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Classification IV: Ensemble methods

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Overview

- Bagging and Random Forests
- **▶** Boosting

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Motivation

Recall model averaging: given T real-valued predictors

https://powcoder.com $\operatorname{mse}(\hat{f}_{\operatorname{avg}}) = \frac{1}{T} \sum_{t=1}^{T} \operatorname{mse}(\hat{f}^{(t)}) - \frac{1}{T} \sum_{t=1}^{T} \mathbb{E}\left[(\hat{f}_{\operatorname{avg}}(X) - \hat{f}^{(t)}(X))^{2}\right].$

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$$\hat{f}_{\text{maj}}(x) := \begin{cases} +1 & \text{if } \sum_{t=1}^{T} \hat{f}^{(t)}(x) > 0\\ -1 & \text{otherwise} \end{cases}$$

 $(\hat{f}_{\mathrm{avg}}$ is the scoring function used for $\hat{f}_{\mathrm{mai}})$

How to get classifiers to combine?

► Starting anew; how should we train classifiers to combine in majority-vote?

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- ightharpoonup all $\hat{f}^{(t)}$ have similar MSEs, and
- ightharpoonup all $\hat{f}^{(t)}$ predict very differently from each other

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- ► To second point, learning algorithm should have "high Add WeChat powcoder

Using the same learning algorithm multiple times I

Running same learning algorithm T times on the same data set

yields T identical classifiers - not helpful!

1 properties the properties of the pr

https://poweoder.com Figure 1: What we want is T data sets drawn fr

Using the same learning algorithm multiple times II

- ► Invoke plug-in principle
 - ▶ In IID model, regard empirical disitribution on training examples
- Assignmented the example distribution Pananity Help algorithm on each data set.
 - ► This is called *bootstrap resampling*.

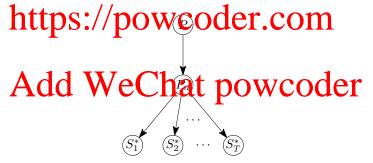


Figure 2: What we can get is T data sets from P_n

Bagging

- ▶ Bagging: bootstrap aggregating (Breiman, 1994)
- Assignment Project Exam Help Randomly draw n examples with replacement from training

data: $S_t^* := ((x_i^{(t)}, y_i^{(t)}))_{i=1}^n$ (bootstrap sample)

- Run learning algorithm on S_t^* to get classifier $\hat{f}^{(t)}$ Ratura paperity-varied asstrict QeV \hat{f} \hat{f} \hat{f}

Aside: Sampling with replacement

Pick n individuals from a population of size n with replacement.

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Implications for bagging:

Each bootstrap sample contains about 63% of the training

Remaining 37% can be used to estimate error rate of classifier trained on bootstrap sample

Random forests

 <u>Random Forests</u> (Breiman, 2001): Bagging with randomized variant of decision tree learning algorithm

Assignmented the learning algorithm.

Assignmented property, per manupseled present the features and only choose split from among those features.

Main idea: trees may use very different features, so less likely to make mistakes in the same way. https://powcoder.com

Classifiers with independent errors

- ► Say we have T binary classifiers $\hat{f}^{(1)}, \dots, \hat{f}^{(T)}$

Assume on a given x, each provides an incorrect prediction Assignment Project Exam Help

 $\Pr(\hat{f}^{(t)}(X) \neq Y \mid X = x) = 0.4.$

Mptetver assumerano exents are interpendent m • Use majority-vote classifier f_{maj}.

- ▶ What is chance that more than half of the classifiers give the

Coping with non-independent errors

Classifier errors are unlikely to be independent; do something else to benefit from majority-vote

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Coping with non-independent errors

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- ► Adaptively choose classifiers
- Re-weight training data

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- ► Start with uniform distribution over training examples
- Loop:

Use learning algorithm to get new classifier for ensemble Re-weight Winting example to emphasize (a) thick new classifier is incorrect

Adaptive Boosting

- ► <u>AdaBoost</u> (Freund and Schapire, 1997)
- ▶ Training data $(x_1, y_1), \dots, (x_n, y_n) \in \mathcal{X} \times \{-1, +1\}$

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lacktriangleright Run learning algorithm on D_t -weighted training examples, get classifier $f^{(t)}$

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$$z_t := \sum_{i=1}^{\infty} D_t(i) \cdot y_i f^{(t)}(x_i) \in [-1, +1]$$

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$$D_{t+1}(i) := \frac{D_t(i) \exp(-\alpha_t \cdot y_i f^{(t)}(x_i))}{Z_t}$$
 for $i = 1, \dots, n$.

Here Z_t is normalizer that makes D_{t+1} a probability distribution.

▶ Final classifier: $\hat{f}(x) = \text{sign}(\sum_{t=1}^{T} \alpha_t \cdot f^{(t)}(x))$

Assignment $\Pr^{\alpha_t = \frac{1}{2} \ln \frac{1+z_t}{1-z_t} \in \mathbb{R}}$ Exam Help https://powcoder.com Add WeChat powcoder -0.5 0.5

Figure 3: α_t as function of z_t

Example: AdaBoost with decision stumps

- ► (From Figures 1.1 and 2.2 of Schapire & Freund text.)
- ▶ Use "decision stump" learning algorithm with AdaBoost

Ittelightforward chardle importance reights of in decision tree learning a gorithm



Figure 4: Training data for example execution

Example execution of AdaBoost I

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Example execution of AdaBoost II

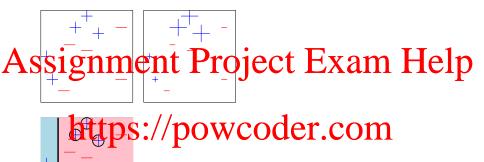




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 $z_1 = 0.40, \, \alpha_1 = 0.42$

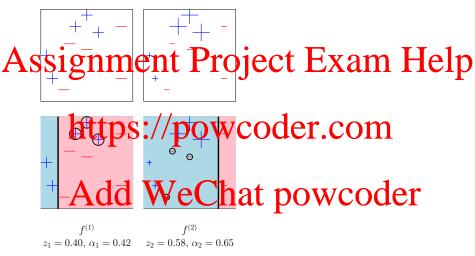
Example execution of AdaBoost III



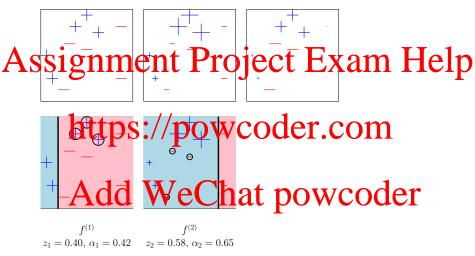
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 $f^{(1)}$ $z_1 = 0.40, \ \alpha_1 = 0.42$

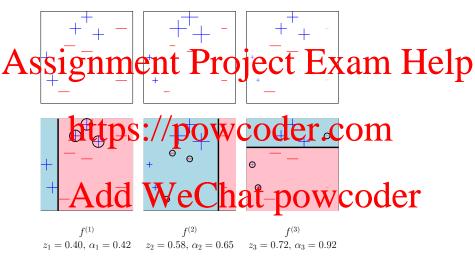
Example execution of AdaBoost IV



Example execution of AdaBoost V



Example execution of AdaBoost VI

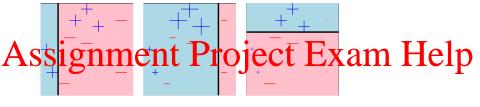


Example execution of AdaBoost VII



z₁ = https://powcoder.com

Example execution of AdaBoost VIII



z₁ = https://powcoder.com

Final classifier:

Training error rate of final classifier

Let $\gamma_t := z_t/2$: advantage over random guessing achieved by

Assignmented Project comparing Project comparing $\text{Project} = \exp\left(-2\sum_{t=1}^{T} \gamma_t^2\right) = \exp\left(-2\bar{\gamma}^2 T\right)$ https://powcoder.com

Training error rate of final classifier

Let $\gamma_t := z_t/2$: advantage over random guessing achieved by

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- - \triangleright Some γ_t can be small (even negative)—only care about average

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- - \triangleright Some γ_t can be small (even negative)—only care about average
- What about true error rate in IID model?
 - A very complex model as T becomes large!

Surprising behavior of boosting

lacktriangle AdaBoost + C4.5 decision tree learning on "letters" data set

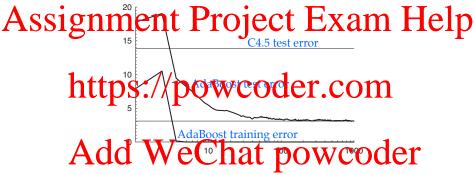


Figure 5: Figure 1.7 from Schapire & Freund text

- ► Training error rate is zero after five iterations.
- ► Test error rate continues to decrease, even up to 1000 iterations.

Margins theory

▶ Look at (normalized) scoring function of final classifier

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 \blacktriangleright Say $y \cdot \hat{h}(x)$ is margin achieved by \hat{h} on example (x,y)

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 Over-fitting in 11D model
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- Similar to be the same as SVM margins) Add WeChat powcoder

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 Theorem (Schapire, Freund, Bartlett, and Lee, 1998): over-fitting in 11D model
 - AdaBoost tends to increase margins on training examples
- (Similar to but not saving as SVM margins)
 On "lefters" data set Chat powcoder

	T = 5	T = 100	T = 1000
training error rate	0.0%	0.0%	0.0%
test error rate	8.4%	3.3%	3.1%
${}$ % margins ≤ 0.5	7.7%	0.0%	0.0%
min margin achieved	0.14	0.52	0.55