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# Computer Graphics

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2021 Term 3 Lecture 5

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# What did we learn last week?

## 2D Graphics

- OpenGL Pipeline
- Textures
- Transforms
- Some ideas on how a 2D game could be made

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# What are we covering today?

## 3D Graphics

- We are entering the 3rd dimension!
- 2D to 3D . . . what changes?
- 3D Objects
- Coordinate Spaces
- Making a (virtual) Camera

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# 2D to 3D

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# What are our current capabilities?

## In our 2D Graphics

- Shapes made of triangles
- Textures on objects
- Transforms

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# Capabilities in 3D

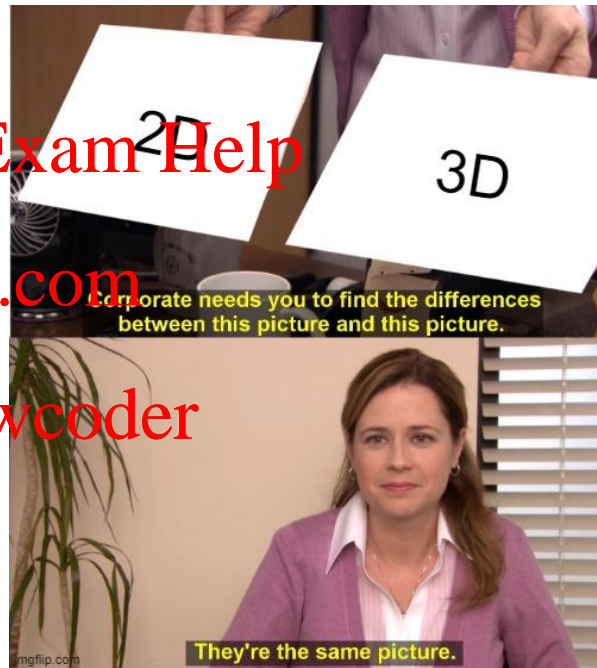
What are we wanting to do in 3D?

- Shapes made of triangles
- Textures on objects
- Transforms

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# Going to 3D

**We've been teaching you 3D graphics all along!**

- Only minor modifications needed
- Coordinates start to use z
- Triangles are always 2 dimensional objects ...
- ... but multiple triangles can make 3D objects
- Textures work with verts exactly as they do in 2D
- Transforms are going to add a dimension

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# 3D Transforms

**Our Transform Matrices are adding a dimension**

- Our Vectors are now  $(x, y, z, w)$
- Our Matrices are now  $4 \times 4$

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# Scale

Reasonably simple expansion into 3D

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Scale x	0	0
0	Scale y	0
0	0	1

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Scale x	0	0	0
0	Scale y	0	0
0	0	Scale z	0
0	0	0	1

# Translate

Reasonably simple also!

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1	0	Tx
0	1	Ty
0	0	1

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1	0	0	Tx
0	1	0	Ty
0	0	1	Tz
0	0	0	1

# Rotate

Gets more interesting here

- In 3D rotation must be done AROUND a vector
- In 2D we were basically rotating around the Z axis

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$\cos\theta$	$-\sin\theta$	0
$\sin\theta$	$\cos\theta$	0
0	0	1

$\cos\theta$	$-\sin\theta$	0	0
$\sin\theta$	$\cos\theta$	0	0
0	0	1	0
0	0	0	1

This row leaves the Z coordinate unaffected by the transform

This column stops the Z coordinate from affecting any others

# Rotate around other axes

We can similarly rotate around the X or Y axes

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1	0	0	0
0	$\cos\theta$	$-\sin\theta$	0
0	$\sin\theta$	$\cos\theta$	0
0	0	0	1

Rotate around X

$\cos\theta$	0	$\sin\theta$	0
0	1	0	0
$-\sin\theta$	0	$\cos\theta$	0
0	0	0	1

Rotate around Y

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# 3D Objects

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# Making 3D Objects

## Meshes of vertices

- We've already seen things like rectangles made up of two triangles
- In 3D triangles can form the outer surface of an object
- Vertices can form surfaces that wrap entirely around an object

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University of Utah  
Computer Science

Image credit: School of Computing, University of Utah

# Inside vs Outside

**The idea of a surface implies an inside and outside**

- Triangles now have a front and a back
- Vertices go from being points in space to being positions on a surface
- These are important properties that we'll be looking at in detail later . . .

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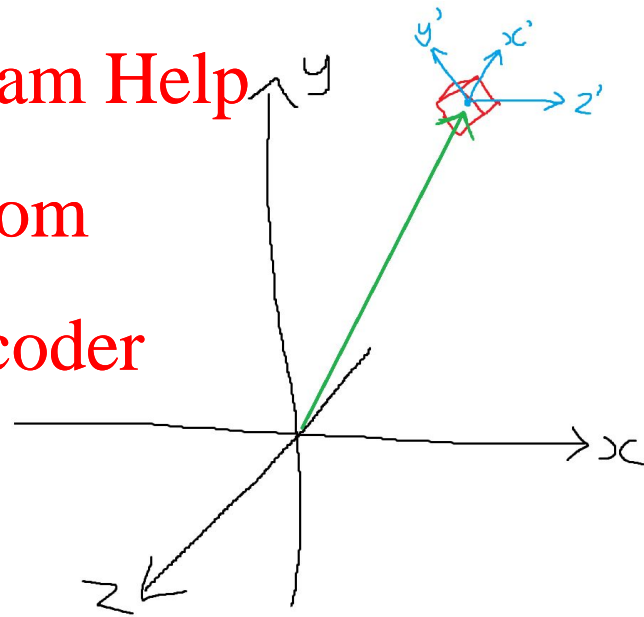
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# Coordinate Spaces

Each object actually exists in its own local coordinate space

- This means each **object** actually has its own **local** origin  $(0,0,0)$
- ... which is a **point in space** in the **world** coordinates
- And its own **local**  $x, y$  and  $z$  axes
- ... which are **vectors** in the **world** space



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# What is a transform?

We've seen them already, but what do they represent?

- A Transform Matrix is actually the **local** origin and axes of an object in relation to the **world** space
- When we're applying a transform, we're actually shifting an object between two coordinate systems

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# Deconstructing the Transform

The Identity Matrix is the World Transform

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The X axis →

The Y axis →

The Z axis →

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1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

↑  
The origin

# Deconstructing a Scale Transform

## What happens in the scale transform?


- The object's X axis is twice as "long" as the world's X axis
- This is in effect what "stretches" the object

The X axis has  
been doubled

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2	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

# Deconstructing a Translate Transform

What happens in the translate transform?

- The object has an origin of (5,6,2)
- This means that its vertices are now positioned relative to that point

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	0	0	5
0	1	0	6
0	0	1	2
0	0	0	1

The origin of the object has moved

# Composing Multiple Transforms

## Multiple Transforms together

- Retain all information from each of the transforms
- Build up a set of axes and origin for an object
- The final transform takes an object from **local** to **world** space
- It's also known as the **model matrix**

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# Break Time

## The Matrix (1999)

- Speaking of important films with CG ...
- The Matrix was rendered in Sydney by Animal Logic
- One of the Silicon Graphics Onyx machines used in the Matrix is in the lobby of the K17 building (donated by Marc Chee and others from iCinema in 2012)

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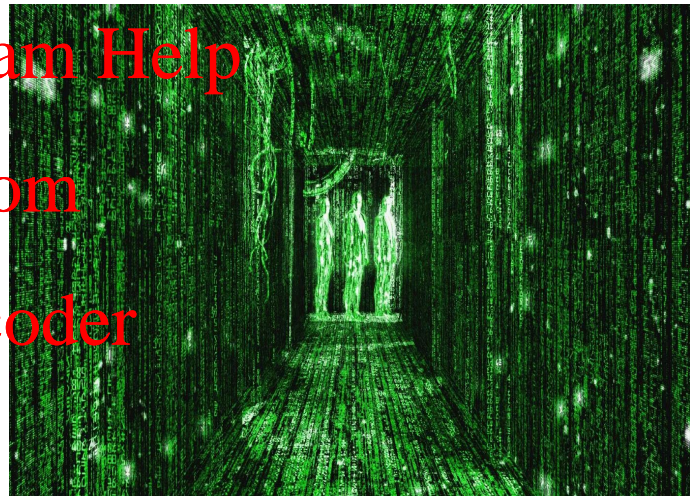


Image credit: Warner Bros Entertainment

# Cameras and Viewpoints

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# Cameras as Objects in a Scene

## They exist in their own coordinate space

- So a camera will have its own transform matrix
- But it's not a 3D model, and has no vertices!
- It's more of a viewpoint that exists in the world space
- OpenGL will treat the camera as if its Z axis points from your screen to your eyes
- Using the camera transform will put all the vertices into the camera's perspective!

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# Making a Camera Transform

How do we make our camera?

- Build up the transform piece by piece

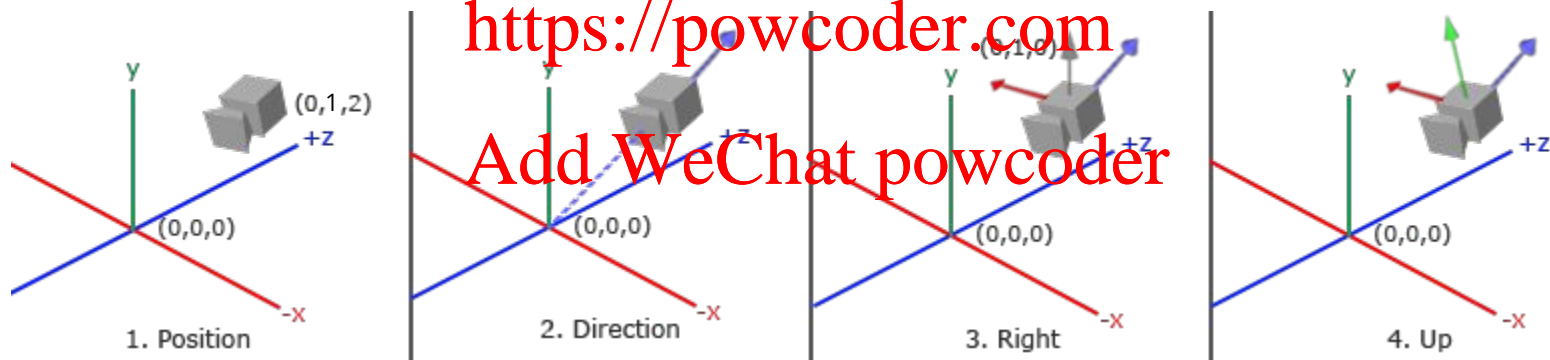


Image credit: learnopengl.com

# Camera Position

## Placing the camera in a position

- Placing something in our scene using a Translate transform
- *Let's use (0,1,2) as an example*
- *Our camera is along and just above the Z axis*

1	0	0	Px
0	1	0	Py
0	0	1	Pz
0	0	0	1

# Camera Direction

Start building the three axes of our camera's coordinate space

- The first vector goes from where the camera is looking
- to the camera itself
- It's directly on the line the camera is looking, but aimed at the camera
- $(\text{Camera Location}) - (\text{What we're looking at})$
- *In this example, we can keep it simple.*
- $(0,1,2) - (0,0,0) = (0,1,2)$

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# Vectors ... Directions with Length?

We're going to want to be careful with all our vectors

- Vectors can represent points or directions
- If they represent a direction and not a distance ...
- Then we should always **normalize** them!
- Normalize roughly means: "Make a vector length 1"
- We do this by dividing a vector by its own length
- $(0,1,2)$  normalized is  $(0, 1/\sqrt{5}, 2/\sqrt{5})$

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# The World's Up Vector

## We have an assumption of gravity

- Humans tend to expect the camera to stay upright
- So there's always an idea of up and down in a virtual world
- We can keep this simple in most worlds by using the Y axis:
- $(0, 1, 0)$
- Is this an acceptable axis to add to the camera?

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# Why have the Up Vector?

## The World's Up vector can't be trusted as an axis

- To make a set of axes, they MUST be orthogonal
- That means they're all 90 degrees from each other
- There's no guarantee the World's Up vector is 90 degrees from the Camera Direction vector
- (in fact it's incredibly unlikely!)
- But we'll use it to make one of our axes . . .

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# The Right Vector

Not the wrong vector.

- One of the axes in our camera is the one that goes to the right
- Like going across the surface of a screen from left to right
- How do we create a vector that's right angle to two other vectors?
- **Cross Product!**
- Up x Camera Direction = Right
- (remember that cross product order is important . . . right hand rule)
- $(0,1,0) \times (0,1,2) = (2,0,0)$
- *We'd normalize this to  $(1,0,0)$*

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# Camera's Up Vector (or the Up Axis)

The third axis is easy to make

- If we have two vectors, we can make a third that's orthogonal
- **Cross Product**
- Camera Direction  $\times$  Right = Up Axis
- $(0, 1, 2) \times (1, 0, 0) = (0, 2, -1)$
- *Normalized to  $(0, 2/\sqrt{5}, -1/\sqrt{5})$*

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# Three Axes make a transform

## Making a Transform

- Use the vectors to make a matrix
- The Right Vector
- The (camera's) Up
- The Camera Direction
- This gives us all our rotation and scaling, but isn't yet using our position

Rx	Ry	Rz	0
Ux	Uy	Uz	0
Dx	Dy	Dz	0
0	0	0	1

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# Combine the Camera Position with Orientation

## Multiplying the two matrices together

- The resulting transform is known as the **LookAt** matrix
- This moves the world relative to the camera

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Rx	Ry	Rz	0
Ux	Uy	Uz	0
Dx	Dy	Dz	0
0	0	0	1

X

1	0	0	Px
0	1	0	Py
0	0	1	Pz
0	0	0	1

# Will we need to do all this maths?

## Thanks again GLM

- The GL Maths Library has a single function for creating a LookAt matrix
- `glm::lookAt(position, target, up)`
- This function allows us to give only three vectors and will calculate the LookAt matrix for us

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# What did we learn today?

## 2D to 3D

- A lot of what we knew still applies in 3D
- Some 3D Transforms
- Objects as meshes
- Transforms as their own coordinate spaces
- Making a Camera LookAt transform

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