

COMP95437/pComputer Vision

Add WeChat powcoder Feature Representation

Part 1

Outline

- Need for feature representation
- Major types of features
 - Colour Assignment Project Exam Help
 - Texture
 - Shape https://powcoder.com
- Feature descriptors and their use in various computer vision applications

Image Features

- Image features are essentially vectors that are a compact representation of images
- They represely important inforcetton shows in age

Intuitive examples of image features: https://powcoder.com

Blobs

Edges

Corners

- Ridges
- Circles
- Ellipses
- Lines
- Etc...



Image Features

- We need to represent images as feature vectors for further processing in a more efficient and robust way
- Examples of further processing include: Help
 - Object detection
 https://powcoder.com
 - Image segmentation
 - Image classificatand WeChat powcoder
 - Content-based image retrieval
 - Image stitching
 - Object tracking

Object Detection



Segmentation



Image Classification



Content-Based Image Retrieval

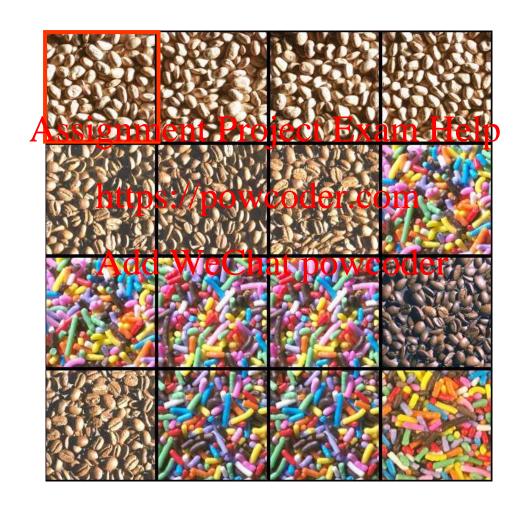


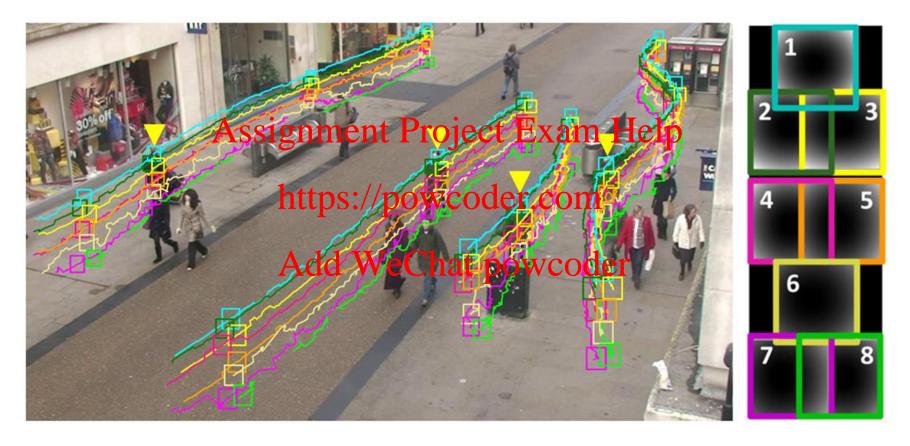
Image Stitching



Add WeChat powcoder



Object Tracking



https://heartbeat.fritz.ai/

Properties of Features

- Why not just use pixels values directly?
 - Pixel values change with light intensity, colour and direction
 - They also shange with campro of jentation an Help
 - And they are highly redundant
- Repeatability (robttoness)owcoder.com
 - Should be detectable at the same locations in different images despite changes in flumination and viewpointer
- Saliency (descriptiveness)
 - Similar salient points in different images should have similar features
- Compactness (efficiency)
 - Fewer features
 - Smaller features

General Framework

Object detection
Image segmentation
Image classification
Image retrieval
Image stitching
Object tracking

Image Pre-processing Assignment Project Exam Help Add WeChat powcoder **Deep Learning** Pattern Recognition Post-processing

Feature Types

- Colour features
 - Colour histogram
 - Colour moments Project Exam Help
- Texture features
 - Haralick texture https://powcoder.com

 - Local binary patterns (LBP)
 Scale-invariant feature transform (SIFT)
 - Texture feature encoding
- Shape features
 - Basic shape features
 - Shape context
 - Histogram of oriented gradients (HOG)

Colour Features

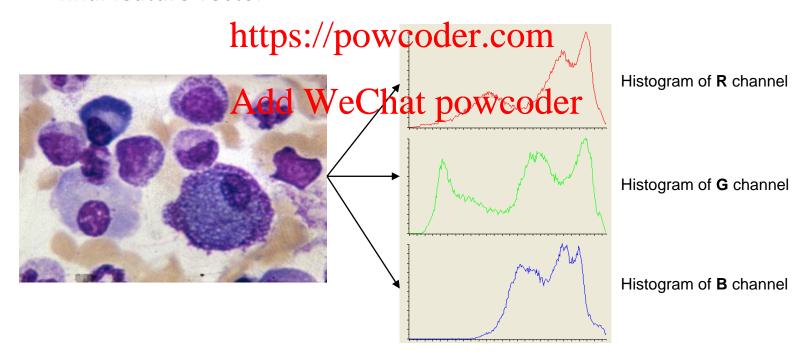
- <u>Colour</u> is the simplest feature to compute, and is invariant to image scaling, translation and rotation.
- Example: colouri basad in Projecti Evalum Help



http://labs.tineye.com/multicolr/

Colour Histogram

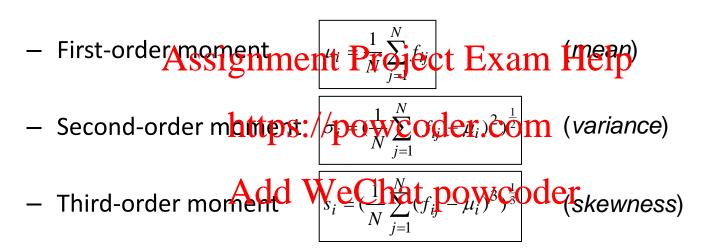
- Represent the global distribution of pixel colours in an image
 - Step 1: Construct a histogram for each colour channel (R, G, B)
 - Step 2: Concatenate the histograms (vectors) of all channels as the final feature vector



Colour Moments

 f_{ij} is the value of the *i*-th colour component of pixel *j* and *N* is the number of pixels in the image

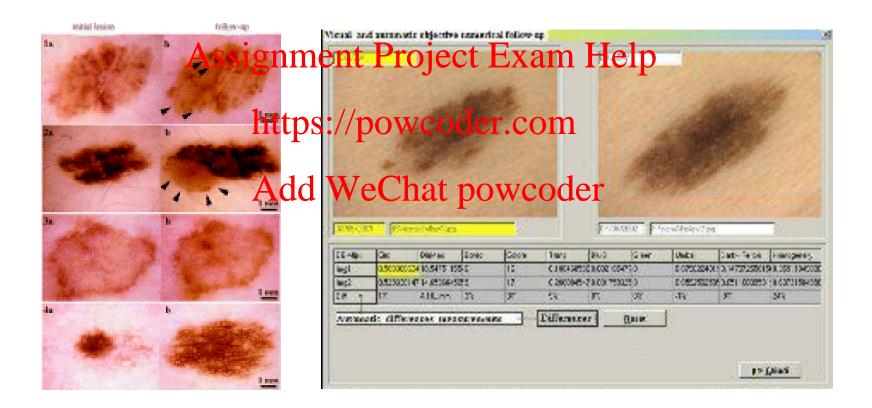
Another way of representing colour distributions



- Moments based representation of colour distributions
 - Gives a feature vector of only 9 elements (for RGB images)
 - Lower representation capability than the colour histogram

Application Example

Colour-based image retrieval



Texture Features

- <u>Texture</u> is a powerful discriminating feature for identifying visual patterns with properties of homogeneity that cannot result from the presence of only a single colour or intensity
- Example: texture classification



https://arxiv.org/abs/1801.10324

- Haralick features give an array of statistical descriptors of image patterns to capture the spatial relationship between neighbouring pixels, that is textures an Help
 - Step 1: Construct the gray-level co-occurrence matrix (GLCM)
 - Step 2: Computentle Barapok recommons from the GLCM

610

Add Wechat powcoder LEEE TRANSACTIONS ON SYSTEMS, MAN, AND CYBERNETICS, VOL. SMC-3, NO. 6, NOVEMBER 197

Textural Features for Image Classification

ROBERT M. HARALICK, K. SHANMUGAM, AND ITS'HAK DINSTEIN

Abstract—Texture is one of the important characteristics used in identifying objects or regions of interest in an image, whether the image be a photomicrograph, an aerial photograph, or a satellite image. This paper describes some easily computable textural features based on graytone spatial dependancies, and illustrates their application in category-

array. If $L_x = \{1, 2, \dots, N_x\}$ and $L_y = \{1, 2, \dots, N_y\}$ are the X and Y spatial domains, then $L_x \times L_y$ is the set of resolution cells and the digital image I is a function which assigns some gray-tone value $G \in \{1, 2, \dots, N_g\}$ to each and every

Step 1: Construct the GLCMs

- Given a distance d at an orientation angle ϑ , then $p_{(d,\vartheta)}(I_1,I_2)$, being the (I_1,I_2) coefficient of the corresponding matrix $P_{(a-b)}$, is the co-occurrence count or probability of solid than the probability o sample spacing of d along the axis making an angle ϑ with the x axis.
- If the number of distrasgrapewscode կան լանավ image is L, then the cooccurrence matrix **P** will be of size $L \times L$.

0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

Add WeChat powcoder
$$\mathbf{P}_{(1,0^{\circ})} = \begin{bmatrix} 4 & 2 & 1 & 0 \\ 2 & 4 & 0 & 0 \\ 1 & 0 & 6 & 1 \\ 0 & 0 & 1 & 2 \end{bmatrix} \qquad \mathbf{P}_{(1,135^{\circ})} = \begin{bmatrix} 2 & 1 & 3 & 0 \\ 1 & 2 & 1 & 0 \\ 3 & 1 & 0 & 2 \\ 0 & 0 & 2 & 0 \end{bmatrix}$$

$$\mathbf{P}_{(1,135^{\circ})} = \begin{bmatrix} 2 & 1 & 3 & 0 \\ 1 & 2 & 1 & 0 \\ 3 & 1 & 0 & 2 \\ 0 & 0 & 2 & 0 \end{bmatrix}$$

co-occurrence matrix construction

Step 1: Construct the GLCMs

- For computational efficiency, the number of gray levels (L) can be reduced by binning (singlerstip histogram binning betgets as for new a constant factor.
- Different co-occurrence matrices can be constructed by using various combinations of distance (d) and angular directions (θ).
- On their own, these ch-powers of texture that can easily be used as texture descriptors.
- The information in the co-occurrence matrices needs to be further extracted as a set of feature values => Haralick descriptors.

- Step 2: Compute the Haralick descriptors from the GLCMs
 - One set of Haralick descriptors for each GLCM corresponding to a particular distance (d) and angular direction (θ).
 Assignment Project Exam Help

Angular Second Moment
$$\sum_{i} \sum_{j} p(i,j)^{2}$$
Contrast
$$\sum_{h\neq 0} \text{DOW-COMPT}(E011) = n$$
Correlation
$$\frac{\sum_{i} \sum_{j} (ij) p(i,j) - \mu_{x} \mu_{y}}{\sigma_{x} \sigma_{y}}$$
Add
$$We Chat power of energy and std. deviations of p_{x} and p_{y} , the partial probability density functions$$

Sum of Squares: Variance

Inverse Difference Moment

Sum Average

$$\sum_{i} \sum_{j} (i - \mu)^{2} p(i, j)$$
$$\sum_{i} \sum_{j} \frac{1}{1 + (i - j)^{2}} p(i, j)$$

$$\sum_{i=2}^{2N_g} i p_{x+y}(i)$$
 where x

where x and y are the coordinates (row and column) of an entry in the co-occurrence matrix, and $p_{x+y}(i)$ is the probability of co-occurrence matrix coordinates summing to x + y

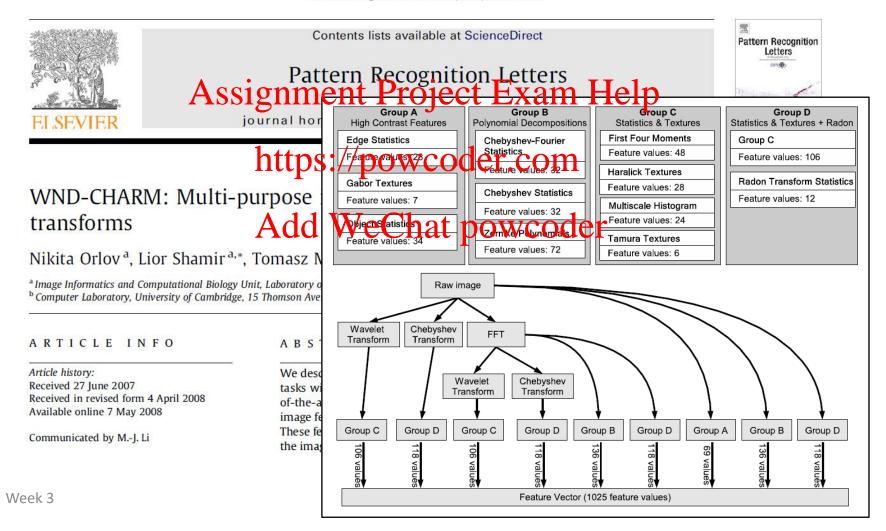
- Step 2: Compute the Haralick descriptors from the GLCMs
 - One set of Haralick descriptors for each GLCM corresponding to a particular distance (d) and angular direction (θ).
 Assignment Project Exam Help

```
\sum_{i=2}^{2N_g} (i - f_8)^2 p_{x+y}(i)
Sum Variance
                           https://poweoder.com
Sum Entropy
                                      -\sum_{i}\sum_{j}p(i,j)log(p(i,j))
Entropy
                           Add We Chat powcoder
Difference Variance
                                      -\sum_{i=0}^{N_g-1} p_{x-y}(i) \log\{p_{x-y}(i)\}
Difference Entropy
                                      \frac{HXY-HXY1}{\max\{HX,HY\}}
Info. Measure of Correlation 1
                                      (1 - \exp[-2(HXY2 - HXY)])^{\frac{1}{2}}
Info. Measure of Correlation 2
                                      where HXY = -\sum_{i}\sum_{j}p(i,j)\log(p(i,j)), HX,
                                          HY are the entropies of p_x and p_y, HXY1 =
                                                 -\sum_{i}\sum_{j}p(i,j)\log\{p_{x}(i)p_{y}(j)\}HXY2 =
                                                        -\sum_{i}\sum_{j}p_{x}(i)p_{y}(j)\log\{p_{x}(i)p_{y}(j)\}
Max. Correlation Coeff.
                                      Square root of the second largest eigenvalue of Q
                                                              where \mathbf{Q}(i,j) = \sum_{k} \frac{p(i,k)p(j,k)}{p_{-i}(i)p_{-i}(k)}
```

Application Example

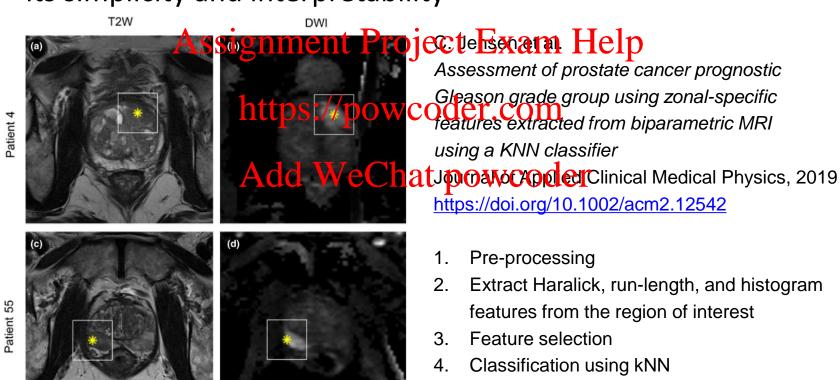
Pattern Recognition Letters 29 (2008) 1684-1693

https://doi.org/10.1016/j.patrec.2008.04.013



Application Example

 Commonly used nowadays in medical imaging studies due to its simplicity and interpretability



- Describe the spatial structure of local image texture
 - Divide the image into cells of $N \times N$ pixels (e.g. N = 16 or 32)
 - Compare each pixel in a cell to each of its a neighbouring pixels:
 If the centre pixel's value is greater than the neighbour's value,
 write "0", otherwise write "1"

 This gives an 8-digit binary pattern per pixel after comparing with all
 - This gives an 8-digit binary pattern per pixel after comparing with all 8 neighbouring pixels, representing a value in the range 0...255

0	0	1	1
0	0	1	1
0	2	2	2
2	2	3	3

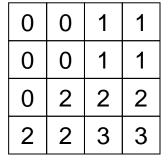
11110000

- Describe the spatial structure of local image texture (cont.)
 - Generate the histogram for all pixels in the cell, computing the frequency of each 8-digit binary number occurring in the cell Assignment Project Exam Help

 This gives a 256-bin histogram (the LBP feature vector)

 - Combine the histograms/of alwells tep by the image-level LBP feature descriptor

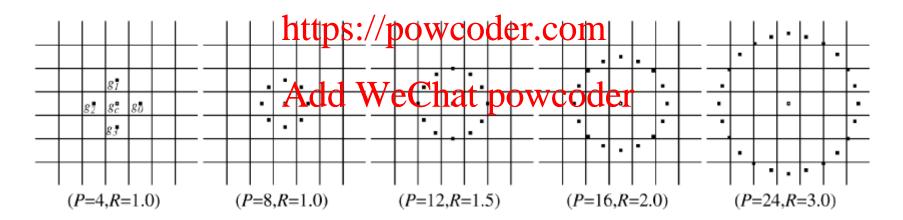
Add WeChat powcoder





A histogram of 256 elements

- LBP can be multi-resolution and rotation-invariant
 - Multi-resolution: varying the distance between the centre pixel and neighbouring pixels, and the number of neighbouring pixels
 Assignment Project Exam Help



T. Ojala, M. Pietikainen, and T. Maenpaa, "Multiresolution gray-scale and rotation invariant texture classification with local binary patterns," IEEE Transactions on Pattern Analysis and Machine Intelligence 24(7):971-987, 2002. https://doi.org/10.1109/TPAMI.2002.1017623

- LBP can be multi-resolution and rotation-invariant
 - Rotation-invariant: varying the way of constructing the 8-digit binary number, e.g. performing bitwise shift to derive the smallest number Assignment Project Exam Help

```
Example: 111 https://pawcoder.com

111000001 tve 135 powcoder

1000011 1 = 135 powcoder

1000011 1 = 15

00011110 = 30

00111100 = 60

01111000 = 120
```

Note: not all patterns have 8 shifted variants (e.g. 11001100 has only 4)

- LBP can be multi-resolution and rotation-invariant
 - Rotation-invariant: varying the way of constructing the 8-digit binary number, e.g. performing bitwise shift to derive the smallest number => this reduces the LBP feature dimension from 256 to 36

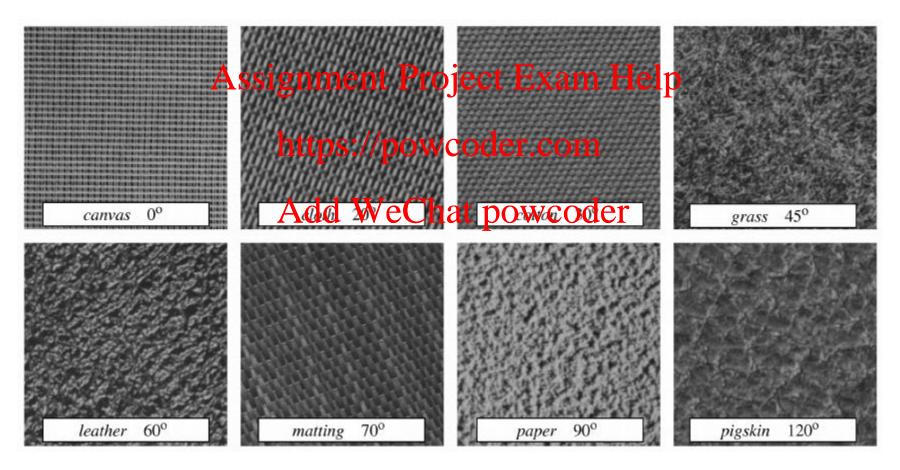


T. Ojala, M. Pietikainen, and T. Maenpaa, "Multiresolution gray-scale and rotation invariant texture classification with local binary patterns," IEEE Transactions on Pattern Analysis and Machine Intelligence 24(7):971-987, 2002. https://doi.org/10.1109/TPAMI.2002.1017623

Application Example

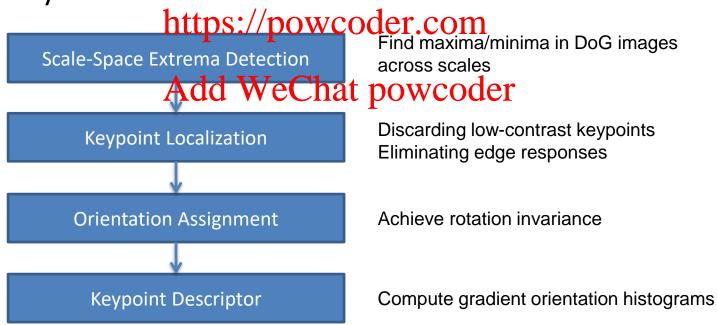
 $LBP_{P,R}$ P,RBINS RESULT 8.1 10 88.2 16,2 18 98.5 24,3 26 99.1 8,1+16,2 10 + 1899.0 8,1+24,310 + 2699.6 16,2+24,318 + 2699.0 8.1+16.2+24.3 10+18+26 99.1

Texture classification



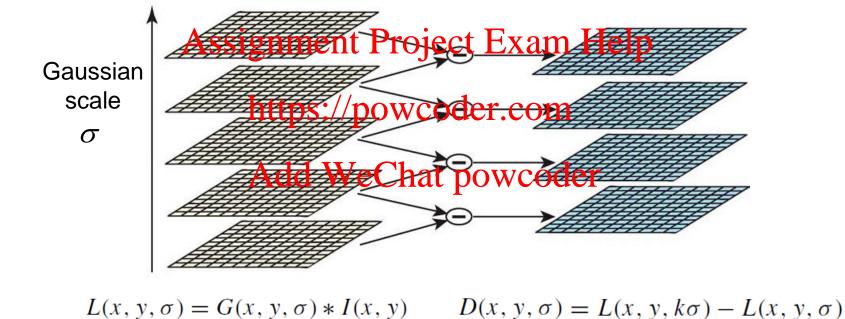
Scale-Invariant Feature Transform

- SIFT feature describes the texture features in a localised region around a keypoint
- SIFT descriptorsisginvariant to affine distortion and illumination changes



SIFT Extrema Detection

Detect maxima and minima in the scale space of the image



D. G. Lowe, "Distinctive image features from scale-invariant keypoints," Int. J. Comput. Vis. 60(2):91-110, November 2004. https://doi.org/10.1023/B:VISI.0000029664.99615.94

SIFT Keypoint Localization

- Improve and reduce the set of found keypoints
 - Use 3D quadratic fitting in scale-space to get subpixel optima
 - Reject lowacontrast and edge pojets using Hessian apalysis



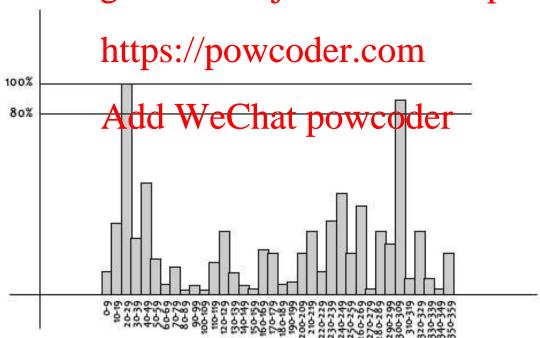
Initial keypoints from scale-space optima

Keypoints after rejecting low-contrast points

Final keypoints after rejecting edge points

SIFT Orientation Assignment

- Estimate keypoint orientation using local gradient vectors
 - Make an orientation histogram of local gradient vectors
 - Find the daminant orientations from the peaks infethe histogram



SIFT Keypoint Descriptor

- 4 x 4 array of gradient histogram weighted by magnitude
- 8 bins in gradient orientation histogram

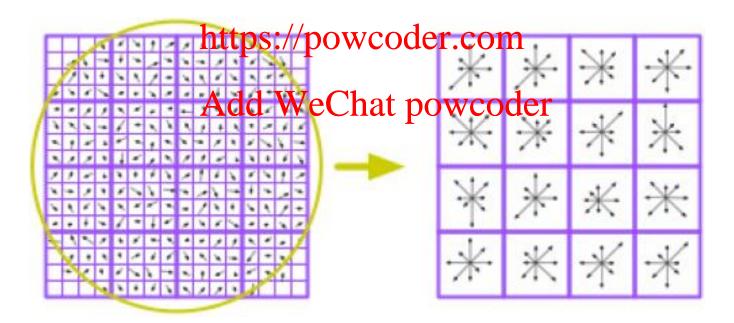


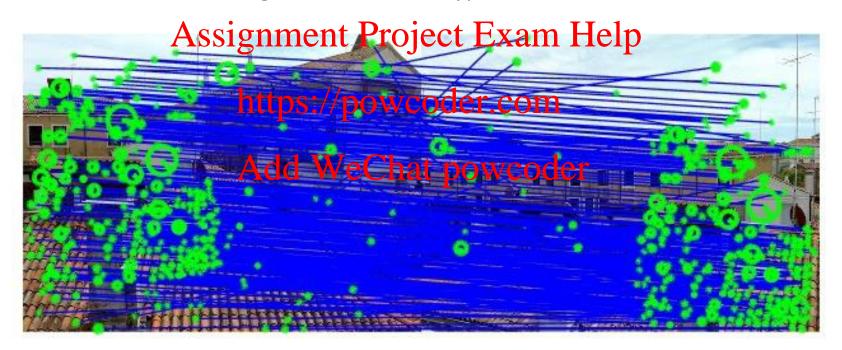
Image matching



- Image matching
 - Find SIFT keypoints



- Image matching
 - Find best matching between SIFT keypoints



Descriptor Matching

Nearest Neighbour Distance Ratio

Assignment
$$d_1$$
 $\overline{D}_A - D_B$ Help

- d1 is the distandettothe fipo wearestore ightour
- d2 is the distance to the second nearest neighbour
- Neighbours in feature spaceChat powcoder

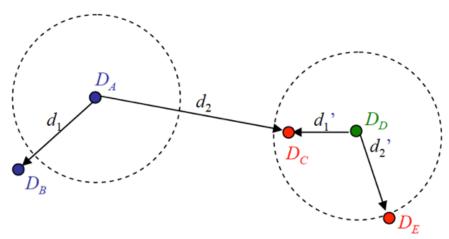
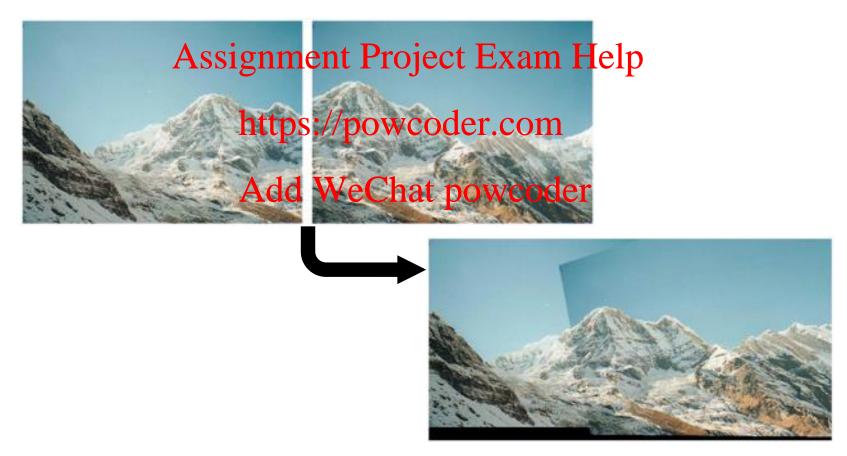
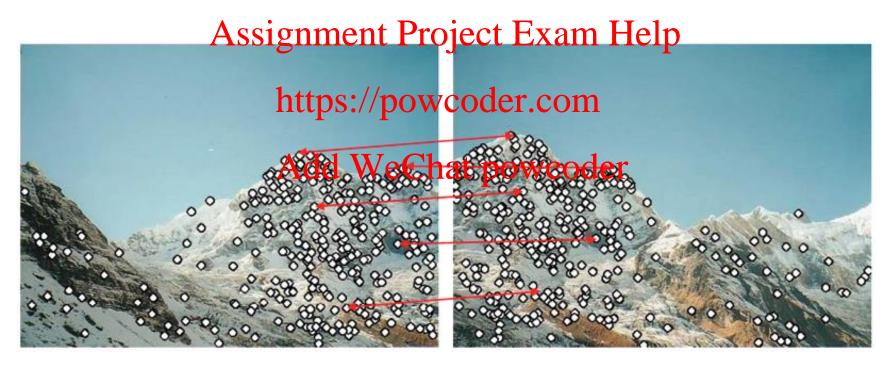


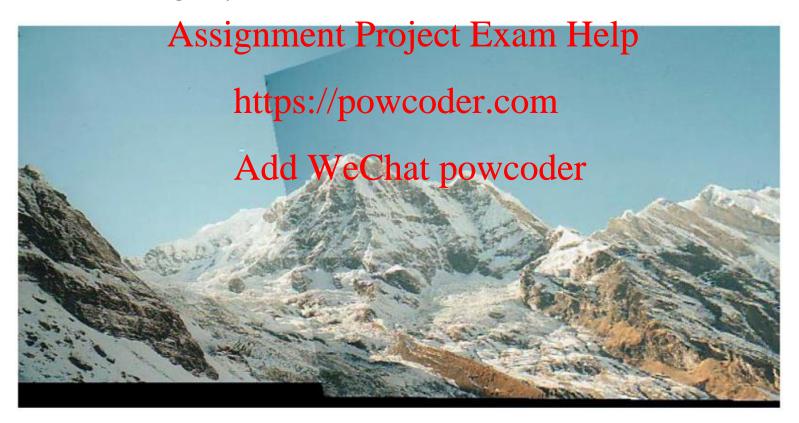
Image stitching



- Image stitching
 - Find SIFT keypoints and feature correspondences



- Image stitching
 - Find the right spatial transformation



Transformations





original



rotation



scale



affine



perspective

Transformations

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} s_x & 0 \\ 0 & s_y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} \qquad \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & \alpha_x \\ \alpha_y & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & \alpha_x \\ \alpha_y & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

Assignment Project Exam Helpar

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \Theta & -\mathbf{kittps} \\ \sin \Theta & \cos \Theta \end{bmatrix} \text{ we Chat powcoder } \begin{bmatrix} 1 & 0 & t_x \\ y' \\ \end{bmatrix} \begin{bmatrix} x \\ 0 & 1 & t_y \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$
Rotate

Translate

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Affine

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$\begin{bmatrix} x' \\ y' \\ w' \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & i \end{bmatrix} \begin{bmatrix} x \\ y \\ w \end{bmatrix}$$

Projective

• Least-squares (LS) fitting of corresponding keypoints $(\mathbf{x}_i, \mathbf{x}_i)$

where \mathbf{p} are the transformation f

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \implies \begin{bmatrix} x & y & 0 & 0 & 1 & 0 \\ 0 & 0 & x & y & 0 & 1 \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ &$$

- RANdom SAmple Consensus (RANSAC) fitting
 - Least-squares fitting is hampered by outliers
 - Some king of suttien detection and refestion is readed
 - Better use a subset of the data and check inlier agreement
 - RANSAC does thistips://epativecooder foodithe optimum

Add WeChat powcoder

RANSAC

Assignment Project Exam Help (line fitting example)

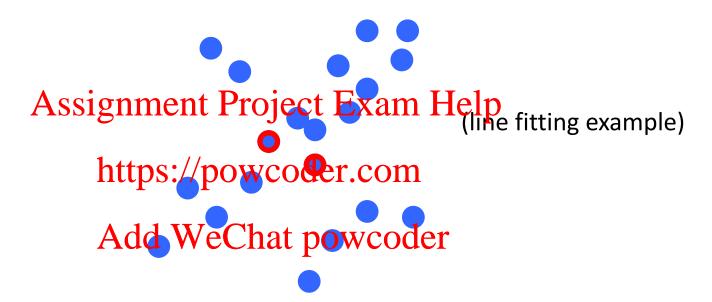
https://powcoder.com

Add WeChat powcoder

Algorithm:

- 1. Sample (randomly) the number of points required to fit the model
- 2. **Solve** for model parameters using samples
- 3. Score by the fraction of inliers within a preset threshold of the model

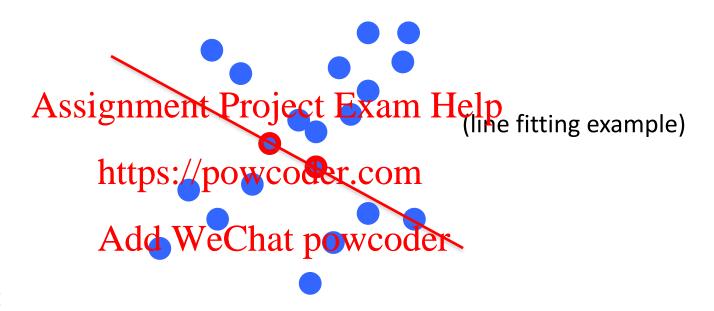
RANSAC



Algorithm:

- 1. Sample (randomly) the number of points required to fit the model
- 2. **Solve** for model parameters using samples
- 3. Score by the fraction of inliers within a preset threshold of the model

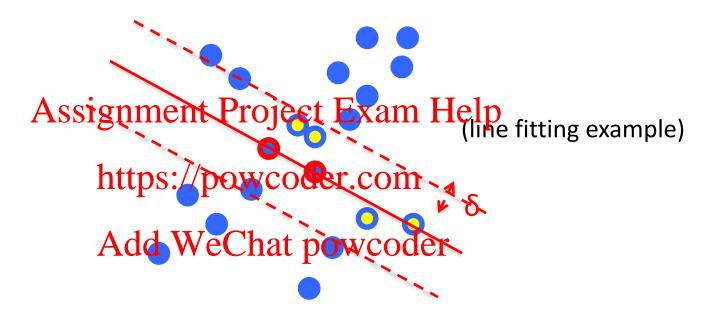
RANSAC



Algorithm:

- 1. Sample (randomly) the number of points required to fit the model
- 2. **Solve** for model parameters using samples
- 3. **Score** by the fraction of inliers within a preset threshold of the model

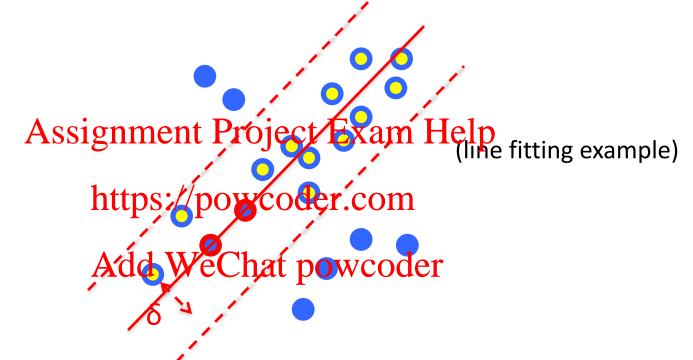
RANSAC



Algorithm:

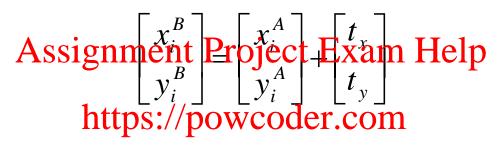
- 1. Sample (randomly) the number of points required to fit the model
- 2. **Solve** for model parameters using samples
- 3. **Score** by the fraction of inliers within a preset threshold of the model

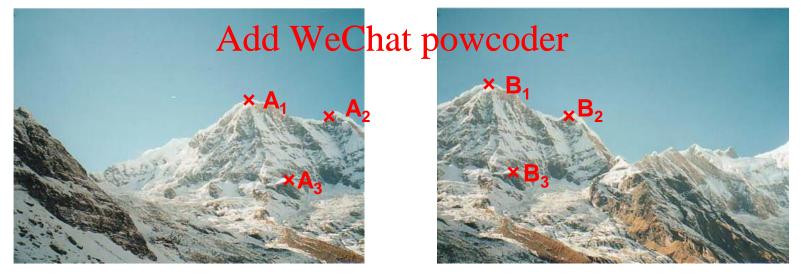
RANSAC



- Algorithm:
- 1. Sample (randomly) the number of points required to fit the model
- 2. **Solve** for model parameters using samples
- 3. **Score** by the fraction of inliers within a preset threshold of the model

Given matched points A and B, estimate the translation

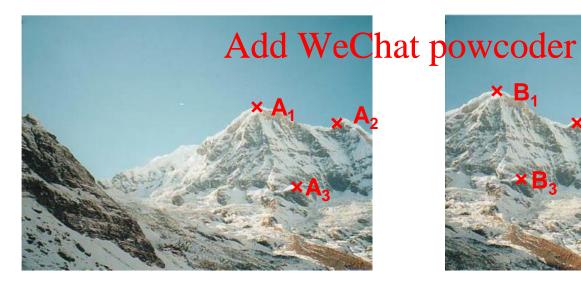


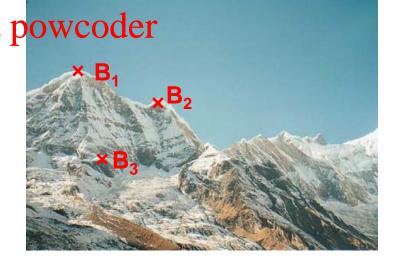


Alignment by Least Squares

- 1. Write down the objective function
- - b) Solve using preudosinyersowcoder.com

1. Write down the objective function
2. Obtain the analytical solution
a) Compute derivative
b) Compute solution
3. Obtain configuration roject Exam
a) Write in form
$$\mathbf{Ap} = \mathbf{b}$$
b) Solve using pseudosinyers we coder com
$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \\ \vdots & \vdots \\ Hedp \end{bmatrix} \begin{bmatrix} t_x \\ t_y \end{bmatrix} = \begin{bmatrix} x_1^B - x_1^A \\ y_1^B - y_1^A \\ \vdots \\ x_n^B - x_n^A \\ y_n^B - y_n^A \end{bmatrix}$$



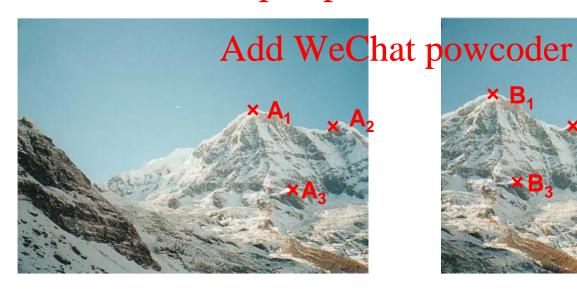


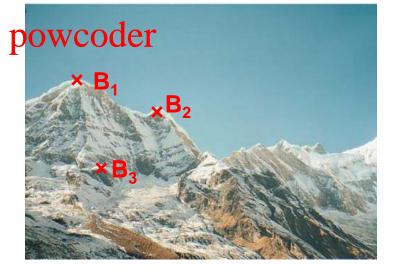
Alignment by RANSAC

- 1. Sample a set of matching points (1 pair)

- 2. Solve for transformation parameters
 3. Score parameters with number of inliers
 4. Repeat steps Signment Project Exam Help $\begin{bmatrix} x_i^A \\ y_i^A \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \end{bmatrix}$

https://powcoder.com



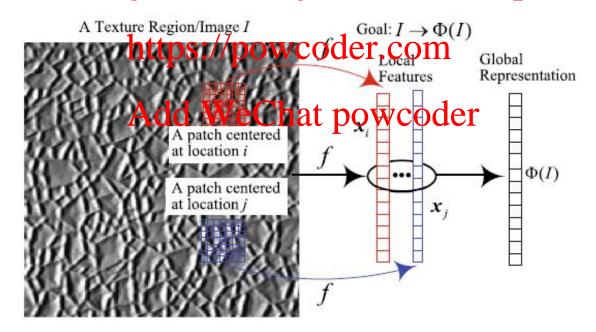


SIFT-based texture classification – how to do this?

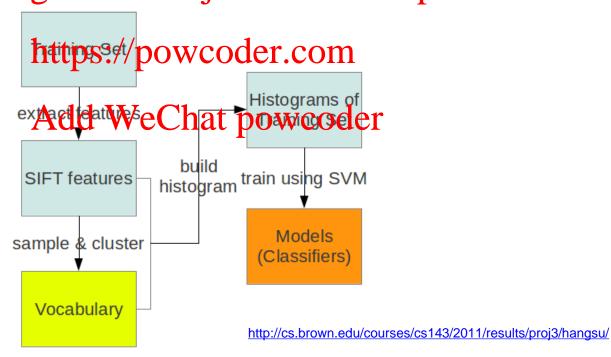


Problem: the number of SIFT keypoints (and thus the number of SIFT feature descriptors) may vary highly between images

- Global encoding of local SIFT features
 - Integrate the local features (SIFT keypoint descriptors) of an image into a global vector to represent the whole image ASSIGNMENT Project Exam Help

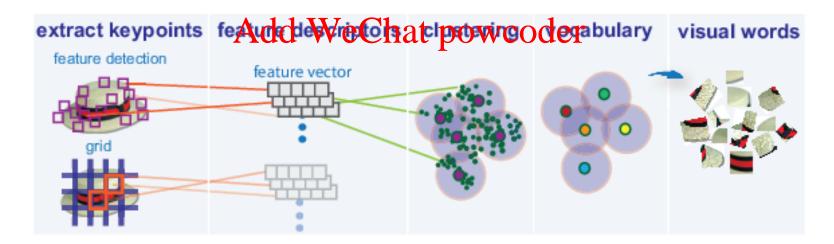


- Most popular method: Bag-of-Words (BoW)
 - The variable number of local image features are encoded into a fixed-dimensional histogram to represent each image ASSIGNMENT Project Exam Help

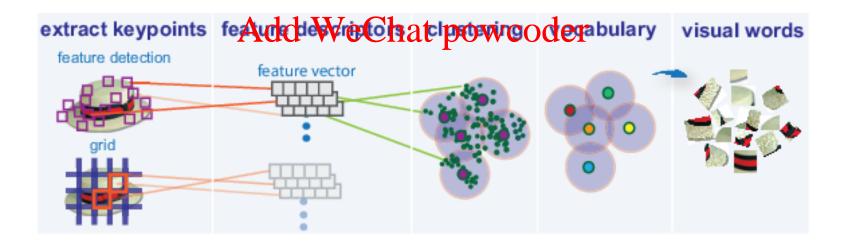


- Bag-of-Words (BoW) step 1
 - Create the vocabulary from the set of local descriptors (SIFT) keypoint descriptors) extracted from the training data
 Assignment Project Exam Help
 This vocabulary represents the categories of local descriptors

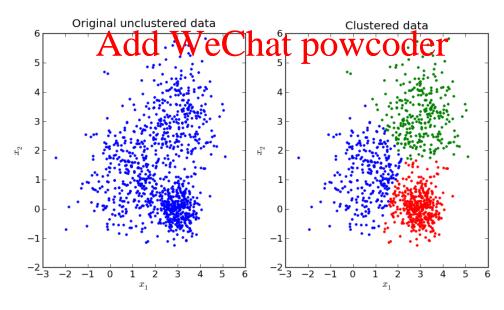
https://powcoder.com



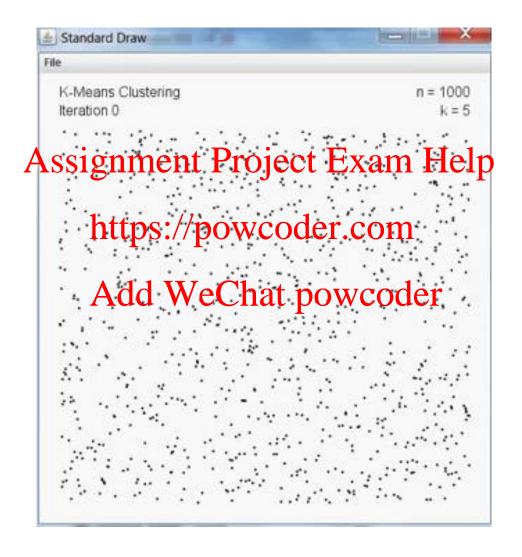
- Bag-of-Words (BoW) step 1
 - Main technique used to create the vocabulary: k-means clustering
 - k-means clustering is one of the simplest and must popular unsupervised learning approaches that perform automatic clustering (partitioning) of the training data into multiple categories



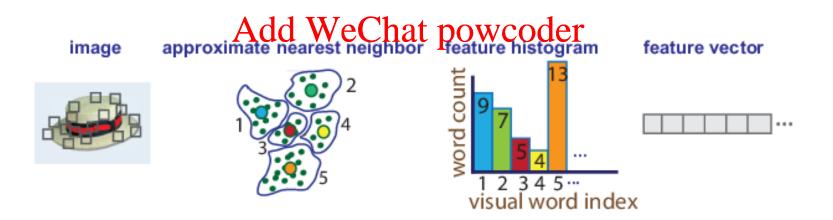
- Bag-of-Words (BoW) step 1
 - K-means clustering:
 - Initialize: k cluster centres, typically randomly
 - o Iterate: A SSI grand (réalure récles) to tre cosest el tele (Euclidean distance)
 - 2) Update cluster centres as the mean of the data samples in each cluster
 - o Terminate: When topy grade on the modern of the prior reaches the maximum



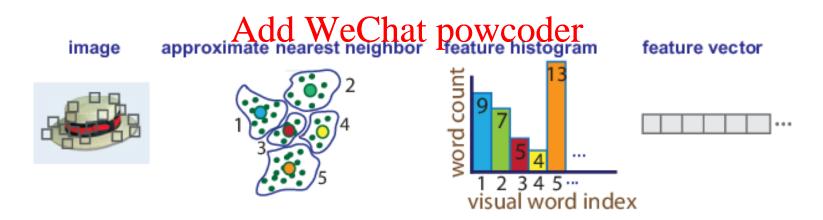
K-Means Clustering



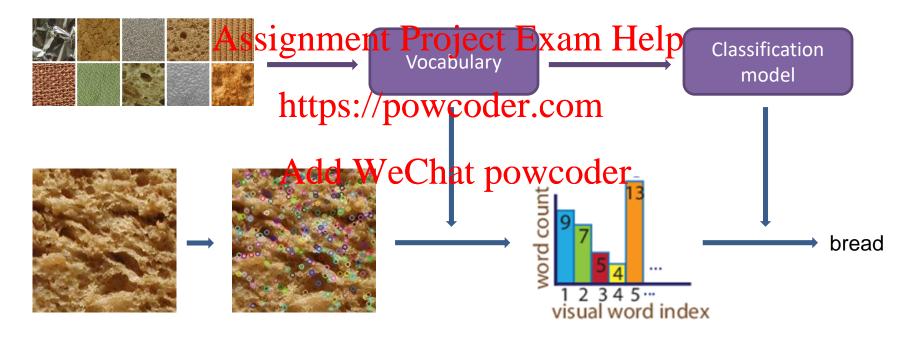
- Bag-of-Words (BoW) step 2
 - The cluster centres are the "visual words" which form the "vocabulary" that is used to represent an image Assignment Project Exam Help
 An individual local feature descriptor (e.g. SIFT keypoint descriptor) is
 - An individual local feature descriptor (e.g. SIFT keypoint descriptor) is assigned to one visual word with the smallest distance



- Bag-of-Words (BoW) step 2
 - For an image the number of local feature descriptors assigned to each visual word is computed.
 Assignment Project Exam Help
 The numbers are concatenated into a vector which forms the
 - The numbers are concatenated into a vector which forms the BoW representation of the image https://powcoder.com



SIFT-based texture classification



1. SIFT feature extraction

2. BoW encoding

3. Classification

Strongest features of Input Training Image each class images (2D is unpractical case, just for illustration SIFT-based texture classification Assignment Project Examily **Bag of Features** (Visual Words) https://pow/rewellers.com **Get Frequencies of Visual** Words (Vocabulary) powcoder **Build vocabulary** Train classifier **Test Image** Classify image **Training Images for all Classes** Train a Model **SVM** Prediction Model (Dolphin!) **Predict using** trained model

http://heragi.blogspot.com/2017/03/BoW.html

- Local features can be other types of features, not just SIFT
 - LBP, SURF, BRIEF, ORB
- There are also more advanced techniques than BoW
 - VLAD, Fisher Verters://powcoder.com
- A very good source of additional information is VLFeat.org
 - http://www.vlfeat.org/

Summary

- Feature representation is essential in solving almost all types of computer vision problems
- Most command with the land of the land of
 - Colour features (Part 1)
 - Colour momentations: h/special coder.com

 - Texture features (Part 1)
 Haralick, LBP, Stedd WeChat powcoder
 - Shape features (Part 2)
 - Basic, shape context, HOG

Summary

- Other techniques described (Part 1)
 - Descriptor matching
 - Feature encoding Bageoft Project Exam Help
 - k-means clustering
 - Alignment and PANDAC/powcoder.com
 - Spatial transformations

Add WeChat powcoder

- To be discussed (Part 2)
 - Shape features
 - Shape matching
 - Sliding window detection

References and Acknowledgements

- Szeliski, Chapter 4 (in particular Sections 4.1.1 to 4.1.3 and 4.3.2), Chapter 6 (in particular Sections 6.1.1 to 6.1.4)
- Some content are extracted from the above resource, James Hays slides, and slides from the language of the l
- L. Liu et al., From BoW to CNN: two decades of texture representation for texture classification, international Journal of Computer Vision, 2019
- And other resources as indicated by the hyperlinks Add Wechat powcoder