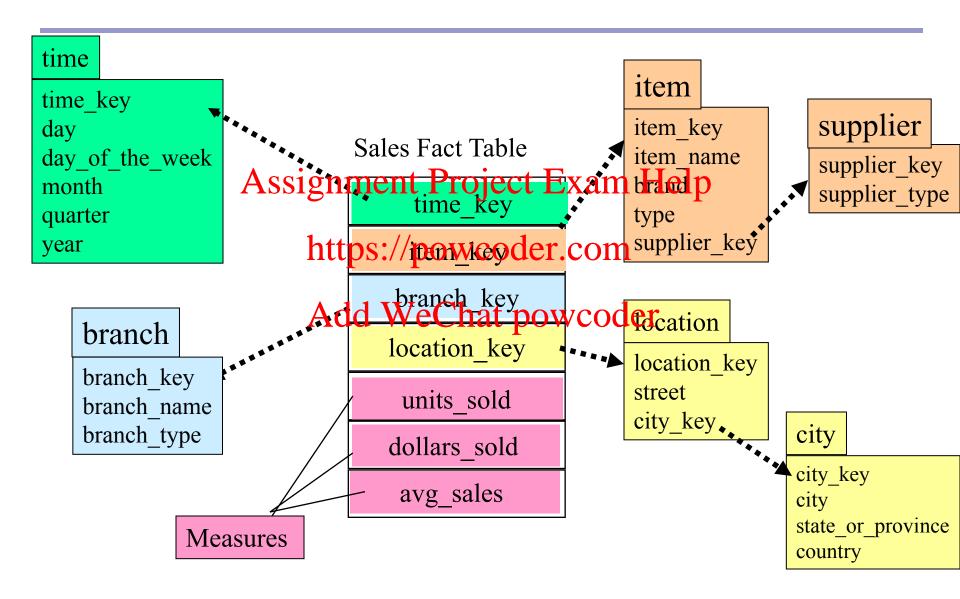
### Typical Models for Data Warehouses

- Modeling data warehouses: dimensions & measures
  - Star schema: A fact table in the middle connected to a set of dimensignment Project Exam Help
  - Snowflake schema://poweinement.nf star schema
    where some dimensional hierarchy is normalized into a
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    set of smaller dimension tables, forming a shape
    similar to snowflake
  - <u>Fact constellations</u>: Multiple fact tables share dimension tables, viewed as a collection of stars, therefore called <u>galaxy schema</u> or fact constellation

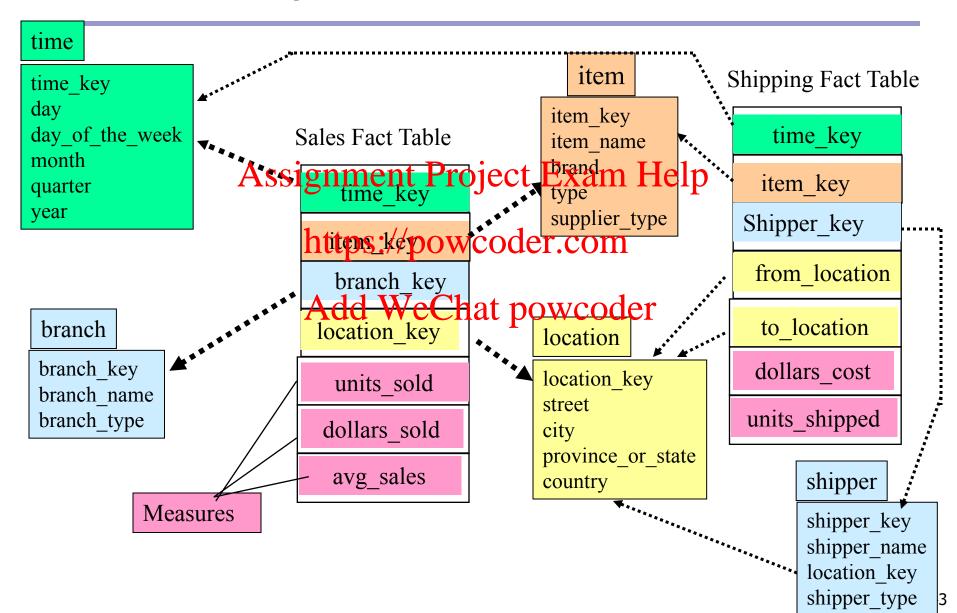
### **Example of Star Schema**



## Example of Snowflake Schema



## **Example of Fact Constellation**



### Advantages of Star Schema

- Facts and dimensions are clearly depicted
  - dimension tables are relatively static, data is loaded (append mestly) timeton fractetable(s)
  - easy to comprehend (and write queries)

```
"Find total sales per product-category in our stores in Europe"
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```

```
SELECT PRODUCT.category, SUM(SALES.amount)
```

```
FROM SALES, PRODUCT, LOCATION
```

**WHERE** SALES.product\_key = PRODUCT.product\_key

**AND** SALES.location\_key = LOCATION.location\_key

**AND** LOCATION.region="Europe"

**GROUP BY PRODUCT.category** 

Operations: Slice (Loc.Region.Europe) + Pivot (Prod.category)

### Query Language

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## Query Language

LOCATION.region="Europe"

Two approaches:

LOCATION.location key

**GROUP BY PRODUCT. category** 

AND

- Using relational DB technology: SQL (with extensions) such as CUBE/PIVOT/UNPIVOT)
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  Using multidimensional technology: MDX

```
https://powcoder.com
SELECT PRODUCT.category,
                                    SELECT
SUM(SALES.amount)
                   Add WeChat (PRODUCE:[category]) on ROWS,
       SALES, PRODUCT, LOCATION
                                    {[MEASURES].[amount]} on COLUMNS
WHERE SALES.product key =
                                           [SALES]
                                    FROM
PRODUCT.product key
                                    WHERE ([LOCATION].[region].[Europe])
AND
       SALES.location_key =
```

Operations: Slice (Loc.Region.Europe) + Pivot (Prod.category, Measures.amnt)

### Physical Model + Query Processing Techniques

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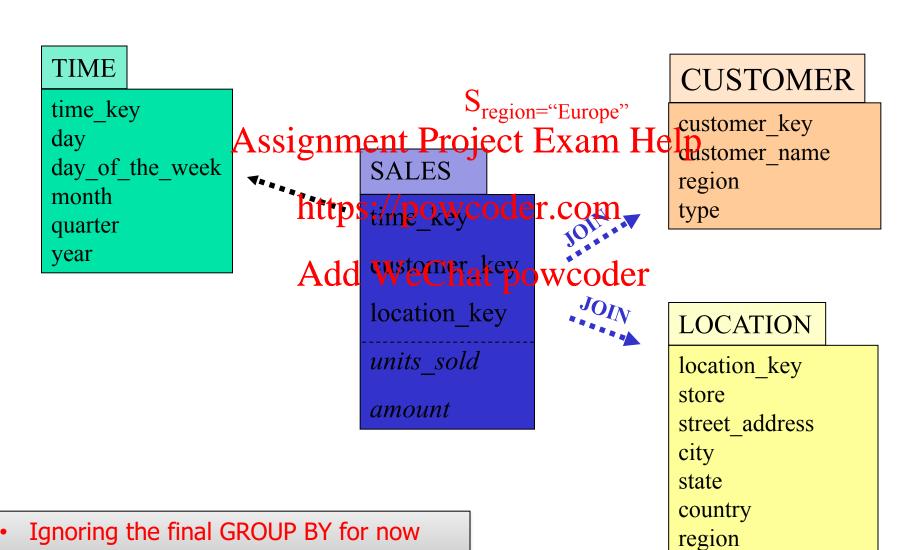
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# Physical Model + Query Processing Techniques

- Two main approaches:
  - Using relational DB technology: ROLAP
  - Using matticiments on indetection by MOLAP
- Hybrid: HOLAPttps://powcoder.com
  - Base cuboid: RQLAP wechat powcoder
  - Other cuboids: MOLAP

# Q1: Selection on low-cardinality attributes



Omitting the Product dimension

## Indexing OLAP Data: Bitmap Index

#### (1) BI on dimension tables

- Index on an attribute (column) with low distinct values
- Each distinct values, v, is associated with a n-bit vector (n = #rows)
  Assignment Project From II-1
- Assignment Project Exam Help
   The +th bit is set if the +th row of the table has the value v for the indexed column wcoder.com
   Multiple BIs can be efficiently combined to enable optimized scan
- Multiple BIs can be efficiently combined to enable optimized scar of the table Add WeChat powcoder

#### **Custom**

Cust	Region	Type
C1	Asia	Retail
C2	Europe	Dealer
C3	Asia	Dealer
C4	America	Retail
C5	Europe	Dealer

#### **BI on Customer.Region**

V	bitmap
Asia	10100
Europe	0 1 0 0 1
America	00010

# Indexing OLAP Data: Bitmap Index /2

- Bitmap join index (BI on Fact Table Joined with Dimension tables)
  - Conceptually, perform a join, map each dimension value to the Bitmap of Colfest Fording faut table rows.

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```
-- ORACLE SYNTAX –

CREATE BITMAP INDEX sales_cust_region_bjix

ON sales(customer.cust_region)

FROM sales, customer

WHERE sales.cust_id = customers.cust_id;
```

## Indexing OLAP Data: Bitmap Index /3

$\alpha$	

time	customer	loc	Sale
101	C1	100	1
173	C1 A	ssign	ıment
208	C2	100	tng./3
863	C3	200	tps:// 5
991	C1	100	dd W
1001	C2	200	13
1966	C4	100	21
2017	C5	200	34

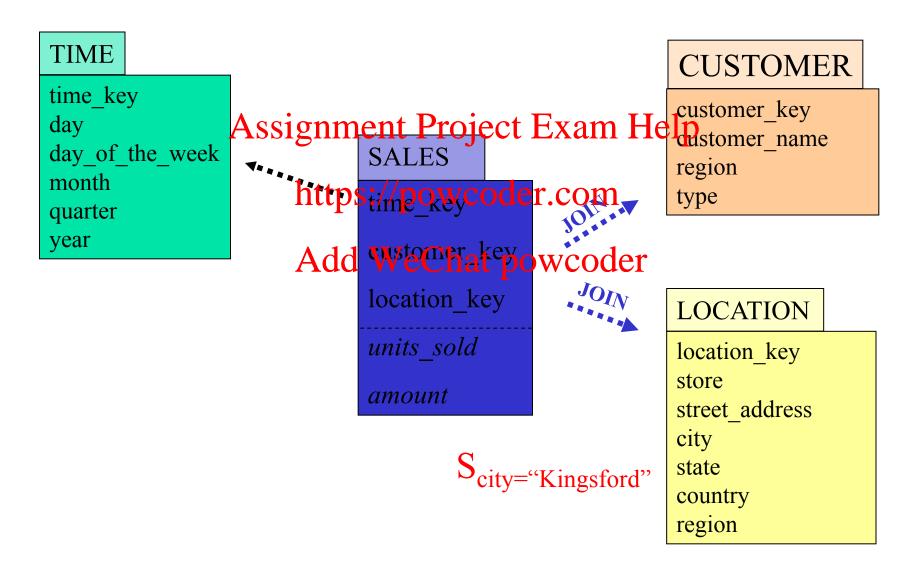
#### **Customer**

	Cust	Region	Type
			Retail
Project	<b>E</b> xai	fiul topp	Dealer
	C3	Asia	Dealer
powcode	CACO1	<b>A</b> merica	Retail
<b>C1</b>	C5	Europe	Dealer
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#### **BI on Sales(Customer.Region)**

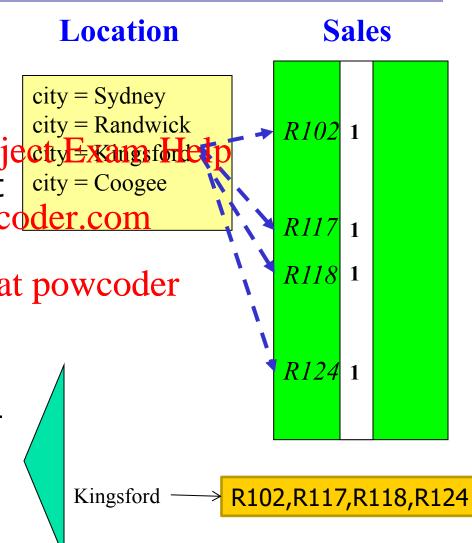
v	bitmap
Asia	11011000
Europe	00100101
America	0000010

# Q2: Selection on high-cardinality attributes

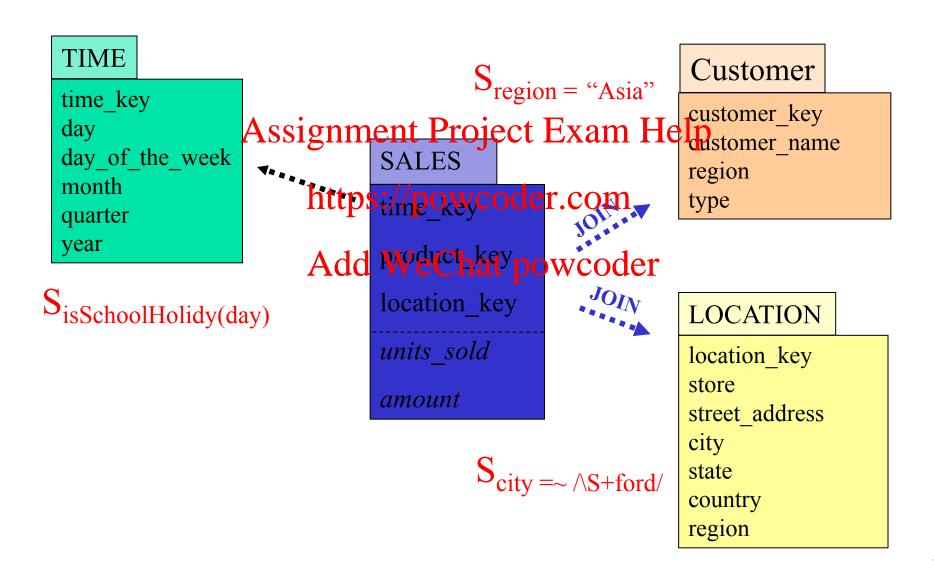


## Indexing OLAP Data: Join Indices

- Join index relates the values of the <u>dimensions</u> of a star schema to <u>rows</u> in the fact table.
  - a join index on withent Projectly Example maintains for each distinct city = Coogee city a list of Rows of the tuples recording the sales in the city dd WeChat powcoder
- Join indices can span multiple dimensions OR
  - can be implemented as bitmapindexes (per dimension)
  - use bit-op for multiple-joins

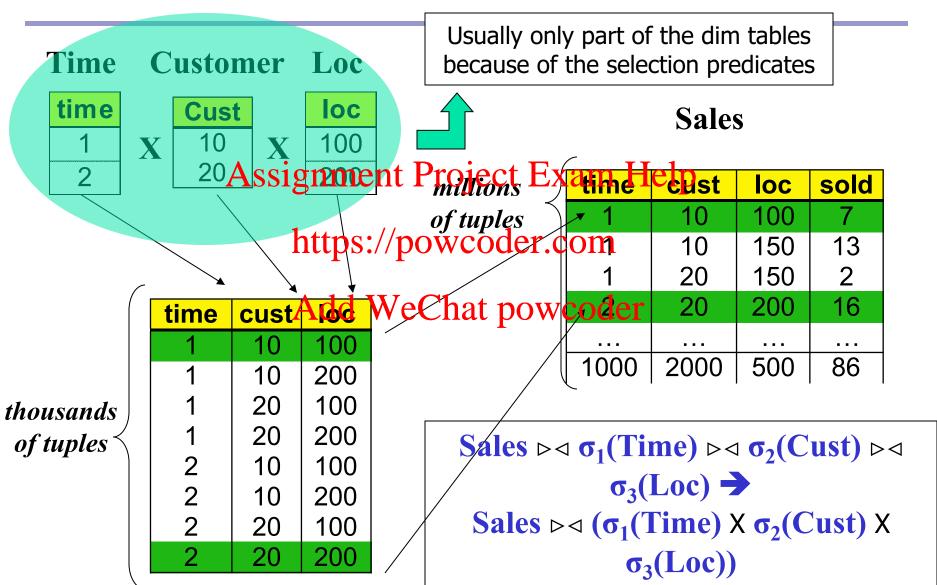


# Q3: Arbitrary selections on Dimensions



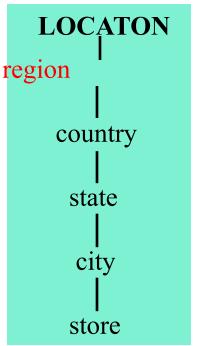
### Chap 4.4 in [JPT10]

# Star Query and Star Join (Cont.)



## Q4: Coarse-grain Aggregations

- "Find total sales per customer type in our stores in Europe"
  - Join-index will prune ¾ of the data (uniform sales), but the remaining ¼ is still large (several millions transactions)
    - Index is undhates powcoder.com
- High-level aggregations are expensive!!!!!
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  - ⇒Long Query Response Times
  - ⇒Pre-computation is necessary
  - ⇒Pre-computation is most beneficial



### Cuboids = GROUP BYs

Multidimensional aggregation = selection on corresponding cuboid

```
GB_{(type, cft)} (sightment Riojee): Exam (Chtelp \triangleleft \sigma_3(Loc))
```



- σ<sub>1</sub> selects some Brands,
- σ<sub>3</sub> selegta a meChitie sow coder

```
GB_{(type, city)}(\sigma_{1'2'3'}(Cuboid(Year, Type, City)))
```

- Materialize some/all of the cuboids
  - A complex decision involving cuboid sizes, query workload, and physical organization

### Two Issues

- How to store the materialized cuboids?
- How to compute the cuboids efficiently?

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### CUBE BY in ROLAP

.1			Produ	ct		Store	Product_key	sum(amout)
ares	1	2	3	4	ALL	1	1 4	454 925
1	454	-	-	925	1379	2	1	468
2	468	800	-	_	1268	2 3	2 1	800 296
3	296	_	Assi	gnme	enti <b>P</b> r	oject Exam	Help	240
4	652	-	540	745	1937	4	<b>4</b> 3	625 240
ALL	1870	800	780	https	://pov	vcoder.com	4	745
	. 1	1			1	1 2	ALL	1379 1268
	•			<b>Xedd</b> 1 gueri	es!!!	hat3powcod	er ALL ALL	536 1937
store)				•		ALL ALL	1 2	1870 800
produ )	ict)			*		ALL ALL	3	780 1670 5120
	3 4 ALL Groustore,	1 1 454 2 468 3 296 4 652 ALL 1870	1 454 - 2 468 800 3 296 - 4 652 - ALL 1870 800  Group-bys here: store,product) store)	1 2 3 1 454 2 468 800 - 3 296 - A361 4 652 - 540 ALL 1870 800 780  Group-bys here: store,product) store)	1 2 3 4 1 454 925 2 468 800 3 296 - A361gnn 4 652 - 540 745 ALL 1870 800 780 https  Group-bys here: store,product) store) product)  Compu	1 2 3 4 ALL 1 454 - 925 1379 2 468 800 - 1268 3 296 - AssignmentsPr 4 652 - 540 745 1937 ALL 1870 800 780 https://pov Group-bys here: store,product) Store) • Neettoweter 4 queries!!! • Compute them	1 2 3 4 ALL 1 454 925 1379 2 2 468 800 1268 3 3 296 - Asci gnmens@roject Exam 4 652 - 540 745 1937 4  ALL 1870 800 780 https://povcoder.com  Group-bys here: store, product)  Store) product)  - Compute them independently.	1 2 3 4 ALL 1 454 925 1379 2 1 2 468 800 1268 3 3 296 - 286   grinnem3 Project Exam Help 4 652 - 540 745 1937 4 3 ALL 1870 800 780   https://powcoder.com   ALL ALL   Store, product) Store) product)  - Compute them independently   ALL   AL

**SELECT** LOCATION.store, SALES.product\_key, SUM (amount)

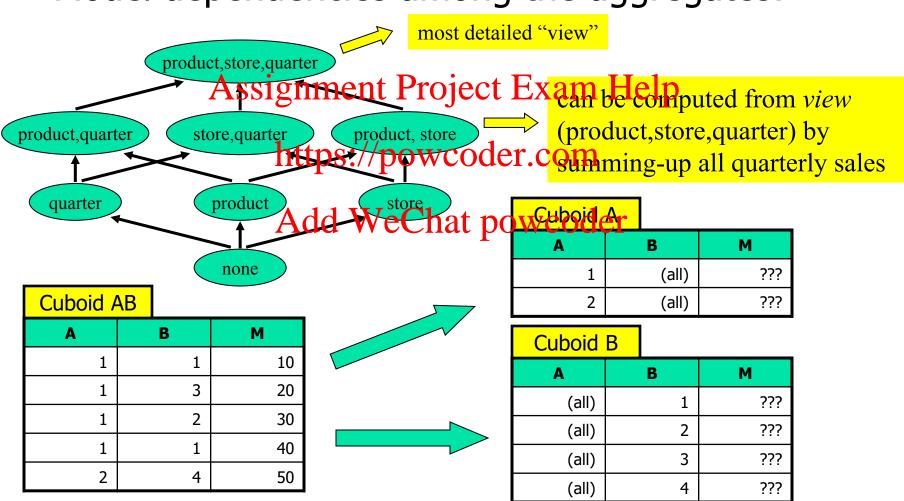
FROM SALES, LOCATION

WHERE SALES.location\_key=LOCATION.location\_key

**CUBE BY** SALES.product\_key, LOCATION.store

## Top-down Approach

Model dependencies among the aggregates:



## Bottom-Up Approach (BUC)

BUC (Beyer & Ramakrishnan, SIGMOD'99)

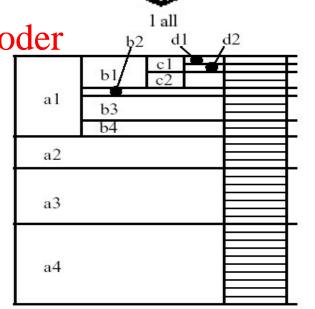
Ideas Assignment Project Exam He

 Compute the cube from bottom up <a href="https://powcoder.com">https://powcoder.com</a>

Divide-and-conquer
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 A simpler recursive version:

BUC-SR

Α	В	
1	1	
1	3	
1	2	
1	1	
2		



5 ABCD

8 ACD

11 BC 13 BD 15 CD

### **Understanding Recursion /1**

- Powerful computing/problem-solving techniques Assignment Project Exam Help
- Examples
  - Factorial: https://powcoder.com
    - f(n) = 1, iAdd WeChat powcoder
    - $f(n) = f(n-1) * n, if n \ge 1$
  - Quick sort:
    - Sort([x]) = [x]
    - Sort([x1, ..., pivot, ... xn]) = sort[ys] ++ sort[zs]), where

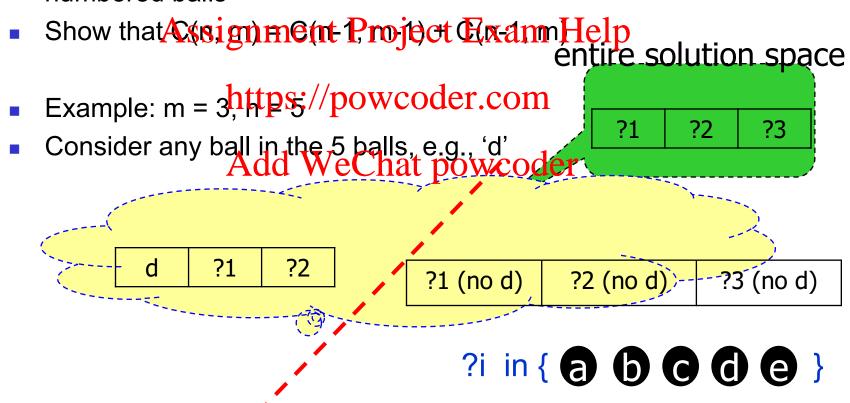
f(0) = 0! =

ys = 
$$[x \mid x \text{ in } xi, x \leq pivot]$$
  
zs =  $[x \mid x \leftarrow xi, x > pivot]$ 

List comprehension in Haskell or python

### **Understanding Recursion /2**

 Let C(n, m) be the number of ways to select m balls from n numbered balls



## **Key Points**

- Sub-problems need to be "smaller", so that a simple/trivial boundary case can be reached Assignment Project Exam Help
- Divide-and-conquer
  - There may be multiple ways the entire solution space can be divided into disjoint sub-spaces, each of which can be conquered recursively.

### **Geometric Intuition /1**

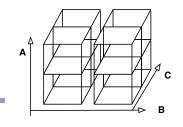
Reduce Cube(in 2D) to Cube(in 1D)



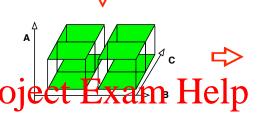
### **Geometric Intuition /2**



## Geometric Intuition /3

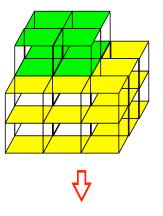


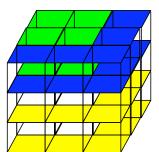
Reduce Cube(in 3D) to Gubenin Project Exam Help



https://powcoder.com

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## **BUC-SR (Simple Recursion)\***

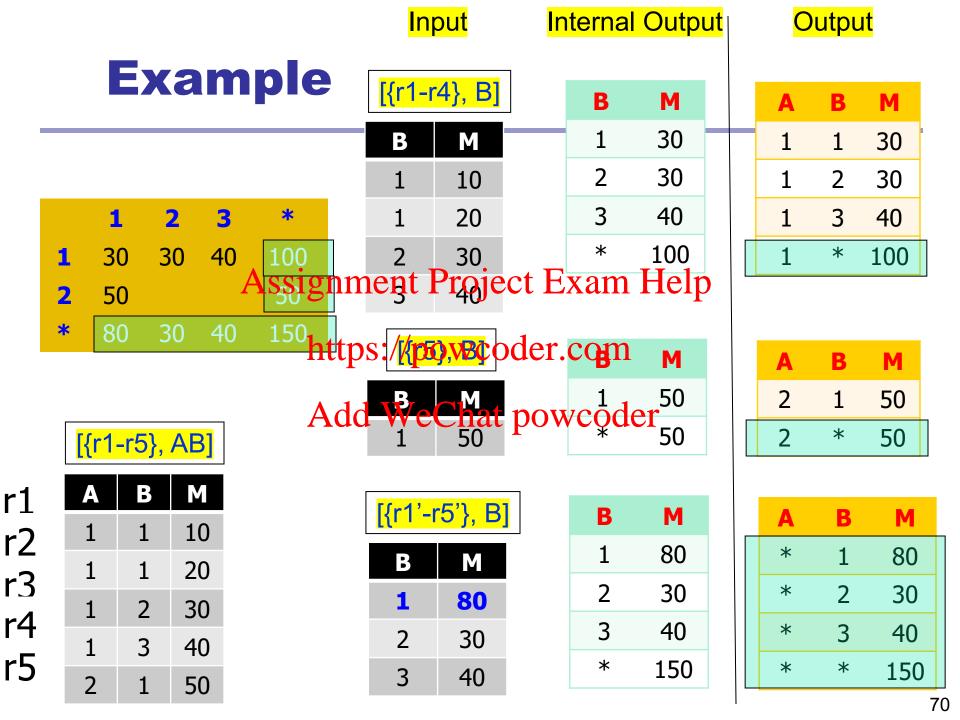
- BUC-SR(data, dims)
  - If (dims is seigpty)nt Project Exam Helpoundary case:
    - Output (sum(data)) https://powcoder.com
  - Else
    - Dims = [dim1, rest of dims]
    - For each distinct value v of dim1
      - slice v = slice of data on "dim1 = v"
      - BUC-SR(slice\_v, rest\_of\_dims)
    - data' = Project(data, rest\_of\_dims)
    - BUC-SR(data', rest of dims)

of measure values

#### General case:

1)Slice on dim1. Call **BUC-SR** recursively for each slice

2)Project out dim1, and call BUC-SR on it recursively



### Try a 3D-Cube by Yourself

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### [{r1-r5}, ABC]

L				J
r1	A	В	С	M
r2	1	1	1	10
r3	1	1	2	20
r4	1	2	1	30
▗╴ ▗	1	3	1	40
<b>5</b>	2	1	1	50
6/3/	10			

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### **MOLAP**

- (Sparse) array-based multidimensional storage engine
- Pros: Assignment Project Exam Help
  - small size (esp. for dense cubes)
  - fast in indexing and query processing Add WeChat powcoder
- Cons:
  - scalability
  - conversion from relational data

### Multidimensional Array

f(time, item) = 4\*time + item

time	item	dollars_sold	
Q1	home entertainment	605	
Q2	home entertainment	680	
Q3	home entertainment	Assign	n
Q4	home entertainment	<b>9</b> 27111	n
Q1	computer	825	P
Q2	computer	952	1 -
Q3	computer	10 <b>23</b> C	lC
Q4	computer	1038	
Q1	phone	14	
Q2	phone	31	
Q3	phone	30	
Q4	phone	38	
Q1	security	400	
Q2	security	512	
Q3	security	501	
Q4	security	580	

	Step 1		
16	Марріоз	pject I	
	Q1	<b>∀alue</b> 0	
S	1 1	code	•
	Q3	2	
1	WeCl	1at 13	V
	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	rw P	•
	item	value	
	home entertain		·
	home	<b>value</b> 0 1	
	home entertain ment	0	

time	item	dollars_s old
0	0	605
1	0	680
xam²	Help	812
3	0	927
¢ <del>om</del> º	1	825
	1	952
code	1	1023
/code	r 1	1038
0	2	14
1	2	31
2	2	30
3	2	38
0	3	400
1	3	512
2	3	501
3	3	580

offset

# **Multidimensional Array**

#### Step 3': If **sparse**

#### Step 3: If dense, only need to store sorted slots

dollars_sold
605
825
14
Acs
680
952
31
512
812
1023
30
501
927
1038
38
580



Think: how to decode a slot?

signmeltidimensional Taxamis Help typically sparse

https://sowereder.avoing., offset + value)

Add Woulding shunk toder further reduce the space

- Space usage:
  - (d+1)\*n\*4 vs 2\*n\*4
- HOLAP:
  - Store all non-base cuboid in MD array
  - Assign a value for ALL

Dense MD array	
	605
	825
	14
	400
	680
	952
	31
	512
	812
	1023
	30
	501
	927
	1038
	38
	580