

Assignment Project Exam Help Announcements

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Reminder: self-grading forms for ps1 and ps2 due 10/5 at midnight (Boston)

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- ps3 out today, due 10/8 (1 week)
- Midterm practice questions out next week

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Today: Outline

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- **Neural networks cont'd:** learning via gradient descent; chain rule review; gradient computation using the backpropagation algorithm

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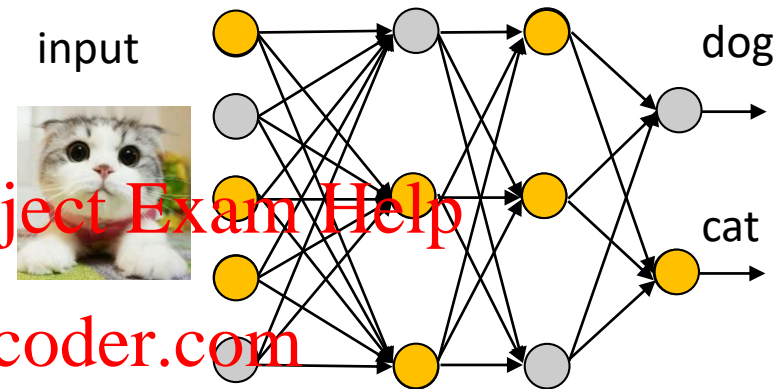
Neural Networks II

Learning

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Artificial Neural Network

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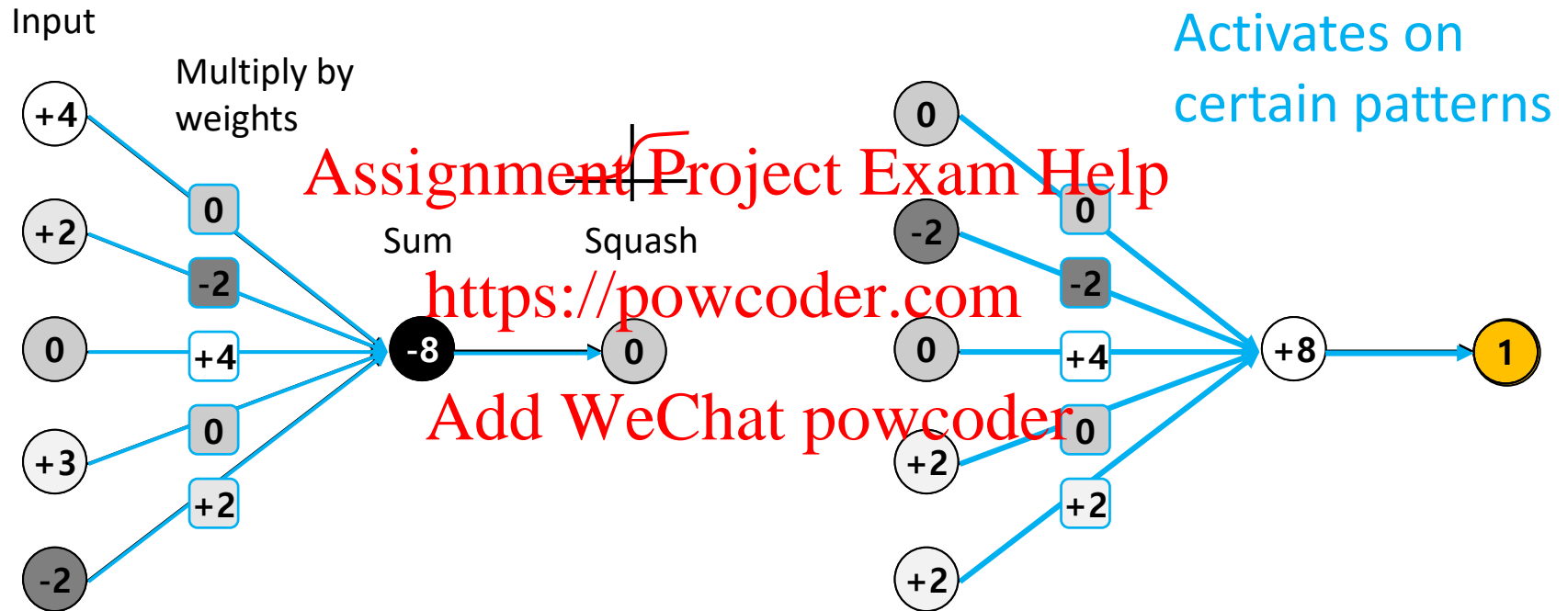
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- **Artificial neural networks:** consist of many inter-connected neurons organized in layers
- **Neurons:** each neuron receives inputs from neurons in previous layer, passes its output to next layer
- **Activation:** neuron's output between 1 (excited) and 0 (not excited)

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Artificial Neuron: Activation



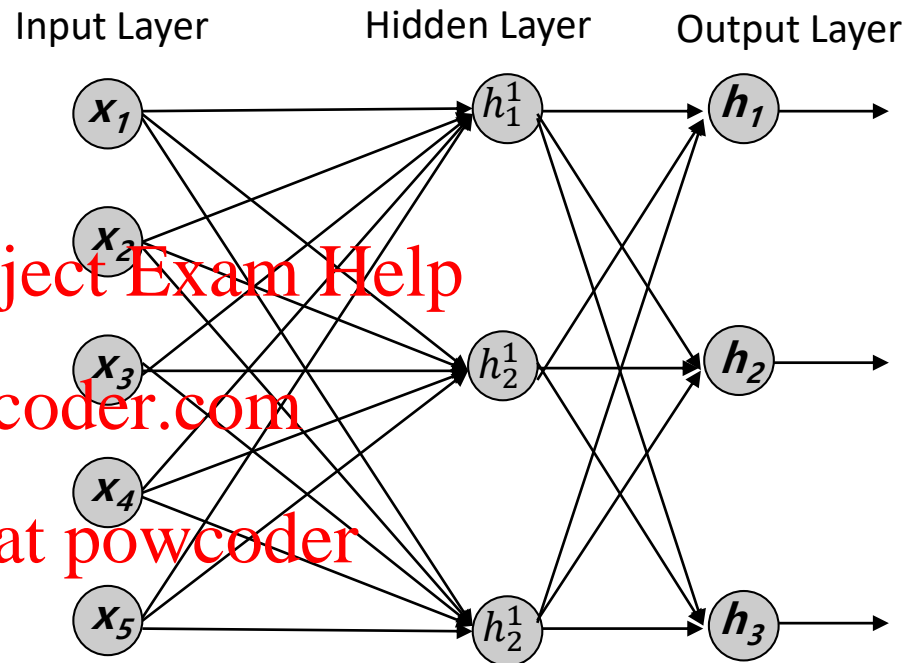
Artificial Neural Network: notation

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input

$$x = \begin{bmatrix} x_1 \\ \dots \\ x_5 \end{bmatrix}$$

hidden layer activations



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Artificial Neural Network: notation

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input

$$x = \begin{bmatrix} x_1 \\ \dots \\ x_5 \end{bmatrix}$$

hidden layer activations

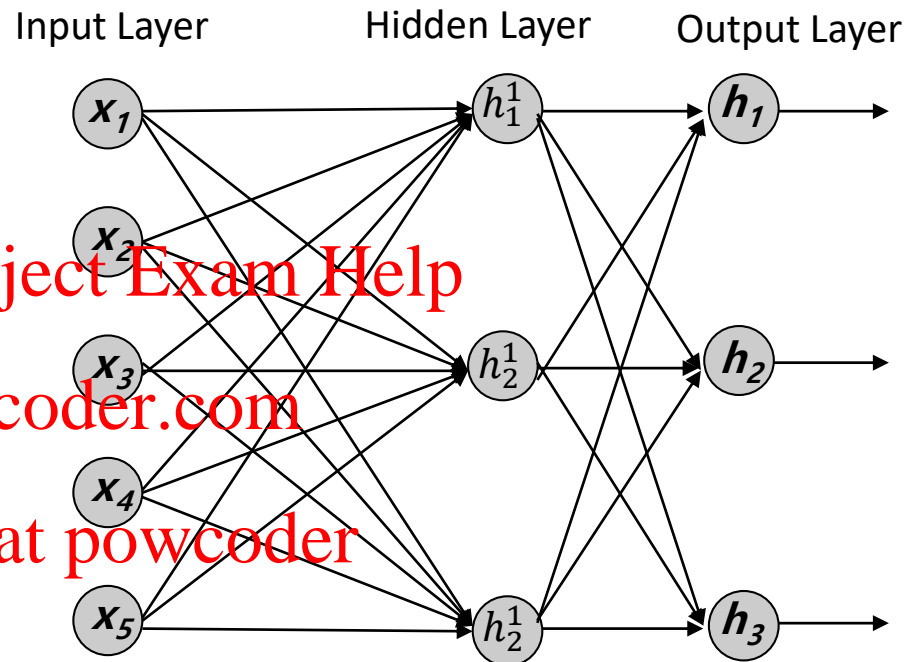
$$h^i = g(\Theta^{(i)}x)$$

$$g(z) = \frac{1}{1 + \exp(-z)}$$

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output

$$h_{\Theta}(x) = g(\Theta^{(2)}h^i) \quad \text{weights} \quad \Theta^{(1)} = \begin{pmatrix} \theta_{11} & \dots & \theta_{15} \\ \vdots & \ddots & \vdots \\ \theta_{31} & \dots & \theta_{35} \end{pmatrix} \quad \Theta^{(2)} = \begin{pmatrix} \theta_{11} & \dots & \theta_{13} \\ \vdots & \ddots & \vdots \\ \theta_{31} & \dots & \theta_{33} \end{pmatrix}$$



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Cost function

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Neural network: $h_{\Theta}(x) \in \mathbb{R}^K$ $(h_{\Theta}(x))_i = i^{th}$ output

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$$J(\Theta) = -\frac{1}{m} \left[\sum_{i=1}^m \sum_{k=1}^K y_k^{(i)} \log(h_{\Theta}(x^{(i)}))_k + (1 - y_k^{(i)}) \log(1 - (h_{\Theta}(x^{(i)}))_k) \right]$$

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$$+ \frac{\lambda}{2m} \sum_{l=1}^{L-1} \sum_{i=1}^{s_l} \sum_{j=1}^{s_{l+1}} (\Theta_{ji}^{(l)})^2$$

regularization

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Gradient computation

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$$J(\Theta) = -\frac{1}{m} \left[\sum_{i=1}^m \sum_{k=1}^K y_k^{(i)} \log h_{\theta}(x^{(i)})_k + (1 - y_k^{(i)}) \log(1 - h_{\theta}(x^{(i)})_k) \right]$$

$$+ \frac{\lambda}{2m} \sum_{l=1}^{L-1} \sum_{i=1}^{s_l} \sum_{j=1}^{s_{l+1}} (\Theta_j^{(l)})^2$$

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$$\min_{\Theta} J(\Theta)$$

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Use “Backpropagation algorithm”

Need code to compute:

- $J(\Theta)$
- $\frac{\partial}{\partial \Theta_{ij}^{(l)}} J(\Theta)$

- Efficient way to compute $\frac{\partial}{\partial \Theta_{ij}^{(l)}} J(\Theta)$
- Computes gradient incrementally by “propagating” backwards through the network



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Neural Networks II

backpropagation

Chain Rule

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- Need to compute gradient of

$$\log(h_{\Theta}(x)) = \log(g(\Theta^{(2)}g(\Theta^{(1)}x))) \quad \text{w.r.t } \Theta$$

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- How can we compute the gradient of several chained functions?

$$f(\theta) = f_1(f_2(\theta)) \quad f'(\theta) = f_1'(f_2(\theta)) * f_2'(\theta)$$

$$f(\theta) = f_1(f_2(f_3(\theta))) \quad f'(\theta) =$$

- What about functions of multiple variables?

$$f(\theta_1, \theta_2) = f_1(f_2(\theta_1, \theta_2)) \quad \frac{\partial f}{\partial \theta_1} = \quad \frac{\partial f}{\partial \theta_2} =$$

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Backpropagation: Efficient Chain Rule

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- Partial gradient computation via chain rule:

$$\frac{\partial f}{\partial \theta_1} = \frac{\partial f_1}{\partial f_2} (f_2(f_3(\theta))) * \frac{\partial f_2}{\partial f_3} (f_3(\theta)) * \frac{\partial f_3}{\partial \theta_1} (\theta)$$

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$$\frac{\partial f}{\partial \theta_2} = \frac{\partial f_1}{\partial f_2} (f_2(f_3(\theta))) * \frac{\partial f_2}{\partial f_3} (f_3(\theta)) * \frac{\partial f_3}{\partial \theta_2} (\theta)$$

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$$\frac{\partial f}{\partial \theta_3} = \frac{\partial f_1}{\partial f_2} (f_2(f_3(\theta))) * \frac{\partial f_2}{\partial f_3} (f_3(\theta)) * \frac{\partial f_3}{\partial \theta_3} (\theta)$$

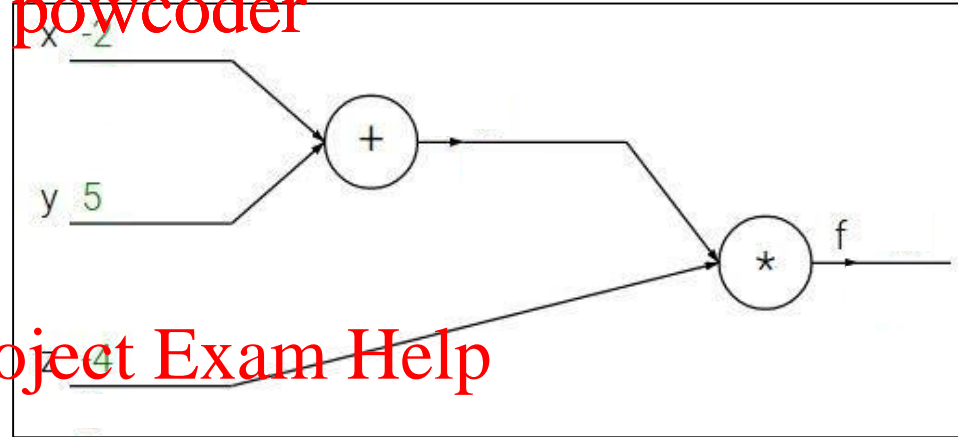
- need to re-evaluate functions many times
- Very inefficient! E.g. 100,000-dim parameters

Chain Rule with a Computational Graph

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$$f(x, y, z) = (x + y)z$$

e.g. $x = -2, y = 5, z = -4$



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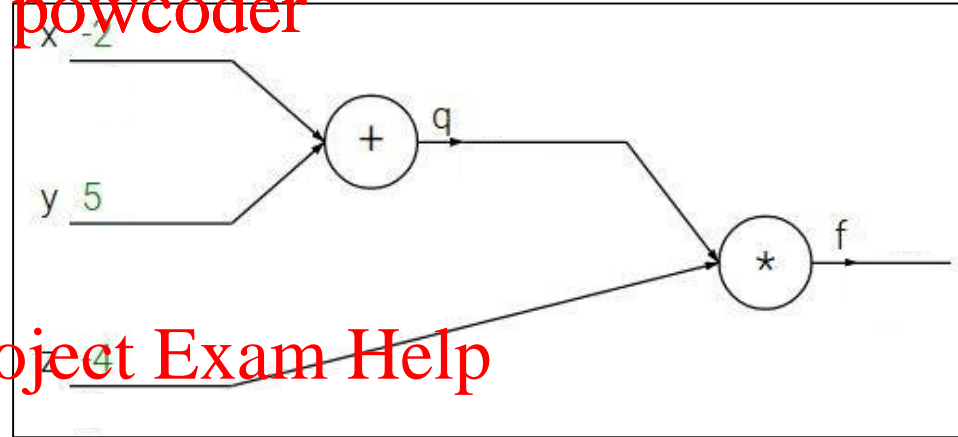
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Chain Rule with a Computational Graph

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$$q = x + y \quad \frac{\partial q}{\partial x} = 1, \frac{\partial q}{\partial y} = 1$$

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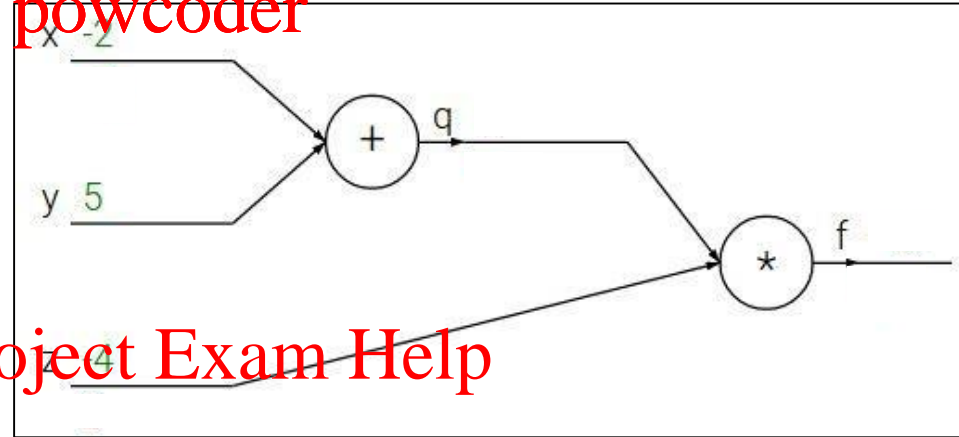
Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

Computation Graph: Forward

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e.g. $x = -2, y = 5, z = -4$



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<https://powcoder.com> compute values

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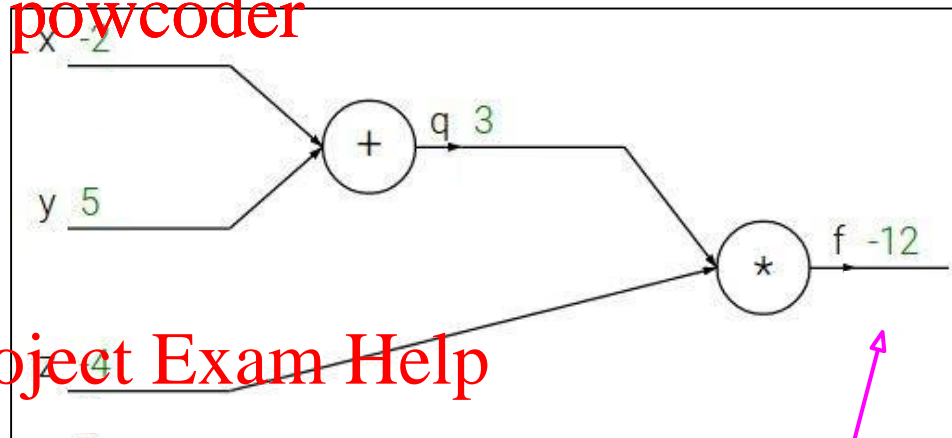
Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

Computation Graph: Backward

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compute gradients

Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

$$\frac{\partial f}{\partial f}$$

Computation Graph: Backward

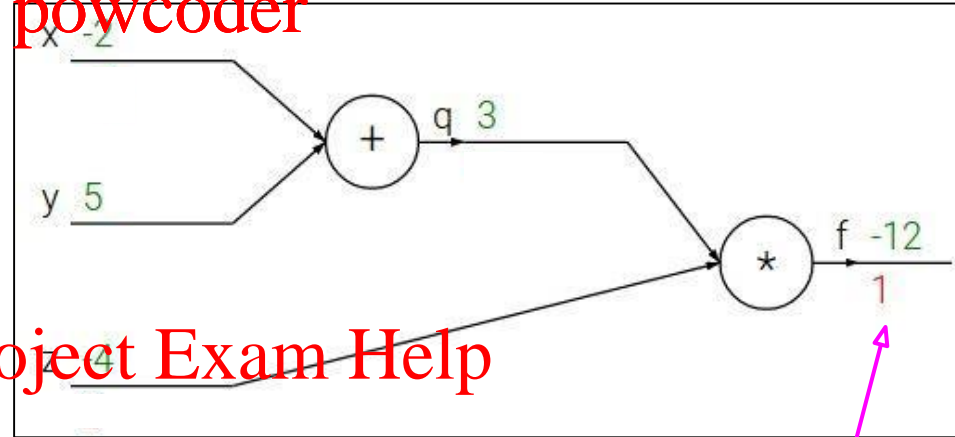
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Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

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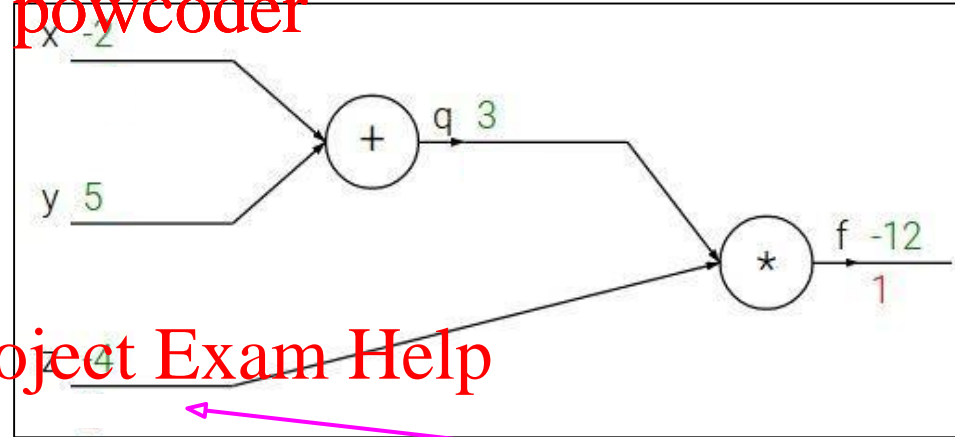
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Computation Graph: Backward

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$$\frac{\partial f}{\partial z}$$

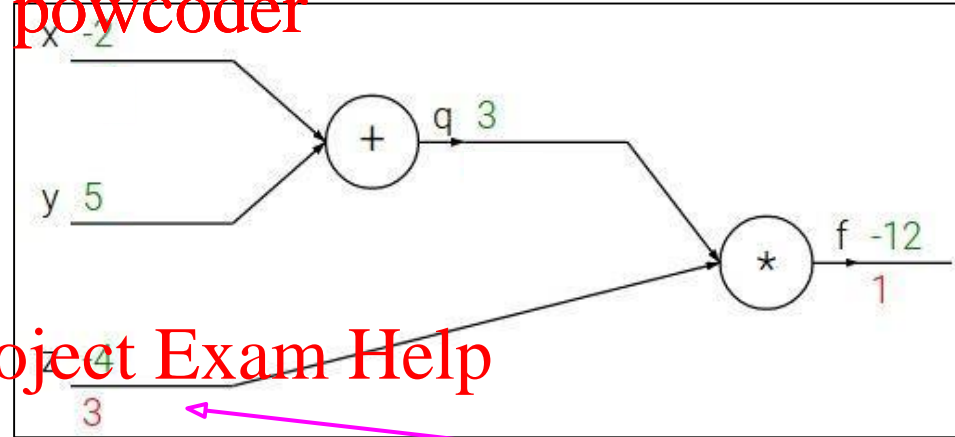
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Computation Graph: Backward

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$$\frac{\partial f}{\partial z}$$

Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

Computation Graph: Backward

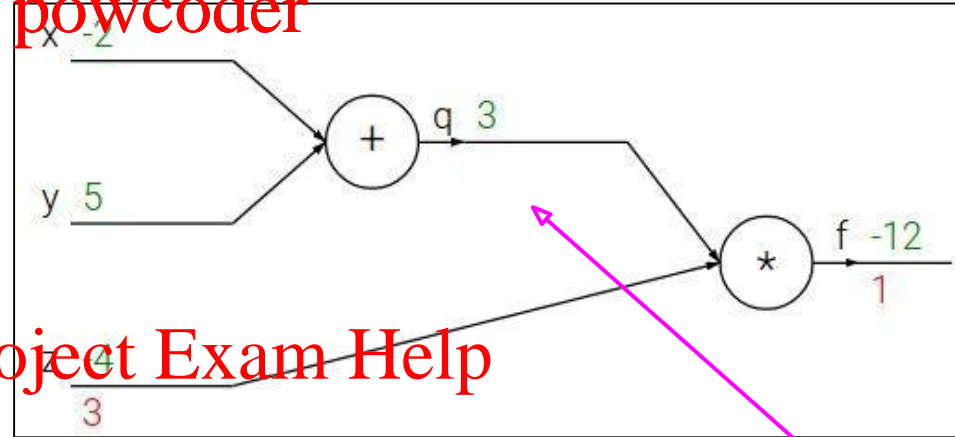
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$$\frac{\partial f}{\partial q}$$

Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

Computation Graph: Backward

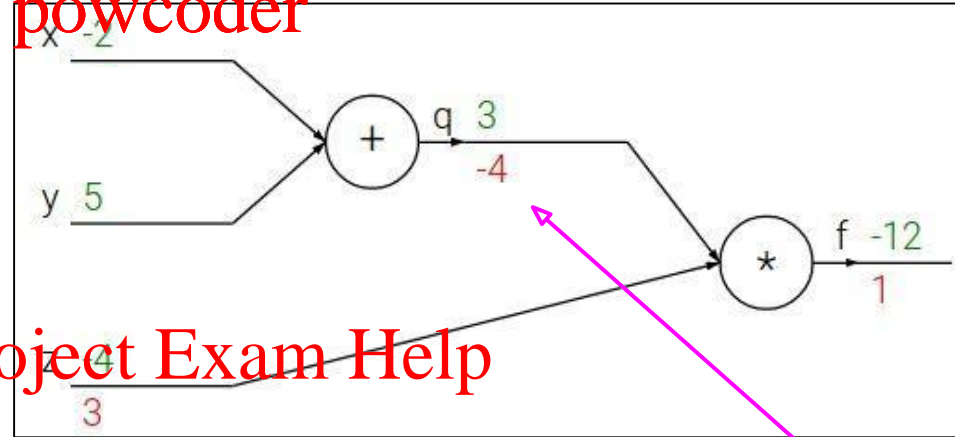
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$$\frac{\partial f}{\partial q}$$

Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

Computation Graph: Backward

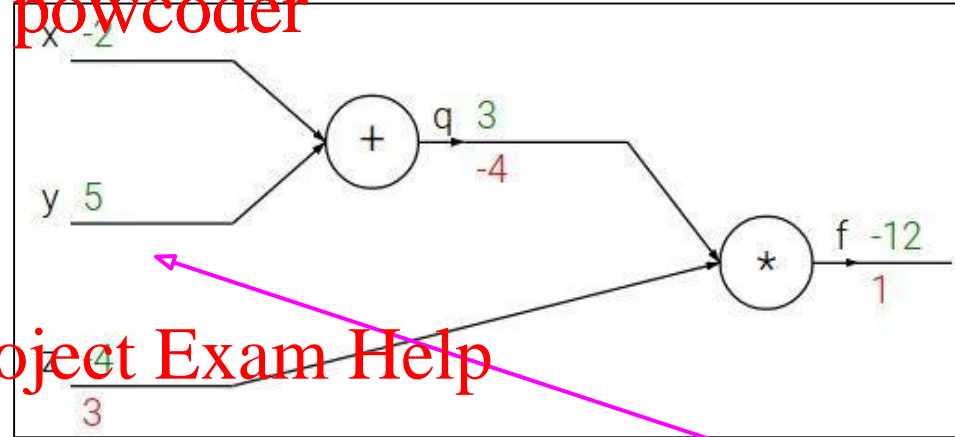
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$$\frac{\partial f}{\partial y}$$

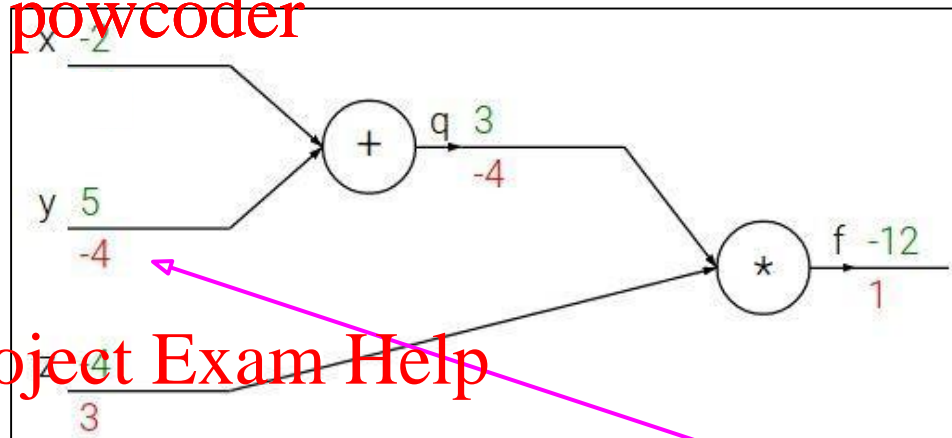
Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

Computation Graph: Backward

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Chain rule:

$$\frac{\partial f}{\partial y} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial y}$$

$$\frac{\partial f}{\partial y}$$

Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

Computation Graph: Backward

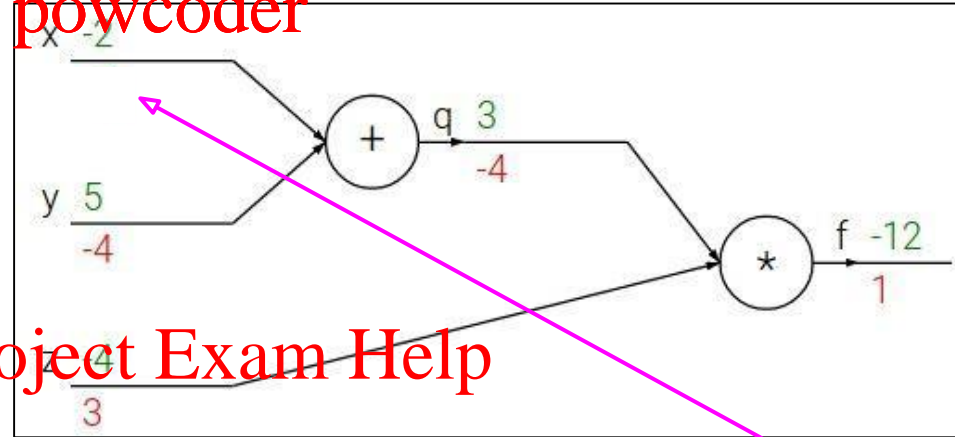
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$$\frac{\partial f}{\partial x}$$

Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$

Computation Graph: Backward

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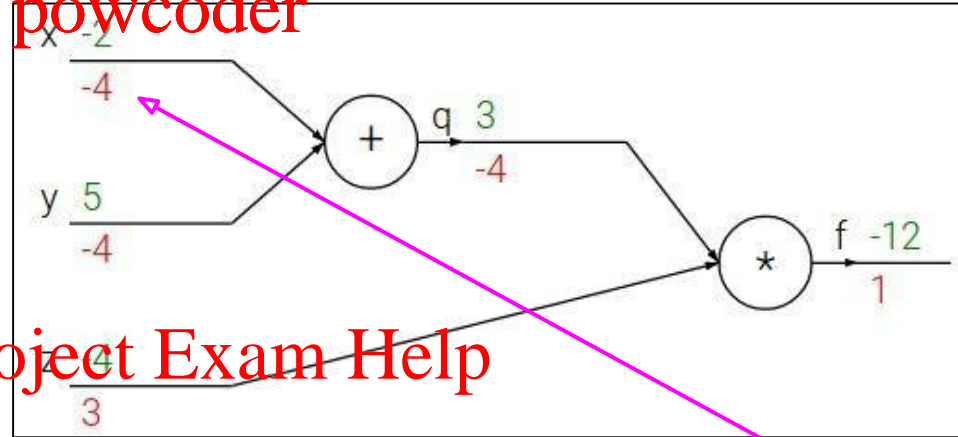
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Want: $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$



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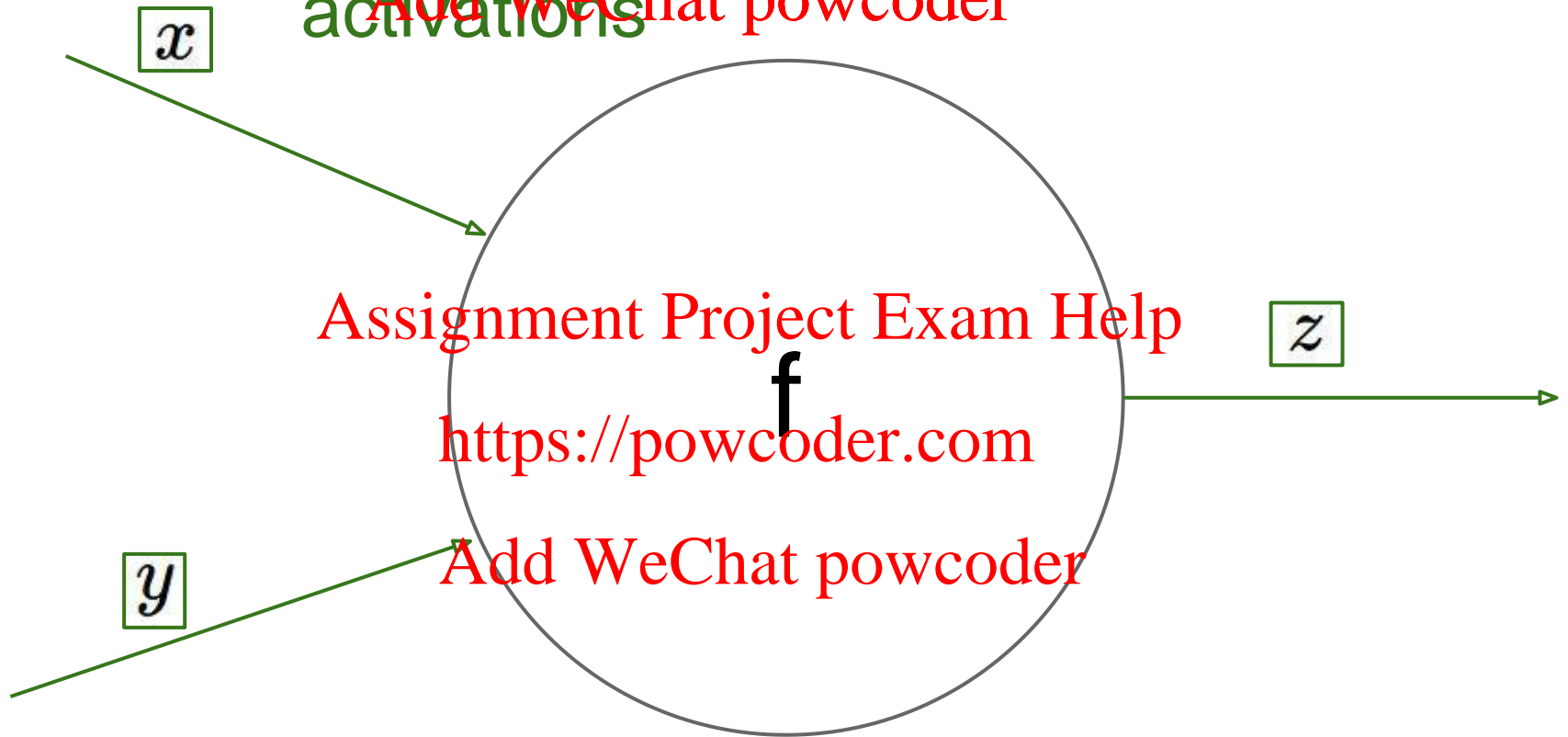
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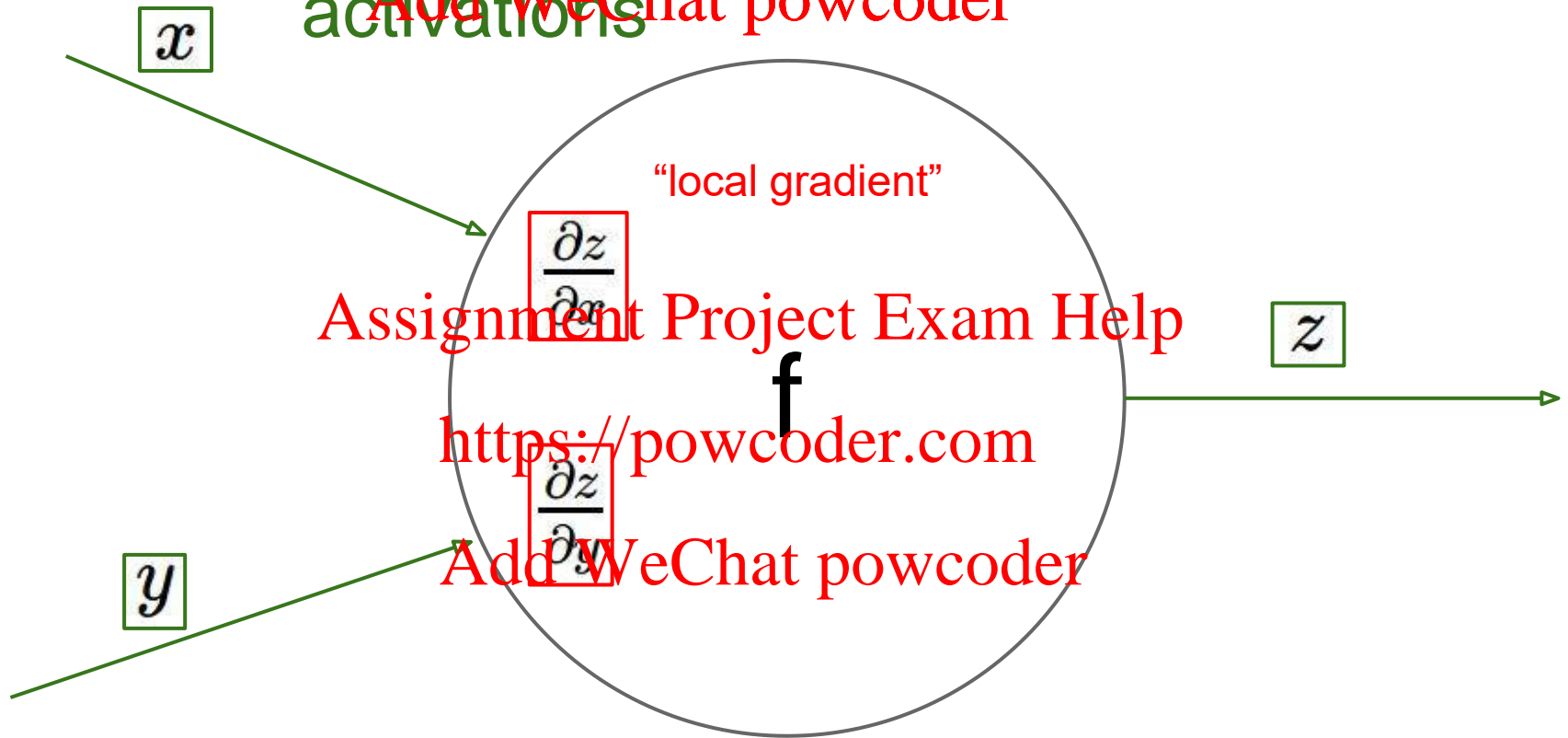
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activations



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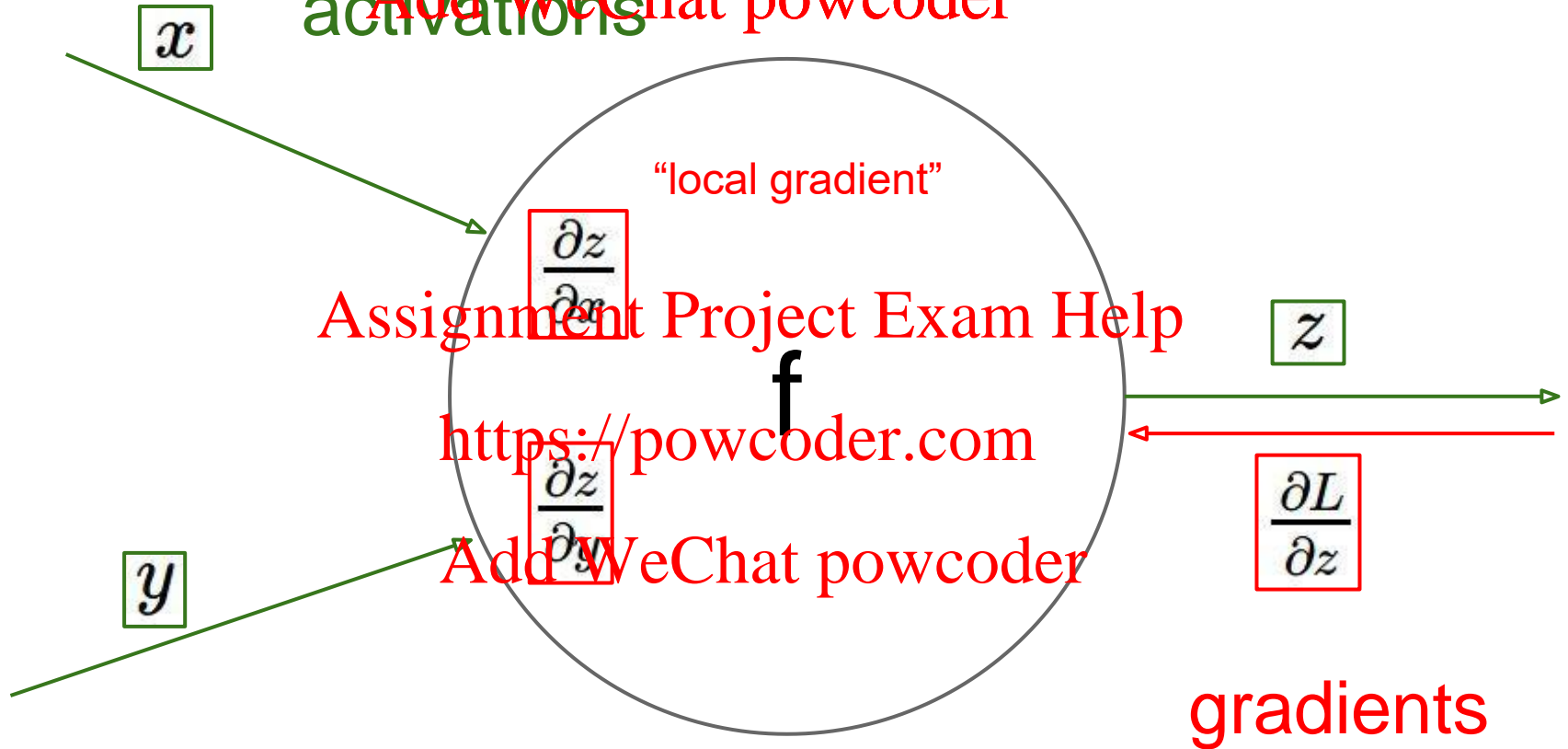
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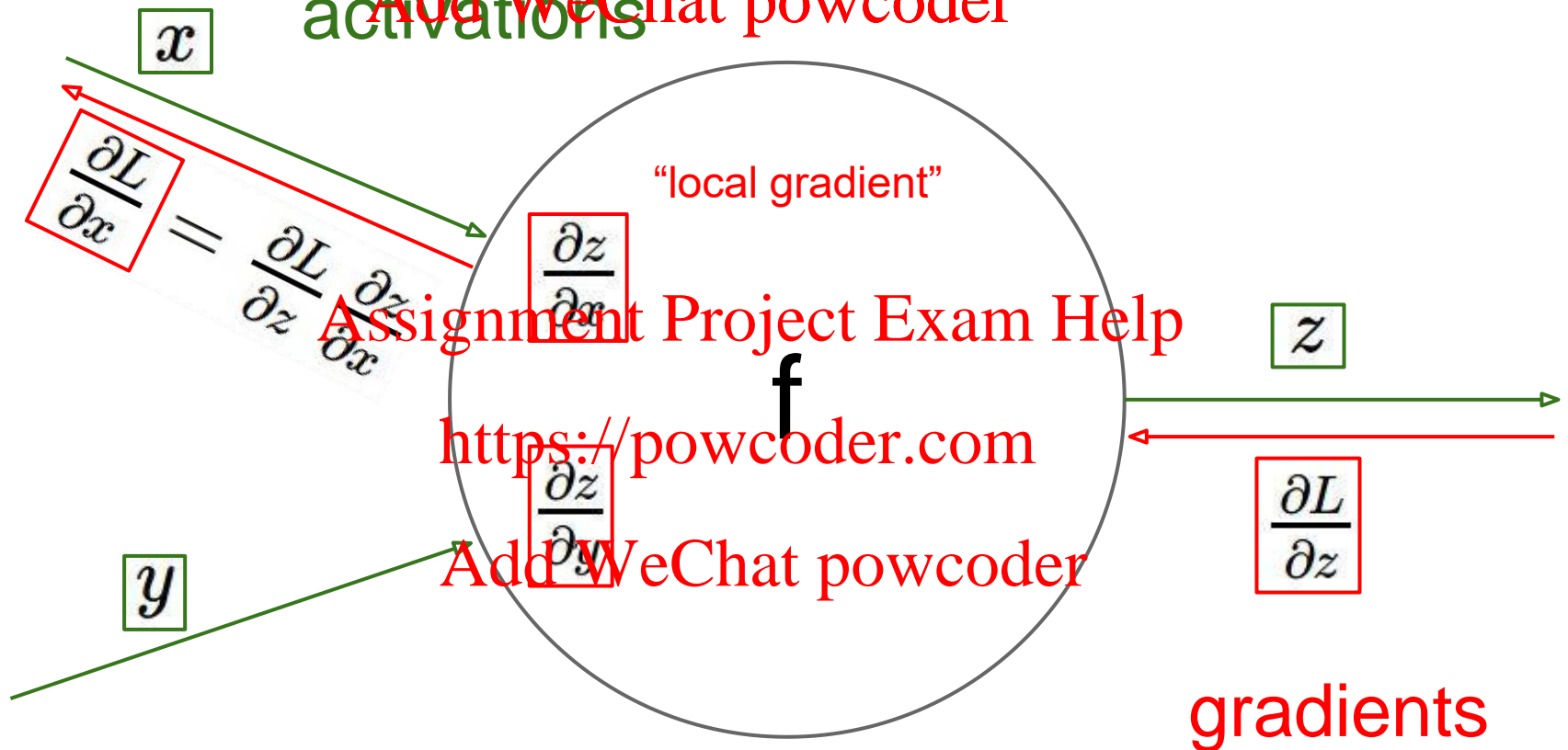
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activations



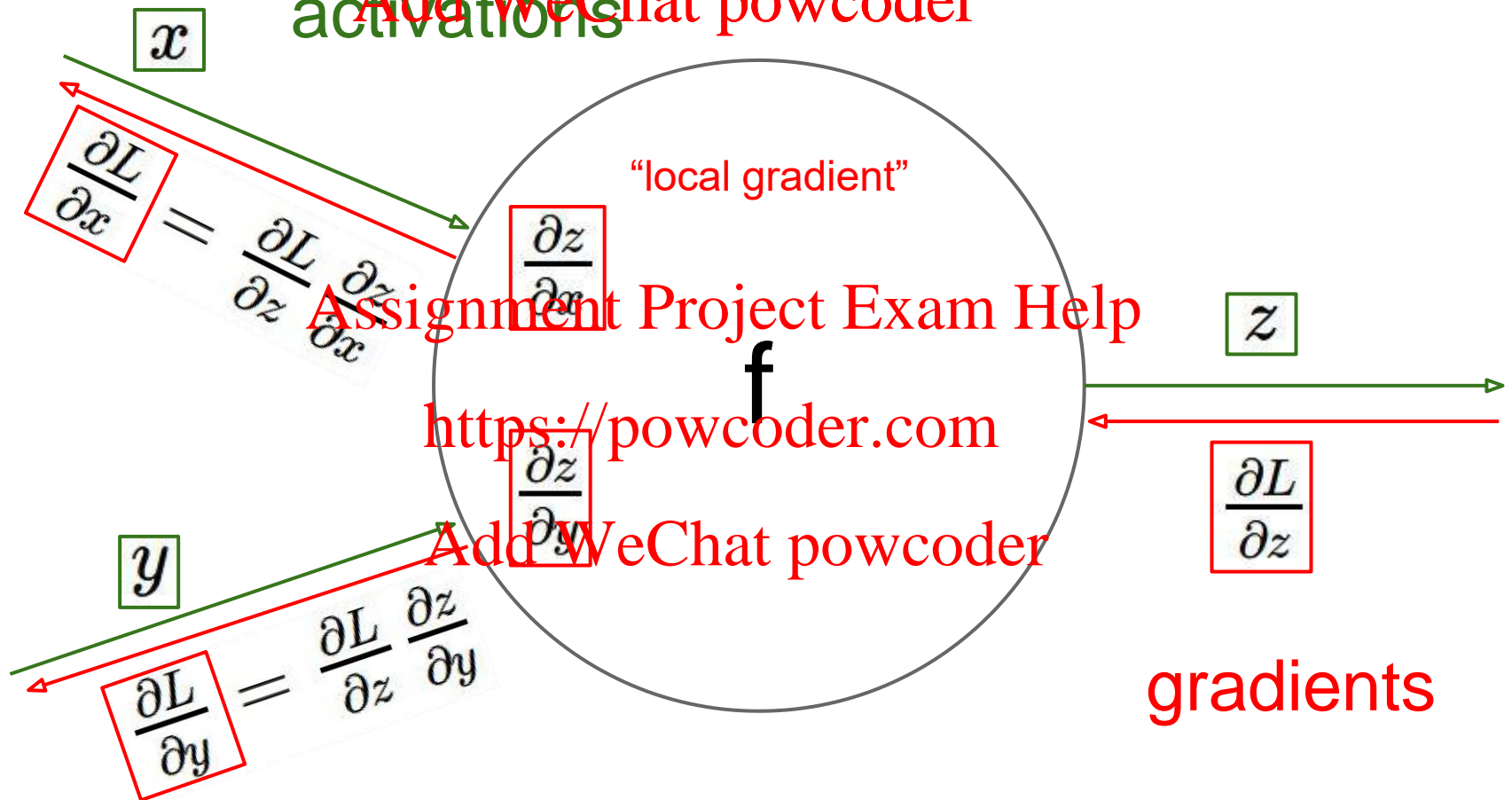
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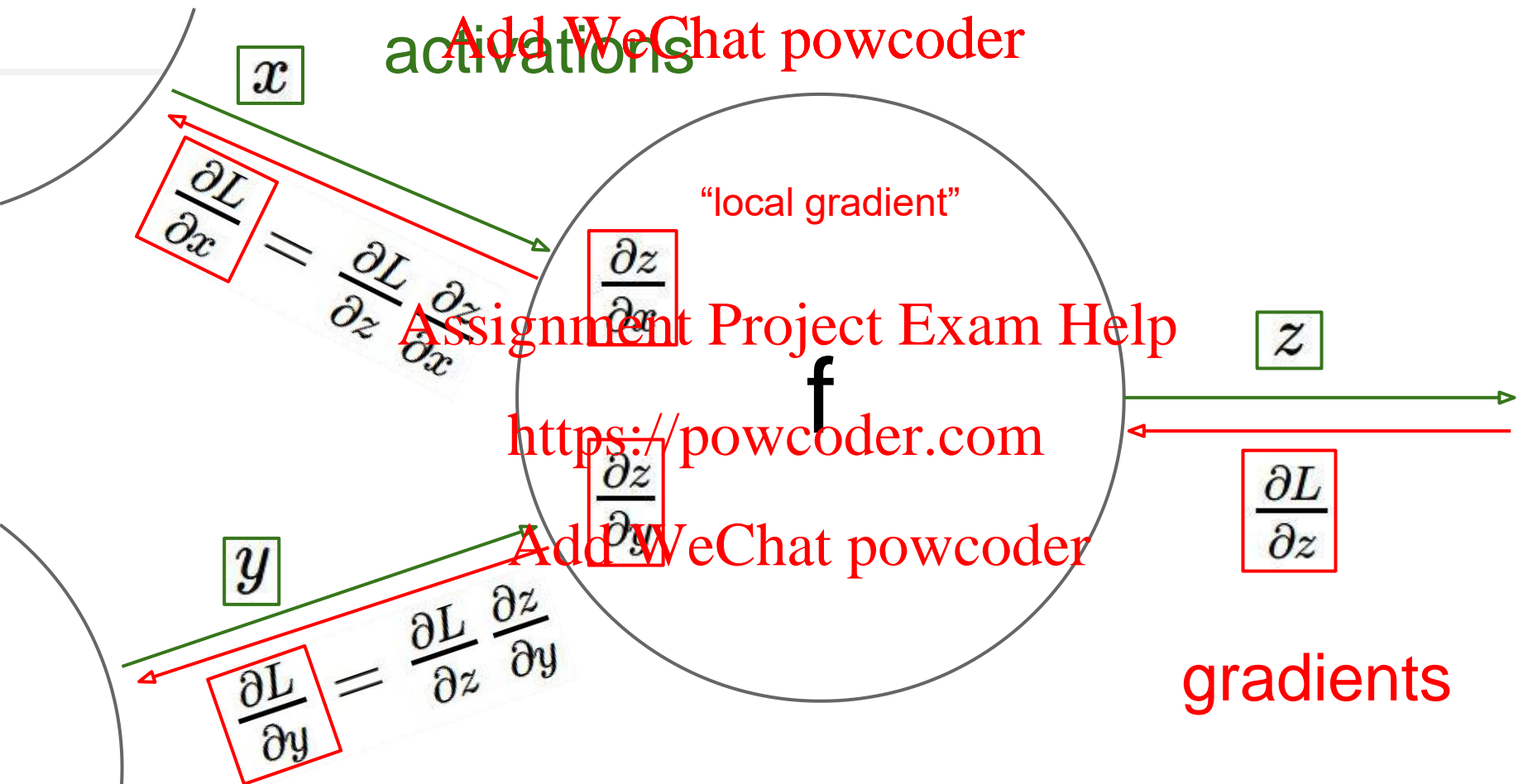
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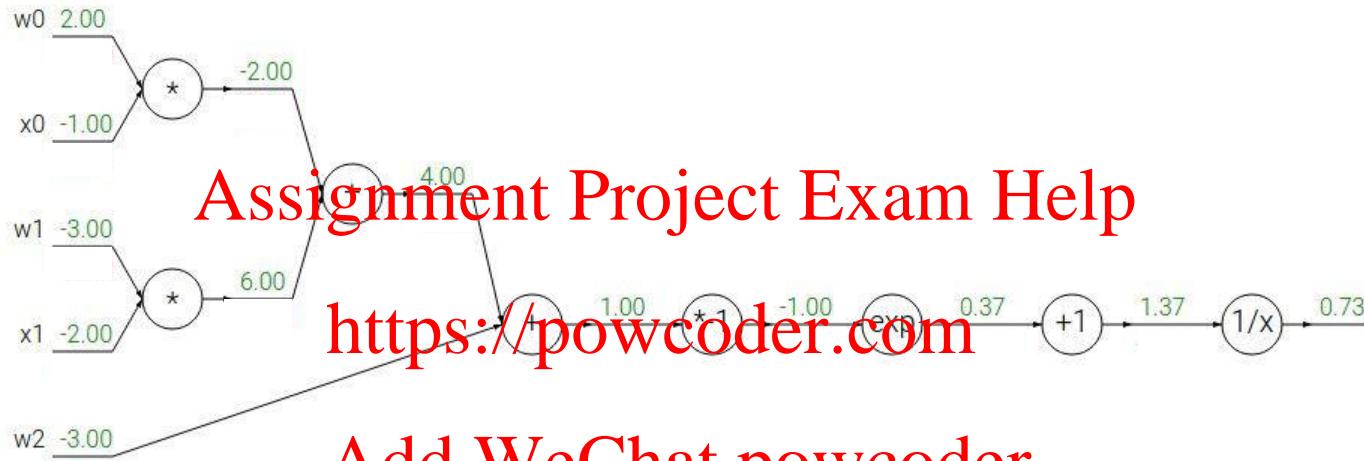
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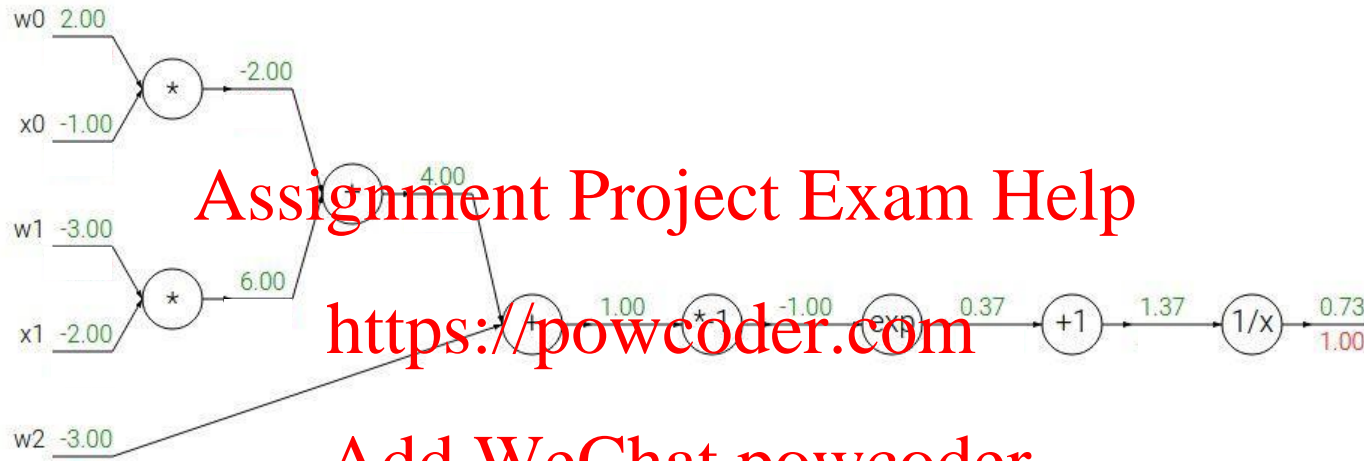
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Another example: $f(w, x) = \frac{1}{1 + e^{-(w_0x_0 + w_1x_1 + w_2)}}$



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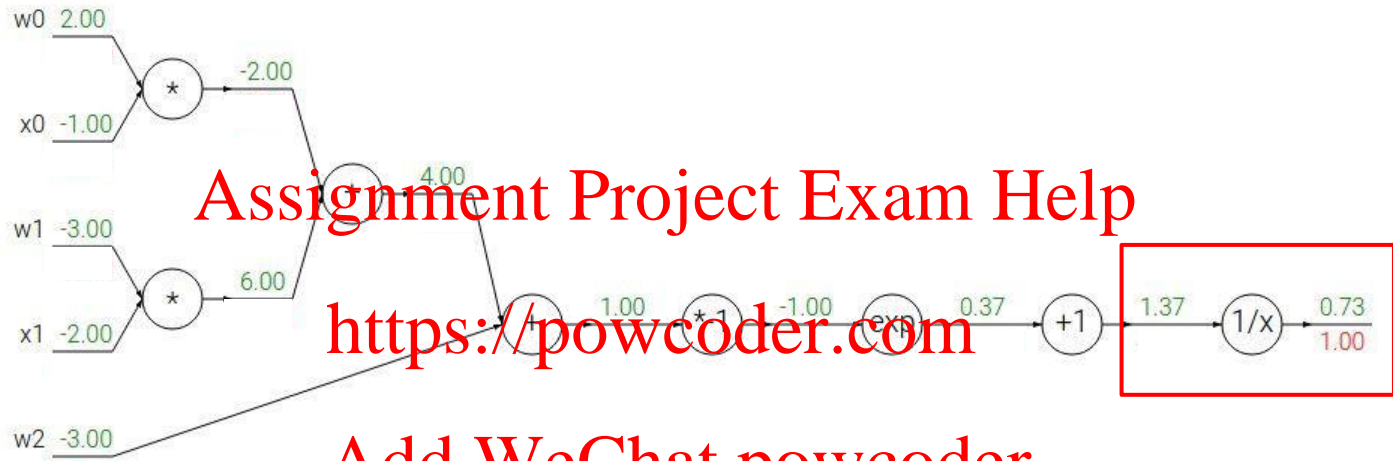
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$$\begin{array}{lcl}
 f(x) = e^x & \rightarrow & \frac{df}{dx} = e^x \\
 f_a(x) = ax & \rightarrow & \frac{df}{dx} = a
 \end{array}
 \quad \Bigg| \quad
 \begin{array}{lcl}
 f(x) = \frac{1}{x} & \rightarrow & \frac{df}{dx} = -1/x^2 \\
 f_c(x) = c + x & \rightarrow & \frac{df}{dx} = 1
 \end{array}$$

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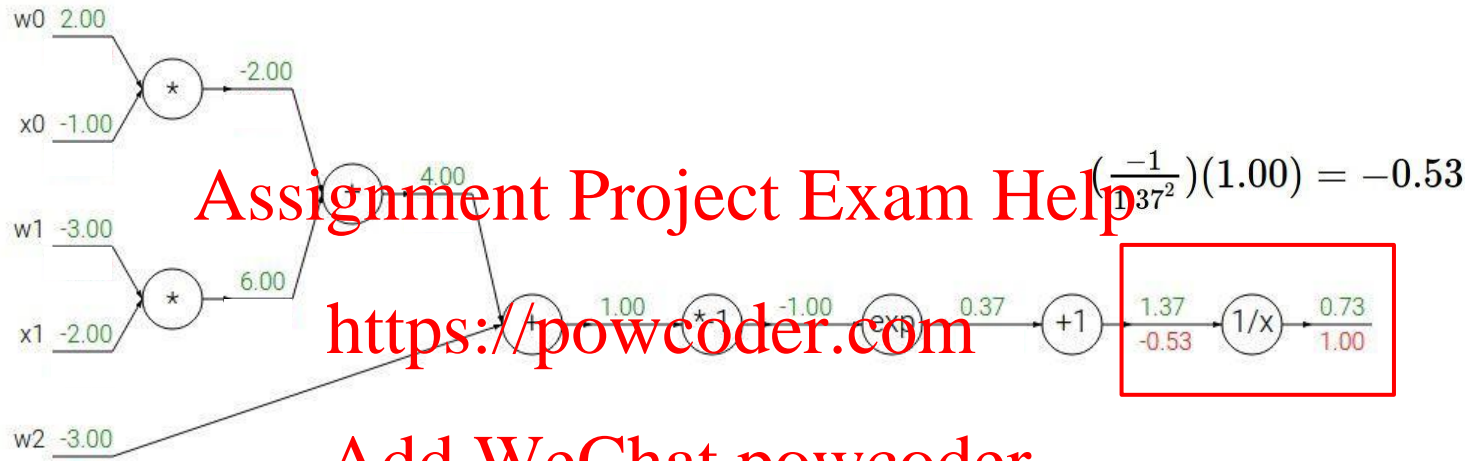
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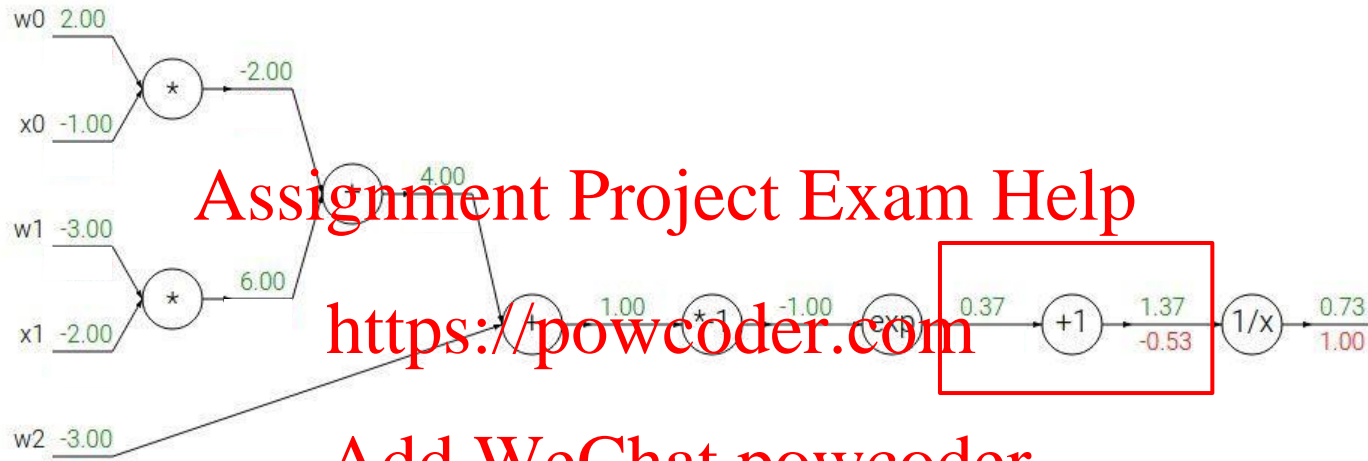


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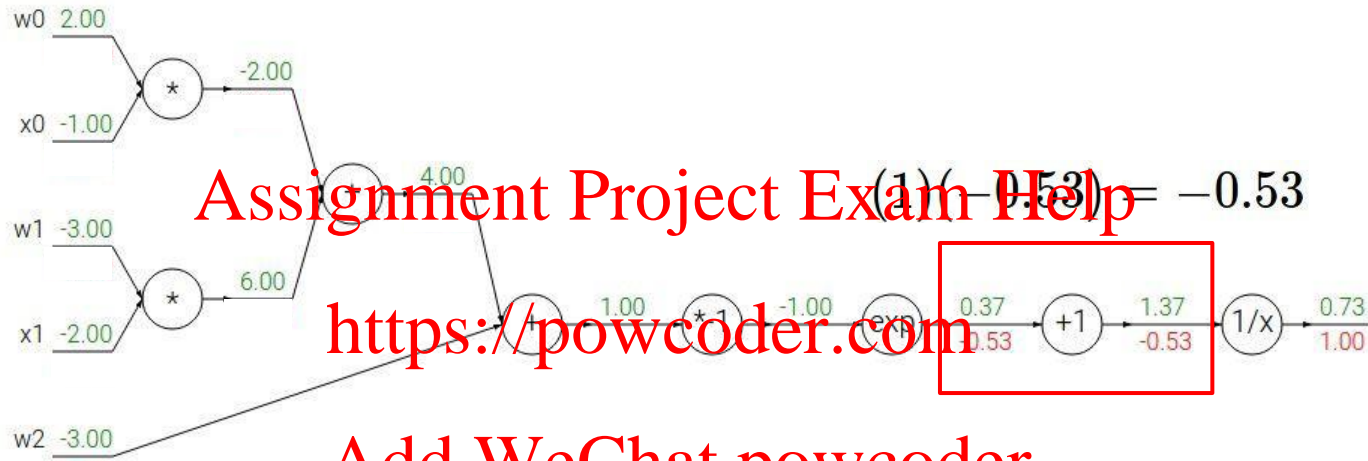
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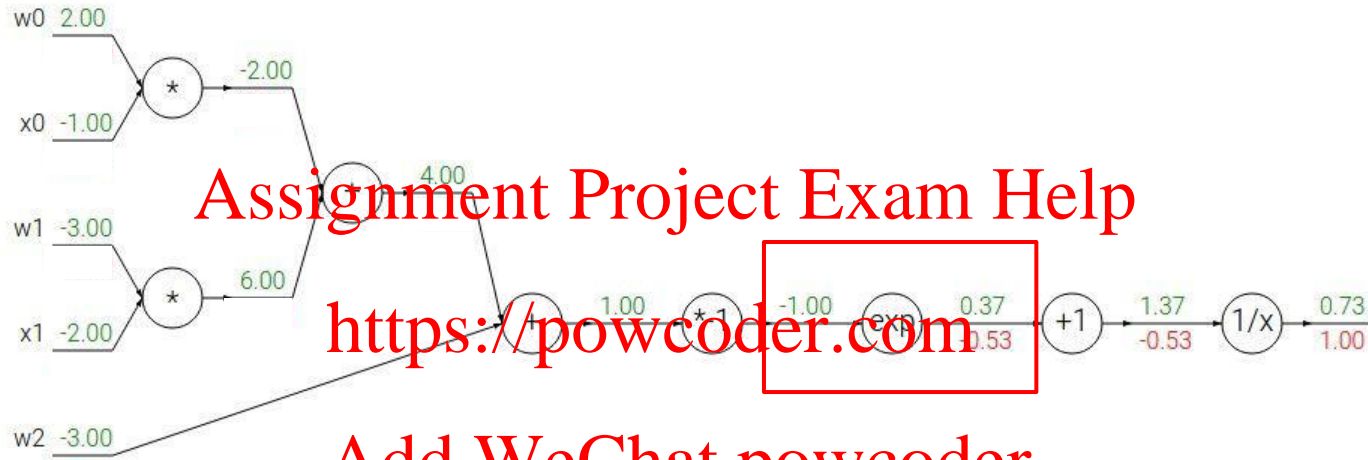


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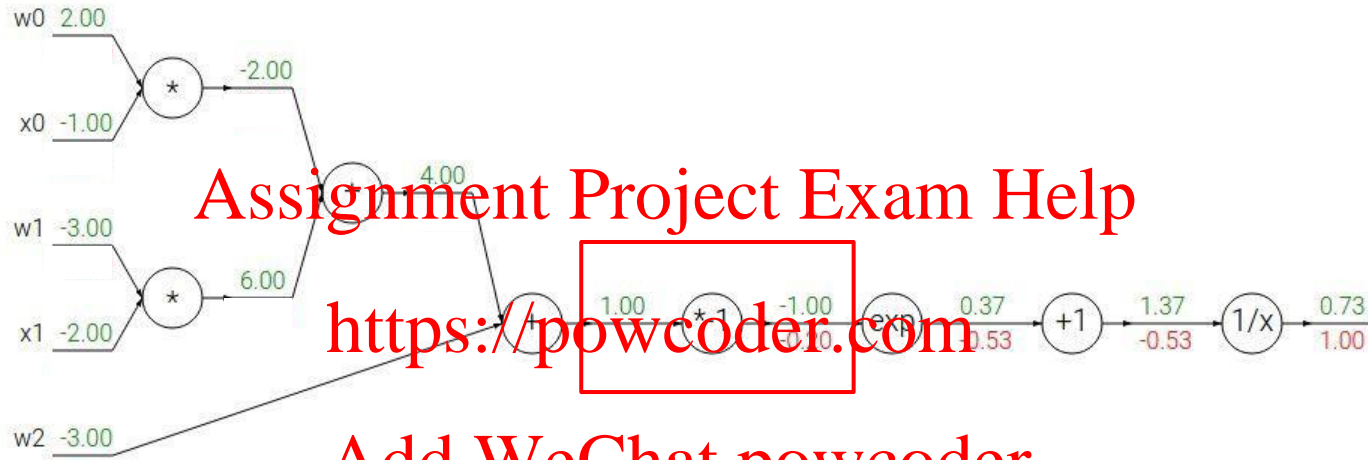
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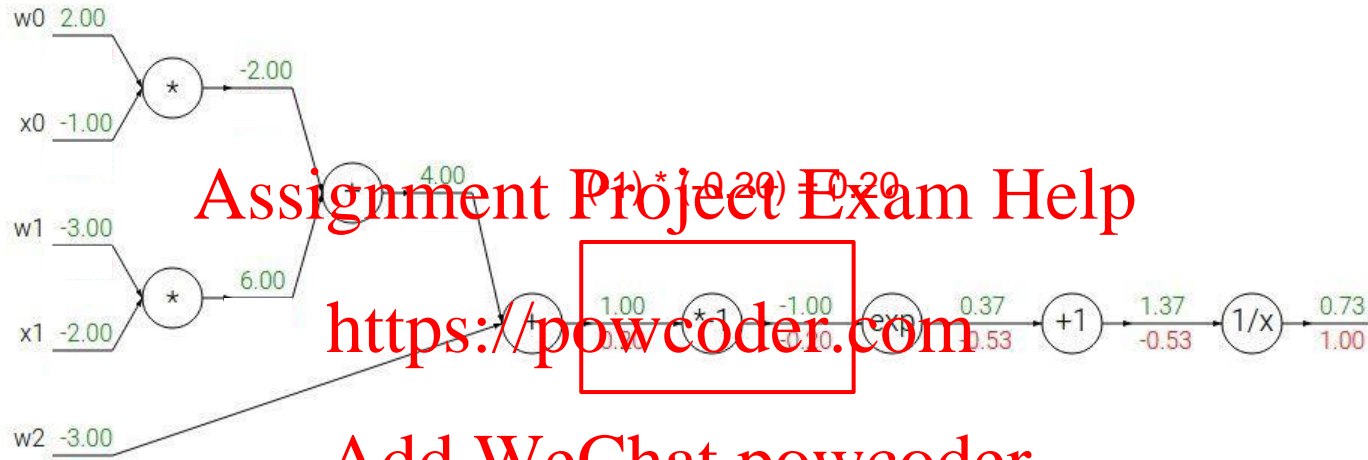


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$f(x) = e^x$	\rightarrow	$\frac{df}{dx} = e^x$		$f(x) = \frac{1}{x}$	\rightarrow	$\frac{df}{dx} = -1/x^2$
$f_a(x) = ax$	\rightarrow	$\frac{df}{dx} = a$		$f_c(x) = c + x$	\rightarrow	$\frac{df}{dx} = 1$

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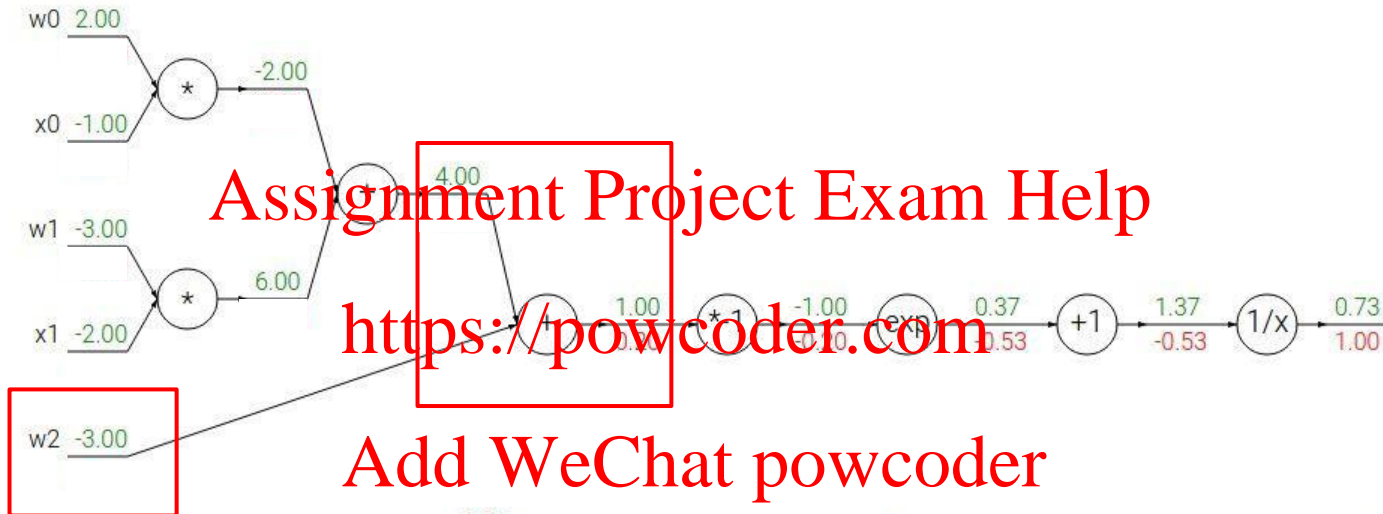


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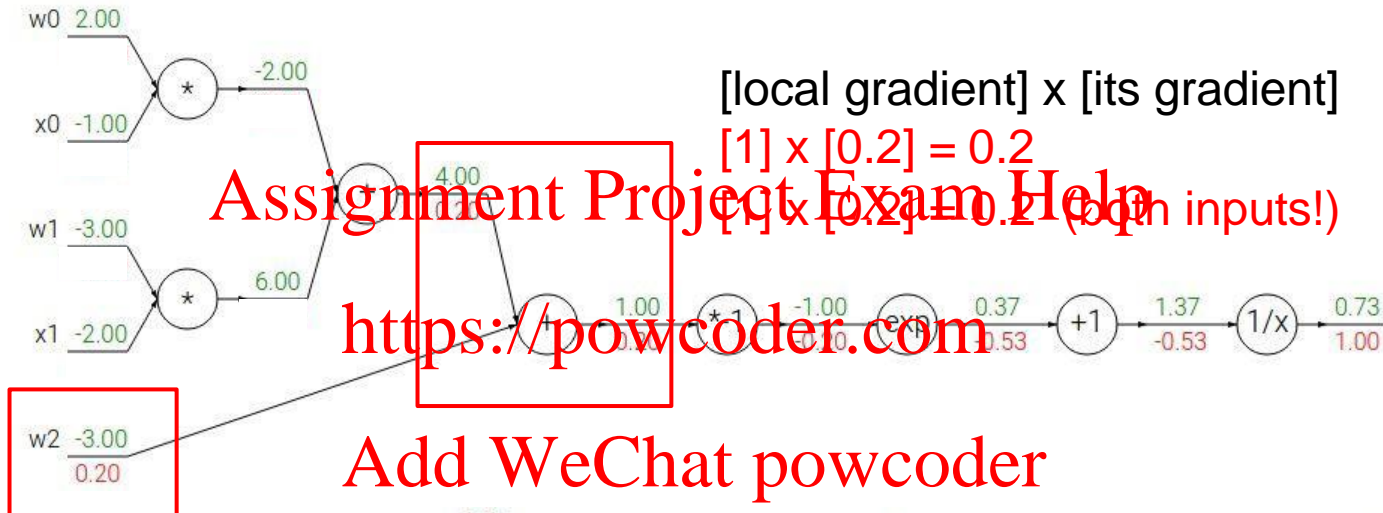
$$\begin{array}{lcl}
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 \end{array}
 \quad \Bigg| \quad
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Another example:

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$$f(x) = e^x$$

→

$$\frac{df}{dx} = e^x$$

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→

$$\frac{df}{dx} = a$$

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→

$$\frac{df}{dx} = -1/x^2$$

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→

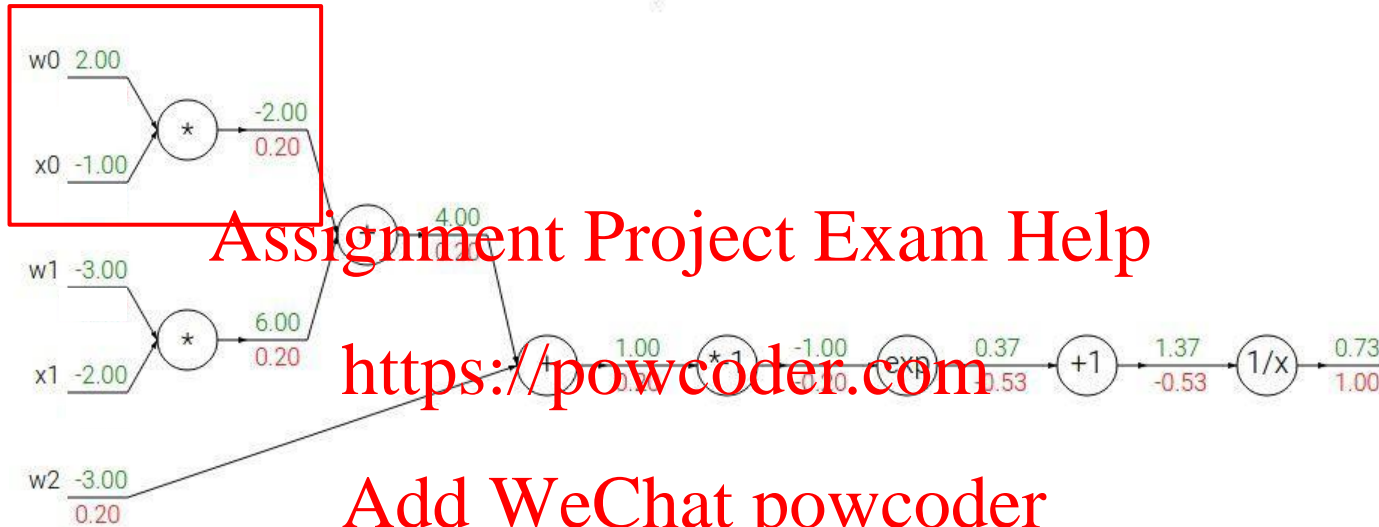
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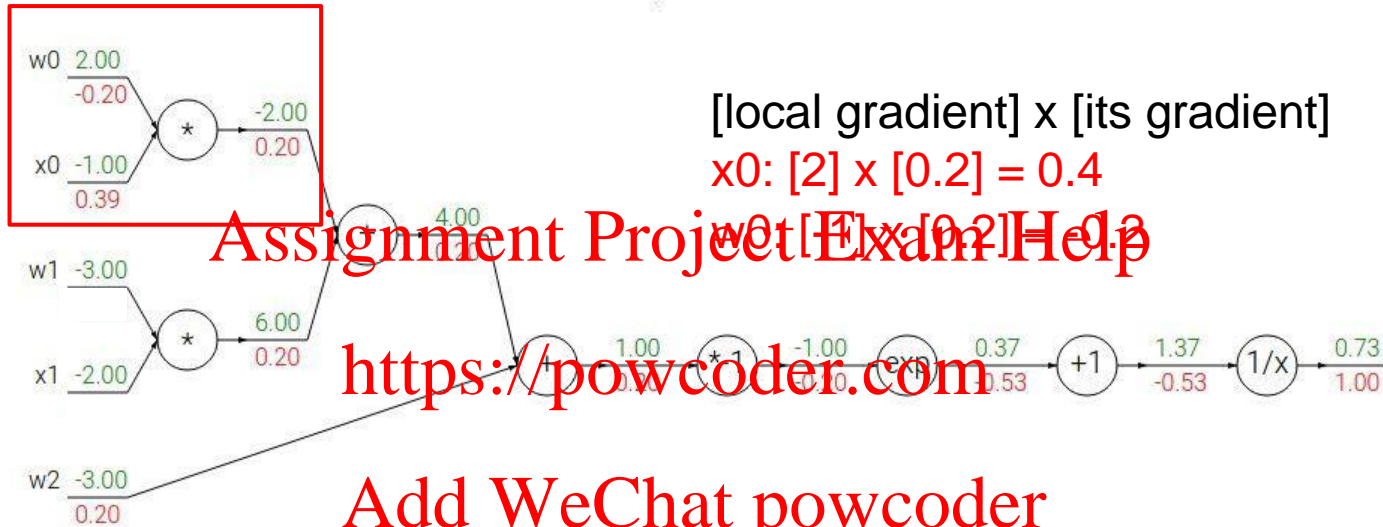
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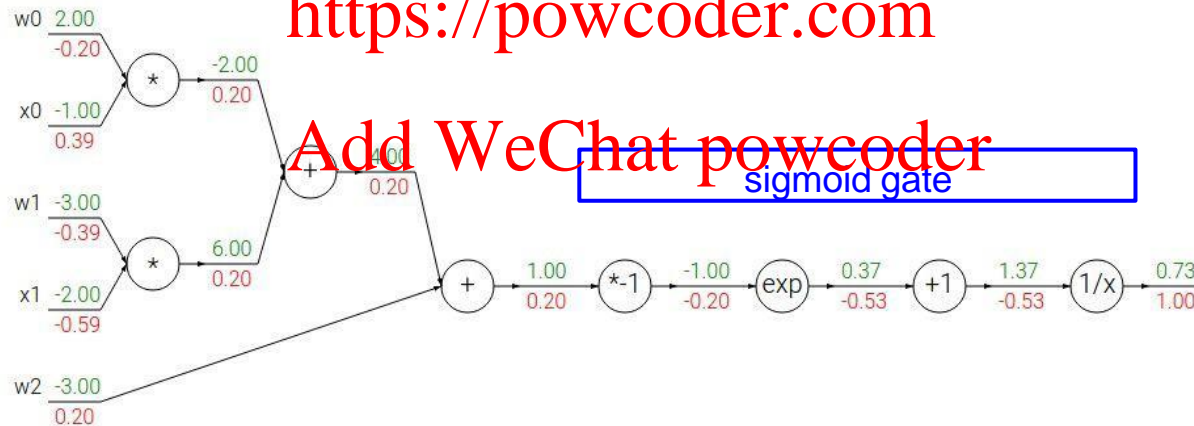
$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

sigmoid function

$$\frac{d\sigma(x)}{dx} = \frac{e^{-x}}{(1 + e^{-x})^2} = \left(\frac{1 + e^{-x} - 1}{1 + e^{-x}} \right) \left(\frac{1}{1 + e^{-x}} \right) = (1 - \sigma(x)) \sigma(x)$$

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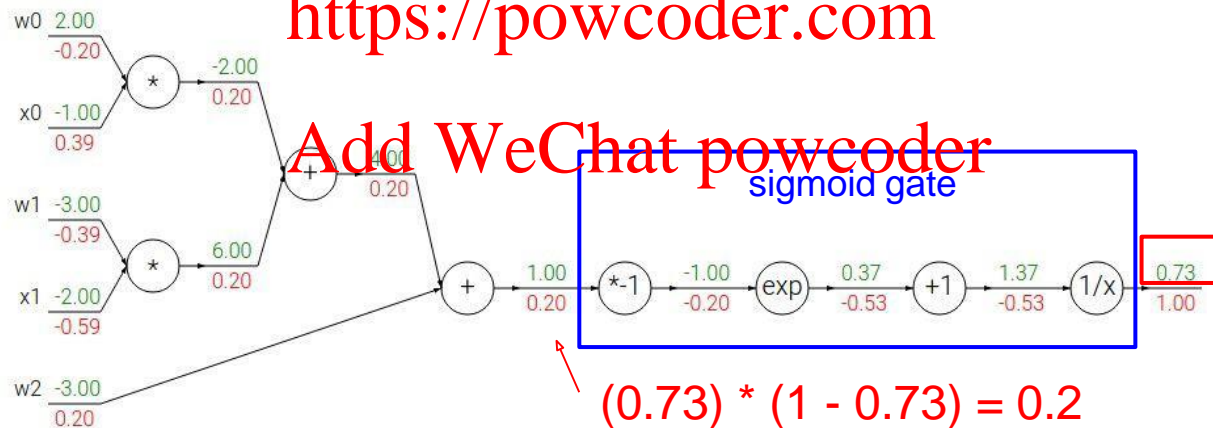
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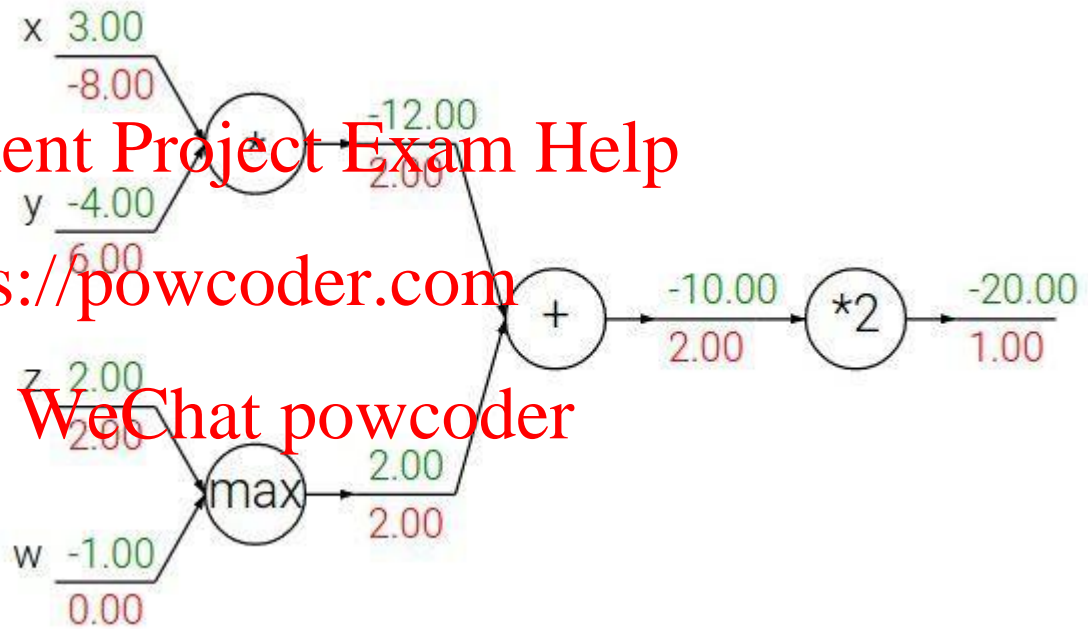
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Patterns in backward flow

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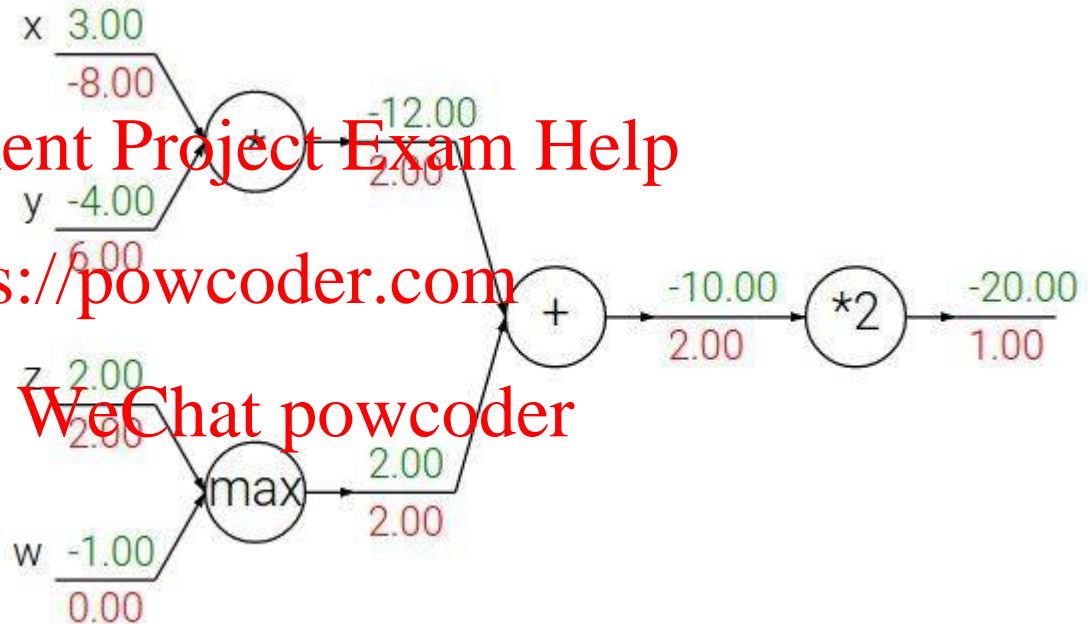
Patterns in backward flow

add gate: gradient distributor

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Patterns in backward flow

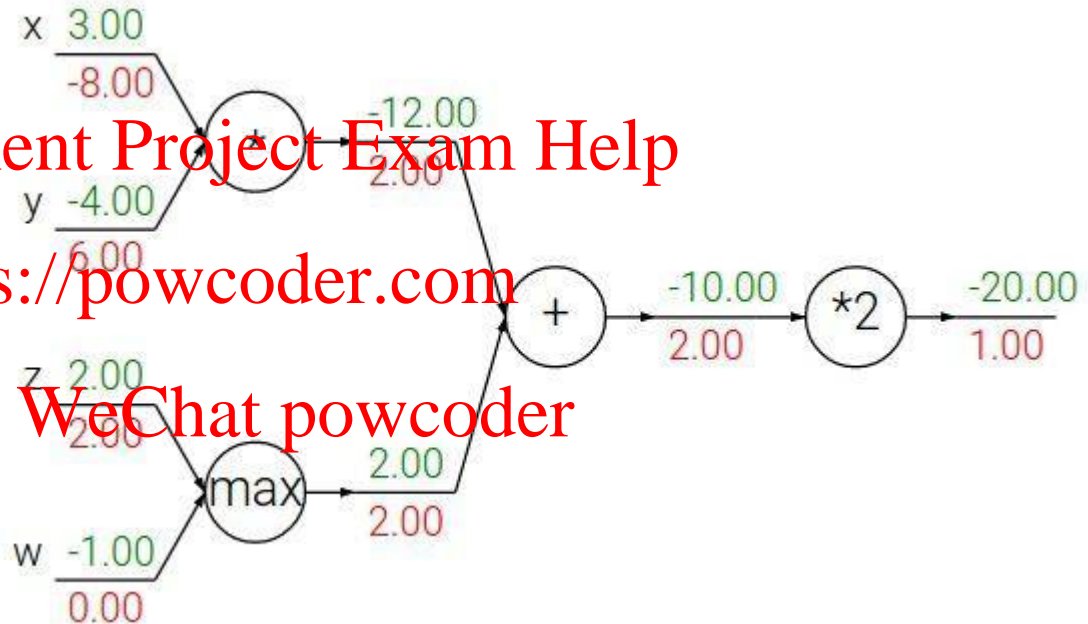
add gate: gradient distributor

max gate: gradient router

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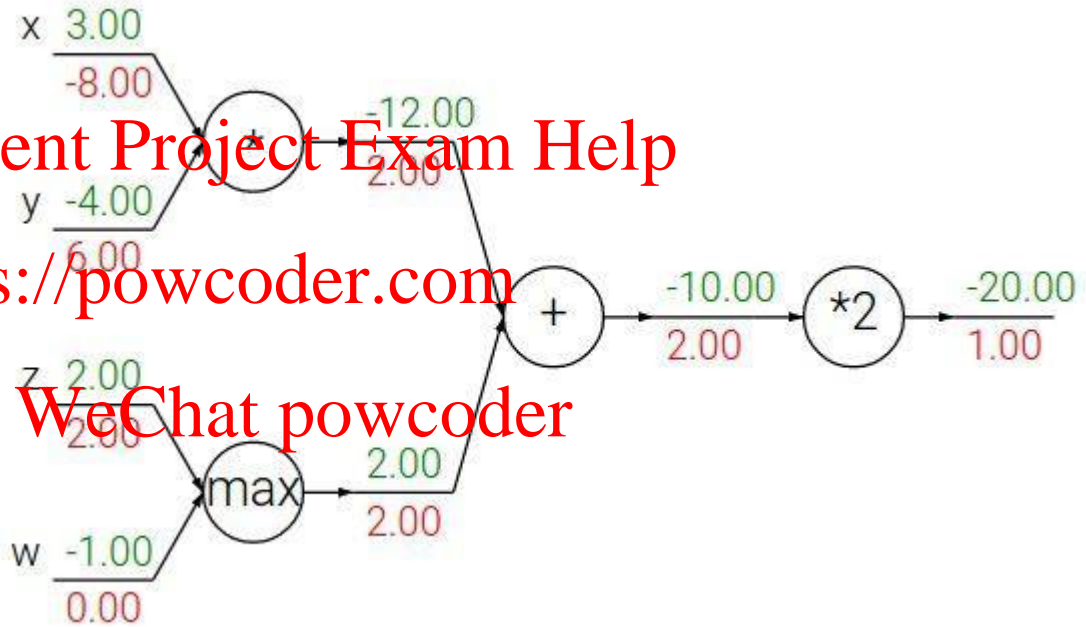
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Patterns in backward flow

add gate: gradient distributor

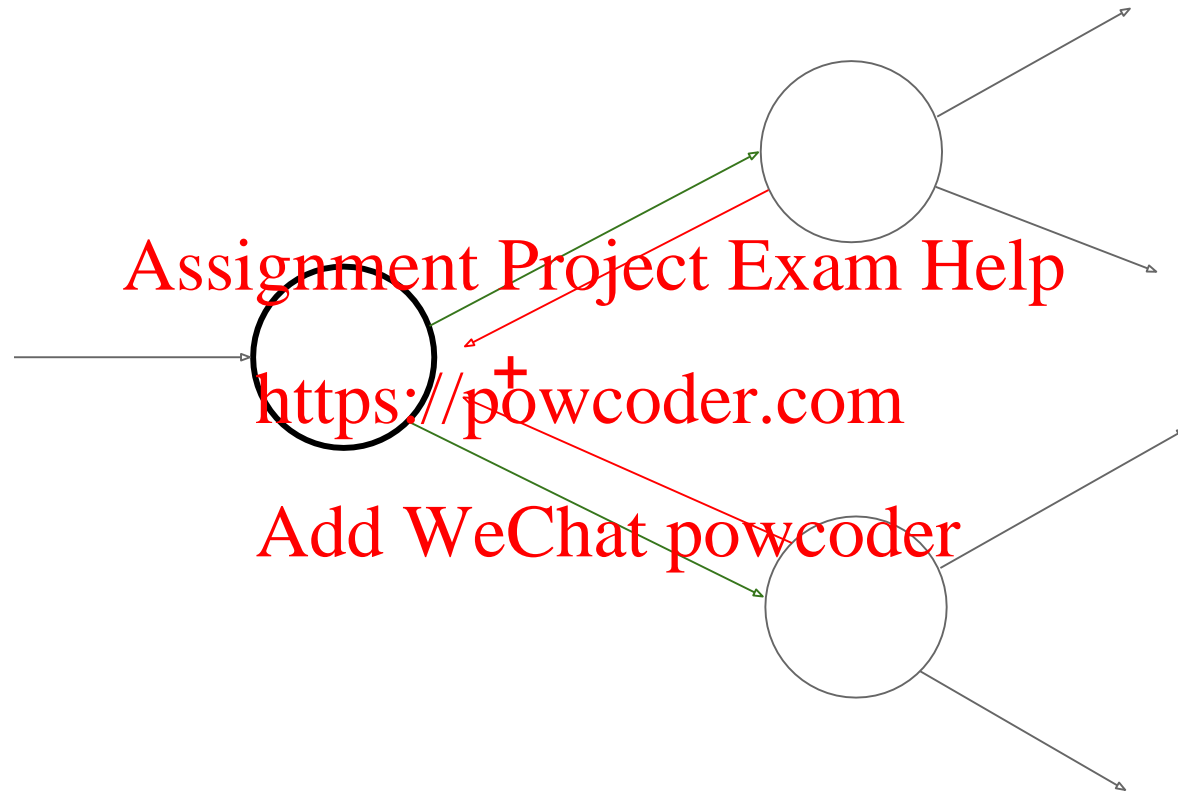
max gate: gradient router

mul gate: gradient... "switcher"?



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Gradients add at branches





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Neural Networks II

Vectorized Backpropagation

Forward Pass

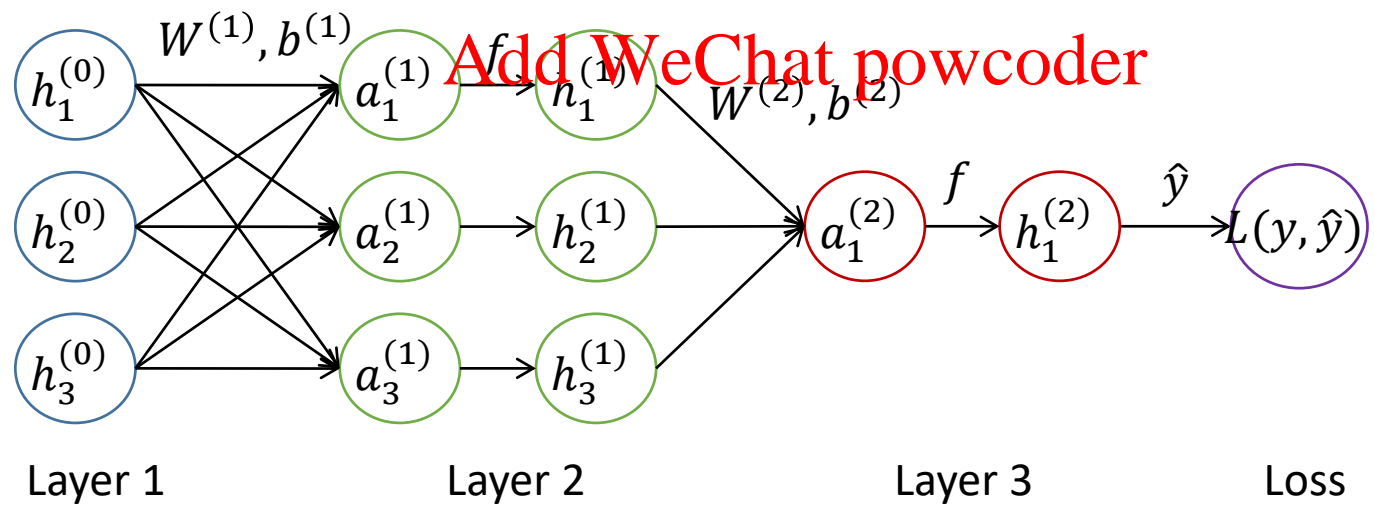
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- Require: Network depth, l
- Require: $W^{(i)}, i \in \{1, \dots, l\}$, the weight matrices of the model
- Require: $b^{(i)}, i \in \{1, \dots, l\}$, the bias parameters of the model
- Require: x , the input to process
- Require: y , the target output

```
h(0) = x
for k = 1, ..., l do
  a(k) = b(k) + W(k)h(k-1)
  h(k) = f(a(k))
end for
ŷ = h(l)
J = L(ŷ, y) + λΩ(θ)
```

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Backward Pass

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After the forward computation, compute the gradient on the output layer:

```
g ← ∇ŷJ = ∇ŷL(ŷ, y)
for k = l, l - 1, ..., 1 do
```

Convert the gradient on the layer's output into a gradient into the pre-nonlinearity activation (element-wise multiplication if f is element-wise):

$$g \leftarrow \nabla_{a^{(k)}} J = g \odot f'(a^{(k)})$$

Compute gradients on weights and biases (including the regularization term, where needed):

$$\nabla_{b^{(k)}} J = g + \lambda \nabla_{b^{(k)}} \Omega(\theta)$$

$$\nabla_{W^{(k)}} J = g h^{(k-1)\top} + \lambda \nabla_{W^{(k)}} \Omega(\theta)$$

Propagate the gradients w.r.t. the next lower-level hidden layer's activations:

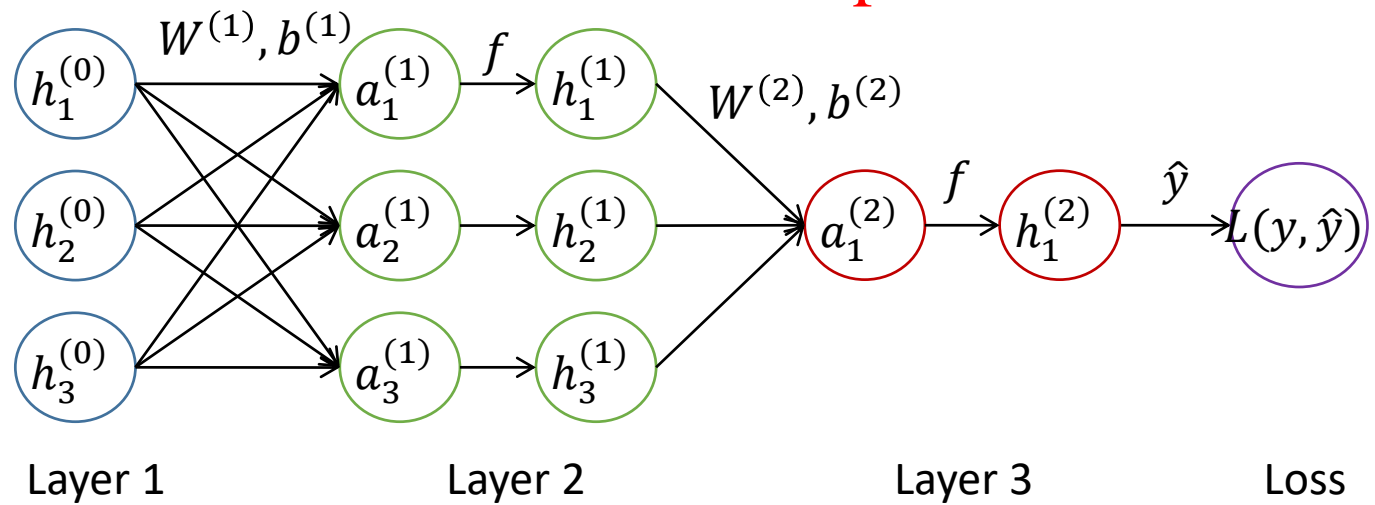
$$g \leftarrow \nabla_{h^{(k-1)}} J = W^{(k)\top} g$$

end for

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Backpropagation example with vectorized gradients:

<https://web.stanford.edu/class/cs224n/readings/gradient-notes.pdf>

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Next Class
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Neural Networks III: Convolutional Nets:

Convolutional networks.

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Reading: Bishop Ch 5.5