# COMP9334 Capacity Planning for Computer Systems and Networks

Assignment Project Exam Help

Week 7AhttpsQ/peweindgrdissoiplines

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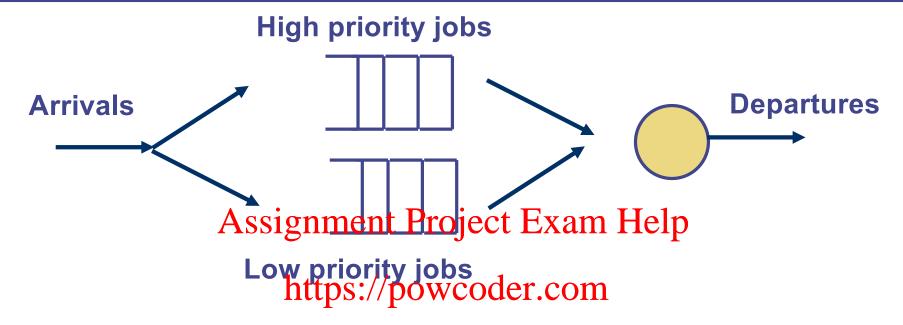
# Queuing disciplines



- We have focused on *first-come first-serve* (FCFS) queues Assignment Project Exam Help so far
- However, sometimes:you may want to give some jobs a higher priority than others
- Priority queues can be classified as
  - Non-preemptive
  - Preemptive resume

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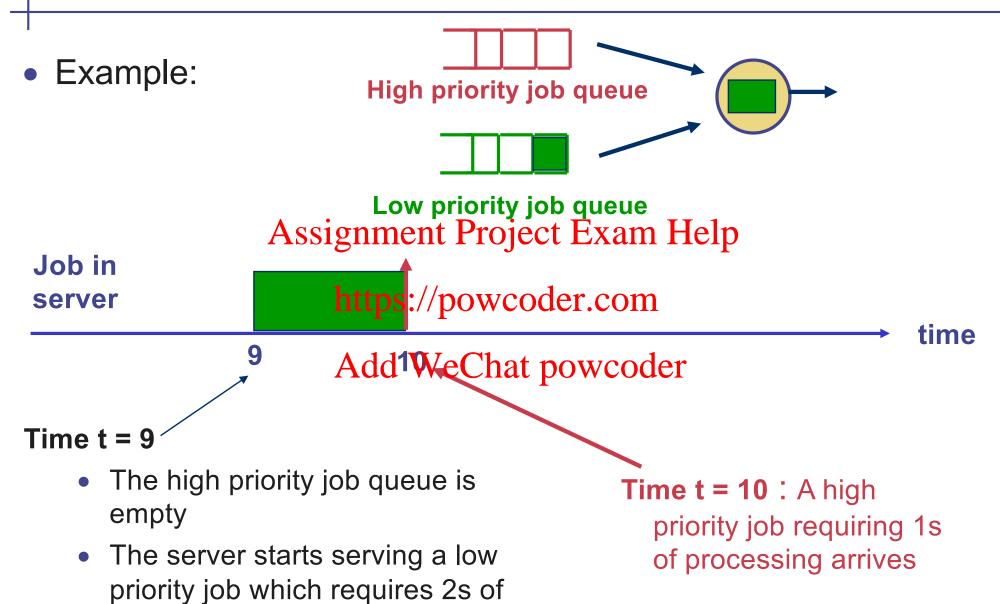
# What is priority queueing?



- A job with low priority will only get served if the high priority queue is empty
- Each priority queue is a FCFS queue
- Exercise: If the server has finished a job and finds 1 job in the high priority queue and 3 jobs in the low priority queue, which job will the server start to work on?
  - Repeat the exercise when the high priority queue is empty and there are 3 jobs in the low priority queue.

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# Preemptive and non-preemptive priority (1)

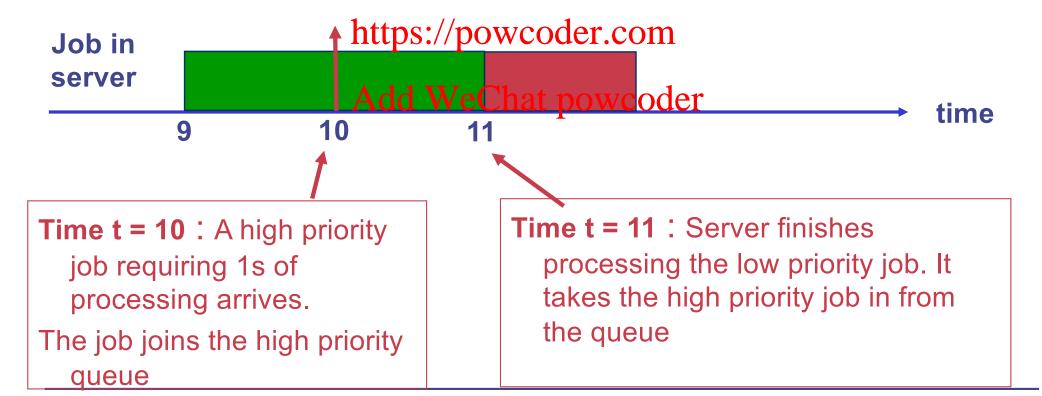


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# Preemptive and non-preemptive priority (2)

- Non-preemptive:
  - A job being served will not be interrupted (even if a higher priority job arrives in the mean time)
- Example: High priority job (red), low priority job (green)
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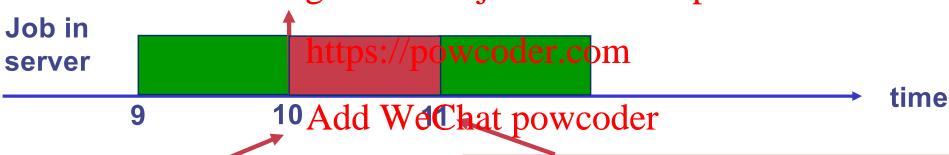


# Preemptive and non-preemptive priority (3)

#### • Preemptive resume:

• Higher priority job will interrupt a lower priority job under service. Once all higher priorities served, an interrupted lower priority job is resumed.

• Example: High priority job (red), low priority job (green) Assignment Project Exam Help

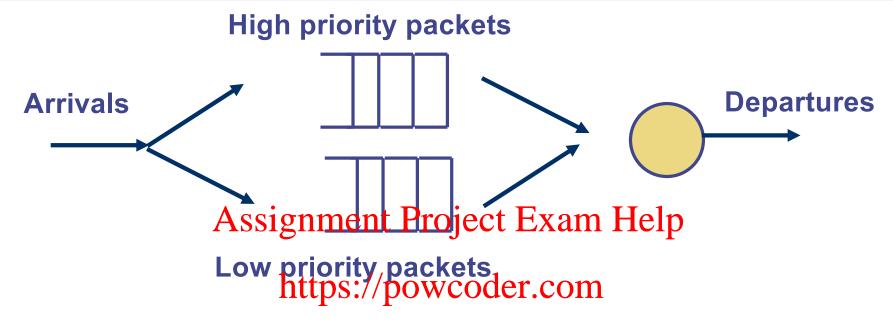


Time t = 10: A high priority job requiring 1s of processing arrives.

The server starts processing the high priority job immediately

Time t = 11: Server finishes processing the high priority job. Since no high priority job arrives in (10,11], the high priority job queue is empty, it resumes processing the low priority job that is pre-empted at time t = 10

## Example of non-preemptive priority queueing



- Example: In the output port of a router, you want to give some packets a higher priority priority
  - In Differentiated Service
    - Real-time voice and video packets are given higher priority because they need a lower end-to-end delay
    - Other packets are given lower priority
- You cannot preempt a packet transmission and resume its transmission later
  - A truncated packet will have a wrong checksum and packet length etc.

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# Example of preemptive resume priority queueing

- E.g. Modelling multi-tasking of processors
- Can interrupt a job but you need to do context switching (i.e. save the registers for the current job so that it can be resumed later)

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# M/G/1 with priorities

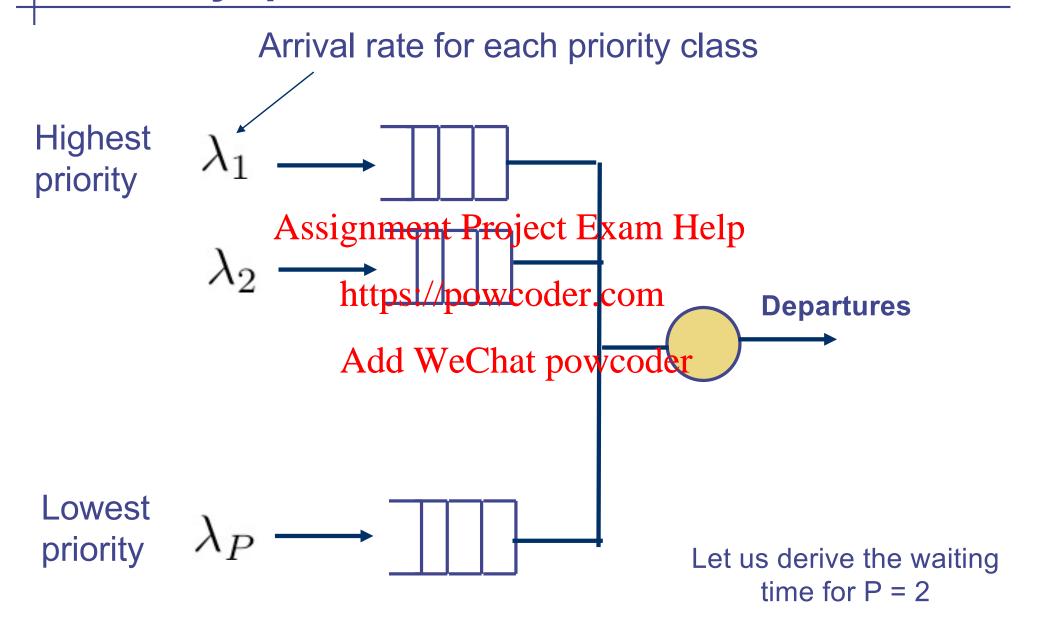
- Separate queue for each priority (see picture next page)
  - Classified into P priorities before entering a queue
  - Priorities numbered 1 to P, Queue 1 being the highest priority
- Arrival rate of priority class p is Assignment Project Exam Help

$$\lambda_p$$
 wherepoweder from  $P$ 

• Average service time and second moment of class p requests is given by

$$E[S_p]$$
 and  $E[S_p^2]$ 

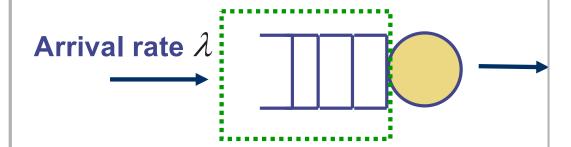
# **Priority queue**



# Lecture 4A: Deriving the P-K formula

- Let
  - W = Mean waiting time
  - N = Mean number of customers in the queue

  - R = Mean residual service time



• 1/  $\mu$  = Mean service time Assignment Project Exam Help • R = Mean residual

https://powcoder.com $N = \lambda W$ 

- We can prove that
  - W = N \*  $(1/\mu)$  + Rdd WeChat powcoder Substitution

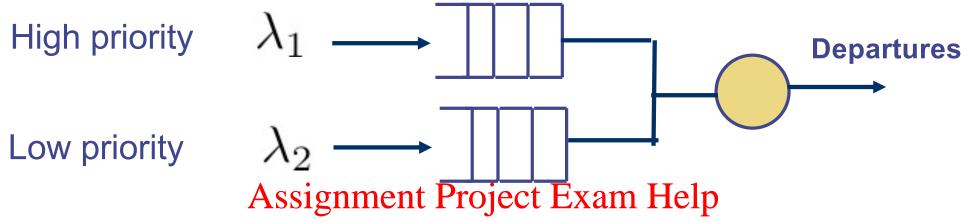
$$W = \lambda \times W \times \frac{1}{\mu} + R$$

Mean residual time R

$$R = \frac{1}{2}\lambda E[S^2]$$

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# Deriving the non-preemptive queue result (1)



- S<sub>1</sub> service time for Class 1 with mean E[S<sub>1</sub>]

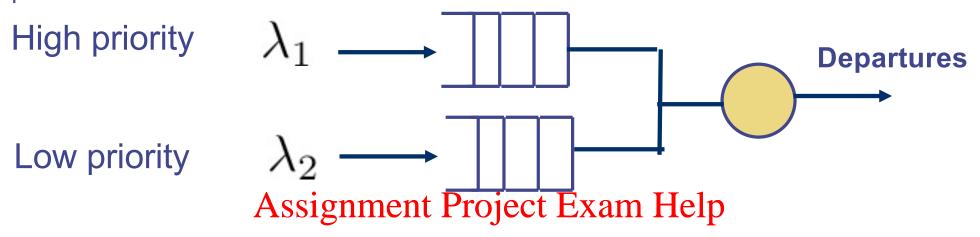
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   W<sub>1</sub> = mean waiting time for Class 1 customers
- N<sub>1</sub> = number of Class Westernewicother queue
- R = mean residual service time when a customer arrives
- We have for Class 1: W₁ = N₁ E[S₁] + R
- Little's Law:  $N_1 = \lambda_1 W_1$

$$W_1 = rac{R}{1-
ho_1}$$
 where  $ho_1 = \lambda_1 E[S_1]$ 

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# Deriving the non-preemptive queue result (2)



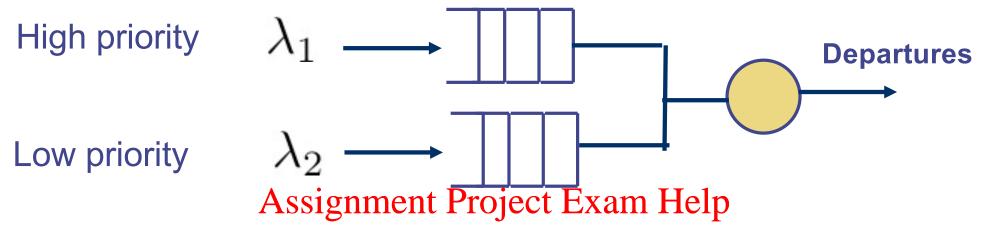
 To find the residual service time R, note that the customer in the server can be a high or low priority customer, we have

$$R = \begin{bmatrix} & \text{Add WeChat powcoder} \\ & + \end{bmatrix}$$

The waiting time is therefore

$$W_1 =$$

# Deriving the non-preemptive queue result (3)



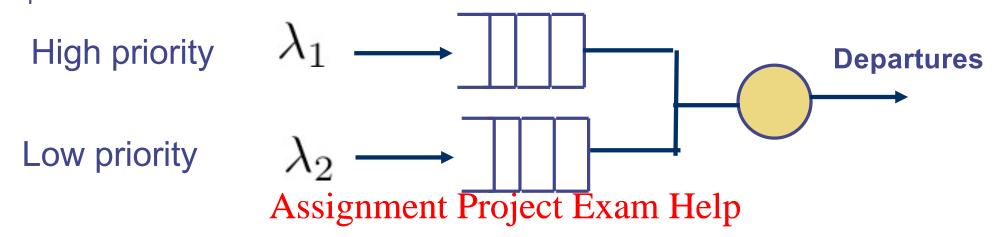
- S<sub>2</sub> service time for Class 2 with mean E[S<sub>2</sub>]

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   W<sub>2</sub> = mean waiting time for Class 2 customers
- N<sub>2</sub> = number of Class 2 Westbaters vir the rqueue
- R = mean residual service time when a customer arrives

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# Deriving the non-preemptive queue result (4)



 For Class 2 customers: https://powcoder.com

#### Question:

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Consider a customer arriving at the low priority queue, when can this customer receive service? This customer has to wait for

- The customer at the server to finish
- The customers who are already in the low priority queue when this customer arrives
- ?????
- ?????

# Deriving the non-preemptive queue result (5)

$$W_2 =$$

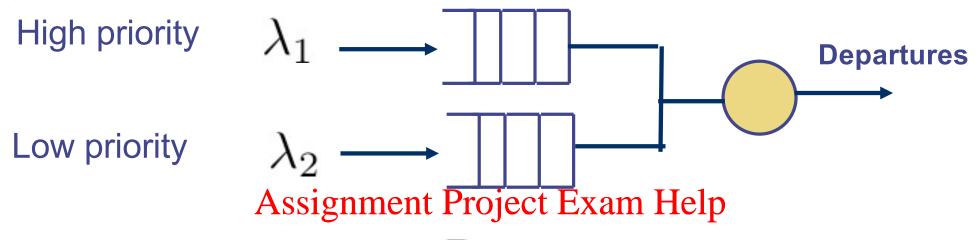
• Little's Law to Queue 1: Project Exam Help aw to Queue 2:

$$N_1 = \lambda_1 W_1^{
m Mttps://powcoder.com} N_2 = \lambda_2 W_2$$
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Combining all of the above

$$W_2 = rac{R + 
ho_1 W_1}{1 - 
ho_1 - 
ho_2} \quad {}^{ ext{Where}} \quad egin{array}{c} 
ho_2 = \lambda_2 E[S_2] \\ 
ho_1 = \lambda_1 E[S_1] \end{array}$$

# Deriving the non-preemptive queue result (6)



$$W_2 = \frac{ \text{https://pBwcoder.com}}{(1 - \text{Add)WeChat/ppowcoder})}$$

$$W_1 = \frac{R}{1 - \rho_1} \qquad \text{where} \qquad \begin{array}{l} \rho_1 = \lambda_1 E[S_1] \\ \rho_2 = \lambda_2 E[S_2] \\ R = \frac{1}{2} E[S_1^2] \lambda_1 + \frac{1}{2} E[S_2^2] \lambda_2 \end{array}$$

## Non-preemptive Priority with P classes

#### Waiting time of priority class k

$$W_k = \frac{R}{(1-\rho_1-\ldots-\rho_{k-1})(1-\rho_1-\ldots-\rho_k)}$$
 
$$\frac{R}{(1-\rho_1-\ldots-\rho_{k-1})(1-\rho_1-\ldots-\rho_k)}$$
 
$$\frac{R}{(1-\rho_1-\ldots-\rho_{k-1})(1-\rho_1-\ldots-\rho_k)}$$
 
$$\frac{R}{(1-\rho_1-\ldots-\rho_{k-1})(1-\rho_1-\ldots-\rho_k)}$$

where

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$$RAdd$$
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$$\rho_i = \lambda_i E[S_i] \text{ for } i = 1, ..., P$$

# Example

- Router receives packet at 1.2 packets/ms (Poisson), only one outgoing link
- Assume 50% packet of priority1, 30% of priority 2 and 20% of priority 3. Mean and second moment given in the table below.
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- What is the average waiting time per class?
- Solution to be discussed in class.

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Priority	Mean (ms)	2nd Moment (ms²)
1	0.5	0.375
2	0.4	0.400
3	0.3	0.180

# Pre-emptive resume priority (1)

- Can be derived using a similar method to that used for nonpreemptive priority
- The key issue to note is that a job with priority k can be interrupted by a job of higher priority even when it is in the server
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- For k = 1 (highest priority), the response time  $T_1$  is: https://powcoder.com

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$$T_1 = E[S_1] + \frac{R_1}{(1-\rho_1)}$$
 where  $R_1 = \frac{1}{2}E[S_1^2]\lambda_1$   $\rho_1 = E[S_1]\lambda_1$ 

A highest priority job only has to wait for the highest priority jobs in front of it.

# Preemptive resume priority (2)

For k ≥ 2, we have response time for a job in Class k:

#### Question:

Consider a customer arriving in priority class k (≥ 2), what are the components of the waiting time footbis customer?

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# Preemptive resume priority (3)

 Solving these equations, we have the response time of Class k jobs is:

$$T_k = T_{k,1} + T_{k,2}$$

#### where

$$T_{k,1} = \frac{Assignment \text{ Project Exam Help}}{(1-\rho_1 - \frac{\text{https://powco}}{\rho_{k-1}})}$$
 
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$$T_{k,2} = \frac{Add \text{ WeChat powcoder}}{(1-\rho_1 - \ldots - \rho_{k-1})(1-\rho_1 - \ldots - \rho_k)}$$

$$R_k = \frac{1}{2} \sum_{i=1}^k E[S_i^2] \lambda_i$$

# Other queuing disciplines

- There are many other queueing disciplines, examples include
  - Shortest processing time first
  - Shortest remaining processing time first
  - Shortest expected precessing time first Help
- Optional: For an advanced exposition on queueing disciplines, see Klerkioth, Wordering Systems Volume 2", Chapter 3.

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#### References

- Recommended reading
  - Bertsekas and Gallager, "Data Networks"
    - Section 3.5.3 for priority queuing
- Optional reading gnment Project Exam Help
  - Harchol-Balter, Chapter 22

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