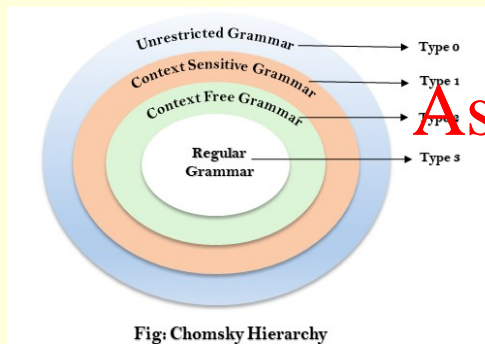


COSC1107 Computing Theory

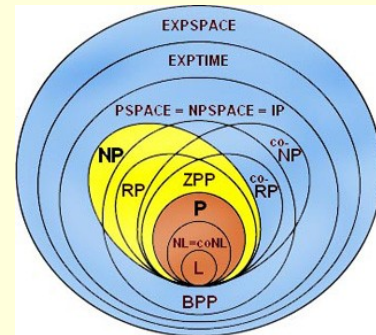
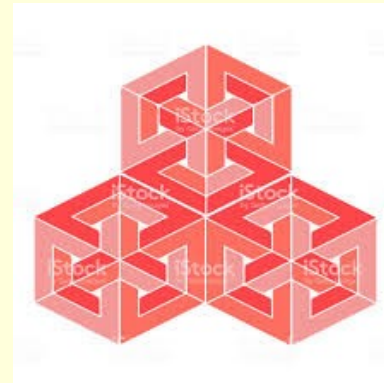
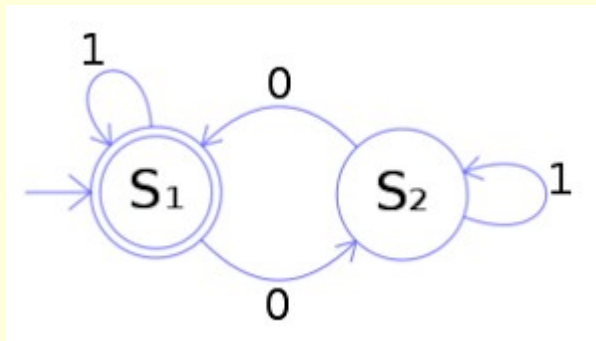
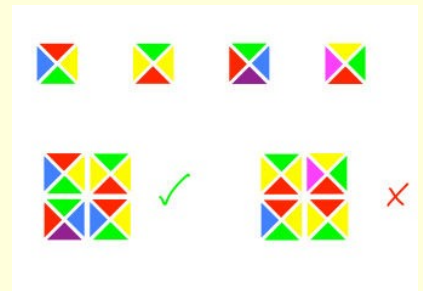
(We will commence soon. We are just allowing a few minutes for people to join and set up. *Please mute your microphone unless you are speaking.* You can raise your hand or use the chat at any time.)

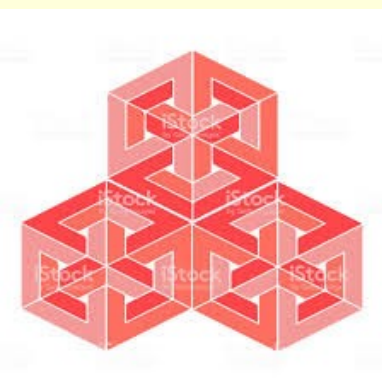
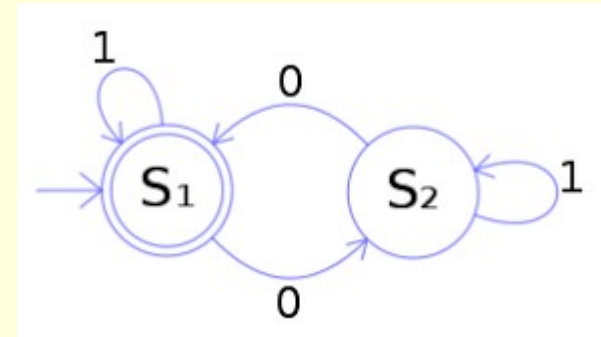
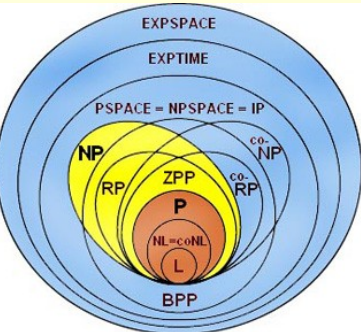


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COSC1107

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Computing Theory

<https://powecoder.com>

Computability, Universality

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Week 5

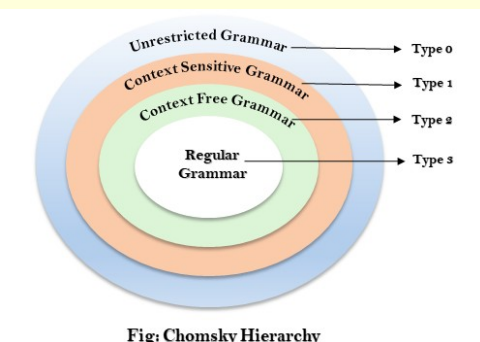
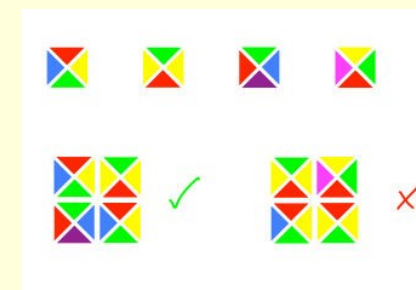


Fig: Chomsky Hierarchy



Week 5

Computing Theory

James Harland

james.harland@rmit.edu.au

* With thanks to Sebastian Sardina

Intro music 'Far Over' playing now ...

Acknowledgement



RMIT University acknowledges the people of the Woi wurrung and Boon wurrung language groups of the eastern Kulin Nations on whose unceded lands we conduct the business of the University. RMIT University respectfully acknowledges their Ancestors and Elders, past and present.

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RMIT also acknowledges the Traditional Custodians and their Ancestors of the lands and waters across Australia where we conduct our business.

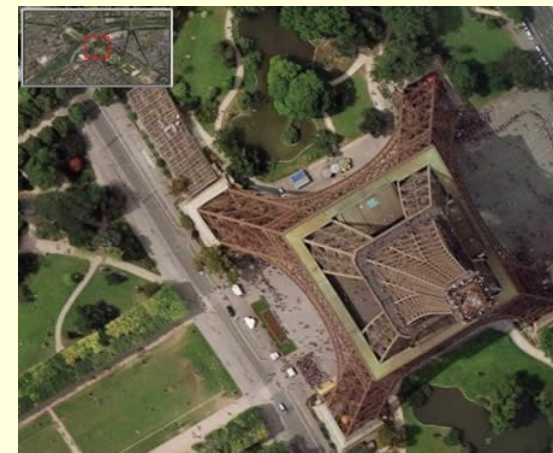
(add your name [here](#) to volunteer for this or email me)

Week 5

Computing Theory

Overview

- Questions?
- Universal Turing Machines
- Questions? Assignment Project Exam Help What can be done
- Computability What can't be done
<https://powcoder.com>
- Questions?
- Platypus Game Add WeChat powcoder Both!
- Questions?



Questions?



Questions?



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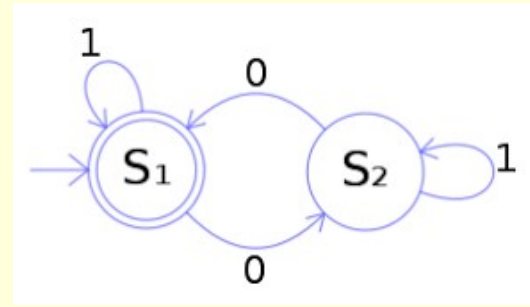


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Questions?



Church-Turing thesis

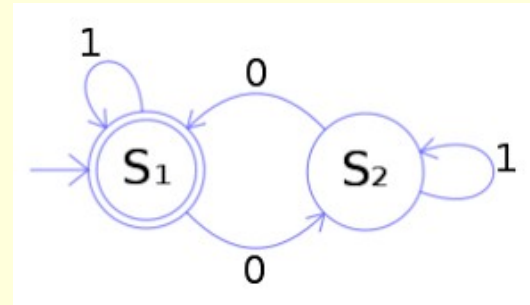


Church-Turing thesis (1936) Any computation can be translated to an equivalent computation on a Turing machine

so Turing machines are adequate for anything that can be computed

- No need to seek anything more powerful (there is nothing!)
- Enables rigorous analysis of computation
- Can't be done by a TM means can't be done at all!
- Thesis, not a theorem
- Observed property of the universe, like scientific laws
- Consistent with observation, no counterexamples known

Church-Turing thesis



"A man* provided with paper, pencil, and rubber, and subject to strict discipline, is in effect a universal machine."

-- Alan Turing

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"The idea behind digital computers may be explained by saying that these machines are intended to carry out any operations which could be done by a human computer."

-- Alan Turing

<https://powcoder.com>

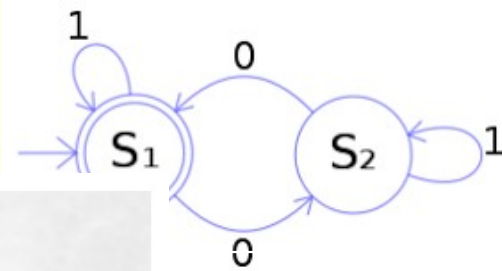
Add WeChat powcoder

"It is possible to invent a single machine which can be used to compute any computable sequence. If this machine U is supplied with a tape on the beginning of which is written the [encoding] of some computing machine M, then U will compute the same sequence as M."

-- Alan Turing

* This now sounds very dated. But that is what he said back in the 1930's ...

Church-Turing thesis



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Add WeChat powcoder

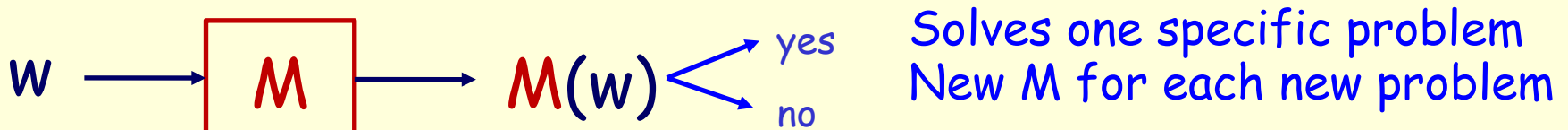
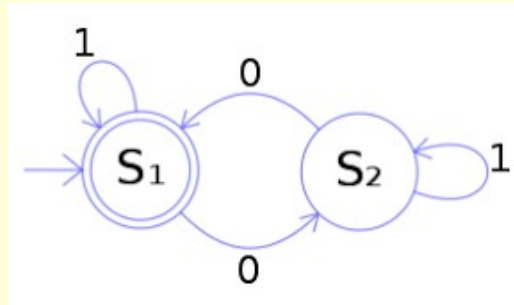
GOTCHA!

ed by linguists

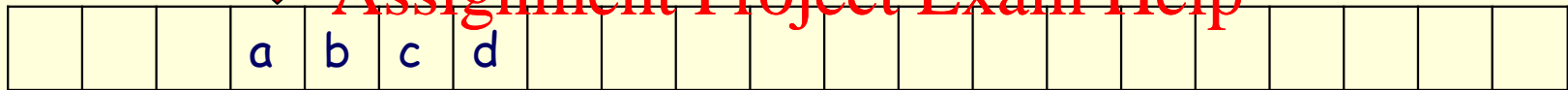
l interactions

m states

Universal Turing machine



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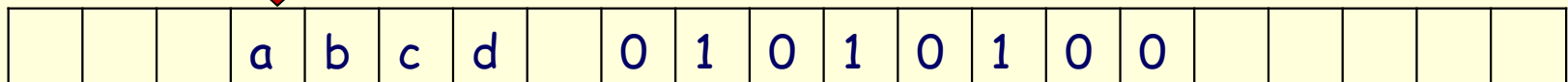
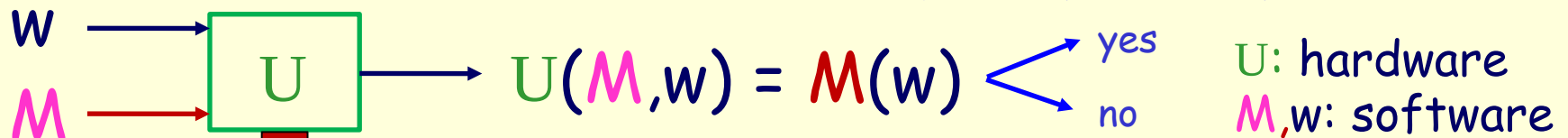
<https://powcoder.com>

"U simulates the action of M on w "

w

Architecture that can solve any (computable) problem!

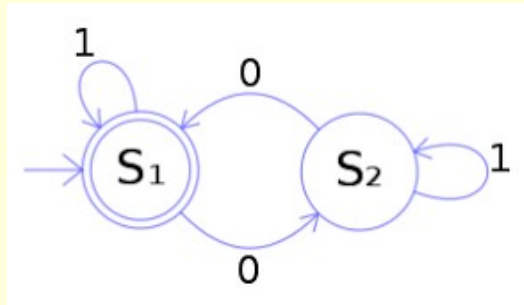
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w

M

Universal Turing machine



I'd like a Turing machine please!



Certainly Master Baggins! Which one? We have many!

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There are so many! It is confusing ...

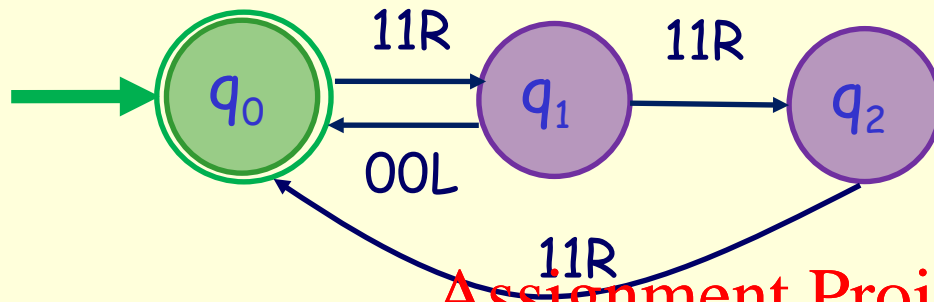
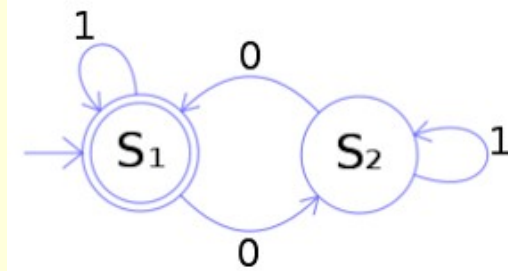


Frodo! Just use this one!
You will never need another!

U

"lean green
Turing
machine!"

Universal Turing machine



$T = (q, x, y, D, r)$

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$en(T) = en(q)0en(x)0en(y)0en(D)0en(r)$

<https://powcoder.com>

q_0	1	1	R	q_1	1011011011011
q_1	1	1	R	q_2	11011011011011
q_1	0	0	L	q_0	1101010101
q_2	1	1	R	q_0	11101101101101

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separate transitions by 00

$code(M) = 000 en(T_1) 00 en(T_2) 00 en(T_3) 00 en(T_4) 000$

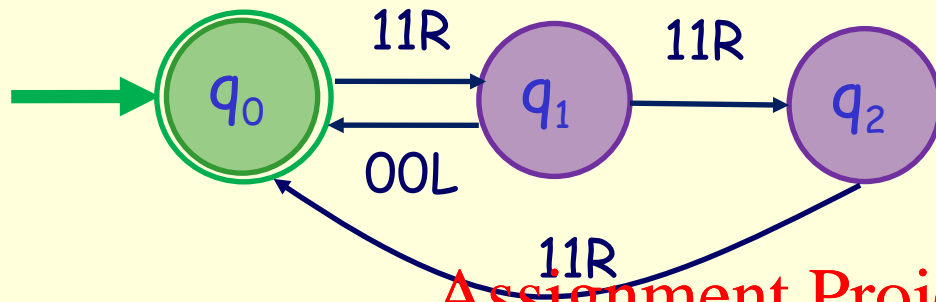
Week 5

start and end encoding with 000

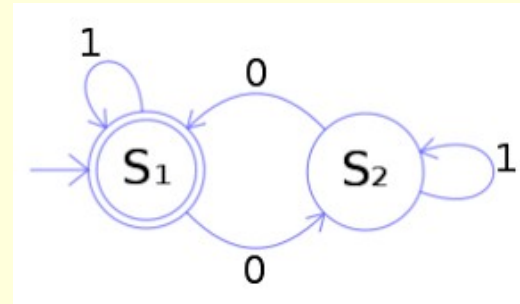
Computing Theory

i	en(i)
q_0	1
q_1	11
q_2	111
0	1
1	11
	111
L	1
R	11

Universal Turing machine



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q_0	1	1	R	q_1	1011011011011
q_1	1	1	R	q_2	110110110110111
q_1	0	0	L	q_0	1101010101
q_2	1	1	R	q_0	11101101101101

<https://powcoder.com>

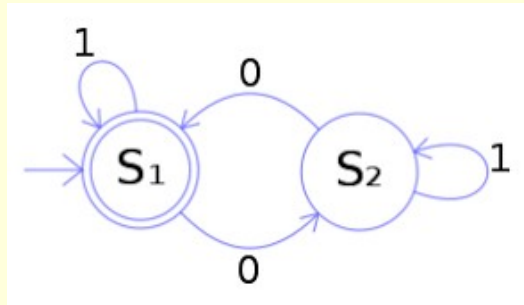
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i	en(i)
q_0	1
q_1	11
q_2	111
0	1
1	11
	111
L	1
R	11

$\text{code}(M) = 000 \text{ en}(T_1) 00 \text{ en}(T_2) 00 \text{ en}(T_3) 00 \text{ en}(T_4) 000$

0001011011011011001101101101101110011010101010011101101101101000

Universal Turing machine



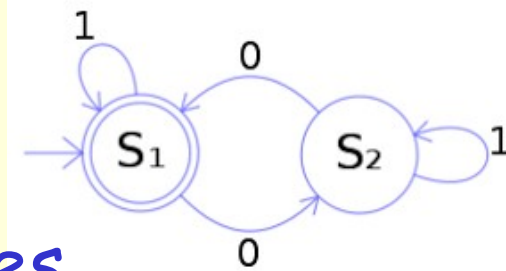
Turing machine **string** input to another TM

"Analyser" TMs can

- determine if (another) TM
 - has a 'halt' transition (ie no transition for a given pair of state & symbol)
 - is deterministic or not (or semi-deterministic)
 - contains a 'platyphus' state
 - simulates an FSA (all moves R, no changing the tape)
 - ...
- Count the transitions, states, symbols, ... in a TM
- Add a transition to a TM
- Change a transition in a TM
- "Join" two TMs (final state of one = initial state of s
- **Simulate the action of the input TM**
- **'Swap' the acceptance behaviour of the input TM**
- **Change the output of the input TM**
- **Be given their own definition as input (!!)**



Universal Turing machine



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w

M

<https://powcoder.com>

"One machine to rule them all;
one machine to find them;
one machine to ..."

Build UTM using 3 tapes

- One for input (encoded machine and input)
- One for the state of M
- One for the tape of M

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Tape 1

code(M)code(w)

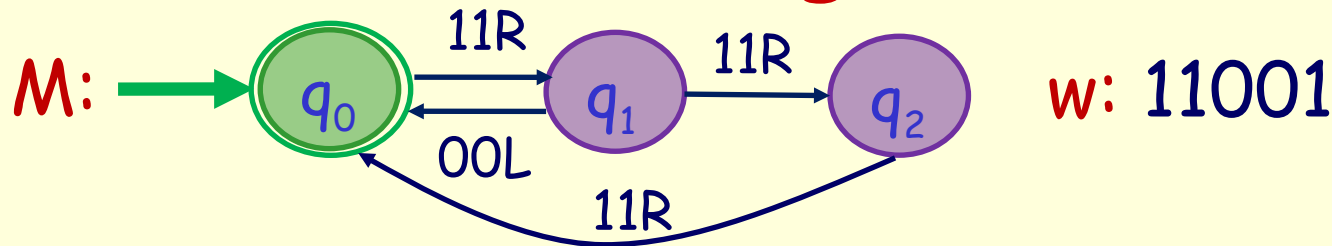
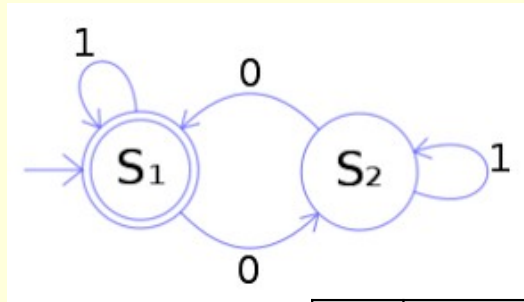
Tape 2

current state of M (encoded)

Tape 3

tape of M (encoded)

Universal Turing machine



U's alphabet may be different from M's ...

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<https://powcoder.com>

$code(M)$

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$code(w)$

U:

M

i	en(i)
q_0	1
q_1	11
q_2	111
0	1
1	11
	111
L	1
R	11

U

000101101101101100110110110110111001101010101001110110110110100011011010101100

$code(M)code(w)$

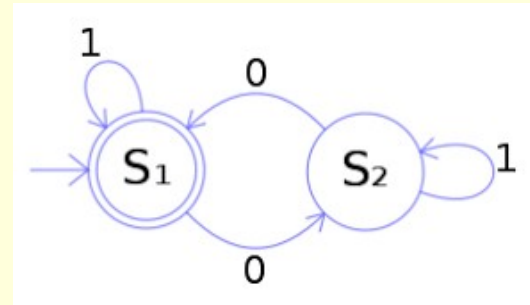
1

M state (encoded)

11011010101100

M tape (encoded)

Universal Turing machine

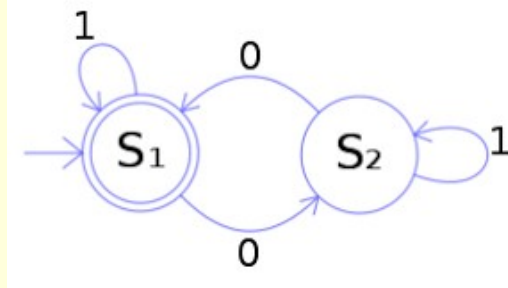


U:

1. Check tape 1. If format wrong, loop forever
2. Write code(w) on tape 3
3. Write $en(q_0)$ on tape 1
4. Find transition matching q on tape 2 & x on tape 3. If none, halt.
5. Given $en(q)0en(x)0en(y)0en(D)0en(r)$
 - Replace $en(q)$ with $en(r)$ on tape 1
 - Write $en(y)$ appropriate on tape 3
 - Move tape 3 according to D (left or right)
6. Go to step 4

000101101101101100110110110110111001101010101001110110110110100011011010101100

Universal Turing machine



U:

1. Check tape 1. If format wrong, loop forever
2. Write code(w) on tape 3
3. Write en(q₀) on tape 1
4. Find transition matching q on tape 2 & x on tape 3. If none, halt.
5. Given en(q)0en(x)0en(y)0en(D)0en(r)
 - Replace en(q) with en(r) on tape 2
 - Write en(y) appropriate on tape 3
 - Move tape 3 according to D (left or right)
6. Go to step 4

Assignment Project Exam Help

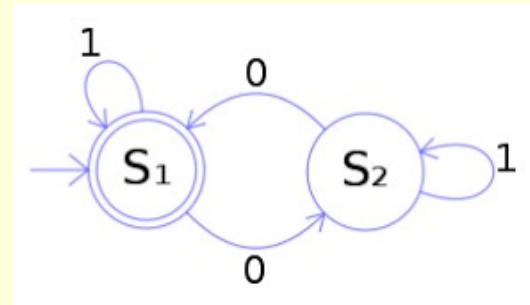
<https://powcoder.com>

Add WhatsApp powder

0001011011011011001101101101101110011010101010100110110110110100011011010101100

11011010101100

Universal Turing machine



U:

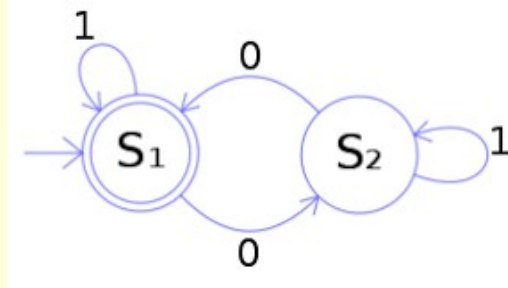
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000101101101101100110110110110111001101010101001110110110110100011011010101100

1

11011010101100

Universal Turing machine



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Assignment Project Exam Help

<https://powcoder.com>

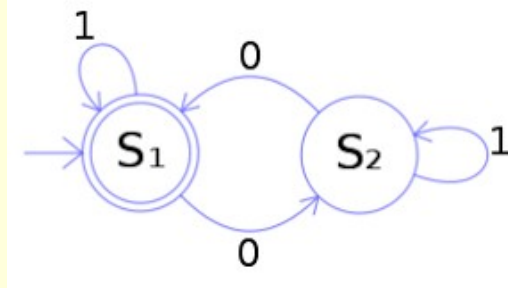
Add WeChat powcoder

000101101101101100110110110110111001101010101001110110110110100011011010101100

1

11011010101100

Universal Turing machine



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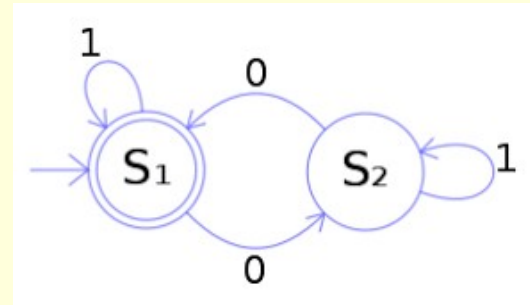
000101101101101100110110110110111001101010101001110110110110100011011010101100

11

11011010101100



Universal Turing machine



U:

1. Check tape 1. If format wrong, loop forever
2. Write code(w) on tape 3
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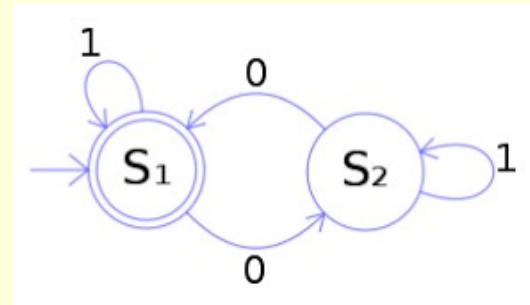
000101101101100110110110110110111001101010101001110110110110100011011010101100

11

11011010101100



Universal Turing machine



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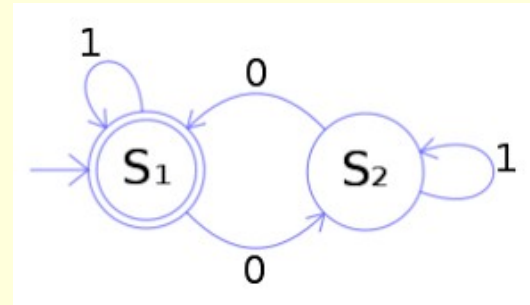
000101101101101100110110110110111001101010101001110110110110100011011010101100

11

11011010101100



Universal Turing machine



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 - Write $en(y)$ appropriate on tape 3
 - Move tape 3 accordingly to D (left or right)
6. Go to step 4

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Add WhatsApp powder

AND SO
ON ...

000101101101101100110110110110111001101010101001110110110110100011011010101100

11

11011010101100



Questions?



Questions?



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Questions?



Impossible? Never?



Mary said Tom would never call her again, but I told her,
"**Never say never.**"

-- 'Pickwick Papers' by Charles Dickens

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"Never is too long a word even for me..."

-- Treebeard in 'The Lord of the Rings' by J.R.R. Tolkien

<https://powcoder.com>

~~"Believe the unbelievable"~~

~~Dream the impossible.~~

~~Never take 'no' for an answer!"~~

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If there is convincing
evidence that
something is
impossible, ...



Week 5



Impossible? Never?



When can you ever say 'never!'?

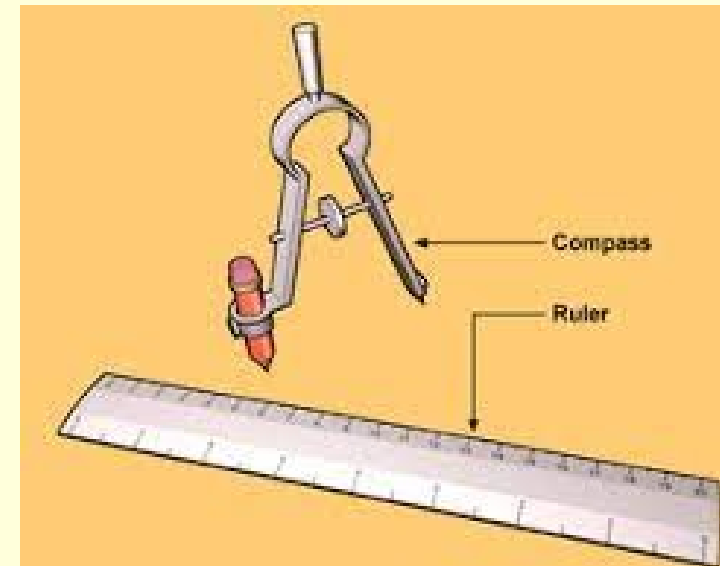
Solutions of polynomial equations

- 'closed' formulae exist for quadratic, cubic & quartic
- No such general formula can exist for degree ≥ 5 (!!)

<https://powcoder.com>

Geometric construction of polygons and other shapes

- Only 'straightedge and compass' allowed
- Impossible constructions
 - 'Square the circle'
 - 'Double the cube'
 - Angle trisection



Impossible? Never?



When can you ever say 'never!'?

Clever people have got this wrong in the past!

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Many predictions along the lines of 'this will never happen' have been incorrect...

<https://powcoder.com>

So can you ever say 'never'?

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Impossible? Never?



???

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Riemann Hypothesis <https://powcoder.com>

$P = NP$

Computers pass Turing test

...

Computers outperform humans at chess

Self-driving cars

Text to speech and speech to text

Computer facial recognition

...

Known to be impossible

Status unknown

Known to be possible

Quiz time!

Go to **Canvas** and find the quiz **Lectorial 5 Question set**

- Not worth any marks
- You can consult other students if you wish
- Time limit will be 10 minutes

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<https://powcoder.com>



Week 5

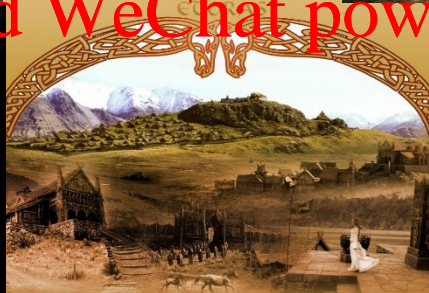


Computing Theory

Go!

The pictures will take 10 minutes to disappear!

Thomas music means 1 minute left!

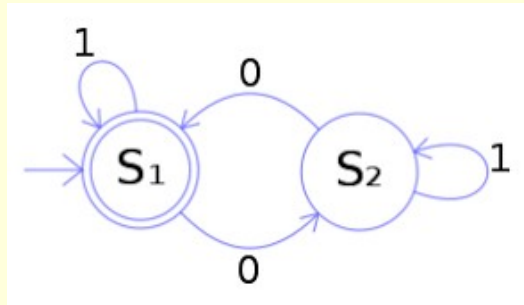


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Decision problems



A decision problem is a **question** in a **formal system** with a **yes-no answer**, depending on some input parameters.

Sort: Is a list of numbers sorted? **Assignment Project Exam Help**

Hamiltonian circuit: Is there a circular path in this graph that visits every node?

<https://powcoder.com>

Primality: Is a given number prime?

Python syntax: Is a given program syntactically correct?

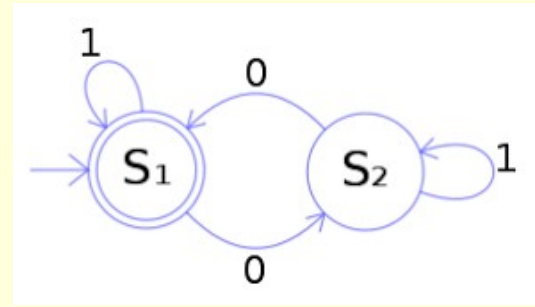
Password: Is the given password correct?

Bank balance: Is the transaction approved?

Halting: Given a TM M and input w , does M halt on w ?

Harder than it may seem ...

Decision problems



% n is an integer ≥ 1

while $n > 1$ do

if $n \bmod 2 == 0$

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else

$n = 3 * n + 1$ <https://powcoder.com>

elihw

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5 16 8 4 2 1

6 3 10 5 16 8 4 2 1

7 22 11 34 17 52 26 13 40 20 10 5 ... 1

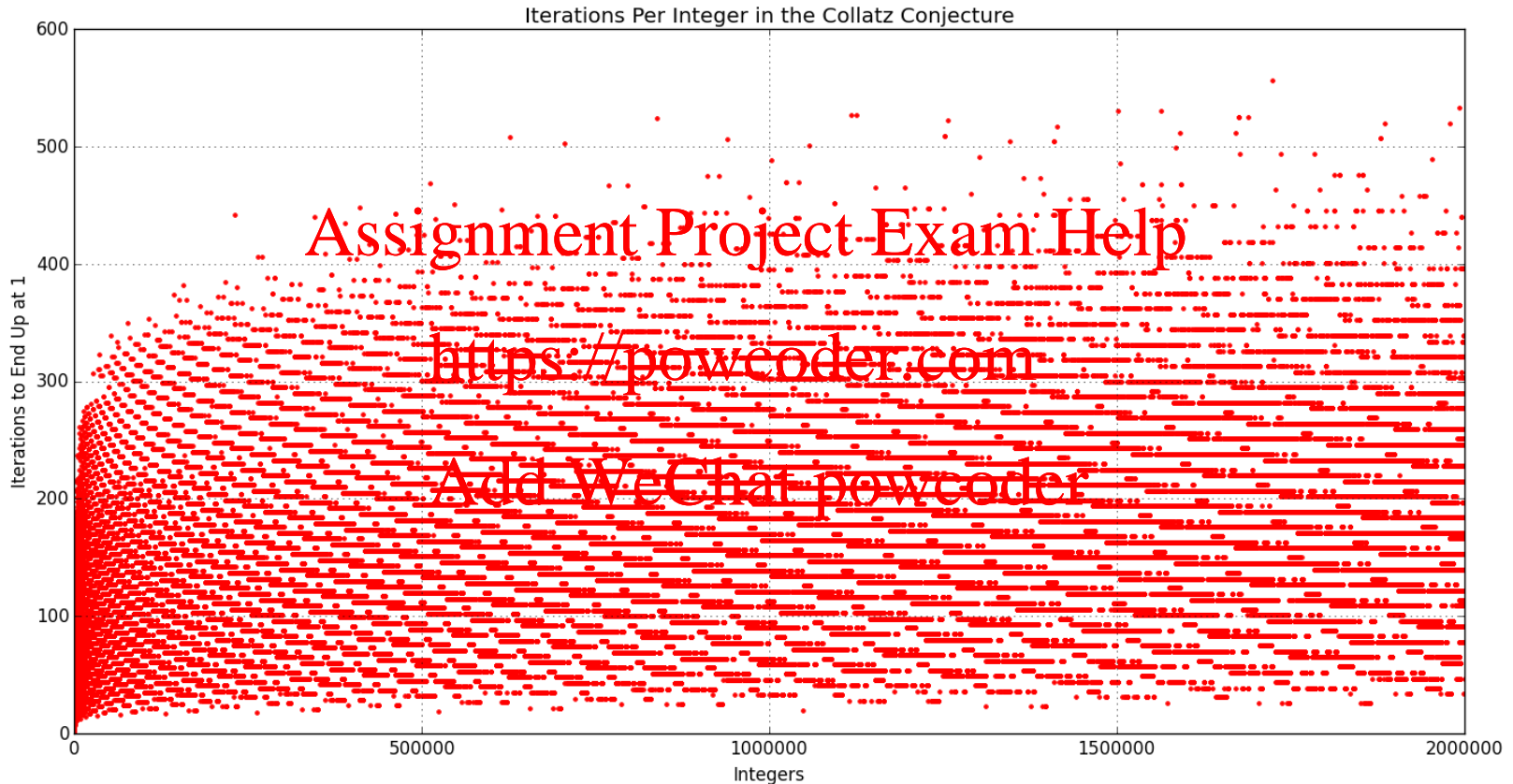
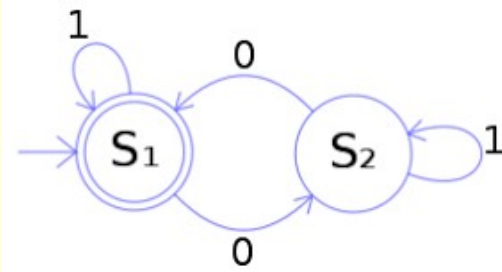
9 28 14 7 ... 1

15 46 23 70 35 106 53 160 80 40 20 ... 1

Does it always terminate?

No-one knows (!!)

Decision problems



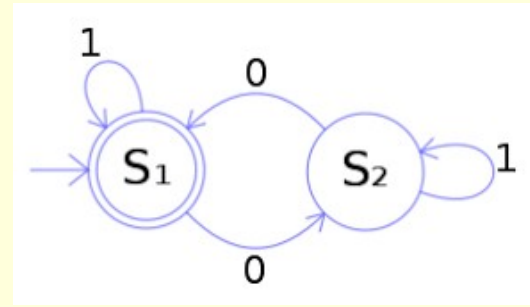
Does it always terminate?

No-one knows (!!)

Week 5

Computing Theory

Decidable problems



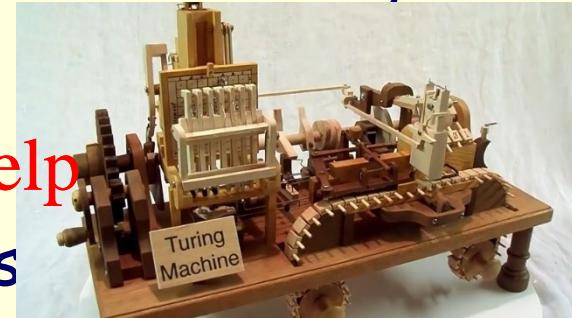
A decision problem is **decidable** if there **exists** a Turing machine **M** that solves it, ie

- **M** halts on all inputs **w**
- **M** outputs **yes** if the decision for **w** is yes
- **M** outputs **no** if the decision for **w** is no
- **M** produces no other outputs (so **M** is a language recogniser)

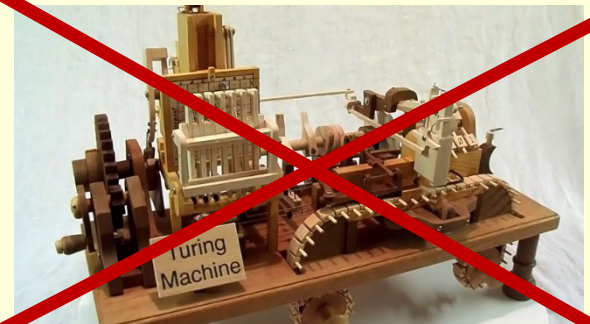
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<https://powcoder.com>

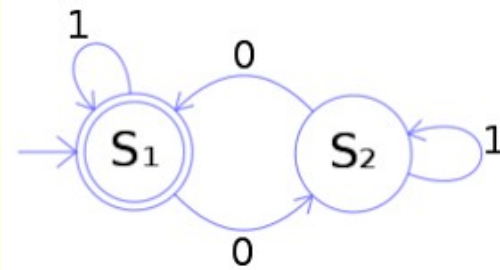
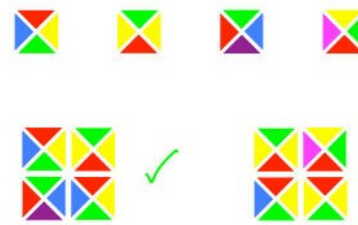
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A decision problem is **undecidable** if there **does not exist** a Turing machine **M** that solves it.



Tile problem



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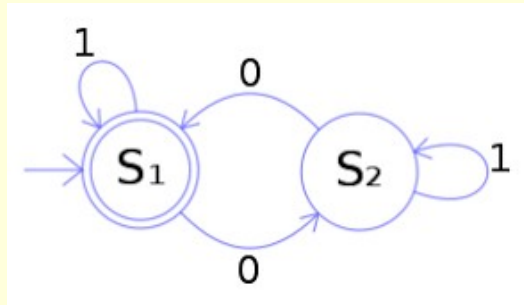
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Can you cover any rectangular area with a given set of tiles?

- Tiles cannot be rotated
- Edge colours must match
- Tiles can be copied

There is no Turing machine that solves this decision problem (!!!)

Halting problem



Halting problem: Given a Turing machine M and an input w , does M halt on w ?

For every TM M and every input w , either

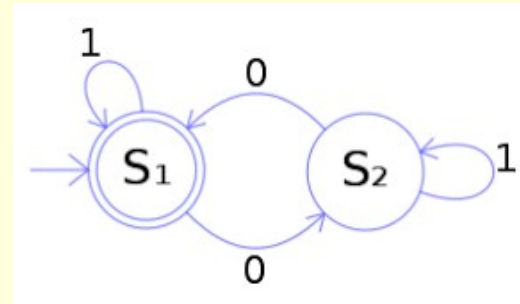
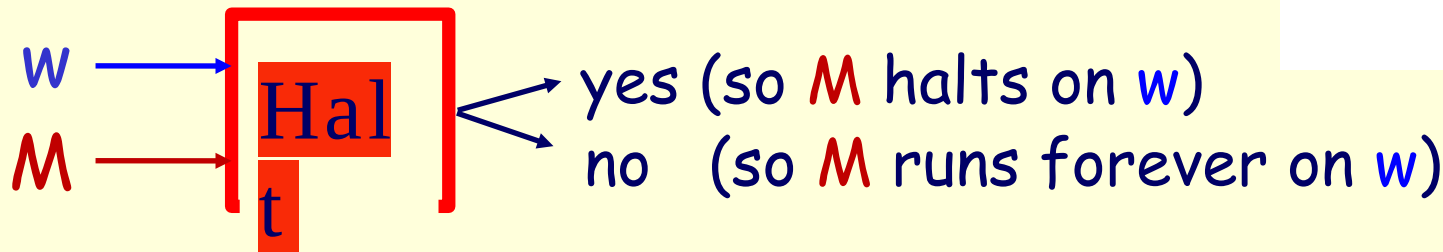
- M halts on w
- M doesn't halt on w

The Halting problem is a decision problem about Turing machines ..

Question: Is there a Turing machine that can solve the Halting problem for Turing machines?

Is the Halting problem decidable?

Halting problem



Is there a TM Halt such that ??

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- Halt terminates on every input (ie every M and every w)
- Halt accepts $\text{code}(M)\text{code}(w)$ if M terminates on w
- Halt rejects $\text{code}(M)\text{code}(w)$ if M does not terminate on w

Option 1:

Halt exists

The Halting problem is decidable

Week 5

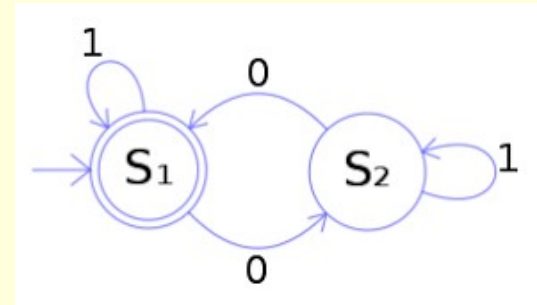
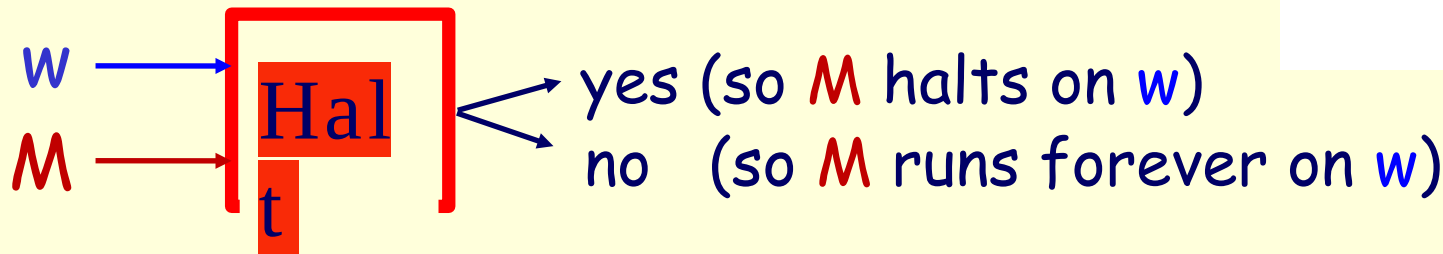
Option 2:

Halt does not exist

The Halting problem is undecidable

Computing Theory

Halting problem



"Gandalf, does the machine **Halting** exist?"



NO!!!

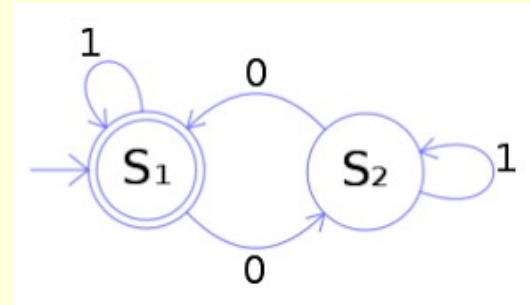
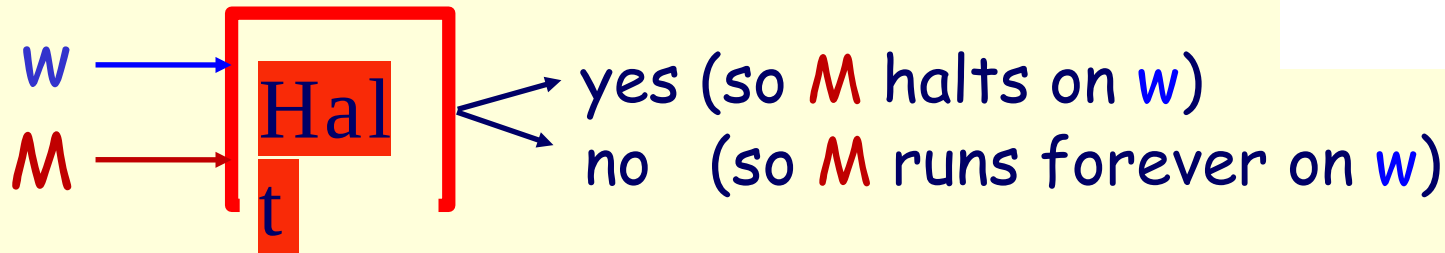
"Let's ask my friend, Frodo ..."

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Clues:

- "This statement is false" (Epiminedes)
- Paradox of the barber
- Self-reference

Halting problem



The Halting problem is **undecidable**

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Proof: Assume that the TM **Halt** exists, ie

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- **Halt** terminates on every input (ie every M and every w)
- **Halt** accepts $\text{code}(M)\text{code}(w)$ if M terminates on w
- **Halt** rejects $\text{code}(M)\text{code}(w)$ if M does not terminate on w

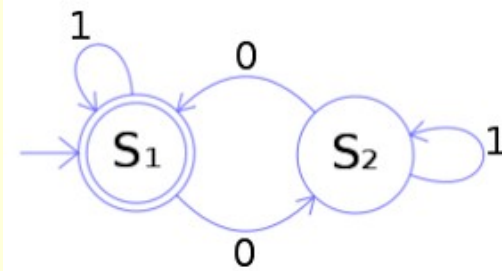
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Use **Halt** to construct TM **Weird** as follows:

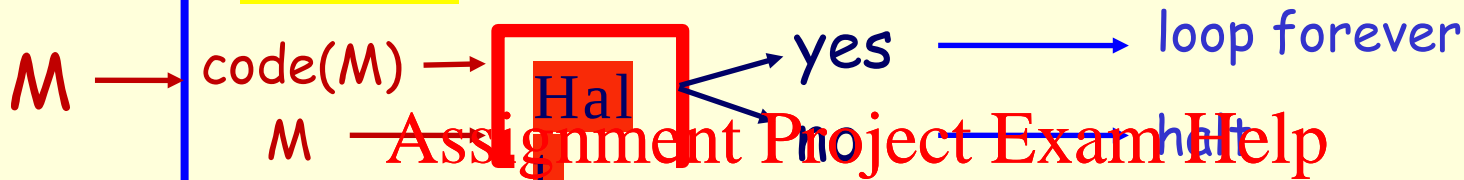
- If **Halt** accepts $\text{code}(M)\text{code}(M)^*$ then loop forever
- If **Halt** rejects $\text{code}(M)\text{code}(M)^*$ then halt

*encode M is as an input to itself

Halting problem



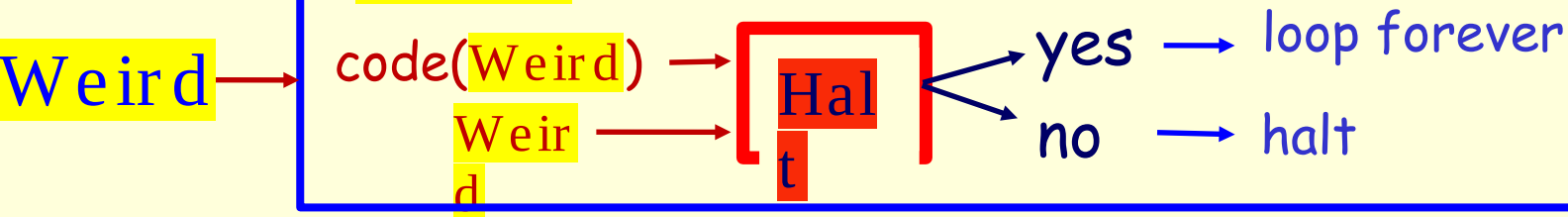
Weird



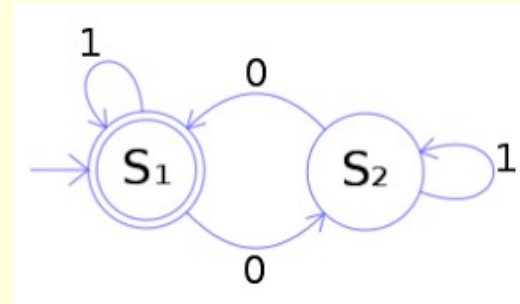
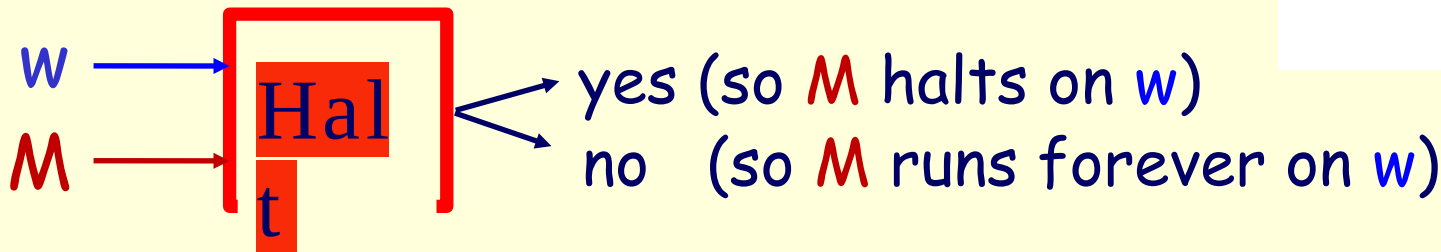
<https://powcoder.com>
What if $M = \text{Weird}$?

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Weird



Halting problem



So if TM **Halt** exists, then TM **Weird** must also exist

Weird takes a TM M as input and

- If M halts on $\text{code}(M)$, then **Weird** does not halt on $\text{code}(M)$
- If M does not halt on $\text{code}(M)$, then **Weird** halts on $\text{code}(M)$

This must work for any TM M ... Including when $M = \text{Weird}$ (!!)

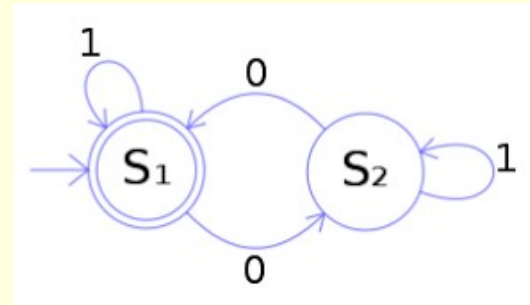
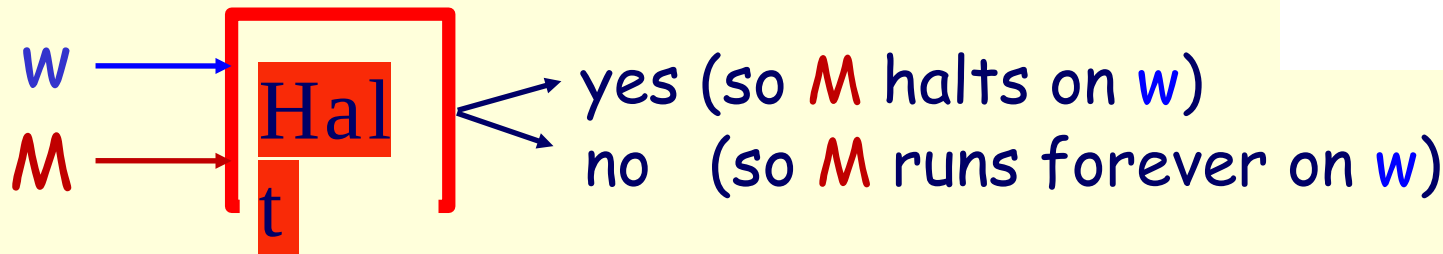
- If **Weird** halts on $\text{code}(\text{Weird})$, then **Weird** does not halt on $\text{code}(\text{Weird})$
- If **Weird** does not halt on $\text{code}(\text{Weird})$, then **Weird** halts on $\text{code}(\text{Weird})$

That's too weird!

CONTRADICTION!



Halting problem



So our assumption is wrong, i.e. the TM **Hal_t** does not exist

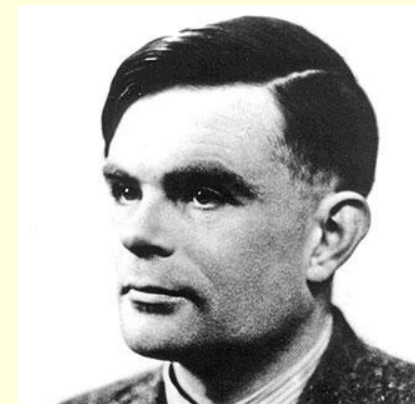
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The Halting problem is therefore **undecidable**

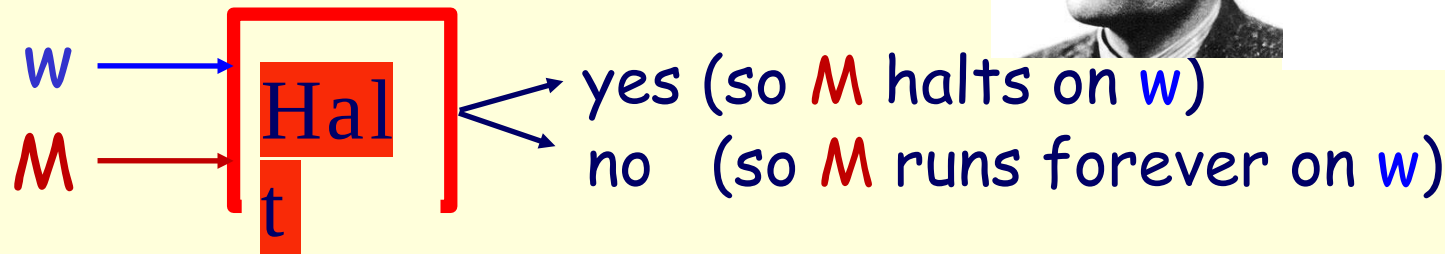
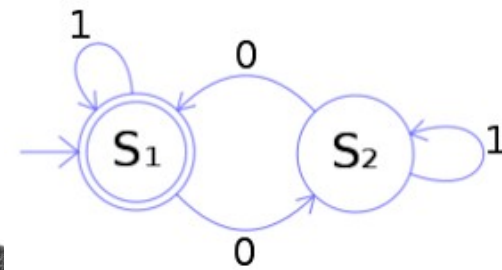
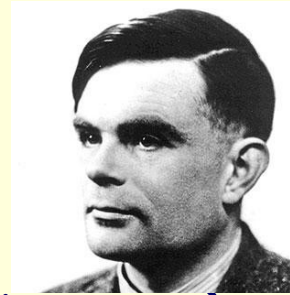
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This means that **there is no TM which**

- Always halts for any M and w
- Outputs 'yes' if M halts on w
- Outputs 'no' if M does not halt on w
- (Does not produce any other output)



Halting problem



This means any attempt to solve the halting program must for some M and w either:

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1. Not halt
2. Halt and output no if M halts on w (!!)
3. Halt and output yes if M doesn't halt on w (!!)
4. Halt and produce some other output (e.g., "Dunno!")

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1 is undesirable, 2 and 3 are insane!

Essentially, we have to accept that an answer "**Don't know**" is sometimes unavoidable ...

Questions?



Questions?



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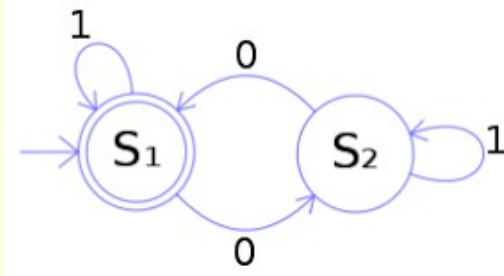
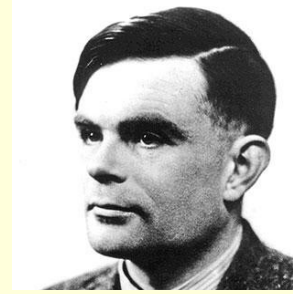
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Questions?



Computability



Decidable

- Primality testing
- Factorisation
- Hamiltonian circuit
- 3-SAT satisfiability
- Sorting
- Travelling Salesperson
- ...

Undecidable

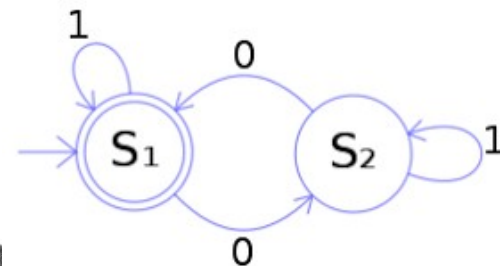
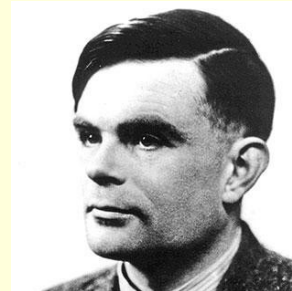
- Does M halt on w ? (halting problem)
- Does M halt on any w ?
- Does M halt on all w ?
- Does M halt on blank input?
- Do M_1 and M_2 halt on the same strings?
- Does M reach a particular state on input w ?
- ...
- Busy beaver problem
- Tile problem
- ...

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Computability



Let Problem **A** be a problem known to be undecidable, and Problem **B** with status unknown.

- Assume Problem **B** is decidable and derive a contradiction
- Reduce Problem **A** to Problem **B**

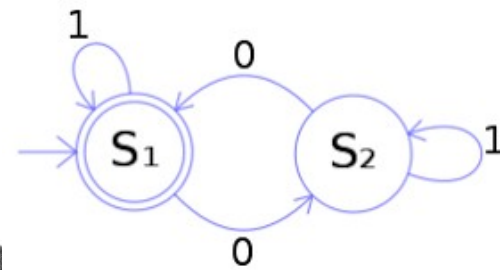
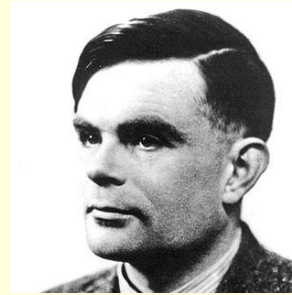
<https://powcoder.com>

Problem reduction is a shortcut:

- Show that a TM for Problem **B** can be used as part of a decision procedure for Problem **A**
- Shows Problem **B** decidable Problem **A** decidable
- Problem **A** undecidable
- So Problem **B** undecidable

Step 1 is the only necessary part ...

Computability



Loops problem: Does TM M run forever on input w ?

Assume there is a TM Loops which solves the Loops problem

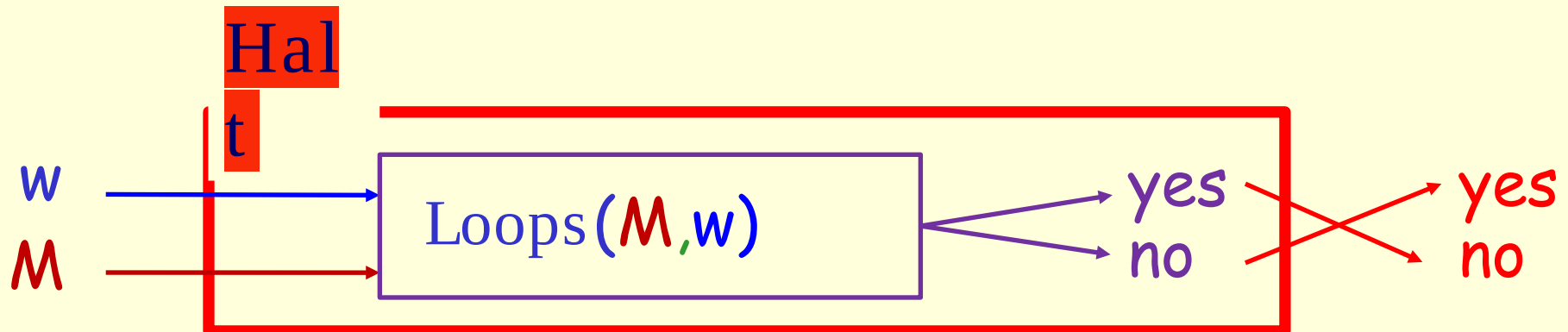
Given M and w **Assignment Project Exam Help**

1. Run Loops on M and w
2. If Loops says yes then output no
3. If Loops says no then output yes

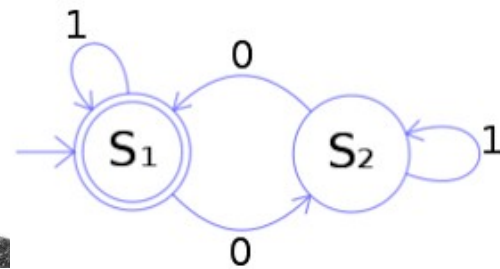
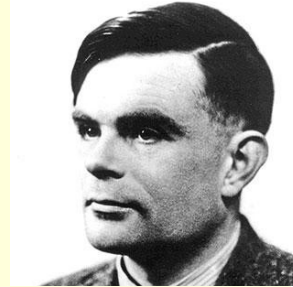
So the Loops problem is undecidable

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Computability



Blank Tape problem: Does TM M halt on the blank tape?

Assume there is a TM $Blank$ which solves the blank tape problem

Assignment Project Exam Help

Given M and w , compute machine N such that N with a blank tape

1. Writes w on the tape
2. Positions tape head to the first symbol in w
3. Goes to start state of M
4. Runs M on w

<https://powcoder.com>

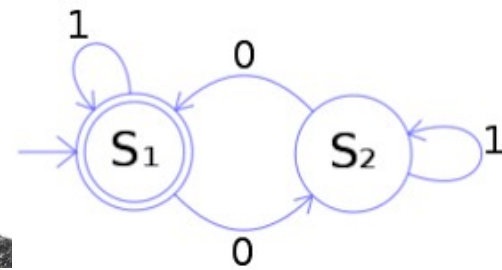
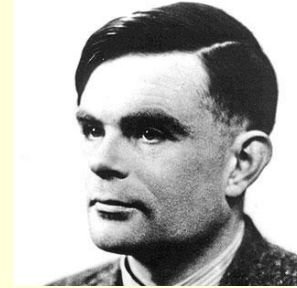
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N halts on the blank tape iff M halts on w

So $Blank$ on input N will solve the Halting Problem for M on w

So the Blank Tape problem is undecidable

Computability



Hal

t

w

M

Build
machine

Blank(N)

yes

no

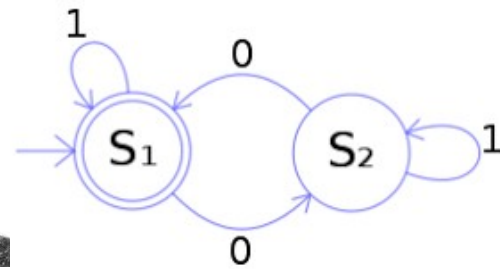
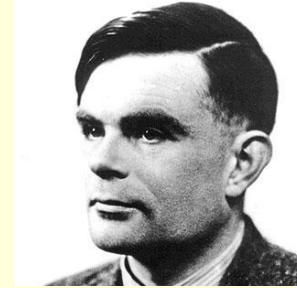
yes

no

<https://powcoder.com>

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Computability



All Inputs problem: Does TM M halt on all inputs?

Assume there is a TM All which solves the All Inputs problem

Assignment Project Exam Help

Given M and w , compute machine O such that O

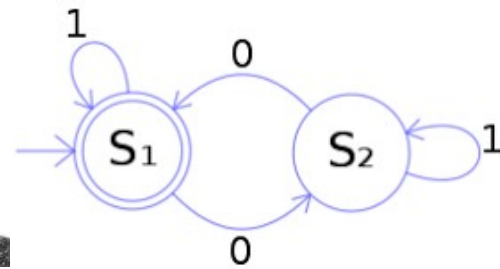
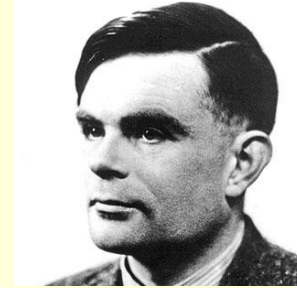
1. Erases its input <https://powcoder.com>
2. Writes w on the tape
3. Positions tape head to the first symbol in w
4. Goes to start state of M
5. Runs M on w

O halts on all inputs iff M halts on w

So All on input O will solve the Halting Problem for M on w

So the All Inputs problem is undecidable

Computability



Hal

t

w

M

Build
machine

O

$All(O)$

yes

no

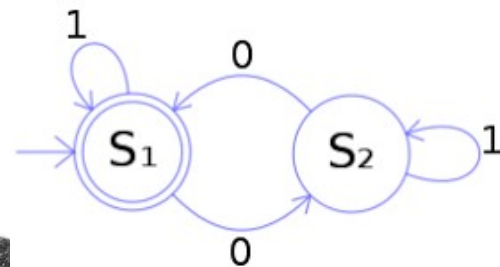
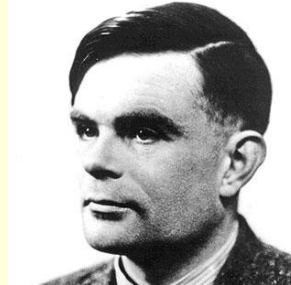
yes

no

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Computability



Undecidable problems include

Halting problem: Give a function f , does it halt on a given input x ?

Totality problem: Give a function f , does it halt on every input x ?

No input halting problem: Give a function f with no input, does it halt?

Program equivalence: Do two functions f and g always return same value?

Uninitialized variables: Is the variable x initialized before it's used?

Dead code elimination: Does this statement ever get executed?

...

Does $L(G) = *$?

Does $L(G_1) = L(G_2)$?

For PDAs, does $L(M_1) = L(M_2)$?

Does a PDA M have the minimal number of states?

Decidable problems include

Does $L(G) = ?$

Is $w \in L(G)$?

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<https://powcoder.com>

Questions?



Questions?



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Questions?



The Platypus Game

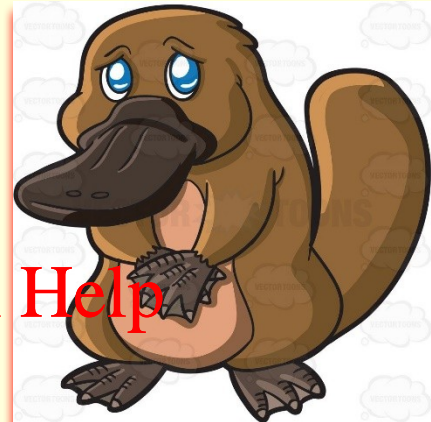


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The Platypus Game

Is the halting problem for the Platypus game decidable?



For the Platypus game the halting problem decidable is?

YES!

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<https://powcoder.com>

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2^{21} possible tapes

21×21 possible head positions

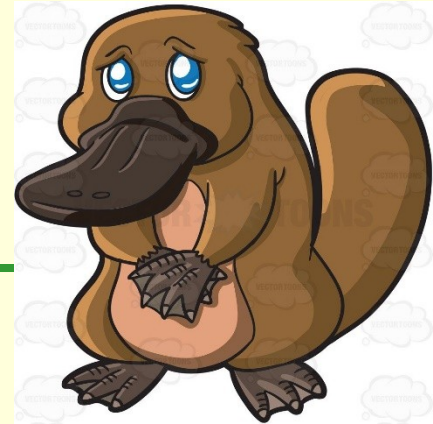
4×4 possible states

$$2^{21} \times 21 \times 21 \times 4 \times 4 = 14,797,504,512$$



The Platypus Game

So there are “only” **14,797,504,512** possible configurations of the Platypus game ...



Halt - Assignment Project Exam Help

platypus <https://powcoder.com>

- P →
1. Set counter to 0
 2. Run game, incrementing counter after each turn
 3. If the game halts, output yes
 4. If the counter exceeds 14,797,504,512, output no

yes

no

Not very practical, but possible in principle



The Platypus Game

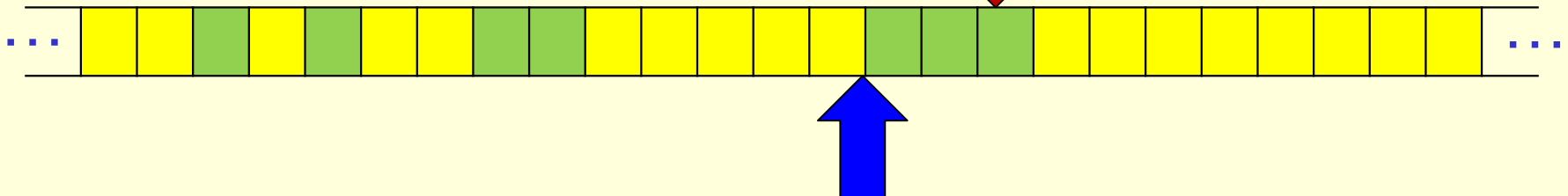
Generalised Platypus game

- Same as Platypus game, but with an infinite tape!
- Ghost gum and Wattle are infinitely far apart
- Arbitrary number of animals
- Still only two colours

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Is the Halting problem for the
Generalised Platypus game decidable?

The Platypus Game



Survey results (final)

Attempts: 56 out of 70

Which of the following approaches should we use to approximate a tournament of 268,435,456 machines?

"Round robin + knockout" means we divide the machines up into chunks of say 1,000, play a full tournament for each chunk, and then have a knockout round for the 268,000 or so winners.

"Champions League" means we play as many random matches as possible, and use a ranking (ie a ladder in sporting terms) to rank all teams. Once the "season" is over (ie we have no time to play any further matches), the machine that is at the top of the rankings is the winner.

Round-robin + knockout	30 respondents	43 %	<div></div> ✓
Champion's League	25 respondents	36 %	<div></div>
Something else	1 respondent	1 %	<div></div>
No Answer	14 respondents	20 %	<div></div>

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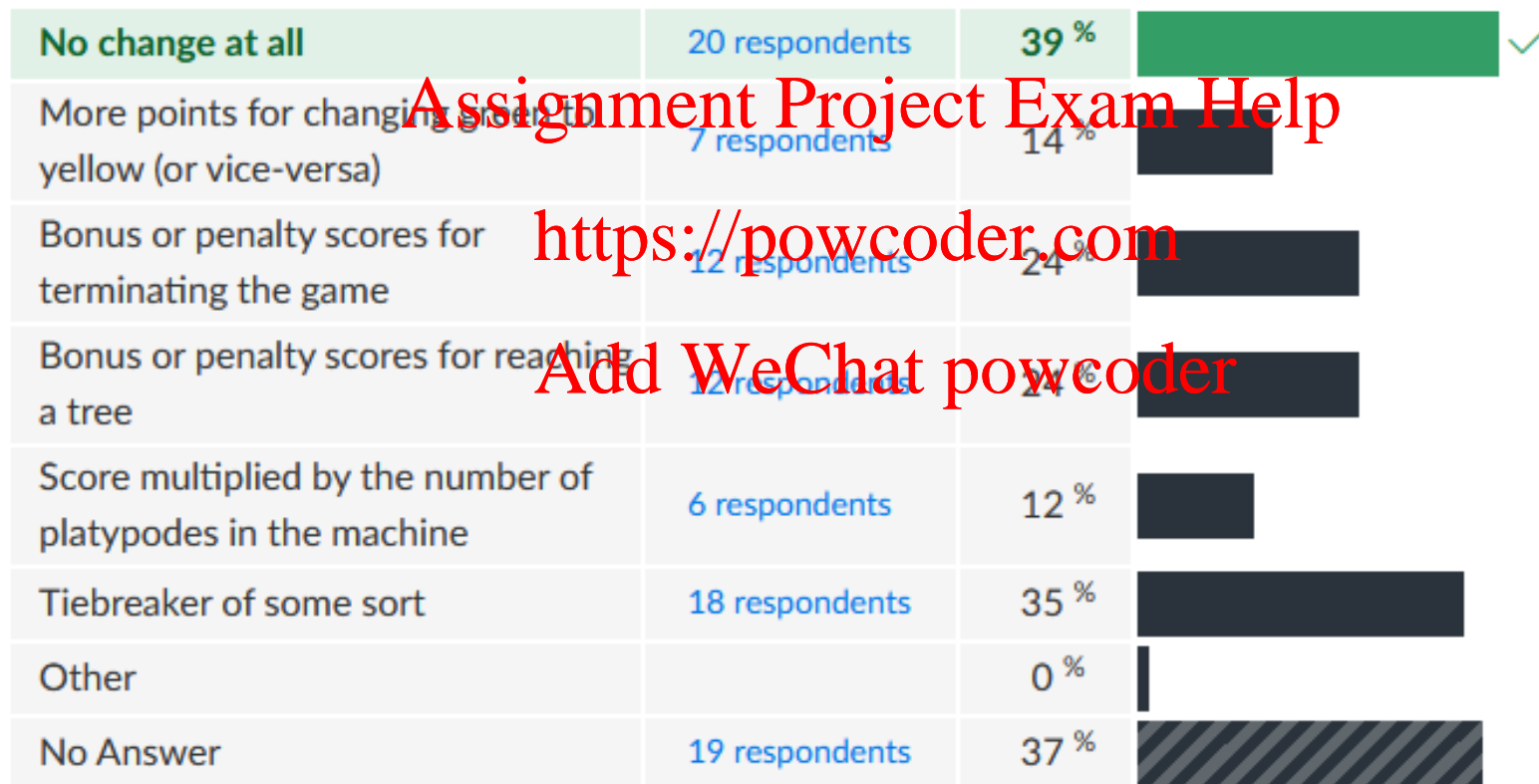
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The Platypus Game

Survey results (final)



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The Platypus Game

Survey results (final)

Attempts: 47 out of 47

Should there be any rule changes? Please indicate all that you think should apply.

No change at all	33 respondents	70 %	<div></div> ✓
Games run on more than one starting set of cells (all green, "chess like", random)	2 respondents	4 %	<div></div>
Shortening or lengthening the maximum number of turns before a game ends (currently 100)	6 respondents	13 %	<div></div>
More players (3 to 8 say)	2 respondents	4 %	<div></div>
Larger or smaller number of cells (eg 11? 31? 101?)	5 respondents	11 %	<div></div>
Different rules for teaching a tree?	1 respondent	2 %	<div></div>
More colours	4 respondents	9 %	<div></div>
More animals	4 respondents	9 %	<div></div>
2-dimensional board	2 respondents	4 %	<div></div>
Machines change somehow during play	5 respondents	11 %	<div></div>
Something else		0 %	<div></div>
No Answer	23 respondents	49 %	<div></div>

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Computing Theory

The Platypus Game



Survey results (final)

Do you have any other suggestions or comments about tournaments?

Maybe instead of a champion's league with random matchups there are brackets to determine which machine you can fight against (like an elo rating system to determine which players are suitable matches to play with)..

Sounds interesting too! <https://powcoder.com>

A rankings system such as used by the Champion's League suggestion is what is used by a majority of online and real world games. Perhaps we can apply what is learned through stimulating a Champion's league to the real world.

Sure! To a real platypus? ☺

The Platypus Game



Survey results (final)

Do you have any other suggestions or comments about tournaments?

Is there any application in creating tournaments that become more ranked then more tournaments that are completed? For example, a single tournament would show how well a set went against each single player, if they were to lose in their round. However, they may have lost to a higher score but a different pairing didn't win to as high a score. That team would progress unfairly.

So completion rate is important?

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Champion's league seems like an interesting way to rank the machines! :)

Ok!

The Platypus Game



Survey results (final)

Are there any other suggestions or comments about scoring?

For the tiebreaker, maybe let the machine that reaches the green cell with platypus be the winner.

Interesting --- so we reward the 'bold platypodes'!

I would like a change to the scoring system that allows the player to be rewarded for taking more risk.

Similar, presumably ...

Simple is better, and changes to rules would not change the outcome too much.

No change is easy to do!

The Platypus Game



Survey results (final)

Are there any other suggestions or comments about scoring?

If we were to use a ranking system, it makes most sense to include a tiebreaker such that there is no draw.

<https://powcoder.com>

Sure, although we can rank for draws as well.

If a grid had could turn a token green with a platypus on it, this would be a terminating play. That should garner a penalty.

There may also be a play that has more changes to green than to yellow, which would also be more likely to trigger an end game, and on the flipside the more yellow would mean the player does not terminate at all which is almost cheating, difficult to say without the context of play...

So certain machines should be outlawed?

The Platypus Game



Survey results (final)

Are there any other suggestions or comments about scoring?

Bonus points for reaching the trees. **Assignment Project Exam Help**

Ok!

<https://powcoder.com>

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The Platypus Game

Survey results (final)



Are there any other suggestions or comments about rule changes?

If we have a larger number of cells, then there might be some bonus for reaching a tree since it'll be harder to achieve..

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Good thought. Presumably the number of cells and tree options should be linked like this.

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Shorter games means faster progression, which I'll deal with happily.

A short game is a good game!

Shortening or lengthening the maximum number of turns before a game ends (currently 100), Larger or smaller number of cells (eg 11? 31? 101?)

Sure.



The Platypus Game

Survey results (final)

Are there any other suggestions or comments about rule changes?

Machines changing somehow during play would make it harder to guess the outcome of matches and thus predict what an ideal winner would look like, however would make it much more visually interesting, with emerging strategies we could perhaps study.

Machines change somehow during play

Sure. How would they change?

Shortening or lengthening the maximum number of turns before a game ends (currently 100)

Sure. More responses yet to be analysed!

Questions?



Questions?



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Questions?



Week 5

Computing Theory

A close-up, low-angle shot of a dinosaur's head, likely a T-Rex, with its mouth wide open, revealing sharp, white teeth and a dark interior. The dinosaur's skin is dark and textured, with visible scales and ridges. The background is dark and out of focus, suggesting an indoor setting like a museum or a film set.

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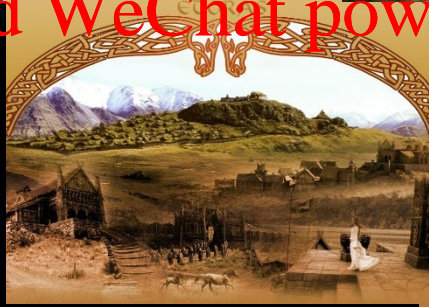
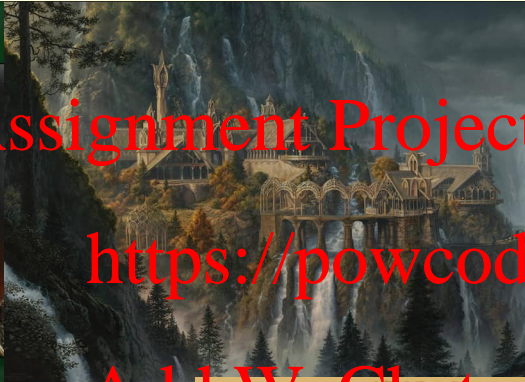
Break time! (We resume when all the pictures are gone! This will take 3 minutes!)



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I AM BACK!

A detailed illustration of a dragon breathing fire. The dragon's head is in the center, with its mouth wide open, revealing sharp teeth and a bright orange and yellow flame. The dragon's body is covered in dark, scaly armor, and its wings are partially visible. The background is a dark, smoky environment with a large, intense fire at the top, casting a warm glow over the scene.

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Alternative Scheme?



Troll	Dreadful	Poor	Acceptable	Exceeds Expectations	Outstanding
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Outstanding - CONGRATULATIONS! Your exemplary powers of deduction and a formidable knowledge of the inner workings of the magical world reveal you to be a witch or wizard of genuine skill and learning.

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Exceeds Expectations - Well done - a most creditable performance!

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Acceptable - demonstrates real magical potential.

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Poor - Alas - we regret to inform you that you have narrowly failed. This may have been due to factors outside your control (eg: poltergeist intervention, examination nerves or a malfunctioning quill.) Please do not disconsolate.

Dreadful - We are sorry to inform you that you have failed.

Troll - You would appear either to have abandoned the test due to factors outside your control (eg, earthquake, poltergeist attack), or else you are a troll, in which case you are to be congratulated on being able to use a computer and have achieved the grade of O.F.T. (Outstanding for Trolls).

Marking

Computing Theory



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