

COMP9334

# Capacity Planning of Computer Systems and Networks

Assignment Project Exam Help

Week 1A: <https://powcoder.com> Revision problems

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## Question 1

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- An important part of performance analysis is to model the workload. In this question, you will look at a very simple model and we will generalise it to a very well known model in performance analysis in the lecture in Week 2.
- Consider a user who may send HTTP requests to a web server. In the time interval  $[k\delta, (k+1)\delta)$  where  $k$  is a non-negative integer, there is a probability of  $p$  that this user will send an HTTP request to a web server and there is a probability of  $(1-p)$  that this user will not send. Assuming that the probability the user sends (or not send) in each time interval is independent. Assuming that the current time is  $10\delta$ , what is the probability that this user will not send an HTTP request to the web server before  $30\delta$ ?

## Question 2

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- This is a revision question on probability distribution which you should be able to solve if you have the pre-requisites.
- Consider a continuous probability distribution with sample space is  $[1, \infty)$  and probability density function
  - $f(x) = a / x^3$  for  $x \geq 1$
- What is the value of  $a$  in order that  $f(x)$  be a valid probability density function?
- What is the probability that a number drawn from this distribution is exactly 10?
- Given this probability density function, what is the probability that a number drawn from this distribution has a value greater than 10?

## Question 1 - Answers

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Prob (the user will not send before  $30\delta$ )

= Prob (the user will not send in  $[10\delta, 11\delta)$ )  $\times$

Prob (the user will not send in  $[11\delta, 12\delta)$ )  $\times \dots$

Prob (the user will not send in  $[29\delta, 30\delta)$ )

(note: the probability to send is independent for each time)

=  $(1-p)^{20}$

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## Question 2 – Answers (Page 1)

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- In order that the probability density function be valid, the probability that the number is drawn between  $[1, \infty)$  is 1.

$$\int_1^{\infty} \frac{a}{x^3} = 1 \Rightarrow \left[ \frac{ax^{-2}}{-2} \right]_1^{\infty} = 1 \Rightarrow \frac{a}{2} = 1 \Rightarrow a = 2$$

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- Probability that a number drawn is exactly 10 is zero
  - Explanation: The numbers that can come from this distribution is in the range  $[1, \infty)$  and there are infinite numbers, hence the probability of getting just one number (in this case 10), is zero.

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## Question 2 – Answers (Page 2)

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- Probability that a number drawn is greater than 10 =

$$\int_{10}^{\infty} \frac{2}{x^3} = \left[ \frac{2x^{-2}}{-2} \right]_{10}^{\infty} = 0.01$$

- Note: The probability distribution that you've worked with is called a Pareto distribution. It has what is known as a heavy tail properties. This probability distribution appears very often in modern computer performance analysis.