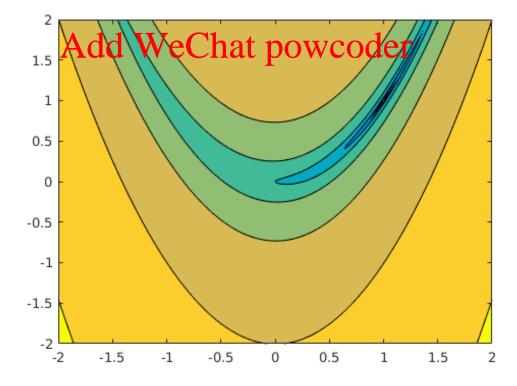
Assignment 0: Exercise 1

```
clear all; close all

a) Rosenbrock function
f = @(x,y) \ 100.*(y - x.^2).^2 + (1 - x).^2;
```

b) Discretisation of the unit square. It can be scaled with factor α using simple multiplication αX , αY Plot the function of two variables



c) Gradient

$$df/dx = -400(y - x^2)x - 2(1 - x)$$

$$df/dy = 200(y - x^2)$$

c) Hessian

$$d^2f/dx^2 = -400(y - 3x^2) + 2$$

$$d^2f/dxdy = -400x$$

$$d^2f/dydx = -400x$$

$$df^2/dy^2 = 200$$

d) Find the minimiser x^* of the function f. Show that x^* is unique and that $\nabla^2 f(x^*)$ is positive definite.

Assignment Project Exam Help we observe the fundament because is the sum of two non-negative terms. Also

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This is only possible if x=1 and y=1. Hence, we have $x^*=(1,1)^T$.

The Hessian at Asid We Chat powcoder

$$\nabla^2 f(x^*) = \begin{pmatrix} 802 & -400 \\ -400 & 200 \end{pmatrix}$$

Hence, to verify that it is positive definite, for all $(x,y) \neq 0$ we must have:

$$\begin{pmatrix} x & y \end{pmatrix} \begin{pmatrix} 802 & -400 \\ -400 & 200 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} > 0$$

This is equivalent to

$$802x^2 - 800xy + 200y^2 > 0$$

Finally, we have

$$2x^2 + 200(2x - y)^2 > 0,$$

that obviously holds for all (x,y)
eq (0,0)

e) Finite difference implementation of the gradient

```
% Construct central finite difference to be applied columnwise
D = 1/(2*h)*spdiags([-ones(n+1,1) ones(n+1,1)], [-1 1], n+1,n+1);
D(1,1:2) = 1/h*[-1 1];
D(n+1,n:n+1) = 1/h*[-1 1];
% Gradient via finate differences
Dyf = D*f(alpha*X, alpha*Y);
% d/dx, central finite difference applied rowwise
Dxf = (D*(f(alpha*X, alpha*Y).')).';
% Hessian via finite difference
% d^2/dxdy
Dxyf = D*Dxf;
% d^2/dx^2
Dxxf = (D*(Dxf.')).';
% d^2/dy^2
Dyyf = D*Dyf;
% d^2/dydx
Dyxf = (D*(Dyf.')).';
```

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