COMP9334 Capacity Planning for Computer Systems and Networks

Assignment Project Exam Help

Week 7Bhttpea/powalederAnalysis

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This lecture

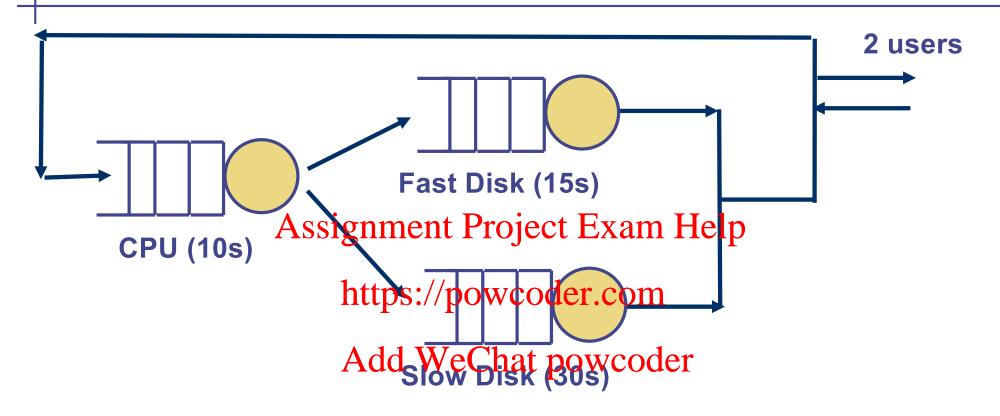
- Methods to efficiently analyse a closed queueing network
- Motivation
 - You have learnt how to analyse a closed queueing network in Week 3B using Markov chain
 - However, the method can pany be used for Heamall number of users
- This week we will study a method that can be used for a large number of https://powcoder.com

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 Let us begin by revisiting the database server example in Week 3B

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DB server example



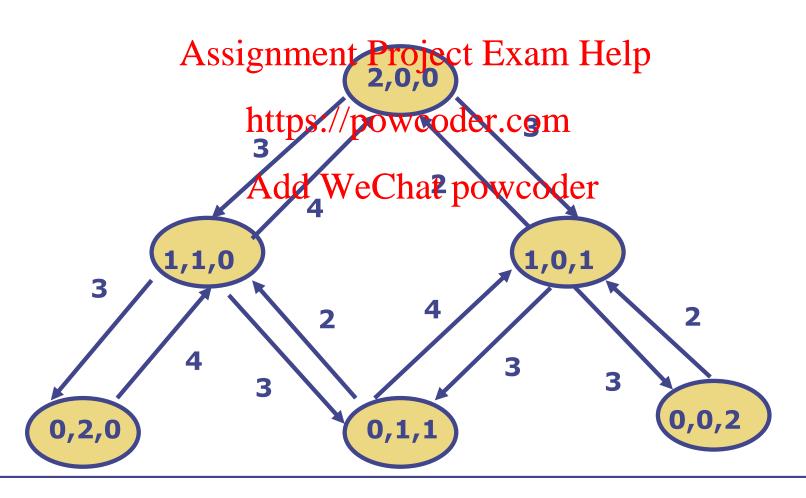
- 1 CPU, 1 fast disk, 1 slow disk.
- Peak demand = 2 users in the system all the time.
- Transactions alternate between CPU and disks.
- The transactions will equally likely find files on either disk
- Service time are exponentially distributed with mean showed in parentheses.

Markov chain solution to the DB server problem

- In Week 3B, we used Markov chain to solve this problem
- We use a 3-tuple (X,Y,Z) as the state
 - X is # users at CPU
 - Y is # user stigated with Project Exam Help
 - Z is # users at slow disk
- https://powcoder.com Examples
 - (2,0,0): both users at CPU Add WeChat powcoder (1,0,1): one user at CPU and one user at slow disk
- Six possible states
 - (2,0,0) (1,1,0) (1,0,1) (0,2,0) (0,1,1) (0,0,2)

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Markov model for the database server with 2 users



Solving the model

- Solve for the probability in each state P(2,0,0), P(1,1,0), etc.
 - There are 6 states so we need 6 equations
- After solving for P(2,0,0), P(1,1,0) etc. We can find
 - Utilisation https://powcoder.com
 - Throughput,
 - Response time, Add WeChat powcoder
 - Average number of users in each component etc.

What if we have 3 users instead?

- What if we have 3 users in the database example instead of only 2 users?
- We continue to use (X,Y,Z) as the state
 - X is the # users at CPU
 - Y is the # users ignment Project Exam Help
 - Z is the # users at the slow disk not be a slow d
- How many states will you need?
- We need 10 states.dd WeChat powcoder
 - **•** (3,0,0),
 - (2,1,0),(2,0,1)
 - (1,2,0),(1,1,1),(1,0,2)
 - (0,3,0),(0,2,1),(0,1,2),(0,0,3)

What if there are *n* users?

 You can show that if there are n users in the database server, the number of states m required will be

$$(n+1)(n+2)$$

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- For n = 100, m =
- You can automate the computational process but where is the computational bottleneck?
 - Solving a system of m linear equations in m unknowns has a complexity of $O(m^3)$
- For our database server with n users, the computational complexity is about $O(n^6)$

Weaknesses of Markov model

- The Markov model for a practical system will require many states due to
 - Large number of users
 - Large number of components

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- Large # states
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 - More transitions to identify
 - Though this can Aelaut Metchat powcoder
 - If you've m states, you need to solve a set of m equations. A larger set of equation to solve.
 - The complexity of solving a set of m linear equations in m unknowns is $O(m^3)$

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Mean value analysis (MVA)

- An iterative method to find the
 - Utilisation
 - Mean throughput
 - Mean response time
 - Mean number of users Assignment Project Exam Help
- The complexity is approximately O(nk) where
 - *n* is the number Afd WeChat powcoder
 - k is the number of devices
- The complexity of MVA makes it a very practical method

MVA - overview

- MVA analysis has been derived for
 - Closed model
 - Single-class
 - Multi-class
 - Open model Assignment Project Exam Help
 Mixed model with both open and closed queueing

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This lecture discusses MVA for single-class closed model

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MVA for closed system

- Consider a closed queueing network with a single-class of customers
- You are given a system with K devices
- You are given that each customer

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 - Visits device j on μης g φρίου times r.com
 - Requires a mean service time of S(j) from device j
 - Note: The servaced merculinate is assometer be exponentially distributed
- From the information given, we can deduce that the service demand D(j) for device j is V(j) S(j)
- How do we obtain D(j) for a practical system?

Key idea behind MVA

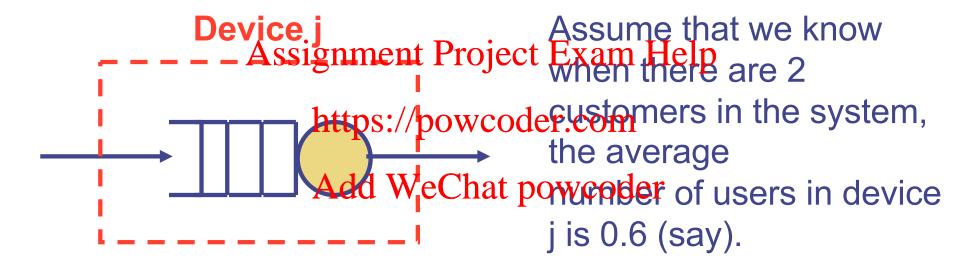
- Key idea behind MVA is iteration
 - If you know the solution to the problem when there are customers in the system, you can find the solution when there are (n+1) customers

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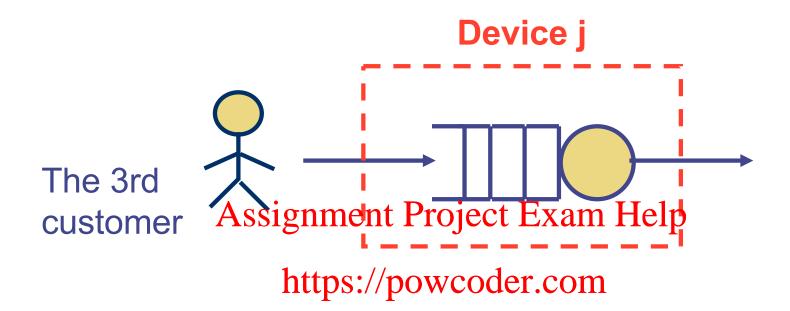
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Let us consider a simple example to motivate the iteration in MVA. Consider device j (say) of a queueing network.



What happens when there are 3 customers?

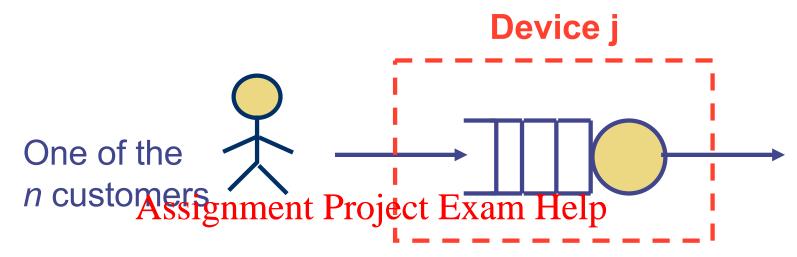
What happens when there are 3 customers?



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- Let us assume the 3rd customer is arriving at device *j*.
- Where will the other 2 customers be? We cannot tell exactly but we know that there is on average of 0.6 customers in device *j* when there are 2 customers.
- The 3rd customer will see on average 0.6 customers when it arrives at device *j*.

When there are n customers ...



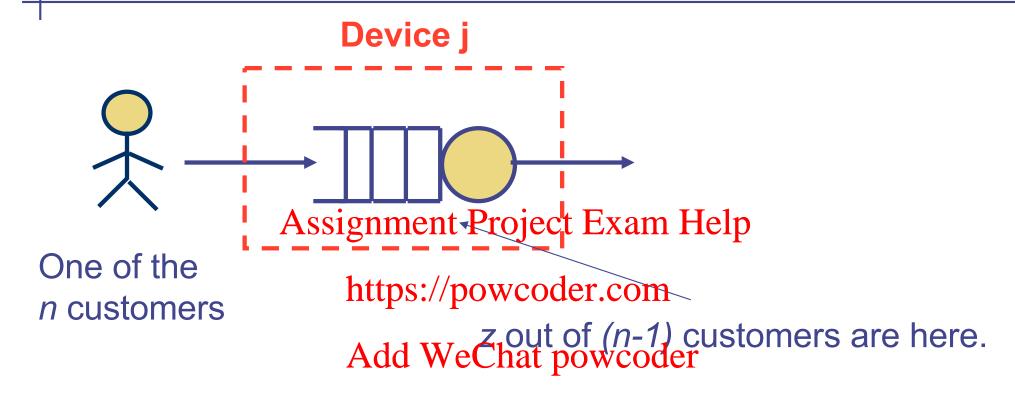
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Arrival Theorem

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- If there are (*n*-1) customers in the system, the mean number of customers in device *j* is *z* customers,
- Then, when there are n customers, each customer arriving at device j will see on average z customers ahead of itself in device j.

How can Arrival Theorem help?



Let S(j) = mean service time at device j. When there are n customers, The mean waiting time at device j = z S(j)The mean response time at device j = (z+1) S(j)

Iterations of MVA:

#customers = Mean number of customers in each device n-1 Assignment Project Exam Help Mean response tirhteps://pow/codericeom Add WeChat powcoder #customers = Mean number of customers in each device Mean response time for each device #customers = n+1

Some notation

Note "(n)" means there are n customers in the system

$$\bar{n}_i(n) = \text{Mean} \#_{\text{roject Example Ip}} \text{device i}$$

 $R_i(n) = \text{Meantipes/powsedetime} \text{ in device i}$

 $R_0(n) = \text{Mean response time of the system}$

 $X_i(n) = \text{Throughput of device i}$

 $X_0(n) = \text{Throughput of the system}$

Mean response time of each device

 $R_i(n)$

$$R_0(n) = \sum_{i=1}^K V_i \times R_i(n)$$

System response time

 $R_0(n)$

Assignment Project Exam Help $X_0(n) = \frac{1}{n}$ https://powcoder.com

Throughput of the system We Chat powcoder

$$X_0(n)$$

$$X_i(n) = V_i \times X_0(n)$$

Throughput of each device

$$X_i(n)$$

$$\bar{n}_i(n) = R_i(n) \times X_i(n)$$

Mean # customers in each device

 $\bar{n}_i(n)_-$

Initialisation of MVA:

Mean number of customers in each device

#customers = 0

$$\bar{n}_i(0) = 0$$

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Mean response tirhteps://pawcoderceom

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Mean number of customers in each device

#customers = 1

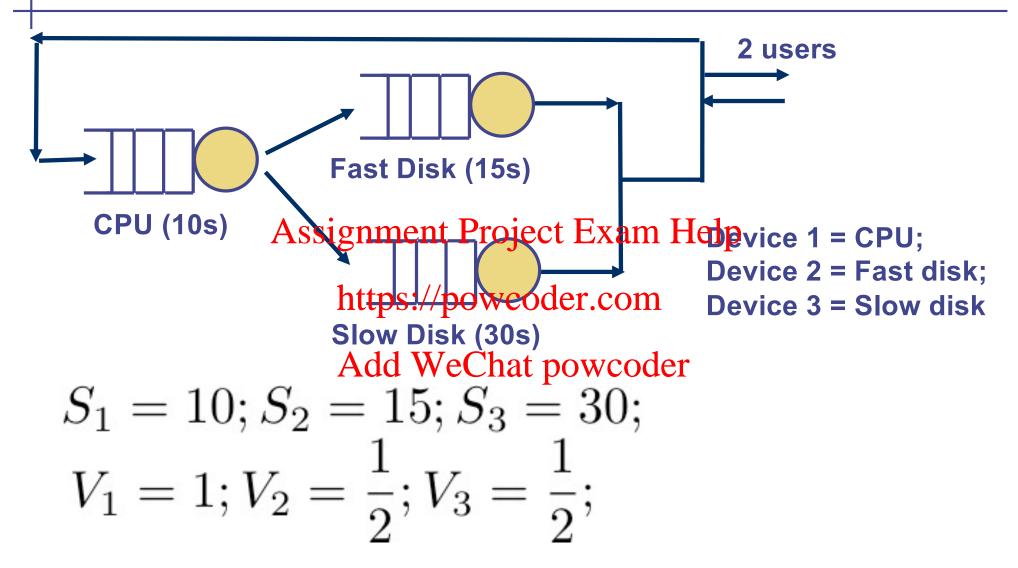
Mean response time for each device

#customers = 2

. . .

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Let us apply MVA to the database server example



- Determine the performance when there are 2 users in the system
- And how about 3 users?

Limitation of MVA

- MVA allows you to find the mean value of throughput, response time etc.
- However, if you are interested to find the probability that the system is in a certain state. MVA cannot give you the answer. You and the probability that the system is in a certain state. MVA cannot give you the answer. You are interested to find the probability that

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Extensions of MVA

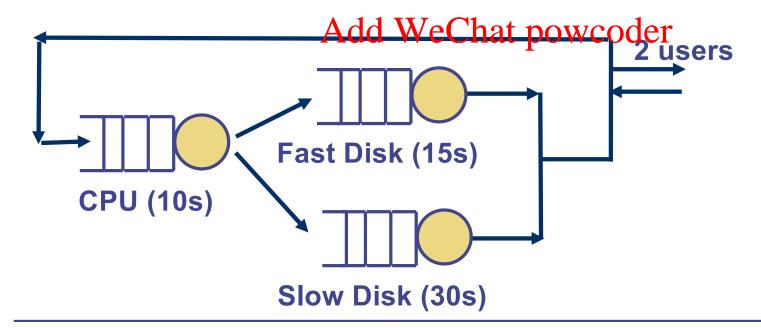
- Closed queueing networks with multiple classes of customers
 - Example: Database servers with 2 classes of customers
 - One class of customers require mean service time of 0.02s, 0.03s and 0.05s from the CPU, fast and slow disk
 - Another class of customers require mean service time of 0.04s, 0.01s and 0.1s from the CPU, fast and slow disk . https://powcoder.com
- Open queueing networks
- Mixed queueing Activity Chat powcoder

Assumptions behind MVA

- The service time is exponentially distributed
- The service time required at each component is independent
 - For example, MVA assumes that the service time required at CPU is independent of the service time at the disk

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Solution to network of queues

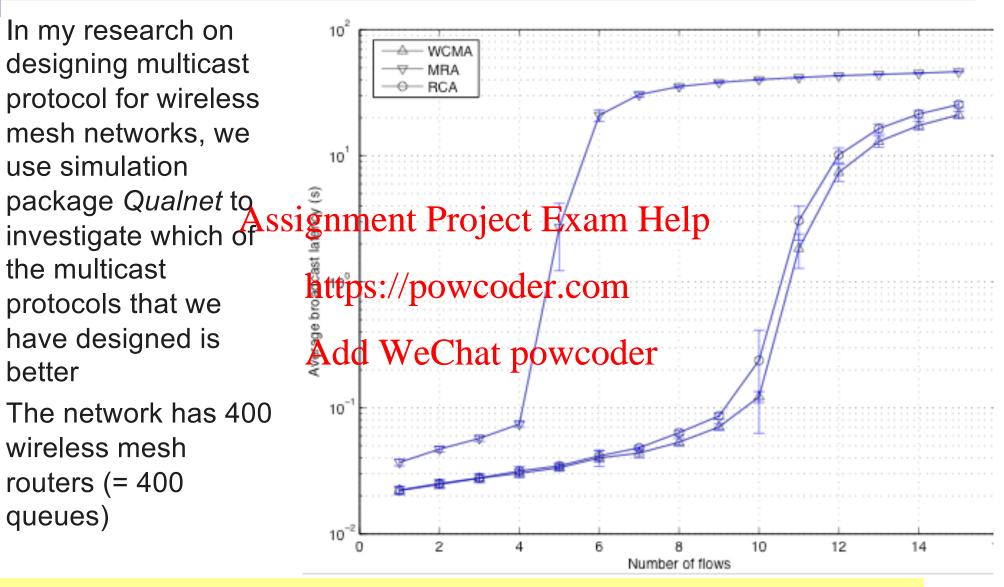
- You have seen two possible methods to solve a network of queues
 - Analytical solution
 - Simulation
- For closed questions of two kerwith and properties with an appropriate of the closed questions of the closed ques
 - Markov chain https://powcoder.com
 - MVA Add WeChat powcoder
- Commercial simulation tools can deal with hundred of nodes

Multicast in wireless mesh networks

In my research on designing multicast protocol for wireless mesh networks, we use simulation package Qualnet to the multicast protocols that we have designed is

The network has 400 wireless mesh routers (= 400 queues)

better



You can find out more on my research from my web site: http://www.cse.unsw.edu.au/~ctchou/

Analytical solution versus simulation

- Analytical solution
 - Limited to specific cases
 - E.g. Exponential assumptions
 - Efficient computation algorithm exists for certain cases
 - MVA for closed queueing networks with exponential service time Assignment Project Exam Help
- Simulation https://powcoder.com
 - Can apply to general settings we construct powcoder
 - Difference classes of traffic, protocols etc.
 - Can apply to reasonably large networks too

References

- The primary reference for MVA for closed queueing networks with one class of customer is:
 - Chapter 12, Menasce et al., "Performance by design"
- An alternative reference for MVA is Chapter 6 of Edward Lazowska etals: Quantitative; System Partigrance, Prentice Hall, 1984. (Now out of print but can be download from http://www.bttps://ppycodercopmmes/lazowska/qsp/)
 - Note that Chapter 6 has a wider coverage. It talks about open queueing network as well as approximation method too.
- For a formal mathematical proof of Arrival Theorem, see Bertsekas and Gallager, "Data networks", Section 3.8.3