# CS 112: Data Structures

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Quicksort Algorithm

## **Divide and Conquer**

Mergesort and Quicksort both use what's called a "divide and conquer" technique

## **Divide and Conquer Algorithms**

The first step is to divide the input list, input: list L in to be sorted Examples, L left and L right.

output: sorted list  $L_{out}$  Each part is sorted recursively by applying https://powcodeth.com/e divide-and-conquer strategy:

divide L in into L left, L right the sorted parts are in L left sorted and L right sorted respectively.

recursively sort L\_left And L. Wie Grant powered, respectively.

recursively sort  $L\_right$  into  $L\_right\_sorted$  combine  $L\_left\_sorted$ ,  $L\_right\_sorted$  into  $L\_out$ )

sorted parts to produce the sorted list,  $L_{-out}$ .

The last step is to combine these two

In Mergesort, the "divide" step is trivial – just divide the array in two halves. All the work is done in "combine", where sorted subarrays are merged

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## Divide and Conquer in Quicksort

In Quicksort, the divide and conquer process works in exactly the opposite way. As in, all the work is done in the "divide" step, and nothing at all is done in the "combine" step.

### Algorithm quicksort(A, left, right)

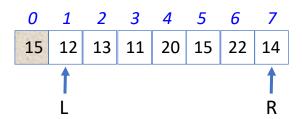
 $splitPoint \leftarrow split(A, left, tipps://powcoderical/plical/$ 

The *split* process selects a *pivot* entry, say x, in the given sublist and rearranges the entries of the sublist in such a way that all the entries less than x are to its left, and all other entries (greater than or equal to x) are to its right.

After the split, the pivot is in its correct sorted place

## Split

Pivot is the first value, 15 Start with L at the next index after the pivot, and R at the last index



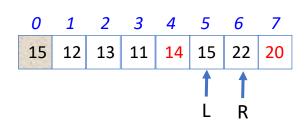
### Iteration 1

otherwise stop – here Sava Bull Project Exam Here way to 20, where it stops because 20 is not < than 15

14 https://powcoder.com

If A[R] >= pivot, then advance R to previous Chat power of the region of index, otherwise stop – here R does not advance at all since 14 is not >= 15

Swap the values at L and R, then advance L up by 1 and R down by 1, to prepare for next iteration



### Iteration 2

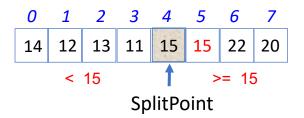
If A[L] < pivot, then advance L to next index, otherwise stop – here L does not advance at all since 15 is not < 15

If A[R] >= pivot, then advance R to previous Project Exam<sup>2</sup>Help 5 6 7 index, otherwise stop – here Radvances to 15 Project Exam<sup>2</sup>Help 5 6 7 Normally it would have also compared 15, but because it has already been toppared powcoder.com via L, R stops without comparing 19 LR against the pivot.

So the condition to advance Risholdfie McGris:hat powcoder If R > L and A[R] >= pivot, then R--

At this point, both L and R have finished moving as far as they could, because R is not > L

So we need wrap up. This is done by swapping A[L-1] with the pivot:



right

5

14

19

19

12

12

# Split Example 2

#### Pivot is 9

#### Iteration 1

left starts at item 3, right starts at item 12 left moves up to 14 and stops (14 not < 9),

right moves down to 5 and stops (5 not  $\geq$  9) swap 14 with 5, then left++, right--

#### Iteration 2

Assignment Project Exam H left starts at item 7, right starts at item 7

left moves past 7, but stops at 14 without comparing 14

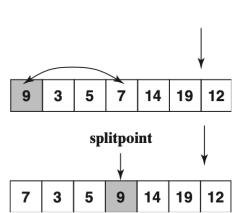
because left has moved past right https://powcoder.com

So the condition to advance L is modified to this:

If L <= R and A[L] < pivot, then L++

left and right have crossed over, so right less to reachat powcoder at all (remember right only moves if right > left)

All items have been compared against pivot (right is not > left) Swap A[left-1] (7) with pivot (9)



left

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# Split: Extreme Case 1 (All items < pivot)

Condition to advance L: If L <= R && A[L] < pivot, then L++ Condition to advance R:

13

15

12

If R > L && A[R] >= pivot, then R--

11

14

14

#### Pivot is 15

#### Iteration 1

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L moves all the way through the array and stops when it moves past R (and goes out of bound)

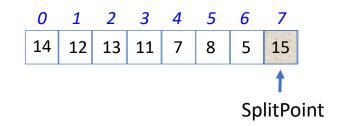
https://powcoder.com3

15 12 13 11

R does not move at all, since R is not > L

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All items have been compared against pivot (R is not > L)
Swap A[L-1] (14) with pivot (15)



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## Split: Extreme Case 2 (All items >= pivot)

#### Condition to advance L:

If L <= R && A[L] < pivot, then L++

Condition to advance R:

12

13

11

If R > L && A[R] >= pivot, then R--

14

#### Pivot is 3

#### Iteration 1

L starts at item12, R starts at item 14 ASSIGNment Project Exam Help

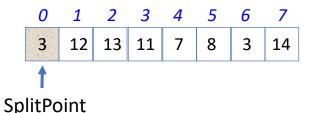
L does not move at all (since 12 not < 3)

R moves all the way across. Pashttipses//powcoder.com<sup>3</sup> <sup>4</sup> <sup>5</sup> <sup>6</sup> <sup>7</sup> to item 12, but stops (without making a comparison) because R not > L

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All items have been compared against pivot (R is not > L)

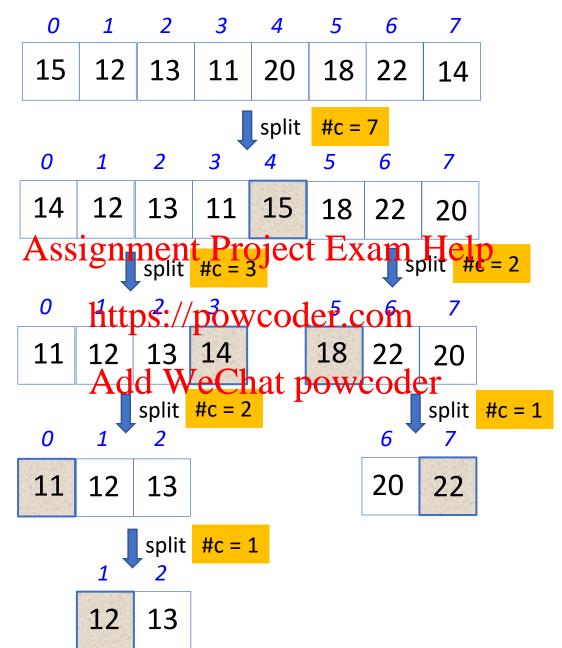
Swap A[L-1] (3) with pivot (3), i.e. swap pivot with itself



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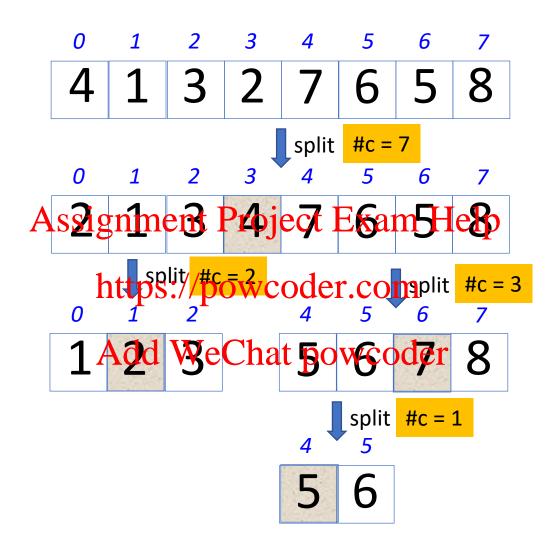
```
Algorithm split(A, lo, hi)
    pivot ← A[lo]
    left ← lo+1, right ← hi
    while (true) do
       while (left <= right) do
          if (A[left] < pivot) then
             left++
          else
                                             Algorithm quicksort(A, left, right)
             break
          endif
       endwhile
                                             input: subarray A[left ... right]
       whas signment Project Example Subarray A [left ... right] if (A[right] < pivot) then
             break;
                                             splitPoint \leftarrow split(A, left, right)
          else https://powcoder.comsort(A, left, splitPoint - 1);
                                             quicksort(A, splitPoint + 1, right);
          endif
       endwhile
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       if (left >= right) then
          break
       endif
        swap(A[left],A[right])
       left++
       right-
    endwhile
    swap(A[left-1],A[lo])
    return left-1
```

# Recursion Tree Example 1



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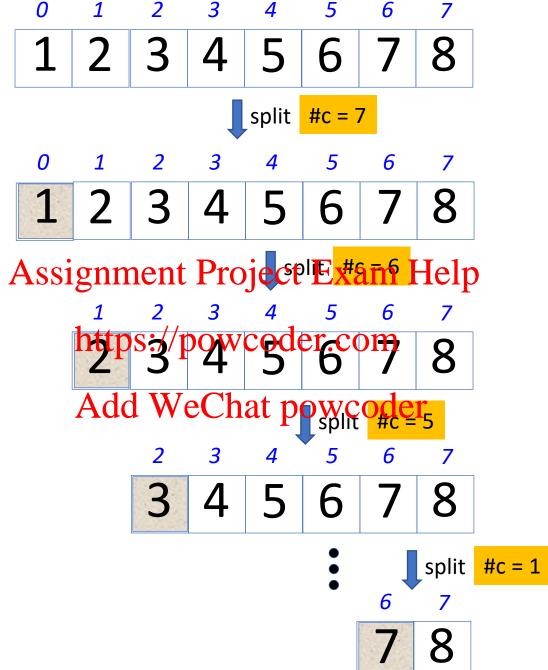
# Recursion Tree Example 2



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12

# Recursion Tree Example 3



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# Assignment Project Exam Help Quicksort Running Time

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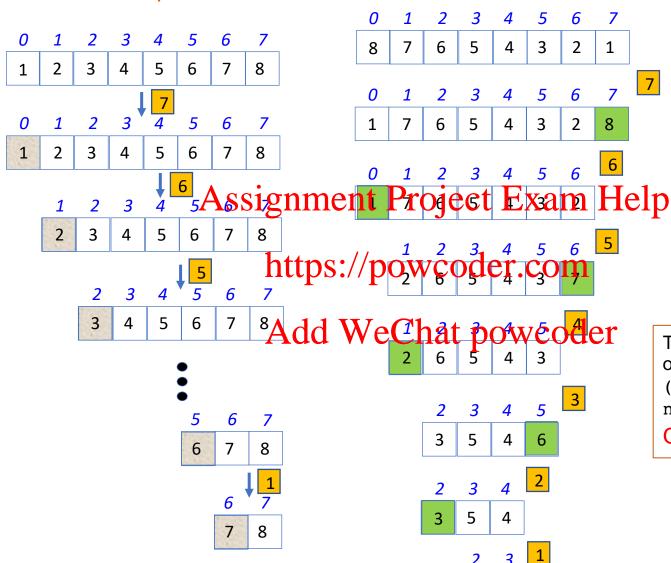
Worst case CS 112: Quicksort

## **Sorted Input**

## **Reverse Sorted Input**

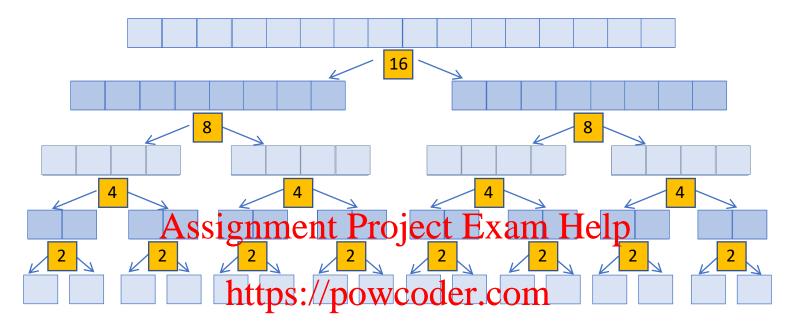
4

5



Total number of comparisons =  $(n-1)+(n-2)+...2+1 = n(n-1)/2 = O(n^2)$ 

## Best case



(n = 16, the number of communications are evered at the somewhat, for ease of analysis but the big O will be unchanged)

Total number of comparisons
= 16 + 16 + 16 + 16 =
= 16\*4 (height)
= 16\*log<sub>2</sub>(16)

Which generalizes to
O(nlogn)

## So why is Quicksort popular?

Worst Case

Best Case

Average Case

Insertion Sort O(n<sup>2</sup>) O(n) O(n<sup>2</sup>) Assignment Project Exam Help

Quicksort

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O(nlogn)

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