## COMP9444 Neural Networks and Deep Learning Term 3, 2020

## Solutions to Exercise 8: Hopfield Networks

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1. https://powcoder.com

a. Compute the weight matrix for a Hopfield network with the two memory restart near Project Exam Help [1, -1, 1, -1, 1, 1, 1] stored in it.

The outersing the diagonal entries to zero) is

The outer product  $W_2$  of [1, 1, 1, -1, -1, -1] with itself (but setting the diagonal entries to zero) is

The weight matrix W is  $(1/6)\times(W_1 + W_2) = (1/3)\times$ 

b. Confirm that both tipes of this network.

$$\begin{array}{l} \operatorname{sgn}(W.[1A-1]signment=\Pr(2/3)x[1E-1]n-1,Help\\ = [1,-1,1,-1,1] \end{array}$$
 so this one is stable Similarly that 
$$\operatorname{political}_{sgn}(W.[1,1],E,-1]=\operatorname{sgn}((2/3)x[1,1,1,-1])=\operatorname{sgn}((2/3)x[1,1,1,-1,-1])$$
 so this one is stable topowcoder.com

2. Consider the following wind with that wowcoder

$$0.0 - 0.2$$
  $0.2 - 0.2 - 0.2$   
 $-0.2$   $0.0 - 0.2$   $0.2$   $0.2$   
 $0.2 - 0.2$   $0.0 - 0.2 - 0.2$   
 $-0.2$   $0.2 - 0.2$   $0.0$   $0.2$   
 $-0.2$   $0.2 - 0.2$   $0.0$   $0.2$ 

a. Starting in the state [1, 1, 1, 1, -1], compute the state flow to the stable state using <u>asynchronous</u> updates.

W.[1, 1, 1, 1, 
$$-1$$
] = [0,  $-0.4$ , 0,  $-0.4$ , 0]. Hence:

If neuron 1, 3, or 5 updates first, its total net input is 0, so it does not change state;

If neuron 2 updates first, its total net input is -0.4, and it's current value is +1, so it changes state to -1, and the new state is [1, -1, 1, 1]

1, -1]. Call this Case A.

If neuron 4 updates first, its total net input is -0.4, and it's current value is one, so it changes state to -1, and the new state is [1, 1, 1, -1, -1]. Call this Case B.

Case A: W.[1, -1, 1, 1, -1] = [0.4, -0.4, 0.4, -0.8, -0.4]. Hence: If neurons 1, 2, 3, or 5 update first, there is no state change. If neuron 4 updates first, it flips, and the new state is [1, -1, 1, -1, -1].

W.[1, -1, 1, -1, -1] = [0.8, -0.8, 0.8, -0.8, -0.8]. So no matter which neuron updates, there is no change. This is a stable state.

b. Starting in the (same) state [1, 1, 1, 1, -1], compute the next state using synchrodical using synchrodic

W.[1, 1, 1, 1, -1] = [0, -0.4, 0, -0.4, 0], so neurons 2 and 4 flip, resulting in a state of

[1, -1, 1, -1, -1]. (We know from the previous part that this is a stable state.)