#### CS 112: Data Structures

Assignment Project Exam Help Sesh Venugopal

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Tree Building, Encoding Text,
Decoding Back to Text

### **Building the Huffman Tree**

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#### Input Symbols with Probabilities

```
p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25
```

Input Symbols, with probabilities of occurrence in text (Pre-sorted in INCREASING ORDER OF PROBABILITIES)

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#### Symbols Queue and Trees Queue - Initialize

```
p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25
```

Initially, enqueue all symbols – taken in increasing order of probabilities -into symbols queue. Lees queue is initially null. (Symbols are actually
wrapped inside tree nodes, which are enqueued.)
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Symbols queue

Trees queue

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#### Building Huffman Tree – Step 1

Dequeue the first two symbols from the symbols queue, build a subtree out of them

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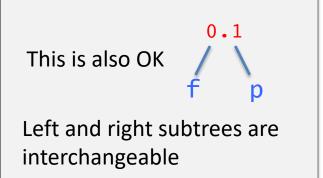


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O.1 Root node probability = 0.05 (p) + 0.05 (f)

Trees queue





#### Building Huffman Tree - Step 2 (a)

```
p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25
```

(a) Compare the probability of front of symbols queue, with that of the front of trees queue

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Symbols queue



Dequeue the lesser of the two. Here, since they are both 0.1, either can be dequeued (pick arbitrarily). Say we pick r from the symbols queue, and dequeue it

#### Building Huffman Tree - Step 2 (b)

```
p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25
```

(b) Compare the probability of front of symbols queue, with that of the front of trees queue

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Symbols queue

Trees queded WeChat powcoder



Dequeue the lesser of the two. Here, the trees queue front has a smaller probability, so it will be dequeued

#### Building Huffman Tree - Step 2 (c)

```
p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25
```

(c) Build a subtree out of the dequeued trees (symbols are single node trees), and enqueue into the trees queue

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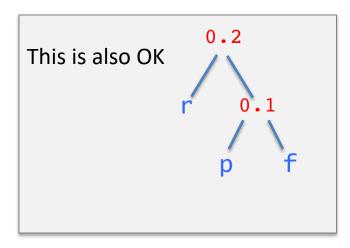
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#### Trees queue

```
O.2 Root node probability = 0.1 (r) + 0.1 (p-f subtree)

O.1 r
```



#### Building Huffman Tree – Step 3 (a)

p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25

(a) Compare the probability of front of symbols queue, with that of the front of trees queue

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Dequeue the lesser of

Trees queue

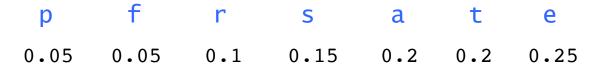
0.2

0.1

p f

Dequeue the lesser of the two. Here s has a smaller probaility, so it is dequeued

#### Building Huffman Tree – Step 3 (b)



(b) Compare the probability of front of symbols queue, with that of the front of trees queue

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Symbols queue

Dequeue the lesser of the two.

0.2 a

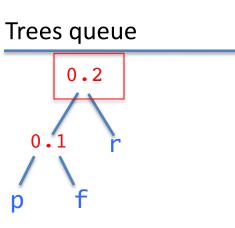
t https://powcoderHeremince they are both 0.2,

either can be dequeued (pick

Add WeChat poweitrerely). Say we pick a from

the symbols queue, and

dequeue it



#### Building Huffman Tree – Step 3 (c)

p f r s a t e 0.05 0.05 0.1 0.15 0.2 0.2 0.25

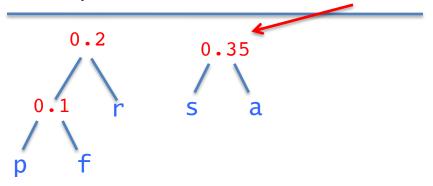
(c) Build a subtree out of the dequeued trees (symbols are single node trees), and enqueue into the trees queue

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t e https://powcoder.com

Trees queue

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Root node probability = 0.15 (s) + 0.2 (a)





#### Building Huffman Tree – Step 4 (a)

p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25

(a) Compare the probability of front of symbols queue, with that of the front of trees queue

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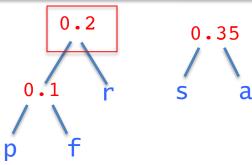
Dequeue the lesser of the two.

0.2 t e

https://powcoderlegnaince they are both 0.2, either can be dequeued (pick

Trees queue

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#### Building Huffman Tree – Step 4 (b)

p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25

(b) Compare the probability of front of symbols queue, with that of the front of trees queue

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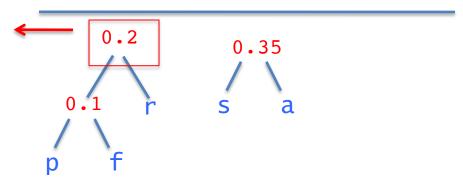
Dequeue the lesser of the two.

0.25 **e** 

https://powcoder!erenthe trees front has a smaller probability, so it is

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Trees queue



#### Building Huffman Tree - Step 4 (c)

```
p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25
```

(c) Build a subtree out of the dequeued trees (symbols are single node trees), and enqueue into the trees queue

#### Symbols quesignment Project Exam Help

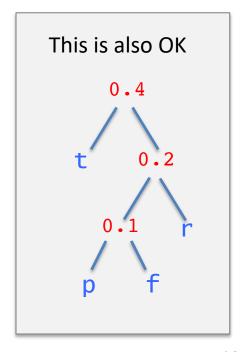
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0.35
0.4

0.1

n f



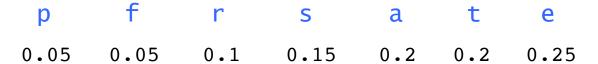
#### Building Huffman Tree – Step 5 (a)

```
p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25
```

(a) Compare the probability of front of symbols queue, with that of the front of trees queue

Symbols queue ignment Project Exam Help

#### Building Huffman Tree – Step 5 (b)



(b) Compare the probability of front of symbols queue, with that of the front of trees queue. But the Symbols queue is empty, so the only option is to dequeue from the Trees queue

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#### Building Huffman Tree – Step 5 (c)

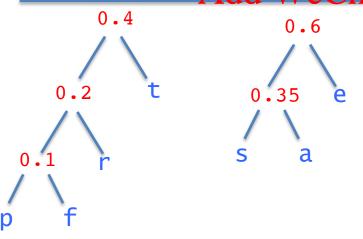
p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25

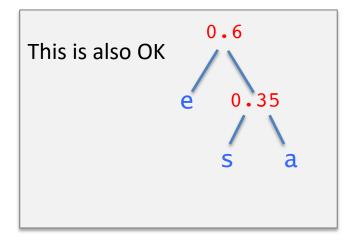
(c) Build a subtree out of the dequeued trees (symbols are single node trees), and enqueue into the trees queue

Symbols quesignment Project Exam Help

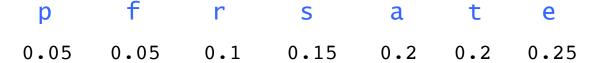
https://powcoder.com

Trees queue Add WeChat powcoder



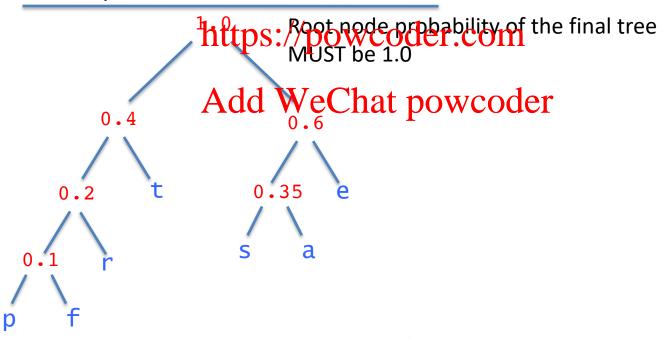


#### Building Huffman Tree – Step 6



Since Symbols queue is empty, dequeue pairs of trees from Trees queue, build subtree, and enqueue, until Trees queue has a single item

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#### Complete Huffman Tree

```
p f r s a t e
0.05 0.05 0.1 0.15 0.2 0.2 0.25
```

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o.1 r s a

### **Assigning Huffman Codes**

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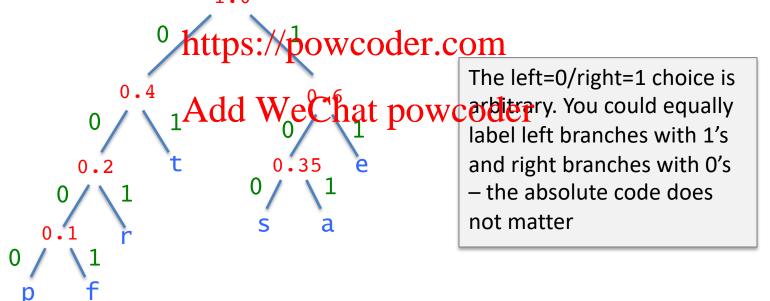
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#### **Assigning Bits to Branches**

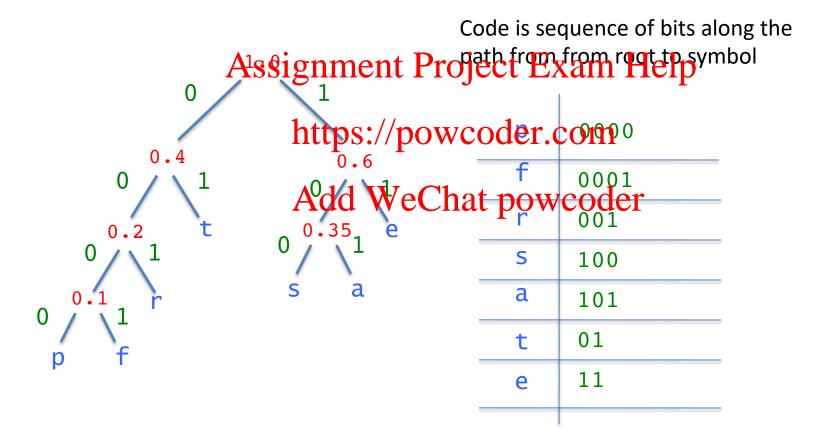
Each left branch is labeled with a 0 (bit) and right branch is labeled with a 1 (bit).

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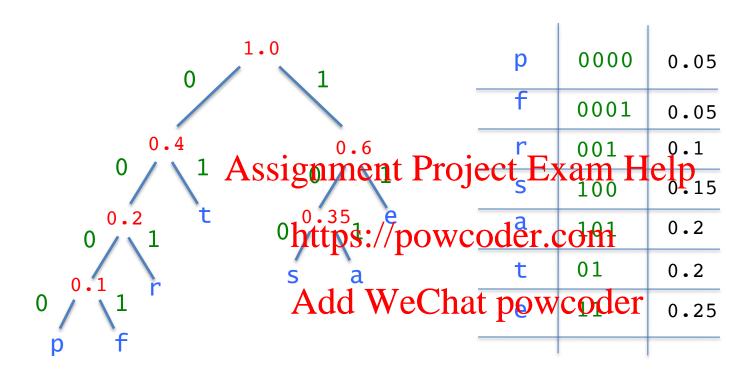
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#### **Gathering Codes for Symbols**



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#### **Codes for Symbols**

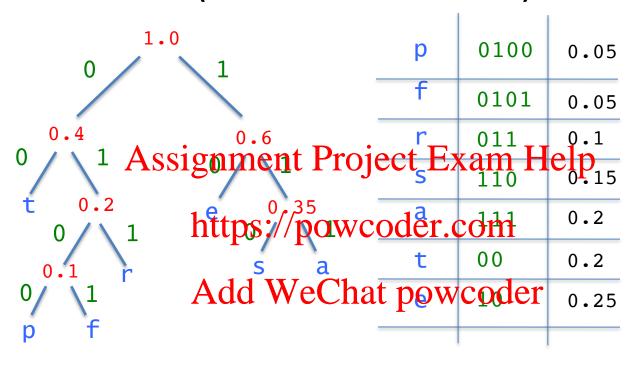


Average code length

= 4\*0.05 + 4\*0.05 + 3\*0.1 + 3\*0.15 + 3\*0.2 + 2\*0.2 + 2\*0.25

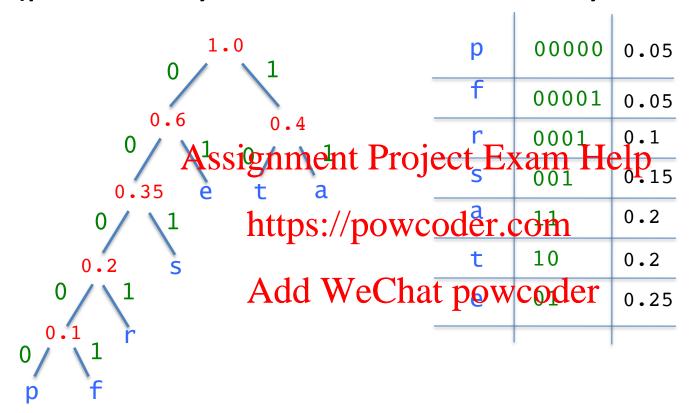
= 2.65

# An Alternative Huffman Tree (subtrees switched)



```
Average code length = 4*0.05 + 4*0.05 + 3*0.1 + 3*0.15 + 2*0.2 + 2*0.2 + 2*0.25 = 2.65
```

# An Alternative Huffman Tree (probability ties broken differently in Step 3(b))



Average code length = 5\*0.05 + 5\*0.05 + 4\*0.1 + 3\*0.15 + 2\*0.2 + 2\*0.2 + 2\*0.25 = 2.65

#### Average Code Length is what matters

Various ways in which alternative Huffman trees can be obtained:

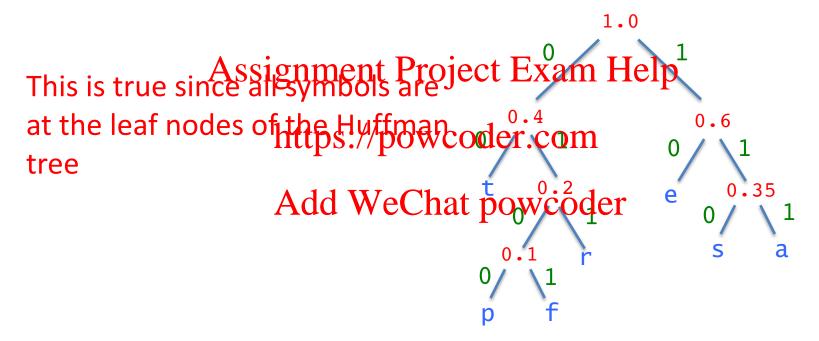
- Tie broken differently when dequeueing equal probability items from Symbols and Trees queues
  - Left and right subtrees switched when building bigger tree
- Left and right branches/switched when numbering with 0 or 1

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Although the actual codes might differ, ALL Huffman trees for a given set of symbols+probabilities will have the SAME average code length!!!

#### **Prefix Property**

No two symbols can have codes such that one is the prefix of the other: for instance 0001 and 000 cannot both be codes since 000 is a prefix of 0001

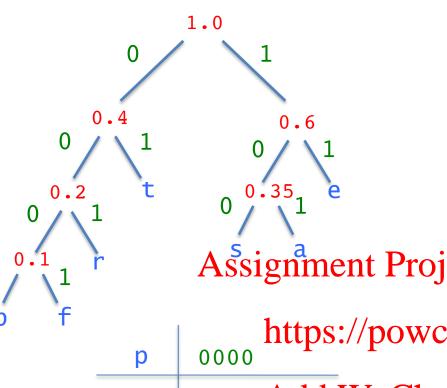


It's critical that a code not be a prefix of another. WHY?

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#### **Encoding Example**

Input text: teaser.

Encoded: 011110110011001

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Scan the text from start to end. For each character look up its code in the table and write out the code. (Huffman tree 0001 Add WeChat itself is not needed.)

f r 001 S 100 a 101 01 t 11 e

Code must be written to file in binary format, so that '11' is written out as 2 bits, not 2 bytes (which would happen if '11' is written as a string)!

#### **Encoding Example**

Input text: teaser

Encoded: 011110110011001

What is the compression compared to ASCII?

ASCII would use 8 bits per character, so the ASCII-coded result would be 8 bits \* 6 characterment by the Exam Help
The Huffman coded result above is 15 bits long.
So the ratio of Huffman coded to the Code of th

BUT WAIT! This is not apples-to-apples. Reason being ASCII needs 8 bits only when all possible characters are considered.

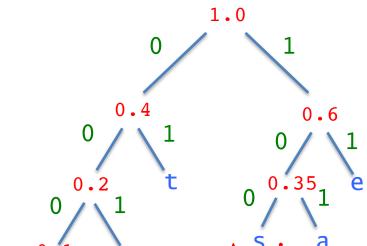
However, the Huffman tree was built to code 7 symbols (p, f, r, s, a, t, e), so to be fair we need to think of how many bits would ASCII need to store 7 possible values (one per symbol) – the answer is 3, since 3 bits can store up to  $2^3$  values.

In which case, the ratio is 15/18 = 0.83, for a roughly 17% compression

## Decoding Back to Original Text

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#### **Decoding Example**

Encoded: 011110110011001

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Flortpscoping, coelerecothe Huffman tree.

Set a pointer to the root of the Huffman tree Scan the encoded bit string from left to right:

If you see a 0 in the encoded string, go to the left child in the tree, otherwise go to the right child. If you hit the bottom (symbol), write that symbol out and reset back to the root of the tree. Go to next bit in the encoded bit string

#### **Encoding/Decoding Example 2**

Alice was beginning to get very tired of sitting by her sister on the bank, and of having nothing to do. Once or twice she had peeped into the book her sister was reading, but it had no pictures or conversations in it, "and what is the use of a book," thought Alice, "without pictures or conversations?"

So she was considering in her own mind (as well as she could, for the making a daisy-chain would select the of got le coded file day made her feel very sleepy and stupid), whether the pleasure of picking the daisies, when suddenly a White Rabbit with pink eyes ran close by her. https://powcoder.com

There was nothing so very remarkable in that, nor did Alice think it so very much out of the way to hear the Rabbit say to itself. "Oh dear! Oh dear! I shall be too late!" But when the Rabbit actually took Digital Coder out of its waistcoat-pocket and looked at it and then hurried on, Alice started to her feet, for it flashed across her mind that she had never before seen a rabbit with either a waistcoat-pocket, or a watch to take out of it, and, burning with curiosity, she ran across the field after it and was just in time to see it pop down a large rabbit-hole, under the hedge. In another moment, down went Alice after it!

File has 6942 characters

would be 6942 bytes long (each character is an 8-bit/1-byte code)

#### Characters, Probabilities, Huffman Codes

Input text file was analyzed, and probabilities of occurrence were computed for all characters that appeared in the file

```
B|1.440507E-4|10010010101000 C|1.440507E-4|100100101010101 F|1.440507E-4|100100101010110 G|1.440507E-4|100100101010111 K|1.440507E-4|1001001011000 L|1.440507E-4|1001001011001 q|2.881014E-4|100100101101 :|4.3215213E-4|010100101110 H|4.3215213E-4|010100101111
```

Assignment Pr A Huffman tree was built, and codes computed

g|0.01627773|100111 f|0.016565831|101000 ewintetibaside DOWCOder.com

> u|0.017862288|101001 u|0.018870642|110010

Add WeChat of other was a second of the control of

1 | 0.037453182 | 11000

r | 0.039325844 | 11010 s | 0.044655718 | 0000

i | 0.047104582 | 0000

n | 0.04897724 | 0100

h|0.05157015|0110 a|0.056179777|0111

0|0.061941803|1000

t|0.07346586|1011

e|0.097522326|001 |0.17660616|111

Blank space character

#### Encoding File/Decoding back to original text

Alice was beginning to get very tired of sitting by her sister on the...

The encoded (compressed) file is a string of bits, total # of bits is 30887

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The ASCII encoded file (uncompressed original) is 6942 bytes long =

6942\*8 = 55536 bits

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Ratio of compressed/uncompressed = 30887/55536 = 0.56 Add WeChat powcoder

Compression factor = 1 - 0.56 = 0.44 = 44%!

NOTE: The encoded file must be written in binary form – you don't want each 1/0 to be written as a 1-byte character!!

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