Linear models: Recap

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Linear models:

Perceptron Assignment Project Exam Help

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Naïve Bayes; https://powcoder.com

$$\log P(y|\mathbf{x}; \boldsymbol{\theta}) = \log P(\mathbf{x}|y; \boldsymbol{\phi}) + \log P(y; \boldsymbol{u}) = \log B(\mathbf{x}) + \boldsymbol{\theta} \cdot \boldsymbol{f}(\mathbf{x}, y)$$
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Logistic Regression

$$\log P(y|\mathbf{x};\boldsymbol{\theta}) = \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}, y) - \log \sum_{y' \in \mathcal{Y}} \exp \boldsymbol{\theta} \cdot \mathbf{f}(\mathbf{x}, y')$$

Features and weights in linear models: Recap

Feature representation: /powcoder.com

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(K-1)×V

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(K-2)×V

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Weights: θ

$$\boldsymbol{\theta} = [\underbrace{\theta_1; \theta_2; \cdots; \theta_V}_{y=1}; \underbrace{\theta_1; \theta_2; \cdots; \theta_V}_{y=2}; \cdots; \underbrace{\theta_1; \theta_2; \cdots; \theta_V}_{y=K}]$$

Rearranging the features and weights

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Represent the features X as a column vector of length V, and represent the weights as a Θ as $K \times V$ matrix

Assignment Project Example V, and represent the weights as a Θ as $K \times V$ matrix $X_1 \quad X_2 \quad \cdots \quad X_V$

$$\mathbf{x} = \begin{bmatrix} x_1^{\text{https://poweo}} & \mathbf{der.com} & \cdots & \theta_{1,V} \\ x_2 & y = 2 \\ \mathbf{der.com} & \theta_{2,1} & \theta_{2,2} & \cdots & \theta_{2,V} \\ \mathbf{powcoder...} & y = K & \mathbf{powcoder...} & \cdots \\ y = K & \mathbf{e}_{K,1} & \mathbf{e}_{K,2} & \cdots & \mathbf{e}_{K,V} \end{bmatrix}$$

 \triangleright What is Θx ?

Scores for each class

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Verify that $\psi_1, \psi_2, \dots, \psi_K$ correspond to the scores for each class Assignment Project Example 1p

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$$\Psi = \Theta x = \begin{cases} \theta_2 \cdot x = \psi_2 \\ \theta_2 \cdot x = \psi_2 \end{cases}$$
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Implementation in Pytorch

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```
MIN [48]: Weights Assignment Project Exam Help
                                                print(weights)
                                                input = torch.randn(9)
                                                print(input)
                                               out at Strength And The Country of the Paymon Period Paymo
                                                print output
                                                softmax = nn.Softmax(dim=0)
                                                probs = softmax(output)
                                                print(probs)
                                                                                       [-1.2000, 1.3527, 1.9529, -1.3182, 0.1101, -0.7105, -0.4409, 0.9753,
                                                                                       -0A821do.W4eChat.po,w.coder633, 1.1353, 0.3069,
                                                                                           -0.0584]])
                                                     tensor([ 0.0148, 0.0565, -0.6462, -0.0155, -0.5532, -0.8514, -0.1339, 0.5056,
                                                                                           0.6025])
                                                     tensor([-1.1695, -0.1363, 0.5428])
                                                     tensor([0.1069, 0.3005, 0.5926])
```

Digression: Matrix multiplication

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Assignment Project Exam Help
Matrix with *m* rows and *n* columns:

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where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ where $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$ and $C_{ij} = \frac{n}{n} \sum_{i=1}^{n} \frac{n}{n}$

Example:

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$$\begin{bmatrix} 2 & 3 \\ 1 & 2 \end{bmatrix} \times \begin{bmatrix} 1 & 0 & 2 \\ 0 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 2 & 3 & 7 \\ 1 & 2 & 4 \end{bmatrix}$$

Digression: 3-D matrix multiplication

```
import torch https://powcoder.com
In [27]: import torch
        print(input)
        mat2 = torch.randint(5, (2, 4, 3))
        print (mat2) signment Project Exam Help
        print(out)
        Assignation (Proper Dampole)
               [[3, 2, 3, 4],
         tensor([[[0, 2, 10], v)powcoder.com
                [4, 4, 2],
                  dd'WeChat powcoder
                [3, 0, 1],
                [0, 0, 4],
               [2, 4, 2]]])
         tensor([[[12, 12, 22],
               [13, 19, 22],
                [8, 8, 10]],
               [[23, 16, 34],
                [29, 16, 35],
                [15, 12, 26]]])
```

Tensor shape: (batch-size, sentence-length, embedding size)

SoftMax

https://powcoder.comSoftMax, also known as normalized exponential function.

Assignment Project* Exam Help
$$\frac{\sum_{j}^{K} \exp \psi_{j}}{\sum_{j}^{K} \exp \psi_{j}}$$
 for $i=1,2,\cdots,K$

Applying Soft Max turns the corts into an robabilistic distribution:

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SoftMax(
$$\Psi$$
) =
$$\begin{bmatrix} P(y=1) \\ P(y=2) \\ \dots \\ P(y=K) \end{bmatrix}$$

Verify this is exactly logistic regression

Logistic regression as a neural network https://powcoder.com

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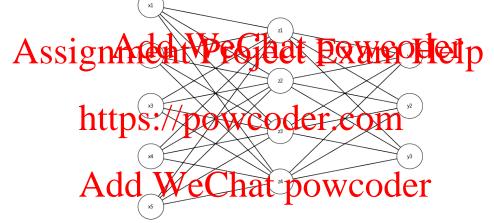
$$y = SoftMax(\Theta x)$$

 $V = 5 K = 3$

Going deep

There is no realith widdle

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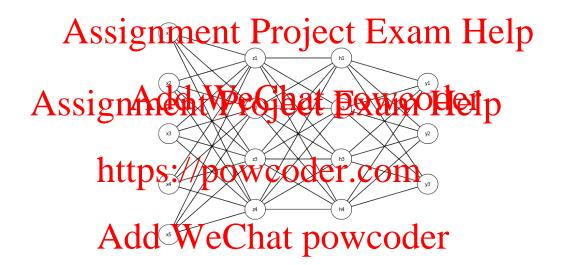


$$z = \sigma(\Theta_1 x)$$

 $y = \text{SoftMax}(\Theta_2 z)$

Going even deeper

There is no reason why we can't add layers in the middle



$$egin{aligned} & oldsymbol{z}_1 = \sigma(oldsymbol{\Theta}_1 oldsymbol{x}) \ & oldsymbol{z}_2 = \sigma(oldsymbol{\Theta}_2 oldsymbol{z}_1) \ & oldsymbol{y} = \mathsf{SoftMax}(oldsymbol{\Theta}_3 oldsymbol{z}_2) \end{aligned}$$

But why?

Non-linear classification

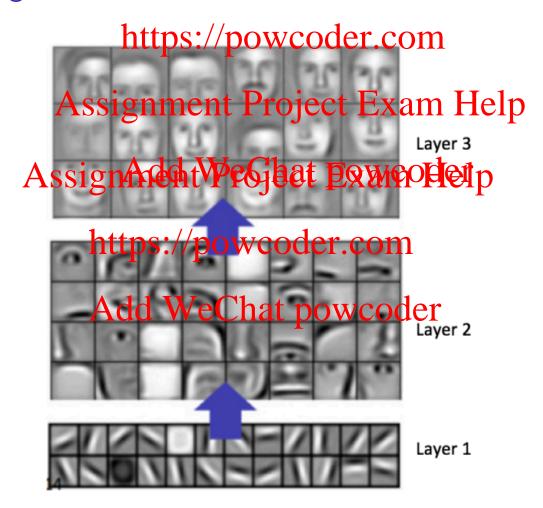
Linear models like Logistic regression can map data into a high-dimensional vector space, and they are expressive enough and work well for many lemperatures, which we have longlex non-linear models?

- There Aski grantified a learn land a family of nonlinear methods that learn complex functions of the input through multiple yer por worm dation on
- Deep learning facilitates the incorporation of word embeddings. Which was dense to representations of words, that can be learned from massive amounts of unlabeled data.
 - ► It has evolved from early static embeddings (e.g., Word2vec, Glove) to recent dynamtic embeddings (ELMO, BERT, XLNet)
- Rapid advances in specialized hardware called graphic processing units (GPUs). Many deep learning models can be implemented efficiently on GPUs.

Feedforward Neural networks: an intuitive justification https://powcoder.com

- In image classification, instead of using the input (pixels) to predict the image type directly, you can imagine a scenario that yous argument of the predict particular mouth, hand, ear.
- In text processings we power gives. Some scenario. Let's say we want to classify movie reviews (or movies themselves) into a label satch! We had powered predicting these labels directly, we first predict a set of composite features such as the story, acting, soundtrack, cinematography, etc. from raw input (words in the text).

Face Recognition



Feedforward neural networks

https://powcoder.com

Formally, this Associatement Project Exam Help

- Use the text x to predict the features z. Specifically, train a logistic regression distribution by the formula $k \in \{1, 2, \cdots, K_z\}$
- **Use the features** $z/t\rho$ predict the labely. Train a logistic regression classifier to compute P(y|z). z is unknown or hidden, so we will use the P(z|x) as the features. Add We Char powcoder

Caveat: it's easy to demonstrate what this is what the model does for image processing, but it's hard to show this is what's actually going on in language processing. Interpretability is a major issue in neural models for language processing.

The hidden layer: computing the composite features

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If we assume each z_k is binary, that is, $z_k \in \{0, 1\}$, then $P(z_k|\mathbf{x})$ are beginned by the bijary (\mathbf{z}_k

$$\begin{array}{l} P(z_k = 1 | \mathbf{x}; \mathbf{\Theta}^{(x \to z)}) = \sigma(\boldsymbol{\theta}_k^{x \to z} \cdot \mathbf{x}) \\ \mathbf{Assignment Project Example 1} \\ + \exp(-\boldsymbol{\theta}_k^{x} \cdot \mathbf{x}))^{-1} \end{array}$$

- The weight https: Θ (power semstructed by stacking (not concatenating, as in linear models) the weight vectors for each θ_k , WeChat power $\Theta^{(x \to z)} = [\theta_1^{x \to z}, \theta_2^{x \to z}, \cdots, \theta_{K_z}^{x \to z}]^{\top}$
- We assume an offset/bias term is included in ${\bf x}$ and its parameter is included in each ${\bf \theta}_k^{{\bf x} \to {\bf z}}$

Notations: $\mathbf{\Theta}^{(x \to z)} \in \mathbb{R}^{k_z \times V}$ is a real number matrix with a dimension of k_z rows and V columns

Activation functions

Sigmoid: The range of sigmoid function is (0.1). https://powcoder.com

Assignment $\Pr^{\sigma(x)} = \frac{1}{\text{ject Exam Help}}$

Question: what's the value of the sigmoid function when

x = 0 Assignment Problet Example 1p Tanh: The range of the tanh activation function is (-1,1)

https://powcoder.com
$$tanh(x) = \frac{e^{2x} \cdot e^{0}m}{e^{2x} + 1}$$

Question: which the control of the

▶ ReLU: The rectified linear unit (ReLU) is zero for negative inputs, and linear for positive inputs

$$ReLU(x) = max(x, 0) = \begin{cases} 0 & x < 0 \\ x & otherwise \end{cases}$$

Sigmoid and tanh are sometimes described as squashing functions.

Activation functions in Pytorch

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from torch Aising import torch Project Exam Help

```
input = Assignment/Legibat Paymothelp
sigmoid = nn. Sigmoid()
output = sightps://povycoder.com

tanh = nn. TaAldd WeChat powcoder
output = tanh(input)

relu = nn. ReLU()
output = relu(input)
```

The output layer

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The output layer is computed by the multiclass logistic regression project Exam Help

▶ The weight matrix $\Theta^{(z \to y)} \in \mathbb{R}^{k_y \times k_z}$ again is constructed by stacking weightlyectors or each power coder $\mathbf{\Theta}^{(z \to y)} = \begin{bmatrix} \boldsymbol{\theta}_1^{z \to y}, \boldsymbol{\theta}_2^{z \to y}, \cdots, \boldsymbol{\theta}_{K_y}^{z \to y} \end{bmatrix}^{\top}$

$$\mathbf{\Theta}^{(z\to y)} = \left[\boldsymbol{\theta}_1^{z\to y}, \boldsymbol{\theta}_2^{z\to y}, \cdots, \boldsymbol{\theta}_{K_y}^{z\to y}\right]$$

The vector of probabilities over each possible value of y is denoted:

$$P(\boldsymbol{y}|\boldsymbol{z};\boldsymbol{\Theta}^{(z\to y)},\boldsymbol{b}) = \operatorname{SoftMax}(\boldsymbol{\Theta}^{(z\to y)}\boldsymbol{z}+\boldsymbol{b})$$

The negative loglikelihood or cross-entropy loss

In a multi-class classification setting, a softmax output produces a probabilistic distribution over possible labels. It works well together with negative consistent mention of the region with negative consistent mention of the region of the

Add
$$\widetilde{y_j}$$
 echat powerder
$$-\mathcal{L} = -\sum_{i=1}^{N} e_{y^{(i)}} \cdot \log \widetilde{y}$$

where $e_{v(i)}$ is a **one-hot vector** of zeros with a value of one at the position $y^{(i)}$

Alternative loss functions

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There are alternatives to SoftMax and cross-entropy loss, just as there are alternatives in linear models.

as there are alternatives in linear models.

Pairing an affine transformation (remember perceptron) with a margin loss:

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 $\Psi(y; \mathbf{x}^{(i)}, \Theta) = \mathbb{Z}hatv$ powcoder

$$\ell_{\mathsf{MARGIN}}(\boldsymbol{\Theta}; \boldsymbol{x}^{(i)}, y^{(i)}) = \max_{y \neq y^{(i)}} \left(1 + \Psi(y; \boldsymbol{x}^{(i)}, \boldsymbol{\Theta}) - \Psi(y^{(i)}; \boldsymbol{x}^{(i)}, \boldsymbol{\Theta}) \right)$$

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Training of the training of th

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A feedforward network with a cross-entropy loss https://powcoder.com

The following Aussi granteen for warde etra Exempel Pone hidden layer, complete with a cross-entropy loss that drives parameter assignation and the power parameter provides the power parameter assignation and the power parameter assignation and the power parameter power parameter parameter power parameter parameter parameter power parameter parameter power parameter p

$$z \leftarrow \frac{\text{https://poy,coder}}{\text{https://poy,coder}}$$

$$\tilde{y} \leftarrow \frac{\text{SoftMax}(\Theta^{z \to y}z + b)}{\text{Add WeChat powcoder}}, \quad \tilde{y} \in R^{k_y}$$

$$\ell^{(i)} \leftarrow -e_{y^{(i)}} \cdot \log \tilde{y}$$

where f is an elementwise activation function (e.g., σ or ReLU), $\ell^{(i)}$ is the loss at instance i

Updating the parameters of a feedforward network

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As usual, $\Theta^{x} \to g$ manch the projection at the partial projection and the projection at the partial projection at the projection at the partial projection at the projecti

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$$\begin{array}{l} \mathbf{h}_{k}^{z \to y} \leftarrow \boldsymbol{\theta}_{k}^{z \to y} - \boldsymbol{\eta}^{(t)} \nabla_{\boldsymbol{\theta}_{k}^{z \to y}} \ell^{(i)} \\ \mathbf{h}_{n}^{x \to z} \leftarrow \boldsymbol{\theta}_{n}^{x \to z} - \boldsymbol{\eta}^{(t)} \nabla_{\boldsymbol{\theta}_{n}^{x \to z}} \ell^{(i)} \end{array}$$

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where $\eta^{(t)}$ is the learning rate at iteration t, $\ell^{(i)}$ is the loss on instance (or minibatch) i, $\theta_n^{x \to z}$ is the nth column of the matrix $\Theta^{x \to z}$, and $\theta_k^{z \to y}$ is the kth column of the matrix $\Theta^{z \to y}$.

Compute the gradient of the cross-entropy loss on hidden layer weights $\Theta^{z \to y}$ https://powcoder.com

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https://powcoder.com

$$\frac{\partial \ell^{(i)}}{\partial \theta_{k,j}^{z \to y}} = - \underbrace{Add}_{\partial \theta_{k,j}^{z \to y}} \underbrace{V_{\theta_{y(i)}^{z \to y}}}_{y(i)} \underbrace{P_{\theta_{y(i)}^{z \to y}}}_{y \in \mathcal{Y}} \underbrace{Chat}_{pow} \underbrace{pow}_{y}^{(z \to y)} \cdot z \right)$$

$$= \left(P(y = j | \mathbf{z}; \mathbf{\Theta}^{(z \to y)}, \mathbf{b}) - \delta \left(j = y^{(i)} \right) \right) z_{k}$$

where $\delta(j = y^{(i)})$ returns 1 if $j = y^{(i)}$ and 0 otherwise, z_k is the kth element in \boldsymbol{z} .

Applying the chain rule to compute the derivatives

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We use the chain rule to break down the gradient of the loss on the hidden layer weignment Project Exam Help

where

$$\ell^{(i)} = -e_{y^{(i)}}$$
 Add We Collaterov coder $\log \sum_{k} e^{o_{k}}$ $\log \sum_{k} e^{o_{k}}$ $\log \sum_{k} e^{o_{k}}$ $\log \sum_{k} e^{o_{k}}$

Note: o_i is the logit that corresponds to the true label $y^{(i)}$

Derivative of the cross-entropy loss with respect to the logits https://powcoder.com

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$$= \frac{e^{o_j}}{\sum_k e^{o_k}} - \frac{\partial}{\partial o_j} o_i$$

$$= \tilde{y}_j - \delta(j = y^{(i)})$$

Gradient on the hidden layer weights $\Theta^{z \to y}$

One more step to compute the gradient of the loss with respect to the weights: https://powcoder.com

$$\frac{\partial o_{j}}{\partial \theta_{k,j}^{(z \to y)}} = \underbrace{\frac{\operatorname{Ssignment}}{\partial \theta_{k,j}^{(z \to y)}} \underbrace{\frac{\operatorname{Project Exame Help}}{\partial \theta_{k,j}^{(z \to y)}}}_{j} \underbrace{\frac{\operatorname{Project Exame Help}}{\partial \theta_{k,j}^{(z \to y)}}}_{k,j} \underbrace{\frac{\operatorname{Project Exame Help}}{\partial \theta_{k,j}^{(z \to y)}}}$$

Similarly, we can also compute the derivative with respect to the hidden units: Add WeChat powcoder

$$\frac{\partial o_j}{\partial z_k} = \theta_{k,j}^{(z \to y)}$$

$$\frac{\partial \ell^{(i)}}{\partial z_k} = \frac{\partial \ell^{(i)}}{\partial o_i} \frac{\partial o_j}{\partial z_k} = (\tilde{y}_j - \delta(j = y^{(i)})) \theta_{k,j}^{(z \to y)}$$

This value will be useful for computing the gradient of the loss function from the inputs to the hidden layer.

Compute the gradient on the input weights $\Theta^{(x \to z)}$

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Apply the old chain rule in differentiation:

Assignment Project Exam Help $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ Assignment Project Exam Help $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$ $\frac{\partial \mathcal{E}_{i}}{\partial z_{k}} = \frac{\partial \mathcal{E}_{i}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}} \frac{\partial z_{k}}{\partial z_{k}}$

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Add $\underline{\underline{W}} = \underline{\underline{\mathcal{C}}} h_{at} = \underline{\underline{p}} \otimes \underline{\underline{w}} c.\underline{\underline{v}} der$

where $f'(\boldsymbol{\theta}_k^{(x \to z)} \cdot \boldsymbol{x})$ is the derivative f the activation function f, applied at the input $\boldsymbol{\theta}_k^{(x \to z)} \cdot \boldsymbol{x}$. Depending on what the actual activation is, the derivative will also be different.

Derivative of the sigmoid activation function

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$$\frac{\partial \ell^{(i)}}{\partial \theta^{x \to z}} = \frac{\partial \ell}{\partial z_k} \sigma \left(\theta_k^{(x \to z)} \cdot \mathbf{x} \right) \left(1 - \sigma \left(\theta_k^{(x \to z)} \cdot \mathbf{x} \right) \right) x_n$$
Assignment Project Exam Help
$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\theta_k^{(x \to z)} \cdot \mathbf{x} \right) \left(1 - \sigma \left(\theta_k^{(x \to z)} \cdot \mathbf{x} \right) \right) x_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) x_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) x_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) x_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

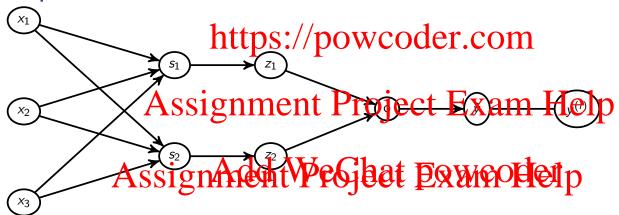
$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

$$= \frac{\partial \ell^{(i)}}{\partial z_k} \sigma \left(\frac{\partial \ell^{(i)}}{\partial z_k} \right) z_k (1 - z_k) z_n$$

- If the negative log-likelihood $\ell^{(i)}$ does not depend much on z_k , then $\frac{\partial \ell^{(i)}}{\partial z_k} \approx 0$. In this case it doesn't matter how z_k is computed, and so $\frac{\partial \ell^{(i)}}{\partial \theta_{n,k}^{\times \to z}} \approx 0$
- If $x_n=0$, then it does not matter how we set the weights $\frac{\partial \ell^{(i)}}{\partial \theta_{n,k}^{x \to z}}$, so $\frac{\partial \ell^{(i)}}{\partial \theta_{n,k}^{x \to z}}=0$

A simple neural network

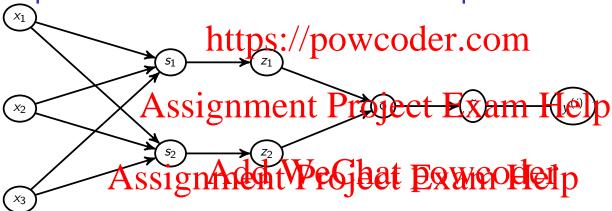


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$$\mathbf{\Theta}^{(x \to s)} = \begin{bmatrix} s_1 \\ \theta_{11}^{x_1} \\ \theta_{21}^{(x \to s)} \end{bmatrix} \begin{bmatrix} s_2 \\ \theta_{12}^{x_2} \\ \theta_{13}^{x_3} \\ \theta_{21}^{(x \to s)} \end{bmatrix}$$

$$oldsymbol{\Theta}^{(z
ightarrow o)} = egin{array}{ccc} z_1 & z_2 \ heta^{(z
ightarrow o)} & heta^{(z
ightarrow o)} \ heta_{11} & heta_{12} \end{array}
brace$$

A simple neural network: forward computation



s₁ =
$$t_{11}^{(x)}$$
 | $t_{12}^{(x)}$ | $t_{12}^{(x)}$ | $t_{12}^{(x)}$ | $t_{13}^{(x)}$ | $t_{13}^{(x)}$

Note: When making predictions with the sigmoid function, choose the label 1 if $\tilde{y} > 0.5$. Otherwise choose 0

A simple neural network with cross-entropy sigmoid loss https://powcoder.com

Cross-entropy sigmoid loss Project Exam Help

$$\mathcal{L}_{H(p,q)} = -\sum_{j} p_{j} \log q_{i} = -y \log \tilde{y} - (1-y) \log(1-\tilde{y})$$
Assignment Project PawroHelp

https://powcoder.com $y \in \{0,1\}$ is the true label

- ▶ ỹ is the predated whe Chat powcoder
- ▶ If the true label is 1, loss is $-\log(\tilde{y})$. Loss is bigger if \tilde{y} is smaller
- ▶ If the true label is 0, loss is $-\log(1-\tilde{y})$. Loss is bigger if \tilde{y} is bigger

A simple neural network: Compute the derivatives https://powcoder.com

$$\frac{\partial \mathcal{L}}{\partial o} \stackrel{\textbf{Assignment Project Exam Help}}{\underbrace{\frac{\partial o}{\partial s_{11}} = \theta_{11}^{(z \to o)} + \theta_{12}^{o}}} \stackrel{\textbf{Assignment Project Exam Help}}{\underbrace{\frac{\partial o}{\partial \theta_{11}^{(z \to o)}} = z_{1}}} \stackrel{\textbf{Assignment Project Exam Help}}{\underbrace{\frac{\partial o}{\partial \theta_{11}^{(z \to o)}} = z_{1}}} \stackrel{\textbf{Assignment Project Exam Help}}{\underbrace{\frac{\partial o}{\partial \theta_{11}^{(z \to o)}} = z_{1}}} \stackrel{\textbf{Assignment Project Exam Help}}{\underbrace{\frac{\partial o}{\partial \theta_{11}^{(z \to o)}} = z_{1}}} = z_{2}$$

$$\frac{\partial o}{\partial \theta_{11}^{(z \to o)}} = z_{1} - \frac{\partial o}{\partial \theta_{12}^{(z \to o)}} = z_{2} - \frac{\partial o}{\partial \theta_{13}^{(z \to o)}} = z_{3}$$

$$\frac{\partial s_{2}}{\partial \theta_{21}^{(x \to s)}} = z_{1} - \frac{\partial s_{2}}{\partial \theta_{22}^{(x \to s)}} = z_{2} - \frac{\partial s_{2}}{\partial \theta_{23}^{(x \to s)}} = z_{3}$$

Compute the derivatives on the weights $\Theta^{z\to o}$ https://powcoder.com

Assignment Project Exam Help Apply the chain rule:

Assignment Property Example Ip $\frac{\partial \theta^{(z \to o)}}{\partial \theta^{(z \to o)}} = \frac{\partial \phi}{\partial o} \frac{\partial \phi^{(z \to o)}}{\partial \phi^{(z \to o)}} = (\tilde{y} - y)z_1$ $\frac{\partial \theta^{(z \to o)}}{\partial z} = \frac{\partial \phi}{\partial o} \frac{\partial \phi}{\partial z} = (\tilde{y} - y)z_2$ Add We Chat powcoder

Compute derivatives with respect to the weights $\Theta^{x \to s}$

 $\frac{\partial \mathcal{L}}{\partial \theta_{11}^{(x \to s)}} = \frac{\partial \mathcal{L}}{\partial \mathbf{c}} \frac{\partial o}{\partial \mathbf{c}} \frac{\partial z_1}{\partial \mathbf{c}} \frac{\partial s_1}{\partial \mathbf{c}} = (\tilde{y} - y)\theta_{11}^{(z \to o)} z_1(1 - z_1)x_1$ $\frac{\partial \mathcal{L}}{\partial \theta_{12}^{(x \to s)}} = \frac{\partial \mathcal{L}}{\partial \mathbf{c}} \frac{\partial o}{\partial \mathbf{c}} \frac{\partial z_1}{\partial \mathbf{c}} \frac{\partial s_1}{\partial \mathbf{c}} = (\tilde{y} - y)\theta_{11}^{(z \to o)} z_1(1 - z_1)x_2$ $\frac{\partial \mathcal{L}}{\partial \theta_{12}^{(x \to s)}} = \frac{\partial \mathcal{L}}{\partial \mathbf{c}} \frac{\partial o}{\partial \mathbf{c}} \frac{\partial z_1}{\partial \mathbf{c}} \frac{\partial s_1}{\partial \mathbf{c}} \frac{\partial s_1}{\partial \mathbf{c}} = (\tilde{y} - y)\theta_{12}^{(z \to o)} z_1(1 - z_1)x_2$ $\frac{\partial \mathcal{L}}{\partial \theta_{13}^{(x \to s)}} = \frac{\partial \mathcal{L}}{\partial \mathbf{c}} \frac{\partial o}{\partial \mathbf{c}} \frac{\partial z_1}{\partial \mathbf{c}} \frac{\partial s_1}{\partial \mathbf{c}} \frac{\partial s_1}{\partial \mathbf{c}} = (\tilde{y} - y)\theta_{12}^{(z \to o)} z_1(1 - z_1)x_3$ $\frac{\partial \mathcal{L}}{\partial \theta_{21}^{(x \to s)}} = \frac{\partial \mathcal{L}}{\partial \mathbf{c}} \frac{\partial o}{\partial \mathbf{c}} \frac{\partial z_2}{\partial \mathbf{c}} \frac{\partial s_1}{\partial \theta_{21}^{(x \to s)}} = (\tilde{y} - y)\theta_{12}^{(z \to o)} z_2(1 - z_2)x_1$ $\frac{\partial \mathcal{L}}{\partial \theta_{23}^{(x \to s)}} = \frac{\partial \mathcal{L}}{\partial o} \frac{\partial o}{\partial z_2} \frac{\partial z_2}{\partial s_2} \frac{\partial s_1}{\partial \theta_{22}^{(x \to s)}} = (\tilde{y} - y)\theta_{12}^{(z \to o)} z_2(1 - z_2)x_2$ $\frac{\partial \mathcal{L}}{\partial \theta_{23}^{(x \to s)}} = \frac{\partial \mathcal{L}}{\partial o} \frac{\partial o}{\partial z_2} \frac{\partial z_2}{\partial s_2} \frac{\partial s_1}{\partial \theta_{23}^{(x \to s)}} = (\tilde{y} - y)\theta_{12}^{(z \to o)} z_2(1 - z_2)x_3$

Vectorizing forward computation

https://powcoder.com

$$s = \Theta^{(x-A)} \underbrace{signatent}_{\theta_{21}^{(x\to s)}} \underbrace{\theta_{22}^{(x\to s)} \theta_{23}^{(x\to s)}}_{\theta_{23}^{(x\to s)}} \underbrace{x_{2}^{(x\to s)}}_{x_{2}} \underbrace{elp}_{x_{3}} \\ + \underbrace{Assignatent}_{\theta_{21}^{(x\to s)}} \underbrace{Power}_{\theta_{22}^{(x\to s)}} \underbrace{Power}_{x_{2}^{(x\to s)}} \underbrace{p}_{x_{3}^{(x\to s)}} \\ = \underbrace{\theta_{11}^{(1)} x_{1} + \theta_{12}^{(x\to s)} x_{2} + \theta_{13}^{(x\to s)} x_{3}}_{\theta_{13}^{(x\to s)}} \underbrace{elp}_{x_{3}^{(x\to s)}} \underbrace{p}_{x_{3}^{(x\to s)}} \underbrace{p}_$$

$$\mathbf{z} = \sigma \begin{pmatrix} \begin{bmatrix} s_1 \\ s_2 \end{bmatrix} \end{pmatrix} = \begin{bmatrix} \mathbf{Add} \\ \sigma(s_2) \end{bmatrix} = \begin{bmatrix} \mathbf{add} \\ z_2 \end{bmatrix}$$

$$\mathbf{o} = \mathbf{\Theta}^{(z \to o)} \mathbf{z} = \begin{bmatrix} \theta_{11}^{(z \to o)} & \theta_{12}^{(z \to o)} \end{bmatrix} \times \begin{bmatrix} z_1 \\ z_2 \end{bmatrix} = \begin{bmatrix} \theta_{11}^{(z \to o)} z_1 + \theta_{12}^{(z \to o)} z_2 \end{bmatrix}$$

$$\tilde{y} = \sigma(\mathbf{o})$$

Note: Summing over inputs in forward computation

Backpropagation

https://powcoder.com

When applying the rhaintrifler died the livatives interfequently reused. For example, ∂£ is used to compute the gradient on both Θ^{z→o} and Θ^{x→s} the would be useful to cache them.
 We can only compute the derivatives of the parameters when

We can only compute the derivatives of the parameters when we have all the necessary "inputs" demanded by the chain rule. So careful sequencing is necessary to take advantage of the cached derivatives.

the cached derivatives.
 This combination of sequencing, caching, and differentiation is called backpropagation.

▶ In order to make this process manageable, backpropagation is typically done in vectorial form (tensors)

Elements in a neural network

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- ► Variables includes input x, hidden units z, outputs y, and the loss functions signment Project Exam Help
 - Inputs are not computed from other nodes in the graph. For example in the graph of the feature vector extracted from a training (or test) instance
 - Backpropagation computes gradient of the loss with respect to all variables parent than Wholes and Grobal ates to parameters.
- Parameters include weights and bias. They do not have parents, and and third and then we gradient descent
- Loss is not used to compute any other nodes in the graph, and is usually computed with the predicted label \hat{y} and the true label y(i).

Backpropagation: caching "error signals"

https://powcoder.com

Let D_o represent the gradient of the loss function with respect to o and o and o be the gradient of the loss function with respect to o. Assuming a cross-entropy loss and a sigmoid (which can be genralized to soft Max) function, the error signal at the output o is: o is: o is: o is:

This error signal **part point** (**POINT OCCOMPANNIN** he gradient with respect to $\Theta^{(z \to o)}$

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$$\nabla_{\mathbf{\Theta}^{(z \to o)}} = \mathbf{D_o} \mathbf{z} = \begin{bmatrix} \tilde{y} - y \end{bmatrix} \begin{bmatrix} z_1 & z_2 \end{bmatrix}$$
$$= \begin{bmatrix} (\tilde{y} - y)z_1 & (\tilde{y} - y)z_2 \end{bmatrix}$$

Backpropagation: Computing error signals https://powcoder.com

Using **D**_o, we **Assignment** e **Rrojects gramm the lip**den layer:

Assignment Project Exmonetp

$$\begin{aligned} & \boldsymbol{D_s} = (\boldsymbol{\Theta}^{(z \to o)} \boldsymbol{D_o}) \odot \boldsymbol{F'} \\ & \text{https://powcoder.com} \\ & = \left(\left[\frac{\partial o}{\partial z_1} \quad \frac{\partial o}{\partial z_2} \right] \times \left[\frac{\partial \ell}{\partial o} \right] \right) \odot \left[\frac{\partial z_1}{\partial s_1} \quad \frac{\partial z_2}{\partial s_2} \right] \\ & = \left(\left[\theta_{11}^{(z \to o)} \quad \boldsymbol{Add} \right] \boldsymbol{WeChat} \right) \boldsymbol{powcoder.com} \\ & = \left[(\tilde{y} - y)\theta_{11}^{(z \to o)} z_1 (1 - z_1) \quad (\tilde{y} - y)\theta_{12}^{(z \to o)} z_2 (1 - z_2) \right] \end{aligned}$$

Backpropagation: caching "error signals"

https://powcoder.com

Assignment Project Exam Help Using error signals D_s , we can now compute the gradient on $\Theta^{(x\to s)}$:

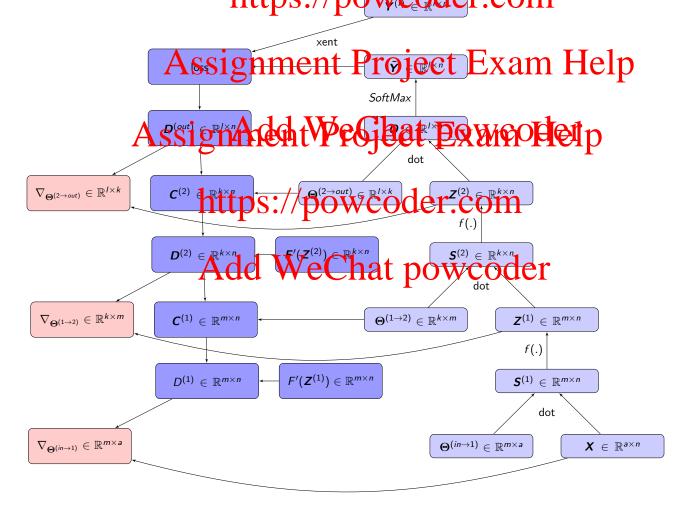
Assign And the Chat Exmontelp

$$\nabla_{\Theta^{(x \to s)}} = \mathbf{D}_{s}^{\top} \mathbf{X}$$

$$= \begin{bmatrix} (\tilde{y} - y)\theta_{11}^{(z \to o)} z_{1} (\mathbf{nttp}) \\ (\tilde{y} - y)\theta_{12}^{(z \to o)} z_{2} (1 - z_{2}) \end{bmatrix} \times \begin{bmatrix} \mathbf{powcoder.com} \\ \mathbf{powcoder.com} \end{bmatrix}$$

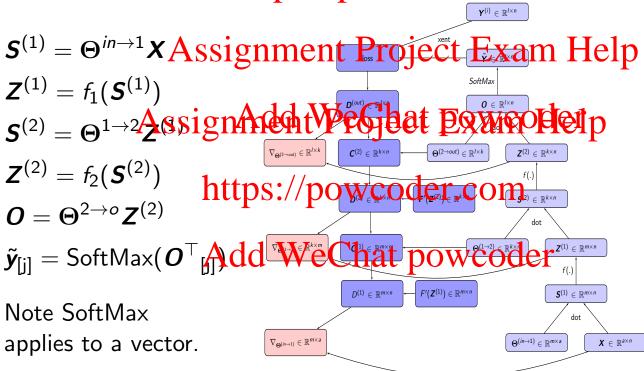
$$= \begin{bmatrix} (\tilde{y} - y)\theta_{12}^{(z \to o)} z_{1} (\mathbf{Addx}_{1} \mathbf{WeChat}^{(z \to o)} \mathbf{powcoder}_{1}^{(z \to o)} \mathbf{powcoder}_{1}^{(z \to o)} z_{1} (1 - z_{1})x_{3} \\ (\tilde{y} - y)\theta_{12}^{(z \to o)} z_{2} (1 - z_{2})x_{1} & (\tilde{y} - y)\theta_{12}^{(z \to o)} z_{2} (1 - z_{2})x_{2} & (\tilde{y} - y)\theta_{12}^{(z \to o)} z_{2} (1 - z_{2})x_{3} \end{bmatrix}$$

Computation graph of a three-layer feedforward neural network https://powcoder.com



Forward computation in matrix form

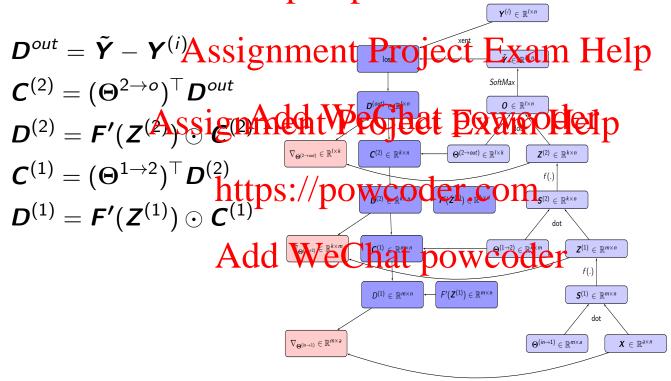
https://powcoder.com



Matrix multiplication in forward computation sums over inputs, hidden units. We assume the input and hidden units in batches

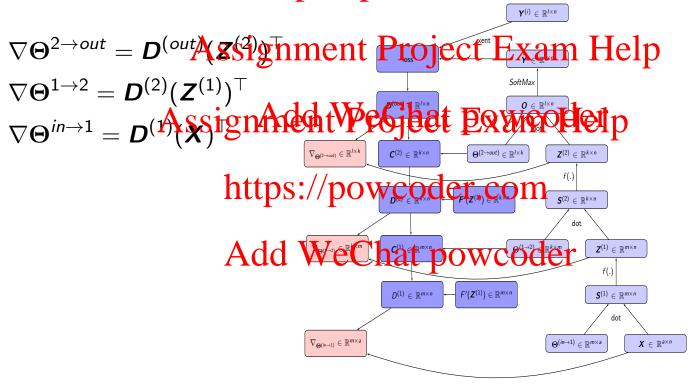
Backpropagation: Computing error signals

https://powcoder.com



Matrix multiplication in error signal computation involves summing over outputs and hidden units.

Backpropagation: Compute the gradient with error signals https://powcoder.com



Matrix multiplication when computing gradient sums over instances in mini-batch.

Notes in backpropagation

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Assignment/Peoplet Exmodelp

Where does caching take place?

- ► Why is sequenting in potent oder.com
- What computation patterns can you observe?

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Pay attention to what you sum over

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- In forward computation, you sum over all inputs (feature vector) for each put the possible possibl
- In backward computation, you sum over the gradient of all outputs for property powcoder.com
- When you compute the gradient for the weights, you sum over the gradient for the gradient for the weights.
- Make sure you line up the columns of the first matrix and the rows of the second matrix. That's what you sum over.

Automatic differentiation software

https://powcoder.com

- Backpropagation mental conjecte Exame Help everyone to repeat the same work
- Curre Als Signy accent Project Land College Pibraries exist, e.g., Torch (PyTorch), MXNet, TensorFlow
- Using these **Interies**, upossing deal. Cospecify the forward computation, and the gradient can be computed automatically these vibrates happeacelord test research and development in deep learning considerably.
- Libraries that support dynamic computation graphs are better suited for many NLP problems.

https://powcoder.com Assignment Project Exam Help

Assignment/Peoplet Example1p
Bells and whistles in neural net training
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Tricks in training neural networks

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There are various tricks that people use when training neural networks: Assignment/Project Example p

- Regularization: Adjusting the gradient
- Dropout: Adjusting the hidden units
- Optimization methods: Adjusting the learning rate Add Wechal powcoder
- Initialization: Using particular forms of initialization

Regularization

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Neural networks can be regularized in a similar way as linear models. Neural networks can also with **Frobenius norm**, which is a trivial extension to L2 norm for matrices. In fact, in many cases it is just referred to as regularization.

$$\mathcal{L} = \sum_{i=1}^{N} \frac{\text{https://powcoder.com}}{\text{Add}} \mathbb{E}^{(i)} + \lambda_{x \to z} \|\Theta^{(z \to y)}\|_F^2 + \lambda_{x \to z} \|\Theta^{(x \to z)}\|_F^2$$

where $\|\Theta\|_F^2 = \sum_{i,j} \theta_{i,j}^2$ is the squred **Frobenius norm**, which generalizes the L_2 norm to matrices. The bias parameters b are not regularized, as they do not contribute to the classifier to the inputs.

L2 regularization

Compute the gradient of ploss with 12 regularization

Assignment Project Exam Help
$$\frac{\partial \theta}{\partial \theta} = \sum_{i} \frac{\partial \theta}{\partial \theta} + \lambda \theta$$
 Assign Additive State Example 1p

► Update the **httgn** // powcoder.com

$$Add \underline{W}_{\theta} \underline{e}Ch(\underbrace{\underbrace{\sum_{i=1}^{N} p_{\theta}(i)}_{\partial \theta} c_{i}d_{\theta}}_{i})$$

- "Weigh decay factor": λ is a tunable hyper parameter that pulls a weight back when it has become too big
- ▶ Question: Does it matter which layer θ is from when computing the regularization term?

L1 regularization

L1 regularization the s://powcoder.com

Assignment Project Exam Help
$$\mathcal{L} = \sum \ell^{(i)} + \lambda_{z \to y} \| \boldsymbol{\Theta}^{(z \to y)} \|_1 + \lambda_{x \to z} \| \boldsymbol{\Theta}^{(x \to z)} \|_1$$
 Assignment Project Exam Help
$$\mathcal{L} = \sum \ell^{(i)} + \lambda_{z \to y} \| \boldsymbol{\Theta}^{(z \to y)} \|_1 + \lambda_{x \to z} \| \boldsymbol{\Theta}^{(x \to z)} \|_1$$

Compute the gradient

https://powcoder.com
$$Add = \sum_{i=1}^{\partial \mathcal{L}} \frac{\partial \ell^{(i)}}{\partial \theta} + \lambda \operatorname{sign}(\theta)$$
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update the weights

$$\theta = \theta - \eta \left(\sum_{i=1}^{N} \frac{\partial \ell^{(i)}}{\partial \theta} + \lambda \operatorname{sign}(\theta) \right)$$

Comparison of L1 and L2

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- When A saign are the Head and a saign and the weight much less than L2 regularization shrinks the weight much less than L2 regularization shrinks the weight much more than L2 regularization and WeChat powcoder
 The net result is that L1 regularization tends to concentrate
- ► The net result is that L1 regularization tends to concentrate the weight of the network in a relatively small number of high-importance connections, while the other weights are driven toward zero. So L1 regularization effectively does feature selection.

Dropout

https://powcoder.com

Assignment Project Exam Help

Nandans is protected and the provent over-reliance on a few features or hidden units, or feature co-adaptation power features are not useful when working together with a few other features. The ultimate goal is to avoid over litting eChat powcoder

Dropout

https://powcoder.com
Dropout can be achieved using a mask:

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Assignment Project Exam Help

Assignment Project Exam Help

$$\tilde{z}^{(1)} = m^{1} \odot z^{(1)}$$
 $\tilde{z}^{(2)} = m^{1} \odot z^{(1)}$
 $m^{2} \sim Bernouli(r^{2})$

Add $\tilde{z}^{(2)} = m^{2} \odot z^{(2)}$

where m^1 and m^2 are mask vectors. The values of the elements in these vectors are either 1 or 0, drawn from a Bernouli distribution with parameter r (usually r=0.5)

Optimization methods

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Assignment Project Exam Help

- Momentssignment Pegleat Exmentelp
- Adgrad
- https://powcoder.com

 Root Mean Square Prop (RMSProp)
- Adam Add WeChat powcoder

Momentum

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Assignment Project Exam Help At each timestep t, compute ∇_{Θ} and , and then compute the momentum as follows: Assignment Project Exam Help and , and then compute the Assignment Project Exam Help and , and then compute the momentum as follows:

https://powcoderedom $\Theta = \Theta - V_t$

Add WeChat powcoder
The momentum term increases for dimensions whose gradient
point in the same directions and reduces updates for dimensions
whose gradient change directions.

Adgrad

https://powcoder.com

Assignment Project Exam Help Weight and bias update for Adgrad at each time step t:

Assign And the Spanning Assign And Assign An

$$\mathbf{V}_{\nabla_{\Theta}} = \mathbf{V}_{\nabla_{\Theta}} + \nabla_{\Theta}^{2}$$
https://powcoder.com
$$\Theta = \Theta - \eta \frac{\sqrt{\mathbf{V}_{\nabla_{\Theta}} + \epsilon}}{\sqrt{\mathbf{V}_{\nabla_{\Theta}} + \epsilon}}$$
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e.g.,
$$\epsilon=10^{-8}$$

Root Mean Square Prop (RMSProp)

https://powcoder.com

Assignment Project Exam Help Weight update for RMSprop at each time step t:

Assign And the Spanning Assign And Assign An

$$S_{\nabla_{\Theta}} = \beta S_{\nabla_{\Theta}} + (1 - \beta) \nabla_{\Theta}^{2}$$

https://powcoder.com
 $\Theta = \Theta - \eta \frac{\sqrt{S_{\nabla_{\Theta}} + \epsilon}}{\sqrt{S_{\nabla_{\Theta}} + \epsilon}}$
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e.g.
$$\beta = 0.9, \eta = 0.001, \epsilon = 10^{-8}$$

Adaptive Moment Estimation (Adam)

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Weight update at time step t for Adam:

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Adam combines Momentum and RMSProp

Define a neural net

```
from torch impress: powcoder.com
class Net(nn. Module):
   def __init__(self, in_dim=25, out_dim=3, batch_
      super (Net self) in it (). Assignment Project Pawordelp
        self.out_dim = out_dim
        selfhttps://powcoline.oomelf.in_dim, self.o
        self.softmax = nn.Softmax(dim=1) \#softmax o
   Add WeChat powcoder def forward(self, input_matrix):
       logit = self.linear(input_matrix)
       return logit #return raw score, not normali
   def xtropy_loss(self, input_matrix, target_labe
        loss = nn. CrossEntropyLoss()
        logits = self.forward(input_matrix)
       return loss(logits,target_label_vec)
```

Use optimizers in Pytorch

```
import torch.optimttps://powcoder.com
net = Net(input_dim , output_dim)
optimizer = Apting Adament Projecte Examt Help)
for epoch in range (epochs):
    total_nll = 0
    for batch in the control by the offer pe ):
        optimizer.zero_grad() #zero out the gradient.
        vectorized = ,vectorize_batch(batch, feat_index, label
        feat_vectorized)
        label_vec = map(itemgetter(1), vectorized)
        feat_listde Wist Chat powcoder
        x = torch. Tensor(feat_list)
        y = torch.LongTensor(label_list)
        loss = net.xtropy_loss(x,y)
        total_nll += loss
        loss.backward()
        optimizer.step()
    torch.save(net.state_dict(), net_path)
```

https://powcoder.com Assignment Project Exam Help

Assignment Peoplet Example of People Sparse and Dense embeddings as input to neural networks

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Input to feedforward neural networks

- Assuming a bag-of-words model, when the input x is the count of each word (feature) x_i .
- To compute the hidden unit z_k :
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Assignment $Z_k = \sum_{j,k} \theta_{j,k}^{x \to z} x_j$

- The connections from word j to each of the hidden units z_k form a vector z_k form a vector z_k as the embedding of word j.
- If there is a Atom the same network as the classification task.
- Word embeddings can also be learned separately from unlabeled data, using techniques such as Word2Vec and GLOVE.
- ➤ The latest trend is to learn *contextualized* word embeddings which are computed dynamically for each classification instance (e.g., ELMO, BERT). The requires more advanced architectures (Transformers) that we will talk about later in

One-hot encodings for features

https://powcoder.com

A one-hot encoding some invalid per dimension desponds to a unique feature, and the resulting feature vector of a classification instance can be it presented to be invalidately per an analysis of the period of th

Example

When considering acting words at presented of 40000 words. A short document of 20 words will be represented with a very sparse 40000-dimensional vector in which at most 20 dimensions have non-zero values

Combination of sparse vectors

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 $\begin{bmatrix} 0 & 1 & 0 & 1 & 0 & 0 & 1 & 0 \end{bmatrix}$

Sparse vs Dense representations

- Sparse representations://powcoder.com
 - Each feature is a sparse vector in which one dimension is 1 and the respective of one-hot vector is same as number of distinct

features

feature "word is 'dog' " is as dissimilar to "word is 'thinking' "

as it is to "yord is to wooder.com

Features for one classifying instance can only combined by summation.

- ► Dense representation We Chat powcoder
 - ightharpoonup Each feature is a d-dimensional vector, with a d that is generally much shorter than that of a one-hot vector.
 - Model training will cause similar features to have similar vectors - information is shared between similar features.
 - Features can be combined via summation (or averaging), concatenation, or some combination of the two.
 - Concatenation if we care about relative position.

Using dense vectors in a classifier

https://powcoder.com

Each core feature is embedded into a d dimensional space (typically 50-300), and the presented great great and the presented great g

- Extract a set of core linguistic features f_1, \dots, f_k that are relevant Soi grandeing the coupled p
- For each feature f_i of interest, retrieve the corresponding vector v_i . https://powcoder.com
- Combine the vectors (either by concatenation, summation, or a combination deboty) einth at ipouvectors.
 - Note: concatenation doesn't work for variable-length vectors such as document classification
- Feed x into a nonlinear classifier (feed-forward neural network).

Relationship between one-hot and dense vectors

https://powcoder.comDense representations are typically pre-computed or pre-trained word embeddings roject Exam Help

One-hot and dense representations may not be as different as

- one might think. Assignment People Equipolities and the state of the s neural network amounts to dedicating the first layer of the network to learning a dense embedding vector [for each feature based on training data.
- With task-specific word embedding, the training set is typically smaller, but the training objective for the embedding and the task objective are one and same
- With pre-trained word embeddings, the training data is easy to come by (just unannotated text), but the embedding object and task objective may diverge.

Two approaches of getting dense word vectors https://powcoder.com

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- Semanio Signal (VSM)
- Predictive methods, originating from the neural network community, aimposat/producing distributed Representations for words, commonly known as word embeddings
 - Distributed word representations were initially a by-product of neural language models and later became a separate task on its own

Distributional semantics

https://powcoder.com

- Based on the same context (Harris, 1954)
- Further summarized the company it keeps." (J. R. Firth, 1957)
- Each word is represented as a sparse vector in a high-dimensional space
- ► Then word distances and similarities can be computed with such a matrix

Steps for building a distributional semantic model https://powcoder.com

- Preproces a significant specific to be prepried to be prepried to be presented to be presented
- Define the i general to the target term, terms that are syntactically related to the target term (subject-of, object-of, etc.).
- Compute a tarm-context matrix where each row corresponds to a term and each column corresponds to a context term for the target term.
- Each target term is then represented with a high-dimensional vector of context terms.

Mathematical processing for building a DSM

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Weight the term-context matrix with association strength metrics such as Positive Poptwise Mural deformation (PPMI) to correct frequency bias

Assignment Pechat Example 1p
$$max(\log \frac{p(x)p(y)}{p(x)p(y)}, 0)$$

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Its dimensionality can also be reduced by matrix factorization techniques such as singular value decomposition (SVD)

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$$m{A} = m{U} m{\Sigma} m{V}^{m{T}}$$

 $m{A} \in \mathbb{R}^{m \times n}, m{U} \in \mathbb{R}^{m \times k}, m{\Sigma} \in \mathbb{R}^{k \times k}, m{V} \in \mathbb{R}^{n \times k}, n >> k$

► This will result in a matrix that has much lower dimension but retains most of the information of the original matrix.

Predictive methods

- https://powcoder.com
 Learns word embeddings from large naturally occurring text, using various language model objectives.

 Assignment Project Exam Help
 Decide on the context window
- Define the objective function that is used to predict the context words based on the target word or predict the target
- word based on context

 https://powcoder.com

 Train the neural network
- The resulting weight matrix will serve as the vector representation for the target word
- "Don't count, predict!" (Baroni et al, 2014) conducted systematic studies and found predict-based word embeddings outperform count-based embeddings.
- One of popular early word emdeddings are Word2vec embeddings.

Word2vec

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Word2vec is a software package that consists of two main

Word2vec is a software package that consists of two main models: CBOW (Continuous Bag of Words) and Skip-gram.
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- It popularized the use of distributed representations as input to neural networks in natural language processing, and inspired many follow-on works, e.g., ECVE, ELMO, BERT, XLNet)
- It has it roots in language modeling (the use of window-based context to predict the target word), but gives up the goal of getting good language models and focus instead on getting good word embeddings.

Understanding word2vec: A simple CBOW model with

only one context ward in put $\mathbf{x} \in \mathbb{R}^V$ is a one-hot vector where $x_k = 1$ and $x_{k'} = 0$ for $k' \neq k$. $\Theta \in \mathbb{R}^{N \times V}$ is the weight matrix from the input layer to the hideen layer. Each column of Θ is an N-dimensional vector representation \mathbf{v}_w of the associated word Assagnate Project Project

 $\begin{array}{c} \textbf{https://powcoder.com} \\ \blacktriangleright \ \Theta' \in \mathbb{R}^{V \times N} \ \text{is the matrix from the hidden layer to the output} \end{array}$ layer and \mathbf{u}_{w} Aisthew th con of \mathbf{p}'_{o} A "similarity" score o_{j} for each target word w_{j} and context word w_{i} can be computed as:

$$o_j = \boldsymbol{u}_{w_j}^{ op} \boldsymbol{v}_{w_i}$$

Finally we use softmax to obtain a posterior distribution

$$p(w_j|w_i) = y_j = \frac{exp(o_j)}{\sum_{j'=1}^{V} exp(o_{j'})}$$

where y_i is the output of the j-th unit in the output layer

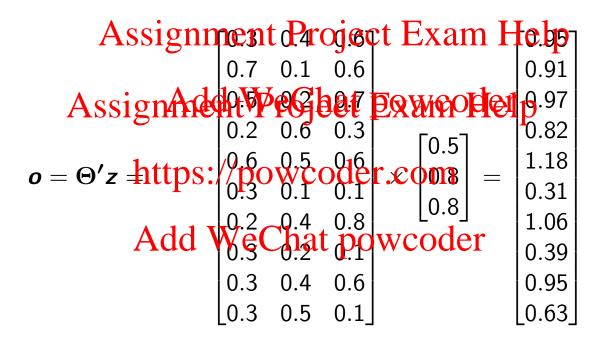
Computing the hidden layer is just embedding lookup

Hidden layer computations: retrieves conder.com

Note there is no activation at the hidden layer (or there is a linear activation function), so this is a "degenerate neural network".

Computing the output layer

https://powcoder.com



Each row of Θ' correspond to vector for a target word w_j .

Taking the softmax over the output

https://powcoder.com

The output \mathbf{y} is a probabilistic distribution over the entire vocabulary.

Input vector and output vector

https://powcoder.com

Assignment Project Exam Help Since there is no activation function at the hidden layer, the output is really just the dot product of the vector of the input context workship the state of the vector of the input context workship the state of the vector of the input context workship the state of the vector of the input context workship the state of the vector of the input context workship to the vector of the v

$$p(w_j|w_i) = y_j = \frac{exp(o_j)}{\sqrt{eCekp(e_j)}} = \frac{exp(\mathbf{u}_{w_j}^\top \mathbf{v}_{w_i})}{\sqrt{eCekp(e_j)}}$$

$$Add \sqrt{eCekp(e_j)} = \sqrt{exp(\mathbf{u}_{w_j}^\top \mathbf{v}_{w_i})}$$

where \mathbf{v}_{w_i} from $\mathbf{\Theta}$ is the **input vector** for word w_i and \mathbf{u}_{w_j} from $\mathbf{\Theta'}$ is the **output vector** for word w_i

Computing the gradient on the hidden-output weights

Use the familiaheross entropy loss der.com

where Assign and the target power Help

• Given y_j is the output of a softmax function, the gradient on the output is the output of a softmax function, the gradient on the output is the output of a softmax function, the gradient on the output is the output of a softmax function, the gradient on the output of a softmax function.

Add We Chat powcoder
$$\frac{\partial \mathcal{L}}{\partial \theta'_{ii}} = \frac{\partial \mathcal{L}}{\partial o_j} \frac{\partial o_j}{\partial \theta'_{ii}} = (y_j - t_j)z_i$$

▶ Update the hidden→output weights

$$\theta'_{ii} = \theta'_{ii} - \eta(y_j - t_j)z_i$$

Updating input→hidden weights

- Compute the error at the hidden layer https://powcoder.com $\frac{\partial \mathcal{L}}{\text{Assign in ento-Project Exam}} \stackrel{\vee}{\text{Exam}} \frac{\partial \mathcal{L}}{\text{Help}}$
- Since Assign Add We Gleat Exmontelp

The derivative of \mathcal{L} on the input—hidden weights: Add WeChat powcoder

$$\frac{\partial \mathcal{L}}{\partial \theta_{ik}} = \frac{\partial \mathcal{L}}{\partial z_i} \frac{z_i}{\theta_{ik}} = \sum_{j=1}^{IV} (y_j - t_j) \theta'_{ji} x_k$$

▶ Update the input→hidden weights

$$\theta_{ki} = \theta_{ki} - \eta \sum_{j=1}^{V} (y_j - t_j) \theta'_{ij} x_k$$

Gradient computation in matrix form

https://powcoder.com

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Computing the errors at the hidden layer

https://powcoder.com

 $D_z = D_o^{\top} \Theta' = Assignment Project Exam Help$

```
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[0.110]
                                                       [080.0]
     0.106
      0.4
      0.1
           0.6
           0.7 https://powcoder.com
      0.2
  0.5
      0.6
           0.3
           0.6
      0.5
              Add We Chat powcoder
      0.1
      0.4
          0.8
           0.1
      0.2
           0.6
      0.4
      0.5
           0.1
```

Computing the updates to Θ'

https://powcoder.com

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Computing the update to Θ

CBOW for multiple context words

https://powcoder.com
$$z = \frac{1}{M}\Theta(x_1 + x_2 + \cdots x_M)$$
Assignment Project Exam Help
$$= \frac{1}{M}(\mathbf{v}_{w_1} + \mathbf{v}_{w_2} + \cdots + \mathbf{v}_{w_M})$$

where M is the number of words in the context, w_1, w_2, \cdots, w_M are the words in the context and \mathbf{v}_w is an input vector. The loss function is https://powcoder.com function is

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$$E = -\log p(w_j|w_1, w_2, \cdots, w_M)$$

$$= -o_{j^*} + \log \sum_{j'=1}^{V} \exp(o_{j'})$$

$$= -\boldsymbol{u}_{w_j}^{\top} \boldsymbol{z} + \log \sum_{j'=1}^{V} \exp(\boldsymbol{u}_{w_{j'}}^{\top} \boldsymbol{z})$$

Computing the hidden layer for multiple context words https://powcoder.com

$$z = \Theta x =$$
 Assignment Project Exam Help

During backprop, update vectors for four words instead of just one.

Skip-gram: model

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Assignment P for \overline{P} \overline{P} \overline{P} \overline{P} \overline{P} \overline{P}

where $w_{c,j}$ is the *j*-th word on the *c*-th panel of the output layer, $w_{O,c}$ is the actual *c*-th word in the output context words; w_I is the only input word, $y_{c,j}$ is the output of the *j*-th unit on the *c*-th panel of the output layer, $o_{c,j}$ is the left input of the *j*-th unit on the *c*-th panel of the output layer.

$$o_{c,j} = o_j = \boldsymbol{u}_{w_i} \cdot \boldsymbol{z}$$
, for $c = 1, 2, \dots, C$

Skip-gram: loss function

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Assignment Project Exam Help
$$\mathcal{L} = -\log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Assignment Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

Add WeChat power Godern Project Exam Help $\sum_{c=1}^{C} \log p(w_{O,1}, w_{O,2}, \cdots, w_{O,C}|w_I)$

where j_c^* is the index of the actual c-th output context word.

Combine the loss of C context words with multiplication. Note: $o_{j'}$ is the same for all C panels

Skip-gram: updating the weights

We take the derivative of powith regard to the net input of every unit on every panel of the output layer, $o_{c,j}$, and obtain

Assignment Project Exam Help
$$e_{c,j} = \frac{1}{\partial o_{c,j}} = y_{c,j} - t_{c,j}$$

Assignment Project Example p which is the prediction error of the unit.

We define a Midimensional vectore \overline{F} . \overline{C} \overline{C} \overline{C} \overline{C} \overline{C} \overline{C} as the sum of the prediction errors of the context word: $E_j = \sum_{c=1}^C e_{c,j}$

Add WeChat powcoder
$$\frac{\partial \mathcal{L}}{\partial \theta'_{ji}} = \sum_{c=1}^{c} \frac{\partial \mathcal{L}}{\partial o_{c,j}} \cdot \frac{\partial o_{c,j}}{\partial \theta'_{ji}} = E_j \cdot z_i$$

▶ Updating the hidden→output weight matrix:

$$\theta'_{ji} = \theta'_{ji} - \eta \cdot E_j \cdot z_i$$

No change in how the input→hidden weights are updated.

Optimizing computational efficiency

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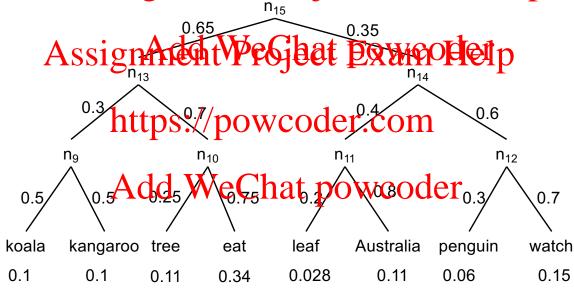
Assignment Project Exam Help

- Computing softmax at the output layer is expensive. It involves iterative of the continuous involves involve
- Two methods for optimizing computational efficiency
 - Hierarchical softmax: an alternative way to compute the probability of a word that reduces the computation complexity from |V| to $\log |V|$.
 - Negative ship in that propusing the weights for all the words in the vocabulary, only sample a small number of words that are not actual context words in the training corpus

Hierarchical softmax

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Computing the probabilities of the leaf nodes https://powcoder.com

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P("Kangargo"|z) A Red (VFFE) to the p(Right|z)

https://powcoder.com $P_n(Right|z) = 1 - P_n(Left|z)$ Add Chat powcoder

where γ_n is a vector from a set of new parameters that replace Θ

Huffman Tree Building

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A simple algorighment Project Exam Help

- Prepare a collection of *n* initial Huffman trees, each of which is a single leaf model two telephone participates organized by weight (frequency).
- Remove the first two trees (the ones with lowest weight). Join these two trees to create a new tree whose root has the two trees as children, and whose weight is the sum of the weights of the two children trees. Put this new tree into the priority queue.
- Repeat steps 2-3 until all of the partial Huffman trees have been combined into one.

Negative sampling

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Computing softmax now the recipied part of particles a small sample of (context) words at a time particle particle.
 Given a pair of words (w, c), let P(D = 1|w, c) be the

Given a pair of words (w, c), let P(D = 1|w, c) be the probability of the pair of words came from the training corpus, and P(D = 0|w, c) be the probability that the pair did not come from the corpus.

come from the corpus.

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This probability can be modeled as a sigmoid function:

$$P(D=1|w,c) = \sigma(\mathbf{u}_w^{\top}\mathbf{v}_c) = \frac{1}{1+e^{\mathbf{u}_w^{\top}\mathbf{v}_c}}$$

New learning objective for negative sampling

We need a new objective for negative sampling, which is to minimize the following loss function:

Assignment
$$P_{w_j \in D'}$$

$$w_j \in D$$

$$w_j \in D'$$

$$w_j \in D'$$

$$where Sign Polyton Correct Context Polyton Pairs and D'$$

is a set of incorrect context - target word pairs.

- Note that white the power policy camples as well as negative samples. In the skip-gram algorithm, there will be multiple position of the compatibility of the compa algorithm, there will be only one positive target word.
- The derivative of the loss function with respect to the output word will be:

$$\frac{\partial \mathcal{L}}{\partial o_{w_i}} = \sigma(o_{w_j}) - t_{w_j}$$

where $t_{w_j}=1$ if $w_j\in D$ and $t_{w_j}=0$ if $w_j\in D'$

Updates to the hidden→output weights

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Assignment Project Exam Help

$$\frac{\partial \mathcal{L}}{\partial \boldsymbol{\mu}_{\mathbf{powcoder.com}}} = (\sigma(o_{w_j}) - t_{w_j})\boldsymbol{z}$$

When updating the output weights, only the weight vectors for words in the positive sample landwigger sample need to be updated:

Updates to the input—hidden weights

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Computing the grivative of the less function with respect to the hidden layer

Assignment People Example Ip
$$\frac{\partial z}{\partial z} = \sum_{(\sigma(o_{w_j}) - t_{w_j})} \mathbf{u}_{w_j}$$
https://powcoder.com

In the CBOW algorithm, the weights for all input context words will be updated. The target word will be updated.

$$\mathbf{v}_{w_i} = \mathbf{v}_{w_i} - \eta(\sigma(o_{w_i}) - t_{w_i})\mathbf{u}_{w_i}x_i$$

How to pick the negative samples?

If we just randomly pick Pword from a corpus, the probability of any given word w_i getting picked is:

of any given word w_i getting picked is:

Assignment Project Exam Help $p(w_i) = \frac{freq(w_i)}{V}$ Assignment Project Exam Help

More frequent words will be more likely to be picked and this may not be https://powcoder.com

Adjust the formula to give the less frequent words a bit more chance to get picked. Chat powcoder

$$p(w_i) = \frac{freq(w_i)^{\frac{3}{4}}}{\sum_{j=0}^{V} freq(w_j)^{\frac{3}{4}}}$$

▶ Generate a sequence of words using the adjusted probability, and randomly pick $n_{D'}$ words

Use of embeddings: word and short document similarity https://powcoder.com

Word embeddings can be used to compute word similarity with cosine single Project Exam Help

Assignment Per Glad Power Help

- How accurately par they be used to evaluate word embeddings
- They can also de use the compute the similarity of short documents

$$sim_{doc}(D_1, D_2) = \sum_{i=1}^{m} \sum_{j=1}^{n} cos(\mathbf{w_i^1}, \mathbf{w_j^2})$$

Use of embeddings: word analogy

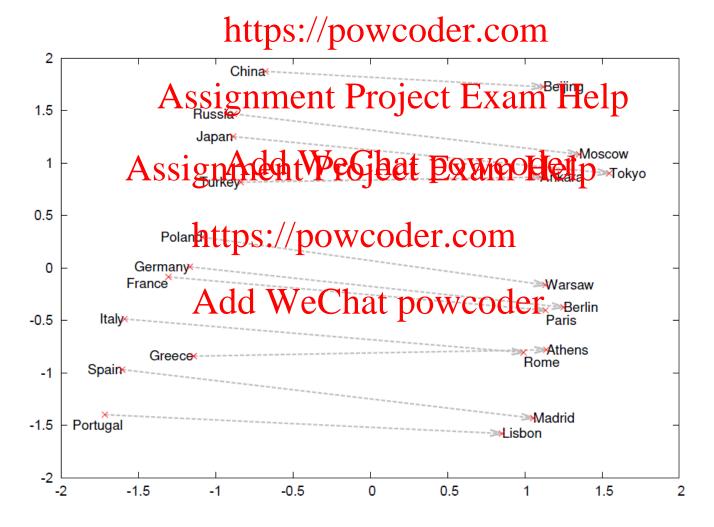
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What's even more impressive is that they can be used to compute Assignment Project Exam Help

Assignment/Project Example Ip analogy
$$(m: w \rightarrow k:?) = \underset{v \in V \setminus m, k, w}{\operatorname{argmax}} cos(\mathbf{v}, \mathbf{k} - \mathbf{m} + \mathbf{w})$$
 analogy $(m: w \rightarrow k:?) = \underset{v \in V \setminus m, k, w}{\operatorname{argmax}} cos(\mathbf{v}, \mathbf{k}) - cos(\mathbf{v}, \mathbf{m})$
$$\underset{v \in V \setminus m, k, w}{\operatorname{Add WeChatspowcoder}}$$

$$analogy(m: w \to k:?) = \underset{v \in V \setminus m, k, w}{\operatorname{argmax}} \frac{\cos(v, k)\cos(v, w)}{\cos(v, m) + \epsilon}$$

Word analogy



Use of word embeddings

https://powcoder.com

- Computing word similarities is not a "real" problem in the eyes of many signment Project Exam Help
- The most important use word embeddings is as input to predict the gillower than the the west applications
- Many follow-on work in develop more effective word embeddings https://pww.coder.com
 - word2vec: http://vectors.nlpl.eu/repository
 - fasttext: https://wfasttext.cc/docs/en/english-vectors.html
 GLOVE: https://nlp.stanford.edu/projects/glove
- Contextualized word embeddings:
 - https://allennlp.org/elmo
 - ► BERT: https://github.com/google-research/bert
 - Roberta: https://pytorch.org/hub/pytorch_fairseq_roberta

Embeddings in Pytorch

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```
In [39]: from torch Acssignment Project Exam Help
        print(embedding)
        input = torch.LongTensor([[1,2,4,5],[4,3,2,9]])
        embedding(input)
                                       Probat PampoHelp
Out[39]: tensor([[[-0.9538,
                        0.3385, -1.6404],
               [ 1.7206, 1.4395, 0.2744],
               [-2.9429, 0.9432, -0.4569],
                        ttps://powcoder.com
              [-2.9429]
               [ 1.2738, 1.1245, 0.6983],
                       1.4395, 0.2744],
               [ 1.7206,
                                1.3246]]], grad_fn=<EmbeddingBackward>)
In [38]: weight = torch.FloatTensor([[1, 2.3, 3], [4, 5.1, 6]3]])
        embedding = nn.Embedding.from pretrained(weight)
        input = torch.LongTensor([0,1,1])
        embedding(input)
Out[38]: tensor([[1.0000, 2.3000, 3.0000],
              [4.0000, 5.1000, 6.3000],
              [4.0000, 5.1000, 6.3000]])
```

Commonly used neural architectures

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- One important aspect of neural network modeling is to figure out the spigned to the part of the part o
- Commonly used architectures
 - Variants of the Recommendation improving many states of the art in NLP
 - Convolutional Networks (CNN), which have been very effective in image processing and some NLP problems (e.g., sentence classification)

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Assignment/Project Exmortelp
Convolutional Networks for text classification
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Convolutional Networks

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A convolutional pretruction is Pasing per to Fidentify Indicators in a large structure, and combine them to produce a fixed size vector representation of the structure with a pooling function, capturing the local aspects that are most informative of the prediction task at hand.

informative of the prediction task at hand.

https://powcoder.com
A convolutional network is not fully connected as a feedforward network is

feedforward network is.

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It has been tremendously successful in image procession (or computer vision), where the input is the raw pixels of an image

In NLP, it has been shown to be effective in sentence classification, etc.

Why it has been so effective in image processing https://powcoder.com

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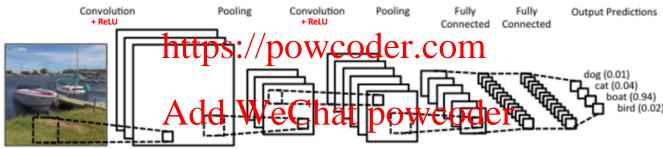
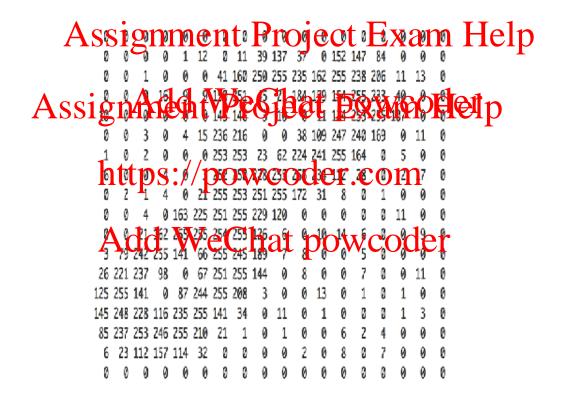


Image pixels



Four operations in a convolutional network https://powcoder.com

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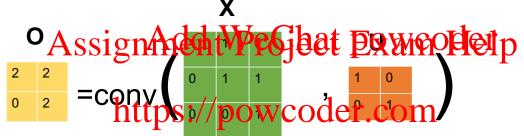
- Conveniesign And the Chat Exmontelp
- Non-linear activation (ReLU)

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 Pooling or subsampling (Max)
- Classification with well connected layer der

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Output "filter" or "feature map" Add Weichat powcoder

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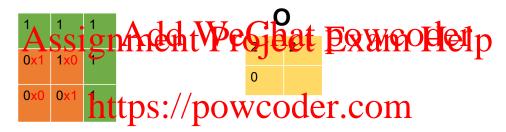
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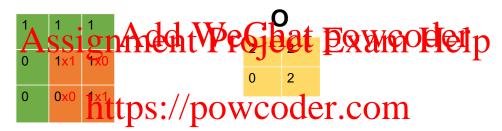
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Forward computation

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Assignated We Ghat Equipole 19

 $\begin{array}{c} o_{12} = x_{12}u_{11} + x_{13}u_{12} + x_{22}u_{21} + x_{23}u_{22} \\ o_{21} = x_{21}u_{11} + x_{22}u_{12} + x_{31}u_{21} + x_{32}u_{22} \end{array}$

O22 Add We Citat powedden 122

ReLU

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- Nonlinear transformation with ReLU

 Assignment/Peoplet Powooffelp

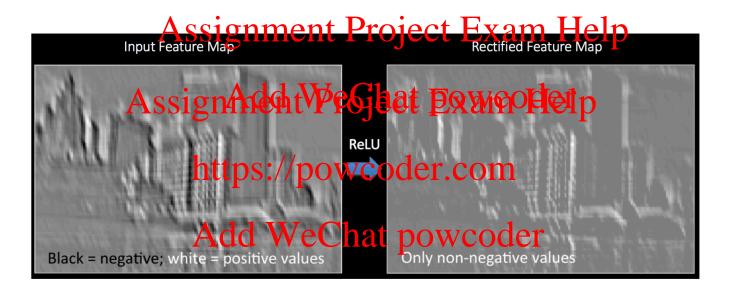
 Output = ReLU(input) = max(0, input)
- As we know, ReLU is an element-wise transformation that does not change the dimension of the feature map
- does not change the dimension of the feature map

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 ReLU replaces all negative pixel values in the featuremap with

 0

Image ReLU



ReLU activation and Max pooling

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ReLU activation is a component-wise function and does not change the same the replect Exam Help

Assignment Project Equipoletp
$$\begin{vmatrix} 2 & 2 \\ 0 & 2 \end{vmatrix} = ReLU \begin{pmatrix} 2 & 2 \\ 0 & 2 \end{pmatrix}$$
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Max pooling does change the dimension of the input. Need to specify the part of this powcoder

$$\begin{bmatrix} 2 \end{bmatrix} = Max \begin{pmatrix} \begin{bmatrix} 2 & 2 \\ 0 & 2 \end{bmatrix} \end{pmatrix}$$
 pool size = (2, 2), strides = 2

Training a CNN

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- Loss fanctions: Area every lost, progred or poss
 What are the parameters of a CNN?
- - The filters (kernels) weight matricies for the feedforward network on top of the convolution and pooling layers, biases
- Computing the gradient for the convolution layers is different from a feedforward neural network...

Computing the gradient on *U*

$$\frac{\partial E}{\partial u_{11}} = \frac{\frac{\partial E}{\partial o_{11}} \frac{\partial o_{11}}{\partial u_{11}} + \frac{\partial E}{\partial o_{12}} \frac{\partial o_{12}}{\partial u_{11}} + \frac{\partial E}{\partial o_{21}} \frac{\partial o_{21}}{\partial u_{11}} + \frac{\partial E}{\partial o_{22}} \frac{\partial o_{22}}{\partial u_{12}} + \frac{\partial E}{\partial o_{22}} \frac{\partial o_{22}}{\partial u_{12}} + \frac{\partial E}{\partial o_{22}} \frac{\partial o_{22}}{\partial u_{12}} + \frac{\partial E}{\partial o_{22}} \frac{\partial o_{22}}{\partial u_{21}} + \frac{\partial E}{\partial o_{22}} \frac{\partial o_{22}}{\partial u_{22}} + \frac{\partial E}{\partial o_{22$$

Summing up errors from all outputs that the filter component has contributed to.

Reverse Convolution

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The computation of the gradient on the filter can be vectorized as a reverse convolution:

$$\begin{bmatrix} \frac{\partial E}{\partial u_{11}} & \frac{\partial E}{\partial u_{22}} & \frac{\partial E}{\partial u_{22}} \\ \frac{\partial E}{\partial u_{21}} & \frac{\partial E}{\partial u_{22}} & \frac{\partial E}{\partial u_{22}} \\ \end{bmatrix} = conv \begin{bmatrix} x_{21} & x_{22} & x_{23} \\ x_{21} & x_{22} & x_{23} \\ x_{21} & x_{22} & x_{23} \\ \end{bmatrix}$$

Computing the gradient on X (if this is not the input layer)

$$\frac{\partial E}{\partial x_{11}} = \frac{hetps://powcoder.com}{\partial o_{11}} u_{11} + \frac{\partial o_{12}}{\partial o_{12}} 0 + \frac{\partial e_{12}}{\partial o_{21}} 0 + \frac{\partial e_{22}}{\partial o_{22}} 0$$

$$\underbrace{AssignmentProject}_{\partial x_{12}} Exam Help$$

$$\frac{\partial E}{\partial x_{12}} = \underbrace{\frac{\partial E}{\partial o_{11}} u_{12}^2 + \frac{\partial E}{\partial o_{12}} u_{12}^2 + \frac{\partial E}{\partial o_{21}} u_{11}^2 + \frac{\partial E}{\partial o_{22}} 0}_{\partial E}$$

$$\underbrace{AssignmentProject}_{\partial x_{12}} Exam Help$$

$$\frac{\partial E}{\partial x_{21}} = \underbrace{\frac{\partial E}{\partial v_{21}} u_{21}^2 + \frac{\partial E}{\partial v_{21}} 0 + \frac{\partial E}{\partial v_{22}} u_{11}^1 + \frac{\partial E}{\partial v_{22}} 0}_{\partial E}$$

$$\underbrace{\frac{\partial E}{\partial x_{22}} = \frac{\partial E}{\partial o_{11}} u_{22}^2 + \frac{\partial E}{\partial o_{12}} u_{21}^2 + \frac{\partial E}{\partial o_{21}} u_{12}^2 + \frac{\partial E}{\partial o_{22}} u_{11}}_{\partial v_{12}}$$

$$\underbrace{\frac{\partial E}{\partial x_{23}} = \frac{\partial E}{\partial o_{11}} 0 + \frac{\partial E}{\partial o_{12}} 0 + \frac{\partial E}{\partial o_{21}} u_{21}^2 + \frac{\partial E}{\partial o_{22}} u_{21}^2}_{\partial v_{12}}$$

$$\underbrace{\frac{\partial E}{\partial x_{32}} = \frac{\partial E}{\partial o_{11}} 0 + \frac{\partial E}{\partial o_{12}} 0 + \frac{\partial E}{\partial o_{21}} u_{22}^2 + \frac{\partial E}{\partial o_{22}} u_{21}^2}_{\partial v_{12}}$$

$$\underbrace{\frac{\partial E}{\partial x_{32}} = \frac{\partial E}{\partial o_{11}} 0 + \frac{\partial E}{\partial o_{12}} 0 + \frac{\partial E}{\partial o_{21}} u_{22}^2 + \frac{\partial E}{\partial o_{22}} u_{22}^2}_{\partial v_{12}}$$

$$\underbrace{\frac{\partial E}{\partial x_{32}} = \frac{\partial E}{\partial o_{11}} 0 + \frac{\partial E}{\partial o_{12}} 0 + \frac{\partial E}{\partial o_{21}} u_{22}^2 + \frac{\partial E}{\partial o_{22}} u_{22}^2}_{\partial v_{22}}$$

Full convolution

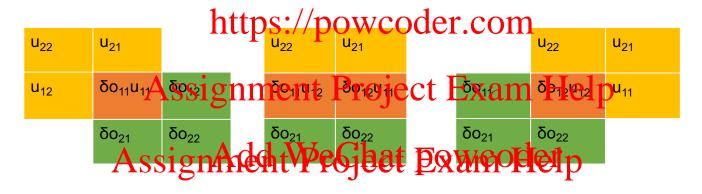
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Assignated type Glat Exmontelp

$$\begin{bmatrix} \frac{\partial E}{\partial x_{11}} & \frac{\partial E}{\partial x_{12}} & \frac{\partial E}{\partial x_{12}} \\ \frac{\partial E}{\partial x_{21}} & \frac{\partial E}{\partial x_{22}} & \frac{\partial E}{\partial x_{22}} \\ \frac{\partial E}{\partial x_{31}} & \frac{\partial E}{\partial x_{32}} & \frac{\partial E}{\partial x_{32}} \end{bmatrix} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{31} \\ \partial x_{31} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{32} \\ \partial x_{32} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{32} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{32} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{32} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{32} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{32} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{32} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{33} \\ \partial x_{33} \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \end{array}} \xrightarrow{\begin{array}{c} \partial E \\ \partial x_{33} \\ \partial x_{3$$

Gradient on X if it is not the inputs



u ₂₂	δο ₁₁ u ₂₁	ohttps://	bury.	onde:	r.cc	7771	X ₁₂	u ₂₁
u ₁₂	δο ₂₁ u ₁₁	Add W	δο ₂₁ u ₁₂	δο ₂₂ u ₁₁	wc	δο ₂₁ Oder	X ₂₂	u ₁₁

	δο ₁₁	δο ₁₂
u ₂₂	δο ₂₁ u ₂₁	δο ₂₂
u ₁₂	u ₁₁	

δο ₁₁	δο ₁₂
δο ₂₁ u ₂₂	δο ₂₂ u ₂₁
u ₁₂	u ₁₁

δο ₁₁	δο ₁₂	
δο ₂₁	δο ₂₂ u ₂₂	u ₂₁
	u ₁₂	u ₁₁

Sample code of 2D convolution with Keras

Why convolutational networks for NLP?

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- Even though bat of the control of the some text classification tasks, they don't account for cases where multiple words combine to create meaning, such as "not interesting".
- The analogy with image processing is if the pixels are treated as separate features. (The analogy might be going too far).

Input to a convolutional network in a text classification task

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The input to a convolutional network can be pretrained word
embeddings (e.g., the weight matrix produced by Word2Vec or
GLOVE¹) and the input sentence:

https://powcoder.com $\mathbf{X}^{(0)} = \mathbf{\Theta}^{(\mathbf{x} \to \mathbf{z})}[\mathbf{e}_{w_1}, \mathbf{e}_{w_2}, \cdots, \mathbf{e}_{w_M}]$ Add We hat powcoder

where e_{w_m} is a column vector of zeros, with a 1 at position w_m , K_e is the size of embeddings

¹https://nlp.stanford.edu/projects/glove

Alternative text representations

- Alternatively sign then the Project telescaped up of word tokens $w_1, w_2, w_3, \cdots, w_M$. This view is useful for models such as **Convolutional Metworks**, or **Convolutional Metworks**, which processes text as a sequence.
- Each word token w_m is represented as a one-hot vector e_{w_m} , with dimension V. The complete document can be represented by the horizontal concatenation of these one-hot vectors: $\mathbf{W} = [e_{w_1}, e_{w_2}, \cdots, e_{w_m}] \in \mathbf{W} \cap \mathbf{W}$
- To show that this is equivalent to the bag-of-words model, we can recover the word count from the matrix-vector product $\mathbf{W}[1,1,\cdots,1]^{\top} \in R^{V}$.

"Convolve" the input with a set of filters

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- A filter is A weight matrix Φ dimension $C^{(k)}$ is the kth filter. Note the first dimension of the filter is the same as the size of the embedding.
 - the same as the size of the embedding.

 In the loage processing, the file doesn't have to cover the full width of the image.
- To merge addition work, we contribe the by sliding a set of filters across it:

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$$X^{(1)} = f(b + C * X^{(0)})$$

where f is an activation function (e.g., tanh, ReLU), b is a vector of bias terms, and * is the convolution operator.

Computing the convolution

- At each position the She parameter k the k-th filter and the compute the element-wise product of the k-th filter and the sequence k-th sequence k-t
- The values of the rection of the the the the test of the computed as:

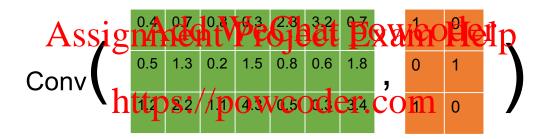
$$\times_{m}^{(1)}$$
 Add $\left(\underbrace{\text{WeChappo}_{k'=1}^{K_e} \underset{n=1}{\overset{h}{\sum}} o_{k'',k''}^{(k)} code_{m+n-1}^{(0)} \right)$

- ▶ When we finish the convolution step, if we have K_f filters of dimension $\mathbb{R}^{K_e \times h}$, then $\boldsymbol{X}^{(1)} \in \mathbb{R}^{K_f \times M h + 1}$
- In practice, filters of different sizes are often used to captured ngrams of different lengths, so $\boldsymbol{X}^{(1)}$ will be K_f vectors of variable lengths, and we can write the size of each vector of h_k

Convolution step when processing text

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Adobites Generoe we o'diter"

Padding

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- To deal with the regime the base matrix is often padded with n − 1 column vectors of zeros at the beginning and end, this is called wide convolution
 If no padding is applied, then the output of each convolution
- If no padding is applied, then the output of each convolution layer will be had units smaller than the input. This is known as narrow convolution.

Pooling

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 After D convolutional layers, assuming filters have identical lengths, we have a representation of the document as a matrix $\mathbf{x}^{(D)}$ Assignment Project Exam Help
- It is very likely that the documents will be of different lengths, so we need to turn them into matricies of the same length before feeding them to a feedward network to perform classification. Add WeChat powcoder
- This can done by **pooling** across times (over the sequence of words)

Prediction and training with CNN

- The CNN needs to be fed into a feedforward network to make a prediction \ddot{y} and compute the loss $\ell^{(r)}$ in training.
- Parameters of a CNN includes the weight matrics for the feedforward betwork and the hitters could be continued in the country of the CNN, as well as the biases.
- The parameters can be updated with backpropagation, which may involve computing the gradient for the max pooling function. Add WeChat powcoder

$$\frac{\partial z_k}{\partial x_{k,m}^{(D)}} = \begin{cases} 1, \ x_{k,m}^{(D)} = \max\left(x_{k,1}^{(D)}, x_{k,2}^{(D)}, \cdots, x_{k,M}^{(D)}\right) \\ 0, \ \text{Otherwise} \end{cases}$$

Different pooling methods

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Max pooling

Average pochttps://powcoder.com

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$$\sum_{z_k = M}^{\infty} \sum_{m=1}^{\infty} x_{k,m}^{\infty}$$

A graphic representation of a CNN

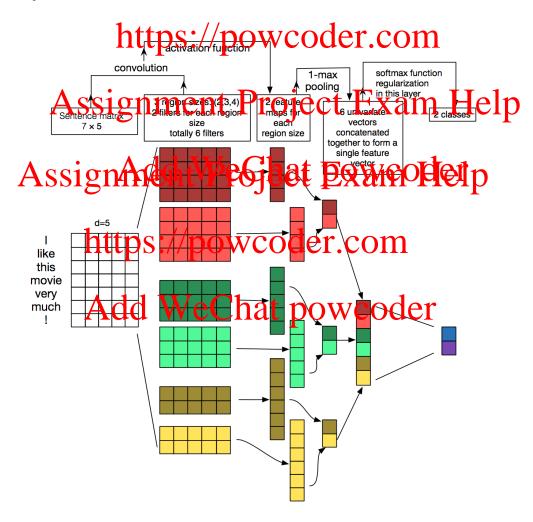


Figure 1: Caption

Sample code of convolution with Keras

An Interim Summary of Supervised Learning Methods

- https://powcoder.comIn all the linear and non-linear models we have discussed so far, we assume we have labeled training data where we can perform supervised learning.
 - ightharpoonup a **training set** where you get observations x and labels y;
 - ► aAessigundentMost partbeathens Help
- A summary of the supervised learning models we have discussed soffetps://powcoder.com
 - Linear models: Naïve Bayes, Logistic Regression, Perceptron,
 - Support Vegter Machines

 Non-linear models: feed-forward networks, Convolutional **Networks**
 - Sparse vs dense feature representations as input to classifiers
- Given sufficient amounts of high-quality data, supervised learning methods tend to produce more accurate classifiers than alternative learning paradigms

NLP problems that can be formulated as simple text classifications https://powcoder.com

- An NLP problem can be formulated as a simple text classification if there is no inter-dependence between the labels Avs sifeth Ades il labels Avs sifeth
 - Word sense disambiguation
 - Sentiment and opinion analysis
 Genre classification

 - Others
- NLP problems that We Chat and We Get imple text classifications (or you can, but the results won't be optimal)
 - Sequence labeling problems such as POS tagging, Named **Entity Recognition**
 - Structured prediction problems such as syntactic parsing

Beyond Supervised Learning

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There are other search and ribs where the search in the search are available to various degree or not available at all

- When Alege is not leave the land is the EM algorithms://powcoder.com
- When there is a small amount of labeled data, we might want to try semi-supervised earning owcoder
- When there is a lot of labeled data in one domain but there is only a small of labeled data in the target domain, we might try domain adaptation

K-Means clustering algorithm

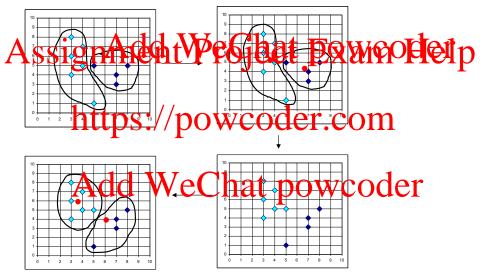
```
Freedrich Ansignment Project Exam Help procedure K-MEANS(x_{1:N}, K)

for i \in 1 \cdots N do an integration of the properties of the prop
```

K-Means training

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- K-means clustering is non-parametric and has no parameters to update
- ► The number of clusters need to be pre-specified before the training process starts

Semi-supervised learning

- Initialize Againsters withts prervised learning and the apply unsupervised learning (such as the EM algorithm)
- - each view
 - Each classifip Spied po Wie oder som of the unlabeled instances, using only the features available in its view. These predictions are the classifiers associated with the other views
 - Named entity example: named entity view and local context view
 - Word sense disambiguation: local context view and global context view

Domain adaptation

Supervised domain adaptation (Daumé III, 2007)

Creates capies of remote feat life of exchind and one for the cross-domain setting

where d is the domain.

Let the learning algorithm allocate weights between domain specific features and cross-domain features: for words that facilitate prediction in both domains, the learner will use cross-domain features. For words that are only relevant to a particular domain, domain-specific features will be used.

Other learning paradigms

- Active learning that is often used to reduce the number of instances that have to be annotated but can still produce the grant that Wesquaty Pawro Help
- Distant supervision: There is no labeled data, but you can generate sor hat (potentially moison external resource such as a dictionary. For example, you can generate named entity amptation with a little of names.
- Multitask learning: The learning induces a representation that can be used to solve multiple tasks (learning POS tagging with syntactic parsing)