

Assignment Project Exam Help

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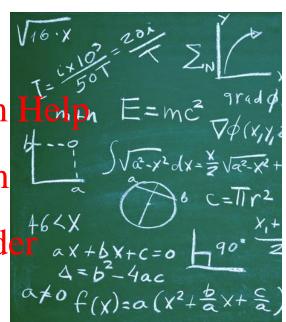
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Who should take this class?

 This is a difficult, math- and programming-intensive class Assignment Project Exam geared primarily towards graduate students powcoder.com

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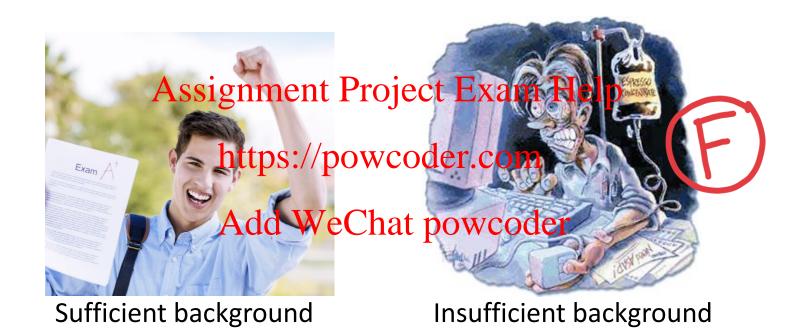
 Historically, much fewer undergraduates manage an A than graduate students



- Linear algebra
- Multivariate Calculus, including partial derivatives
- Probability
 Assignment Project Exam Help
 Comfort with programming in Python

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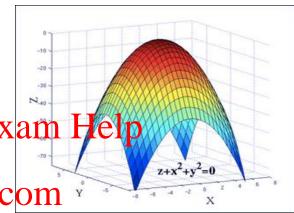
- Fundamentals of Data Science (CS 365) is a great pre-requisite for this course Chat powcoder
 - serves as a preparation including, but not limited, to the courses CS460, CS506, CS542 and CS565
- Intro to Optimization (CAS CS 507)
 - is not a formal prerequisite, but is highly recommended before taking this class



Multivariate Calculus

- Vectors; dot product
- Determinants: cross product
 Matrices; inverse matrices

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- Square systems; equations of planes
- Parametric equations for lines and curves der.com
- Max-min problems; least squares
- Second derivative test; boundaries and infinity
- Level curves; partial April vatives et and antiplane expereximation
- Differentials; chain rule
- Gradient; directional derivative; tangent plane
- Lagrange multipliers
- Non-independent variables
- Double integrals
- Change of variables
- and other Calculus concepts such as convexity, etc.



Linear algebra



• Determinants stormosy to a der. com

• Special Matrices WeChat powcoder



- Matrix rank
- Eigenvalues and Eigenvectors
- Matrix Calculus

Probability

- Rules of probability, conditional plansing Paraject Exam Help independence, Bayes rule https://powcoder.com/
- Random variables (expected value, variance, their powcoder properties); discrete and continuous variables, density functions, vector random variables, covariance, joint distributions
- Common distributions: Normal, Bernoulli, Binomial,
 Multinomial, Uniform, etc.

A review: http://cs229.stanford.edu/section/cs229-prob.pdf

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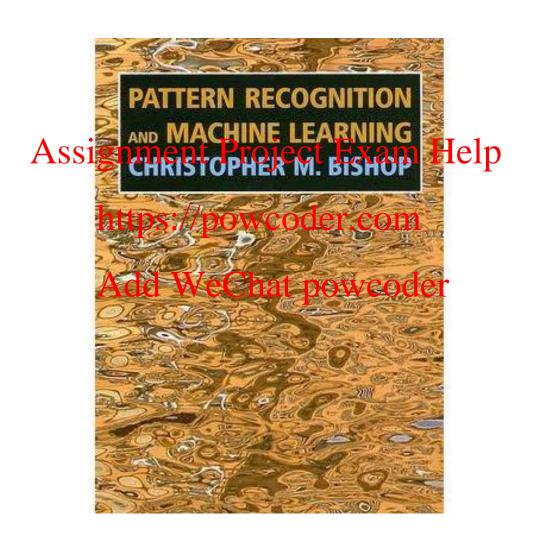
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Add WeChat powcoder NumPy

"..but I really want to take this course!"

- If you lack any of these prerequisites, you SHOULD NOT take this class
- we cannot teach you the class material and also the prerequisite material powcoder.com
- we are not miracle workers! Add WeChat powcoder
- instead, please consider these alternative courses:
 - EC 414 Introduction to Machine Learning
 - CS 506 Computational Tools for Data
 - CS 504 Data Mechanics

Read the book



Matrix Algebra Review

- Vectors and matrices
 - Basic Matrix Operations
 Assignment Project Exam Help
 Determinants, norms, trace

 - Special Matrices://powcoder.com
- Matrix inversedd WeChat powcoder
- Matrix rank
- Eigenvalues and Eigenvectors
- Matrix Calculus

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Vector

• A column vector $\mathbf{v} \in \mathbb{R}^{n \times 1}$ where

$$\begin{array}{c} \text{Assignment Project Exam Help} \\ \text{v} = \\ \text{https://powcoder.com} \\ \text{Add WeChat}^n \text{powcoder} \\ \bullet \text{ A row vector } \mathbf{v}^T \in \mathbb{R}^{1 \times n} \text{ where} \end{array}$$

$$\mathbf{v}^T = \begin{bmatrix} v_1 & v_2 & \dots & v_n \end{bmatrix}$$

T denotes the transpose operation

Vector

We'll default to column vectors in this class

```
Assignment Project Exam Help v = \begin{bmatrix} v_1 \\ v = \end{bmatrix} https://powcoder.com v_n Add WeChat powcoder
```

Matrix

• A matrix $\mathbf{A} \in \mathbb{R}^{m \times n}$ is an array of numbers with size m by n, i.e. m rows and n columns. Assignment Project Exam Help

$$\mathbf{A} = \begin{bmatrix} \frac{a_{11}}{a_{21}} & \frac{a_{12}}{a_{22}} & \frac{a_{13}}{a_{23}} & \dots & a_{1n} \\ a_{21} & a_{22} & a_{23} & \dots & a_{2n} \\ \mathbf{Add \ WeChat \ powcoder} & \vdots \\ a_{m1} & a_{m2} & a_{m3} & \dots & a_{mn} \end{bmatrix}$$

• If m=n , we say that ${\bf A}$ is square.

Basic Matrix Operations

- What you should know:
 - Addition
 - Scaling Assignment Project Exam Help
 - Dot product
 - Multiplication

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 - Transpose Add WeChat powcoder
 - Inverse / pseudoinverse
 - Determinant / trace

Vectors

Norm

$$||x||_2 = \sqrt{\sum_{i=1}^n x_i^2}.$$

• More formally, a norm is any function $f: \mathbb{R}^n \to \mathbb{R}$ that satisfies up to the satisfies appropriate expression of the satisfies of the

- https://powcoder.com Non-negativity: For all $x \in \mathbb{R}^n, f(x) \geq 0$
- Definiteness: fixed bawarder o.
- **Homogeneity:** For all $x \in \mathbb{R}^n$, $t \in \mathbb{R}$, f(tx) = |t|f(x)
- Triangle inequality: For all

$$x, y \in \mathbb{R}^n, f(x+y) \le f(x) + f(y)$$

Example Norms

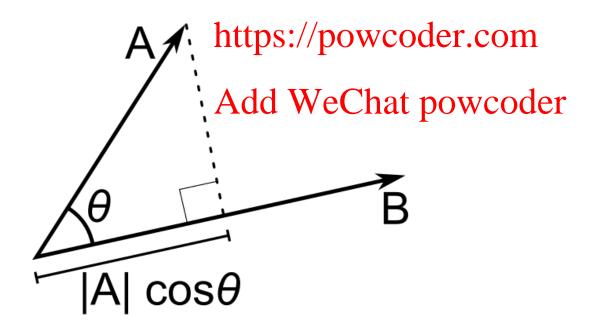
$$||x||_1 = \sum_{i=1}^n |x_i|$$
 $||x||_\infty = \max_i |x_i|$ Assignment Project Exam Help

• General
$$\ell_p$$
 norms: https://powcoder.com $\|x\|_p = \sum_{i=1}^{n} |x_i|^p$ Add WeChat powcoder.

- Inner product (dot product) of vectors
 - Multiply corresponding entries of two vectors and add up the result
 - x·y is also [x] [y] Cos (the angle between x and y) https://powcoder.com

$$\mathbf{x}^{T}\mathbf{y} = \begin{bmatrix} x_{1} & \dots & x_{n} \end{bmatrix} \begin{bmatrix} \mathbf{y}_{n} \\ \vdots \\ \mathbf{y}_{n} \end{bmatrix} = \sum_{i=1}^{n} x_{i}y_{i} \quad \text{(scalar)}$$

- Inner product (dot product) of vectors
 - If B is a unit vector, then A·B gives the length of A which lies in the direction of Bam Help



The product of two matrices

Matrix multiplication is associative: (AB)C = A(BC).

Matrix multiplication is distributive: A(B+C) = AB + AC.

Assignment Project Exam Help Matrix multiplication is, in general, not commutative; that is, it can be the case that $AB \neq BA$. (For example, if $A \in \mathbb{R}^{m \times n}$ and $B \in \mathbb{R}^{n \times q}$, the matrix product BA does not even exist if m and the short power coder.com

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Powers

- By convention, we can refer to the matrix product
 AA as AAsangh AAAt Braje at Exam Help
- Obviously only square matrices can be multiplied that way

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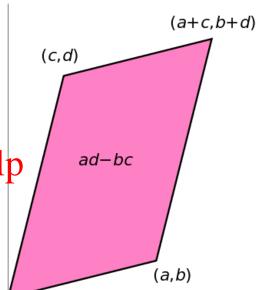
 Transpose – flip matrix, so row 1 becomes column 1

• A useful identity: Add WeChat powcoder

$$(ABC)^T = C^T B^T A^T$$

- Determinant
 - $-\det(\mathbf{A})$ returns a scalar
 - Represents area (or volume) of the parallelegram described by Help the vectors in the rows of the https://powcoder.com

 - Properties: $\det(\mathbf{A}\mathbf{B}) = \det(\mathbf{B}\mathbf{A})$ $\det(\mathbf{A}^{-1}) = \frac{1}{\det(\mathbf{A})}$ $\det(\mathbf{A}^{T}) = \det(\mathbf{A})$ $\det(\mathbf{A}) = 0 \Leftrightarrow \mathbf{A} \text{ is singular}$



Trace

 $tr(\mathbf{A}) = sum \text{ of diagonal elements}$ $tr(\begin{bmatrix} 1 & 3 \\ 5 & 7 \end{bmatrix}) \overline{\mathbf{Assignment Project Exam Help}}$

- Invariant to https://optwocsflormetions, so it's used sometimes in proofs. (Rarely in this class though.)
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- Properties:

$$tr(\mathbf{AB}) = tr(\mathbf{BA})$$

 $tr(\mathbf{A} + \mathbf{B}) = tr(\mathbf{A}) + tr(\mathbf{B})$

Vector Norms

$$||x||_1 = \sum_{i=1}^n |x_i|$$
 $||x||_{\infty} = \max_i |x_i|$

$$\|x\|_2 = \sqrt{\sum_{i=1}^n \frac{\text{https://powcoder.com}^n}{\|x\|_p}} |x_i|^p$$

 Matrix norms: Norms can also be defined for matrices, such as

$$||A||_F = \sqrt{\sum_{i=1}^m \sum_{j=1}^n A_{ij}^2} = \sqrt{\operatorname{tr}(A^T A)}.$$

Special Matrices

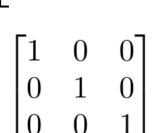
- Symmetric matrix
- Skew-symmetric matrix $\begin{bmatrix} \mathbf{A}^T = \mathbf{A} \\ \mathbf{Assignment Project Exam Help} \\ \mathbf{Attps://powcoder.com} \\ \mathbf{Attps://powcoder$

https://powcoder.com
$$\mathbf{A}^T = -\mathbf{A}$$
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Identity matrix I

Diagonal matrix

$$egin{bmatrix} 1 & 2 & 5 \ 2 & 1 & 7 \ 5 & 7 & 1 \ \end{bmatrix}$$



$$\begin{bmatrix} 3 & 0 & 0 \\ 0 & 7 & 0 \\ 0 & 0 & 2.5 \end{bmatrix}$$

Matrix Algebra Review

- Vectors and matrices
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 Determinants, norms, trace

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- Matrix inversedd WeChat powcoder
- Matrix rank
- Eigenvalues and Eigenvectors
- Matrix Calculate

Inverse

• Given a matrix A, its inverse A^{-1} is a matrix such that $AA^{-1} = A^{-1}A = I$

• E.g.
$$\begin{bmatrix} 2 & As & -1 & 1 \\ 0 & 3 & 1 \end{bmatrix}$$
 E.g.
$$\begin{bmatrix} 2 & As & -1 & 1 \\ 0 & 3 & 1 \end{bmatrix}$$
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- Inverse does not always exist. If A-1 exists, A is invertible or non-singular. Otherwise, it's singular.
- Useful identities, for matrices that are invertible:

$$(\mathbf{A}^{-1})^{-1} = \mathbf{A}$$
$$(\mathbf{A}\mathbf{B})^{-1} = \mathbf{B}^{-1}\mathbf{A}^{-1}$$
$$\mathbf{A}^{-T} \triangleq (\mathbf{A}^{T})^{-1} = (\mathbf{A}^{-1})^{T}$$

Pseudoinverse

- Say you have the matrix equation AX=B, where A and B are known, and you want to solve for X
- You could sagurate the piver sex and prelimitiply by it: $A^{-1}AX=A^{-1}B \rightarrow X=A^{-1}B$ https://powcoder.com – Python command would be np.linalg.inv(A)*B
- But calculating the Workington forwarge enatrices often brings problems with computer floating-point resolution (because it involves working with very small and very large numbers together).
- Or, your matrix might not even have an inverse.

Pseudoinverse

- Fortunately, there are workarounds to solve AX=B in these situations. And python can do them!
- Instead of the ingent inverse, directly lask python to solve for X in AX=B, by typing np.linalg.solve(A, B)

 https://powcoder.com
 Python will try several appropriate numerical methods
- Python will try several appropriate numerical methods (including the pseudoinyarse if the inverse doesn't exist)
- Python will return the value of X which solves the equation
 - If there is no exact solution, it will return the closest one
 - If there are many solutions, it will return the smallest one

Python example:

```
AX = B
A = \begin{bmatrix} 2 & A \\ 3 & 4 \end{bmatrix}, B = \begin{bmatrix} 1 \\ https!//powcoder.com \end{bmatrix}
```

```
>> import numby las paycoder
>> x = np.linalg.solve(A,B)
x =
1.0000
-0.5000
```

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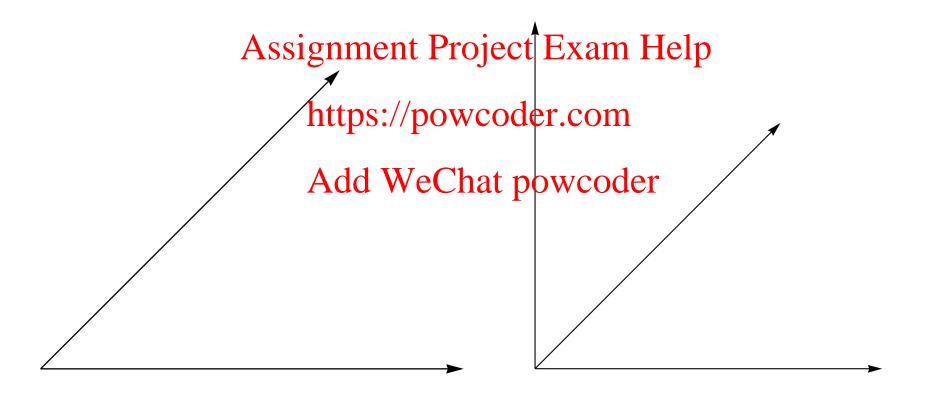
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Linear independence

- Suppose we have a set of vectors $v_1, ..., v_n$
- If we can express \mathbf{v}_1 as a linear combination of the other vectors \mathbf{v}_1 as a linear combination of the other vectors.
 - The direction v_1 can be expressed as a combination of the directions v_4 . Where v_5 is v_4 that v_6 is v_4 .
- If no vector is linearly dependent on the rest of the set, the set is linearly *independent*.
 - Common case: a set of vectors $\mathbf{v_1}$, ..., $\mathbf{v_n}$ is always linearly independent if each vector is perpendicular to every other vector (and non-zero)

Linear independence

Linearly independent set Not linearly independent



Matrix rank

Column/row rank

```
\operatorname{col-rank}(\mathbf{A}) = \text{ the maximum number of linearly independent column vectors of } \mathbf{A} \operatorname{row-rank}(\mathbf{A}) = \text{ the maximum number of linearly independent row vectors of } \mathbf{A}
```

Column rank always equals row rank
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Matrix rank

$$rank(\mathbf{A}) \triangleq col-rank(\mathbf{A}) = row-rank(\mathbf{A})$$

Matrix rank

- For transformation matrices, the rank tells you the dimensions of the output
- E.g. if rank of A is 1, then the transformation Assignment Project Exam Help

https://powcoder.com maps points onto a line.

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• Here's a matrix with rank 1:

$$\begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix} \times \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} x+y \\ 2x+2y \end{bmatrix} - \text{All points get mapped to the line y=2x}$$

Matrix rank

- If an m x m matrix is rank m, we say it's "full rank"
 - Maps an m x 1 vector uniquely to another m x 1 vector
 - An inverse matrix can be found am Help
- If rank < m, we say it's "singular"
 <p>https://powcoder.com
 — At least one dimension is getting collapsed. No way to
 - At least one dimension is getting collapsed. No way to look at the result and tell type the imput was
 - Inverse does not exist
- Inverse also doesn't exist for non-square matrices

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- Matrix rank
- Eigenvalues and Eigenvectors(SVD)
- Matrix Calculus

Eigenvector and Eigenvalue

 An eigenvector x of a linear transformation A is a non-zero vector that, Assignment Project Exam Help when A is applied to it, does not change direction. https://powcoder.com

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$$Ax = \lambda x, \quad x \neq 0.$$

Eigenvector and Eigenvalue

- An eigenvector x of a linear transformation A is a non-zero vector that, Assignment Project Exam Help when A is applied to it, does not change direction. https://powcoder.com
- Applying A to the Weigenvector of the eigenvector by the scalar value λ, called an eigenvalue.

$$Ax = \lambda x, \quad x \neq 0.$$

Properties of eigenvalues

The trace of a A is equal to the sum of its eigenvalues:

$$\operatorname{tr} A = \sum_{i=1}^{n} \lambda_{i}$$
.
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- The determinant of A is equal to the product of its eigenvalues https://powcoder.com
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- The rank of A is equal to the number of non-zero eigenvalues of A.
- The eigenvalues of a diagonal matrix D = diag(d1, . . .
 dn) are just the diagonal entries d1, . . . dn

Diagonalization

Eigenvalue equation:

$$\begin{array}{c} AV \equiv VD \\ \text{Assignment Project Exam Help} \\ A \equiv VDV^{-1} \\ \text{https://powcoder.com} \\ - \text{ Where D is a diagonal matrix of the eigenvalues} \\ \text{Add WeChat powcoder} \\ \lambda_1 \\ & \ddots \\ \end{array}$$

Diagonalization

Eigenvalue equation:

$$\begin{array}{c} AV \equiv VD \\ \text{Assignment Project Exam Help} \\ A \equiv VDV^{-1} \\ \text{https://powcoder.com} \end{array}$$

• Assuming all λ_i 's are unique: Add WeChat powcoder

$$A = VDV^T$$

 Remember that the inverse of an orthogonal matrix is just its transpose and the eigenvectors are orthogonal

Symmetric matrices

• Properties:

- For a symmetric matrix A, all the eigenvalues are Assignment Project Exam Help
- The eigenvettors of ware or the mormal.

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$$A = VDV^T$$

Symmetric matrices

Therefore:

$$x^TAx$$
 Assigning of Project By an $\sum_{i=1}^n |y_i|^2$

 $- \ \, \text{where} \ \, y = V^T x$

- So, if we wanted to find the vector x that:

$$\max_{x \in \mathbb{R}^n} x^T A x$$
 subject to $||x||_2^2 = 1$

Symmetric matrices

• Therefore:

$$x^TAx$$
 Assignible of Project By am $\sum_{i=1}^n |\mathbf{p}_i y_i^2|$

- $\ \, \text{where} \ \, y = V^T x$
- So, if we wanted to find the vector x that:

$$\max_{x \in \mathbb{R}^n} x^T A x$$
 subject to $||x||_2^2 = 1$

 Is the same as finding the eigenvector that corresponds to the largest eigenvalue.

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- Matrix Calculus

Matrix Calculus – The Gradient

• Let a function $f: \mathbb{R}^{m \times n} \to \mathbb{R}$ take as input a matrix A of size $m \times n$ and returns a real value. • Then the gradient of f:

$$\nabla_{A}f(A) \in \mathbb{R}^{m \times n} = \begin{bmatrix} \frac{\partial f(A)}{\partial A_{11}} & \frac{\partial f(A)}{\partial A_{12}} & \dots & \frac{\partial f(A)}{\partial A_{1n}} \\ \frac{\partial f(A)}{\partial A_{21}} & \frac{\partial f(A)}{\partial A_{22}} & \frac{\partial f(A)}{\partial A_{2n}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial f(A)}{\partial A_{m1}} & \frac{\partial f(A)}{\partial A_{m2}} & \dots & \frac{\partial f(A)}{\partial A_{mn}} \end{bmatrix}$$

Matrix Calculus – The Gradient

- Every entry in the matrix is: $(\nabla_A f(A))_{ij} = \frac{\partial f(A)}{\partial A_{ij}}$.
- the size of ∇ f(A) is always the same as the size of A. So if A is just a vector x:

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$$\nabla_x f(x) = \begin{bmatrix} \frac{\partial f(x)}{\partial x_1} \\ \frac{\partial f(x)}{\partial x_2} \\ \vdots \\ \frac{\partial f(x)}{\partial x_n} \end{bmatrix}$$

Exercise

Example:

For $x \in \mathbb{R}^n$, let $f(x) = b^T x$ for some known vector $b \in \mathbb{R}^n$ Assignment Project Exam Help

$$\begin{array}{c} \text{https://powcoder.com} \\ f(x) = \begin{bmatrix} b_1 & b_2 & \dots & b_n \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \\ \text{Add WeChat powcoder} \\ \underline{(x)} = ? \\ \end{array}$$

• Find:

$$\nabla_x f(x) = ?$$

Exercise

Example:

For $x \in \mathbb{R}^n$, let $f(x) = b^T x$ for some known vector $b \in \mathbb{R}^n$ Assignment Project Exam Help

$$\frac{\text{Add WeChat powcoder}}{\partial f(x)} = \frac{\partial}{\partial x_k} \sum_{i=1}^{n} b_i x_i = b_k.$$

• From this we can conclude that: $\nabla_x b^T x = b$.

Matrix Calculus – The Gradient

Properties

- $\nabla_{\mathcal{A}} f(x) + q(x) = \nabla_{\mathcal{A}} f(x) + q($
- For $t \in \mathbb{R}$, $\nabla_x (t f(x)) = t \nabla_x f(x)$.

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Matrix Calculus – The Jacobian

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$$J = \begin{pmatrix} \frac{\partial y_1}{\partial x_1} & \frac{\partial y_1}{\partial x_1} \\ \vdots & \ddots & \vdots \\ \frac{\partial y_m}{\partial x_1} & \dots & \frac{\partial y_m}{\partial x_n} \end{pmatrix}$$

• The Hessian matrix with respect to x, written $\nabla_x^2 f(x)$ or simply as H is the n × n matrix of partial derivatives

$$\nabla_{x}^{2} f(x) \in \mathbb{R}^{n \times n} = \begin{bmatrix} \frac{\partial^{2} f(x)}{\partial x_{1}^{2}} & \frac{\partial^{2} f(x)}{\partial x_{1} \partial x_{2}} & \cdots & \frac{\partial^{2} f(x)}{\partial x_{1} \partial x_{n}} \\ \frac{\partial^{2} f(x)}{\partial x_{2}^{2}} & \frac{\partial^{2} f(x)}{\partial x_{1} \partial x_{2}} & \cdots & \frac{\partial^{2} f(x)}{\partial x_{1} \partial x_{n}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial^{2} f(x)}{\partial x_{n} \partial x_{1}} & \frac{\partial^{2} f(x)}{\partial x_{n} \partial x_{2}} & \cdots & \frac{\partial^{2} f(x)}{\partial x_{2}^{2}} \end{bmatrix}$$

• Each entry can be written as: $\nabla_x^2 f(x))_{ij} = \frac{\partial^2 f(x)}{\partial x_i \partial x_j}$

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• Exercise: Why is the Hessian always https://powcoder.com

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Each entry can be written as:

$$\nabla_x^2 f(x))_{ij} = \frac{\partial^2 f(x)}{\partial x_i \partial x_j}$$

• The Hessiansian way Prsyleon Textric, Hoecause

 This is known as Schwarz's theorem: The order of partial derivatives don't matter as long as the second derivative exists and is continuous.

• Note that the hessian is not the gradient of whole gradient of a vector (this is not defined). It is actually the gradient of every entry of the gradient of the weetor.

$$\nabla_{x}^{2} f(x) \in \mathbb{R}^{n \times n} = \begin{bmatrix} \frac{\partial^{2} f(x)}{\partial x_{1}^{2}} & \frac{\partial^{2} f(x)}{\partial x_{1} \partial x_{2}} & \frac{\partial^{2} f(x)}{\partial x_{1} \partial x_{2}} & \frac{\partial^{2} f(x)}{\partial x_{2} \partial x_{n}} \\ \frac{\partial^{2} f(x)}{\partial x_{2} \partial x_{1}} & \frac{\partial^{2} f(x)}{\partial x_{2}^{2}} & \cdots & \frac{\partial^{2} f(x)}{\partial x_{2} \partial x_{n}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial^{2} f(x)}{\partial x_{n} \partial x_{1}} & \frac{\partial^{2} f(x)}{\partial x_{n} \partial x_{2}} & \cdots & \frac{\partial^{2} f(x)}{\partial x_{n}^{2}} \end{bmatrix}$$

• Eg, the first column is the gradient of $\frac{\partial f(x)}{\partial x_1}$

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$$\nabla_{x}^{2} f(x) \in \mathbb{R}^{n \times n} = \begin{bmatrix} \frac{\partial^{2} f(x)}{\partial x_{1}^{2}} & \frac{\partial^{2} f(x)}{\partial x_{1} \partial x_{2}} & \frac{\partial^{2} f(x)}{\partial x_{1} \partial x_{2}} \\ \frac{\partial^{2} f(x)}{\partial x_{2} \partial x_{1}} & \frac{\partial^{2} f(x)}{\partial x_{2}^{2}} & \cdots & \frac{\partial^{2} f(x)}{\partial x_{2} \partial x_{n}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial^{2} f(x)}{\partial x_{n} \partial x_{1}} & \frac{\partial^{2} f(x)}{\partial x_{n} \partial x_{2}} & \cdots & \frac{\partial^{2} f(x)}{\partial x_{n}^{2}} \end{bmatrix}$$

Common vector derivatives

| Scalar derivative | | | Vector derivative | | |
|-------------------|---------------|-----------------------|--------------------------------------|---------------|--|
| f(x) | Assign | $ \frac{dx}{dx} $ Pro | ojegt(Ex)am | Help | $\frac{\mathrm{d}f}{\mathrm{d}\mathbf{x}}$ |
| bx | / | U | rcoder.com | / | В |
| bx | \rightarrow | ia weci | $\mathbf{x}^T\mathbf{b}$ | \rightarrow | b |
| x^2 | \rightarrow | 2x | $\mathbf{x}^T\mathbf{x}$ | \rightarrow | $2\mathbf{x}$ |
| bx^2 | \rightarrow | 2bx | $\mathbf{x}^T \mathbf{B} \mathbf{x}$ | \rightarrow | $2\mathbf{B}\mathbf{x}$ |

PSet 1 Out Today

Due in 1 week: 9/15 11:59pm GMT -5 (Boston Time)

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Diagnostic homework covering topics covered in prereqs

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 Additional examples in lab this week (Group A for in-person lab rotations)

Next Class

Supervised Learning I: Regression:

```
regression, linear hypothesis, SSD cost; gradient Assignment Project Exam Help descent; normal equations; maximum https://powcoder.com
```

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Reading: Bishop 1.2-1.2.4,3.1-3.1.1