

Assignment Project Exam Help Announcements

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Reminder: self-grading forms for ps1 and ps2 due 10/5 at midnight (Boston)

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- ps3 out on Thursday, due 10/8 (1 week)
- LAB this week: go over solutions for the first two homeworks

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Agglomerative Clustering Example

(bottom-up clustering)

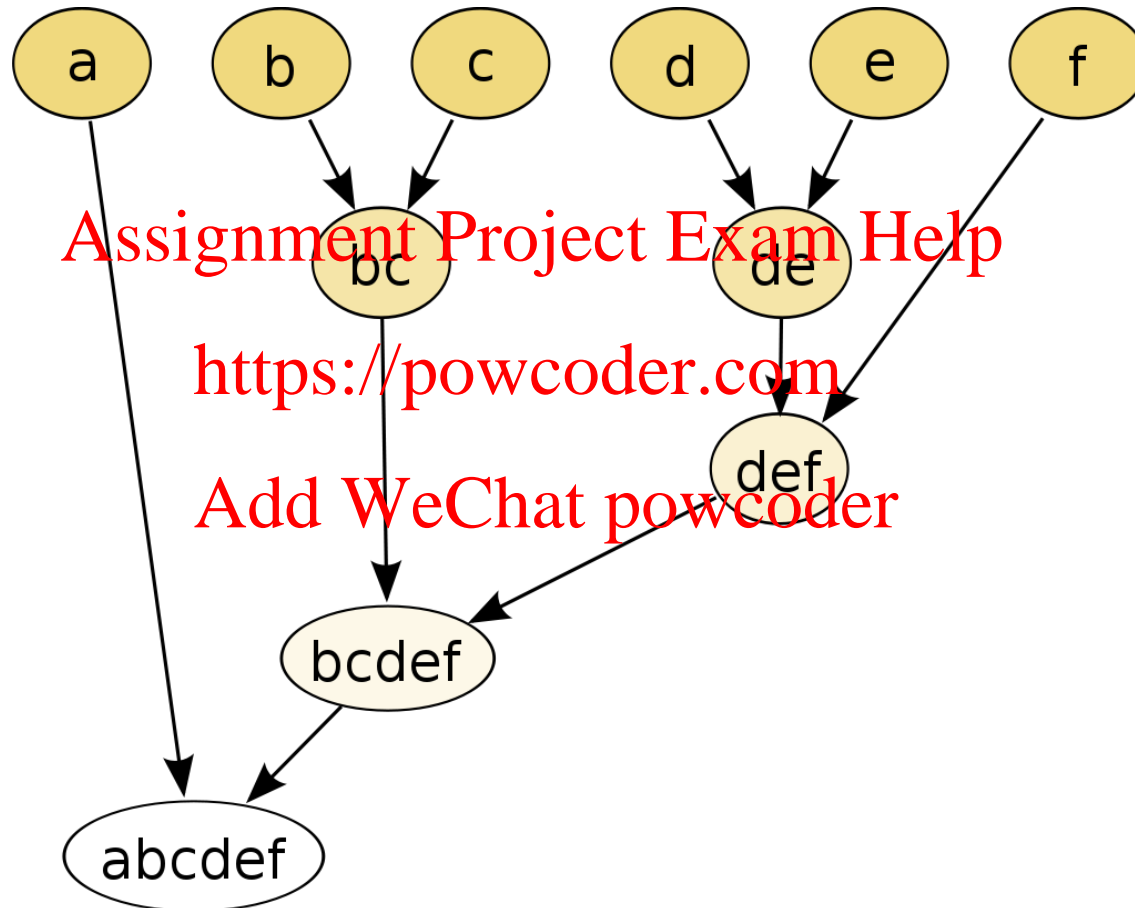


Image source: https://en.wikipedia.org/wiki/Hierarchical_clustering

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K-Means for Image Compression

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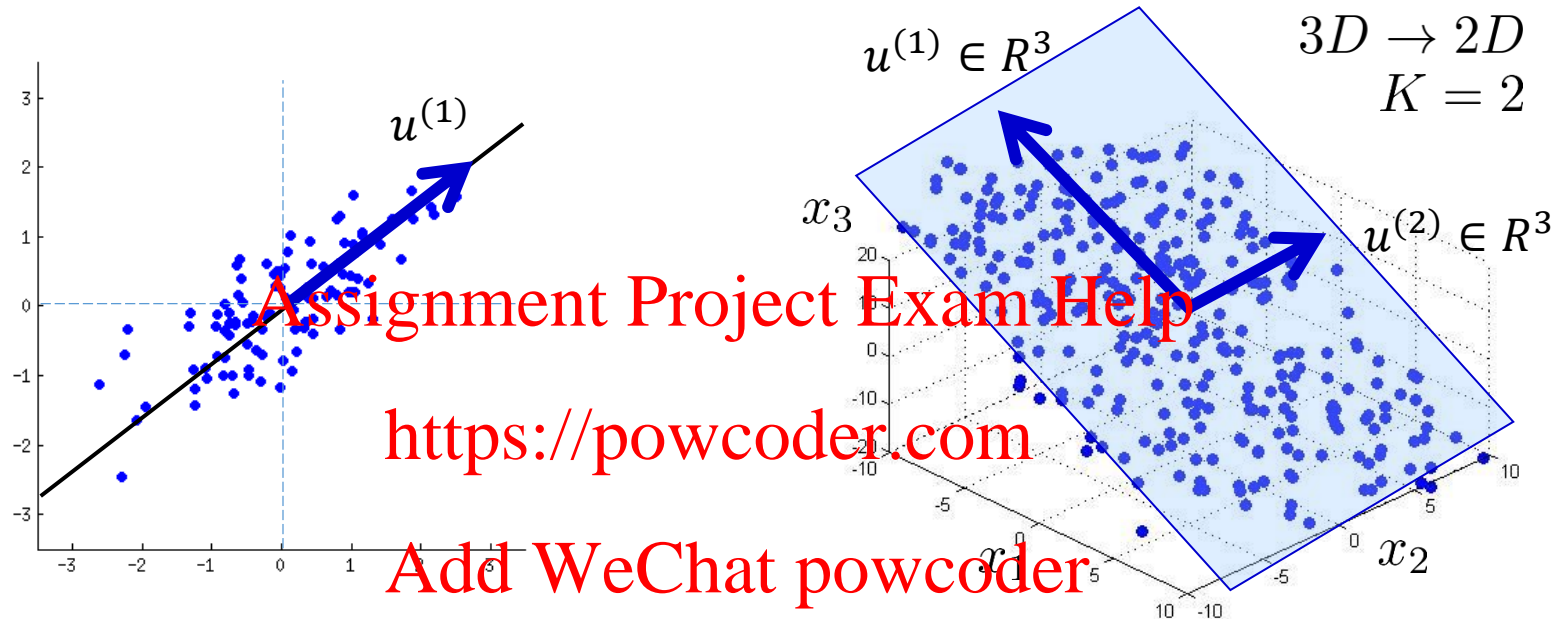


Figure 9.3 Two examples of the application of the K -means clustering algorithm to image segmentation showing the initial images together with their K -means segmentations obtained using various values of K . This also illustrates of the use of vector quantization for data compression, in which smaller values of K give higher compression at the expense of poorer image quality.

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Choose subspace with minimal “information loss”

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Reduce from 2-dimension to 1-dimension: Find a direction (a vector $u^{(1)}$) onto which to project the data, so as to minimize the projection error.

Reduce from n-dimension to K-dimension: Find K vectors $u^{(1)}, u^{(2)}, \dots, u^{(K)}$ onto which to project the data so as to minimize the projection error.

PCA Solution

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- The solution turns out to be the first K eigenvectors of the data covariance matrix (see Bishop 12.1 for details)

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- Closed-form, use Singular Value Decomposition (SVD) on covariance matrix

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What features to use?

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Today: Outline

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- **Neural networks:** artificial neuron, MLP, sigmoid units; neuroscience inspiration, output vs hidden layers; linear vs nonlinear networks;

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- **Feed-forward networks**

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Intro to Neural Networks

Motivation

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Recall: Logistic Regression

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$$0 \leq h_{\theta}(x) \leq 1$$

$$h_{\theta}(x) = g(\theta^T x) = \frac{1}{1 + e^{-\theta^T x}}$$

$$g(z) = \frac{1}{1 + e^{-z}}$$

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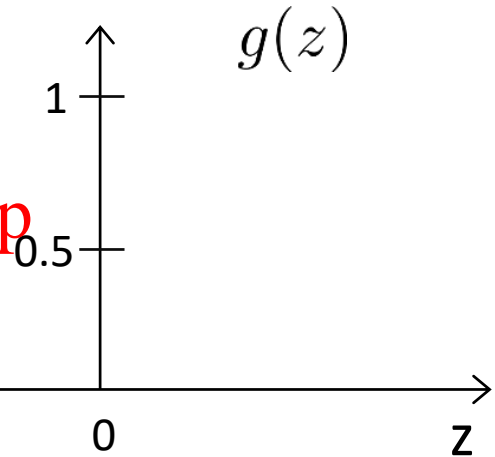
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Output is probability of label 1 given input

$$p(y = 1|x) = \frac{1}{1 + e^{-\theta^T x}}$$

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sigmoid/logistic function



predict “ $y = 1$ ” if $h_{\theta}(x) \geq 0.5$

predict “ $y = 0$ ” if $h_{\theta}(x) < 0.5$

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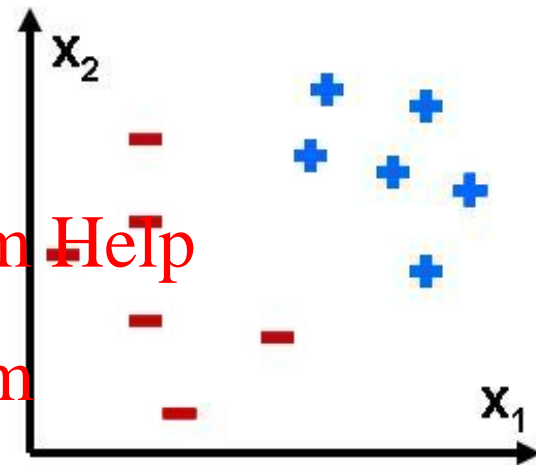
Recall: Logistic Regression Cost

Logistic Regression Hypothesis:

$$h_{\theta}(x) = g(\theta^T x) = \frac{1}{1 + e^{-\theta^T x}}$$

θ : parameters

$D = \{x^i, y^i\}$: data <https://powcoder.com>



Logistic Regression Cost Function:

$$\begin{aligned} J(\theta) &= \frac{1}{m} \sum_{i=1}^m \text{Cost}(h_{\theta}(x^{(i)}), y^{(i)}) \\ &= -\frac{1}{m} \left[\sum_{i=1}^m y^{(i)} \log h_{\theta}(x^{(i)}) + (1 - y^{(i)}) \log (1 - h_{\theta}(x^{(i)})) \right] \end{aligned}$$

Goal: minimize cost $\min_{\theta} J(\theta)$

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Cost: Intuition

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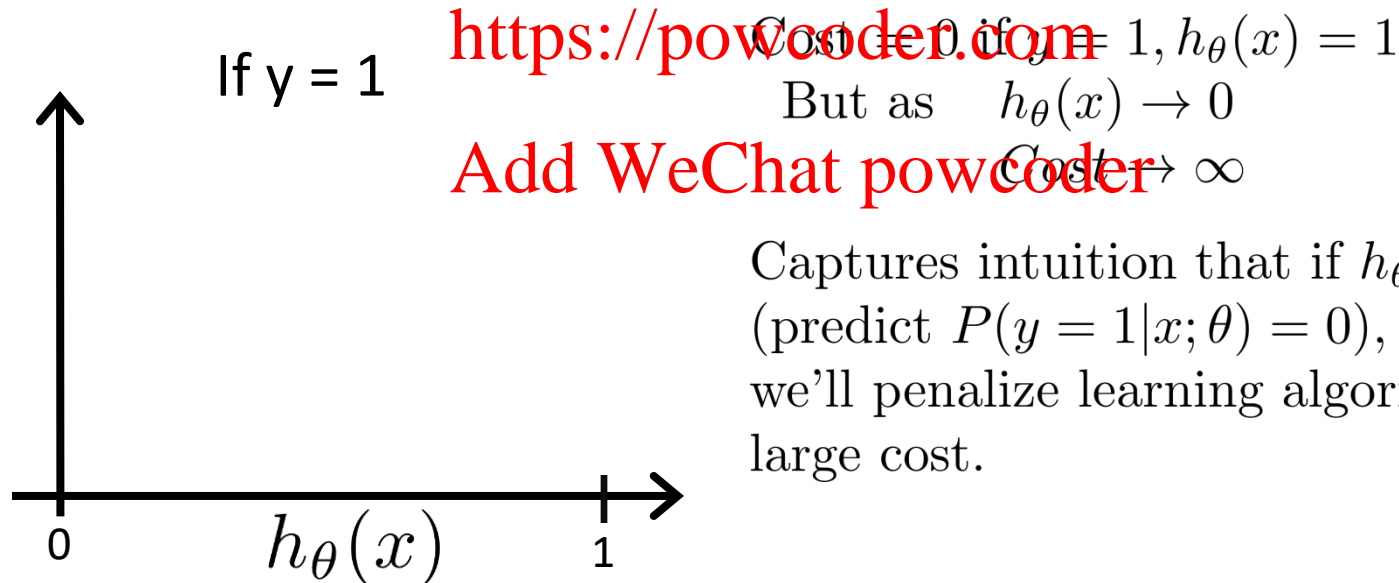
Logistic regression cost function

$$\text{Cost}(h_{\theta}(x), y) = \begin{cases} -\log(h_{\theta}(x)) & \text{if } y = 1 \\ -\log(1 - h_{\theta}(x)) & \text{if } y = 0 \end{cases}$$

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Captures intuition that if $h_{\theta}(x) = 0$, (predict $P(y = 1|x; \theta) = 0$), but $y = 1$, we'll penalize learning algorithm by a very large cost.

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Cost: Intuition

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Logistic regression cost function

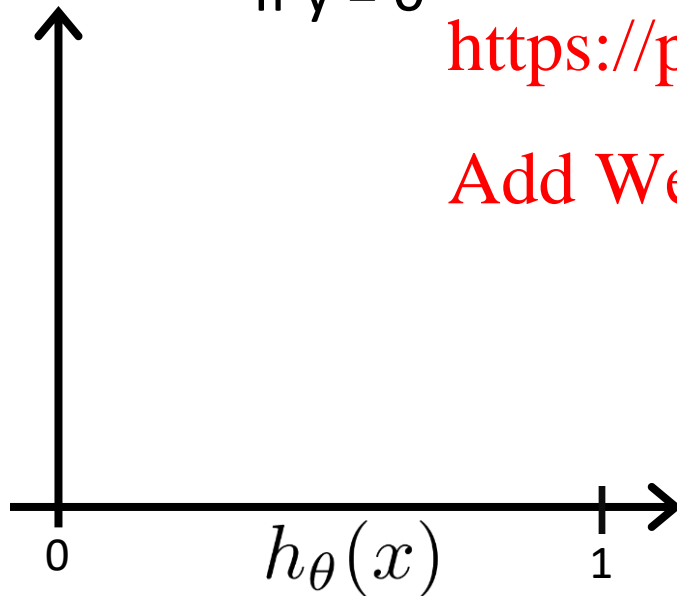
$$\text{Cost}(h_{\theta}(x), y) = \begin{cases} -\log(h_{\theta}(x)) & \text{if } y = 1 \\ -\log(1 - h_{\theta}(x)) & \text{if } y = 0 \end{cases}$$

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If $y = 0$

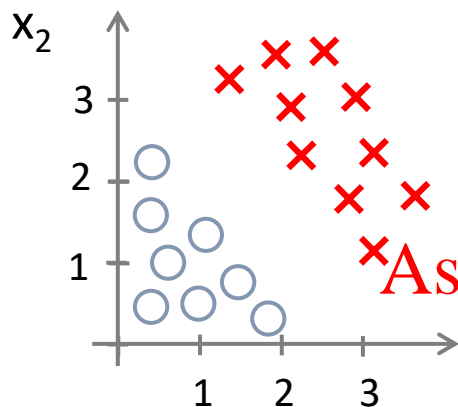
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Decision boundary

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$$h_{\theta}(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2)$$

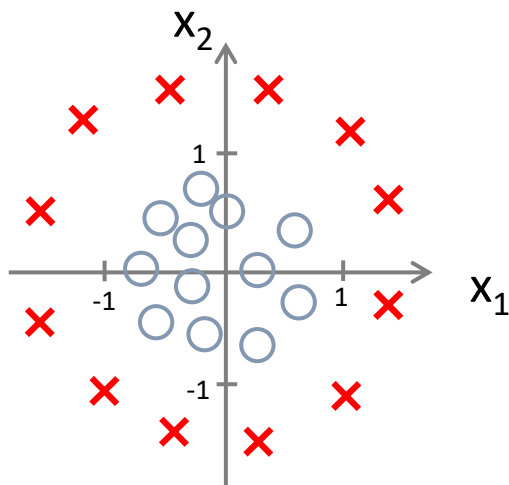
Predict “ $y = 1$ ” if $-3 + x_1 + x_2 \geq 0$

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Non-linear decision boundaries

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Replace features with non-linear functions
e.g. log, cosine, or polynomial

$$h_{\theta}(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2 + \theta_3 x_1^2 + \theta_4 x_2^2)$$

Predict “ $y = 1$ ” if $-1 + x_1^2 + x_2^2 \geq 0$

Limitations of linear models

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- Logistic regression and other linear models cannot handle nonlinear decision boundaries
 - Must use non-linear feature transformations
 - Up to designer to specify which one
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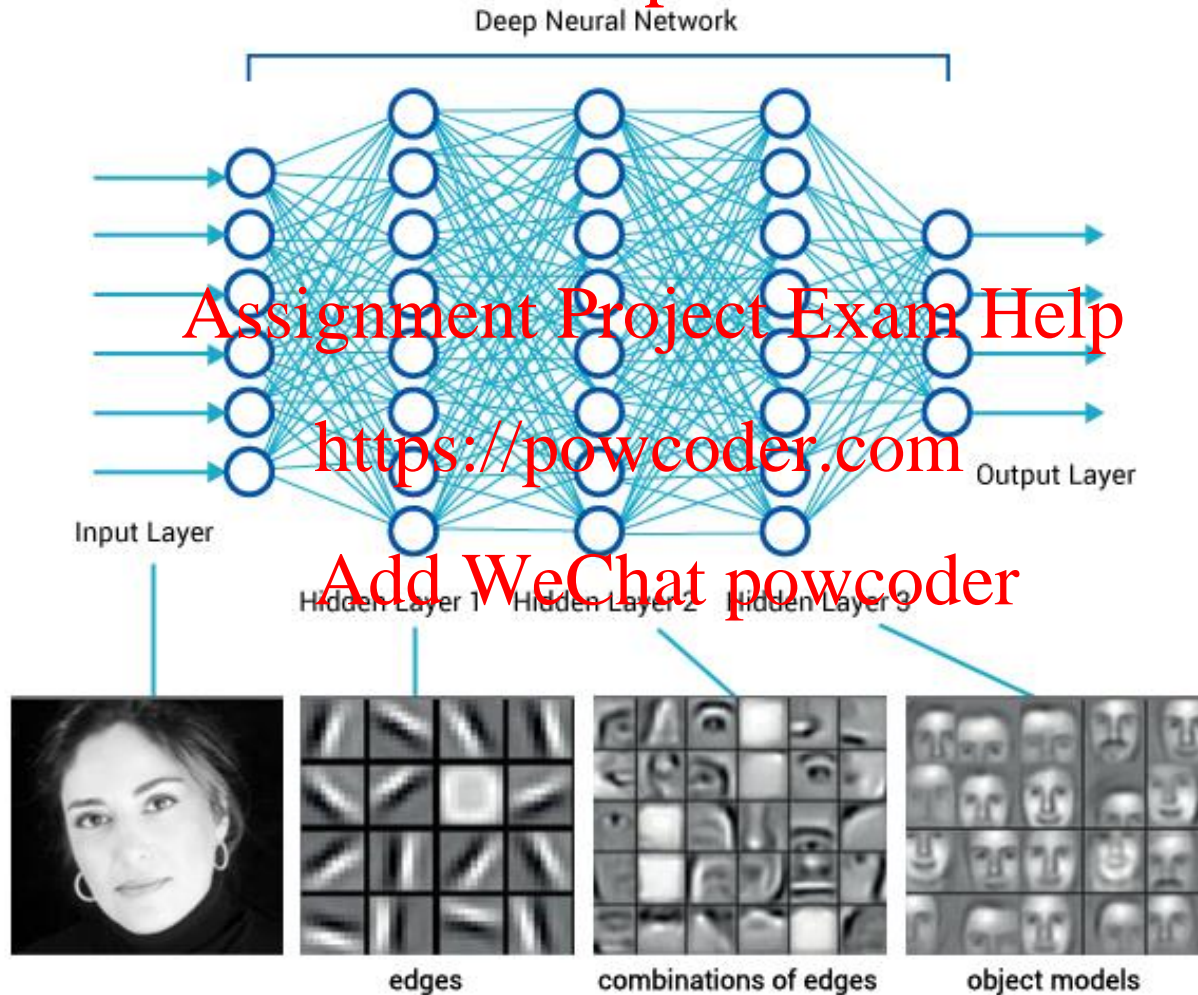
- Can we instead <https://powcoder.com> learn the transformation?

- Yes, this is what neural networks do!
 - A **Neural network** chains together many layers of “neurons” such as logistic units (logistic regression functions)
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Neural Networks learn features

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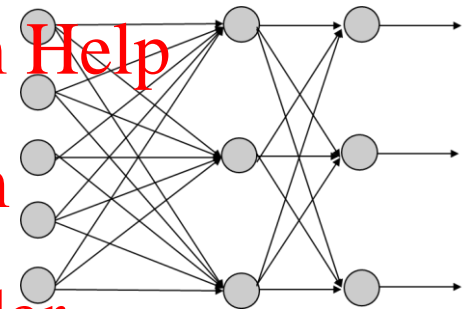
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Neurons in the Brain

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Inspired “Artificial Neural Networks”



Neurons are cells that process chemical and electrical signals and transmit these signals to neurons and other types of cells

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Neuron in the brain

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nucleus

dendrites
“Input wire”

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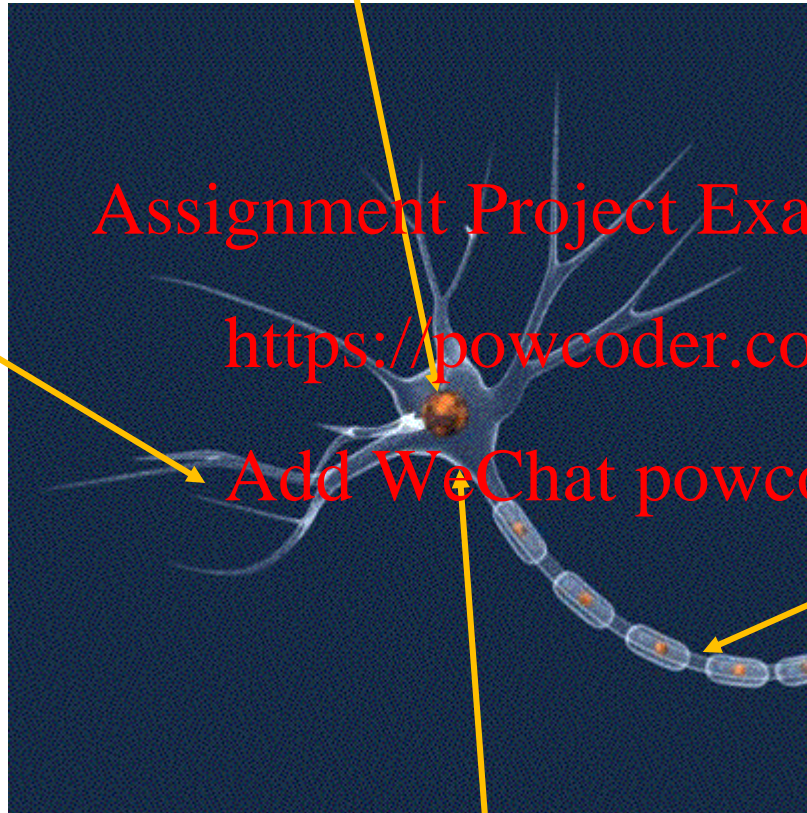
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Can measure
electrical activity
(spike) of a single
neuron by placing
electrodes

axon
“Output wire”

Cell body



Neural network in the brain

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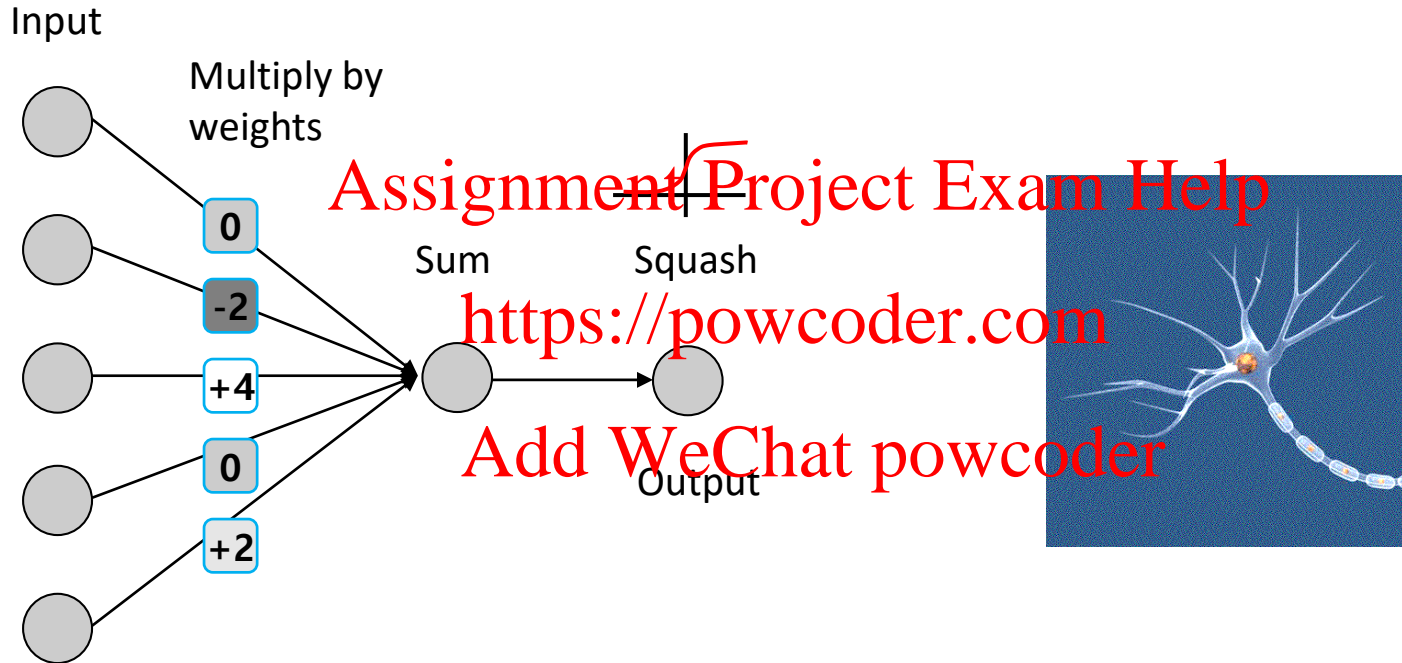
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- **Micro networks:** several connected neurons perform sophisticated tasks: mediate reflexes, process sensory information, generate locomotion and mediate learning and memory.
- **Macro networks:** perform higher brain functions such as object recognition and cognition.

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Logistic Unit as Artificial Neuron

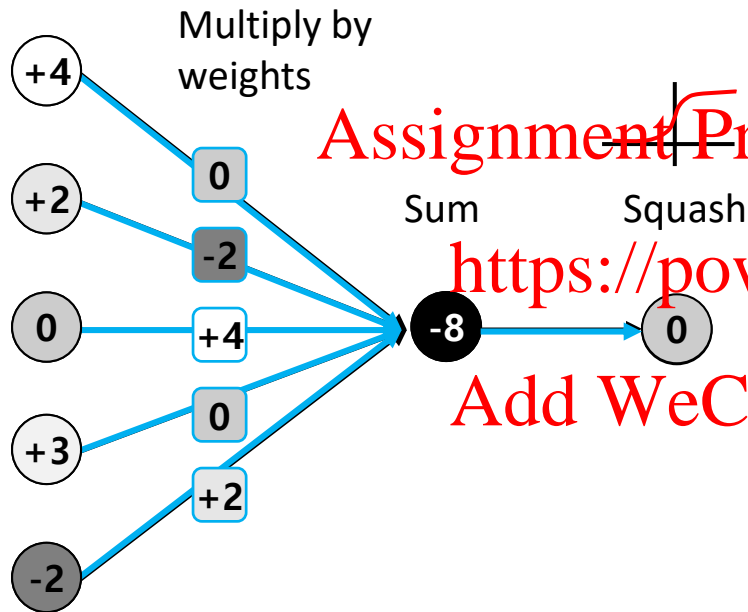


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Logistic Unit as Artificial Neuron

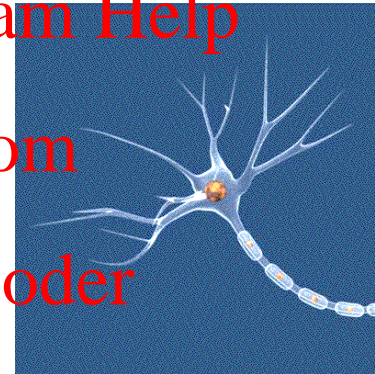
Input



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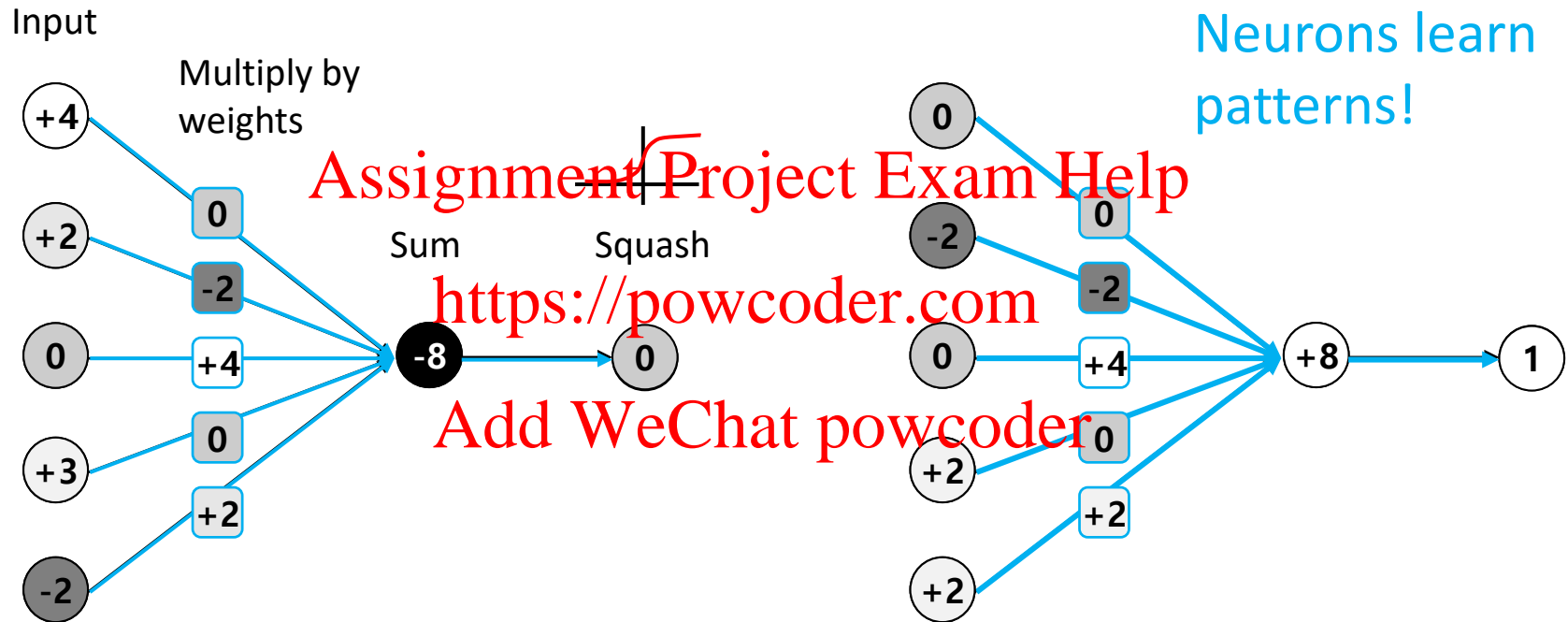
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Logistic Unit as Artificial Neuron



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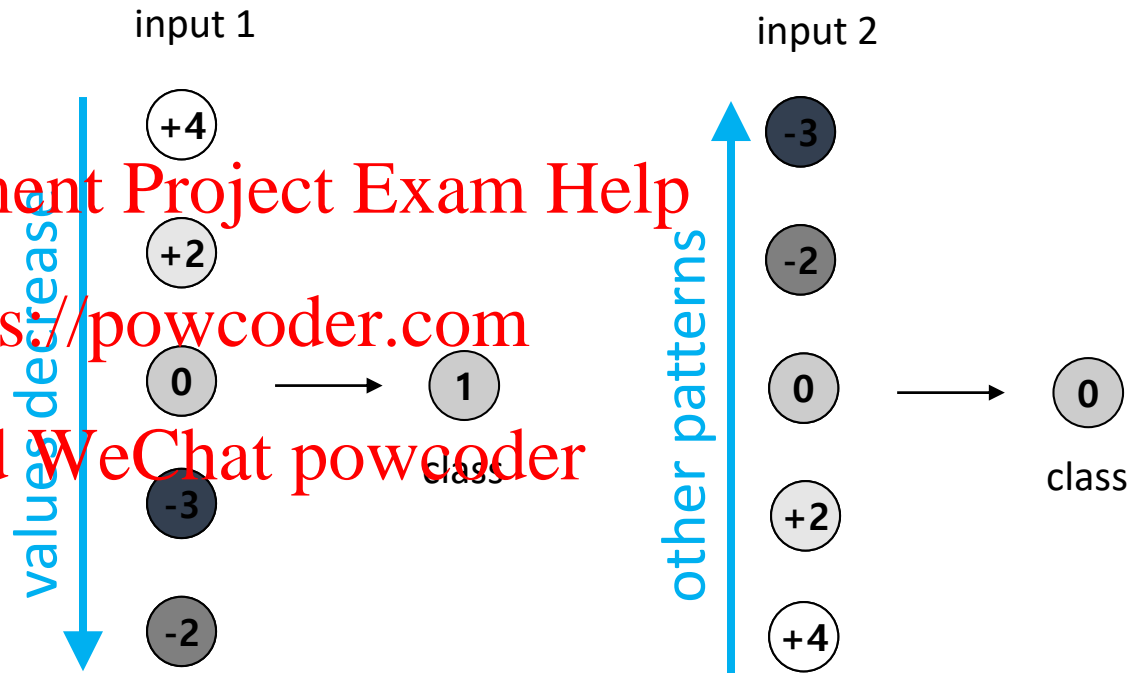
Artificial Neuron Learns Patterns

- Classify input into class 0 or 1
- Teach neuron to predict correct class label
- Detect presence of a simple "feature"

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Example



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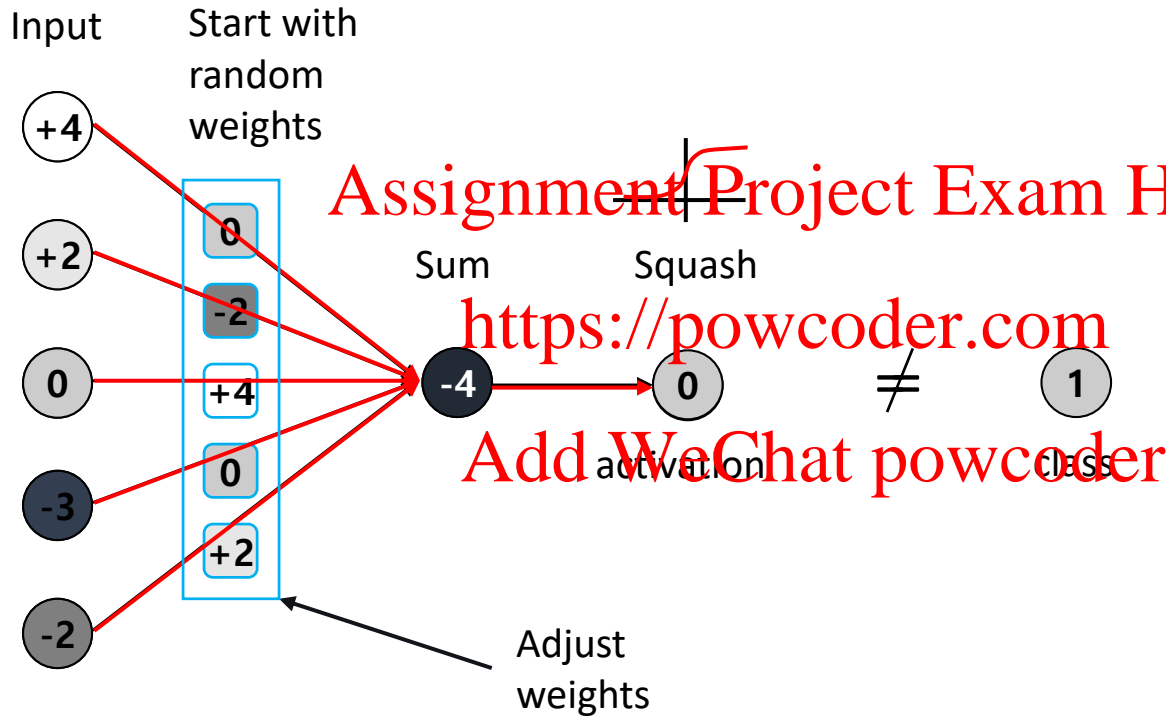
Neural Networks: Learning

Intuition

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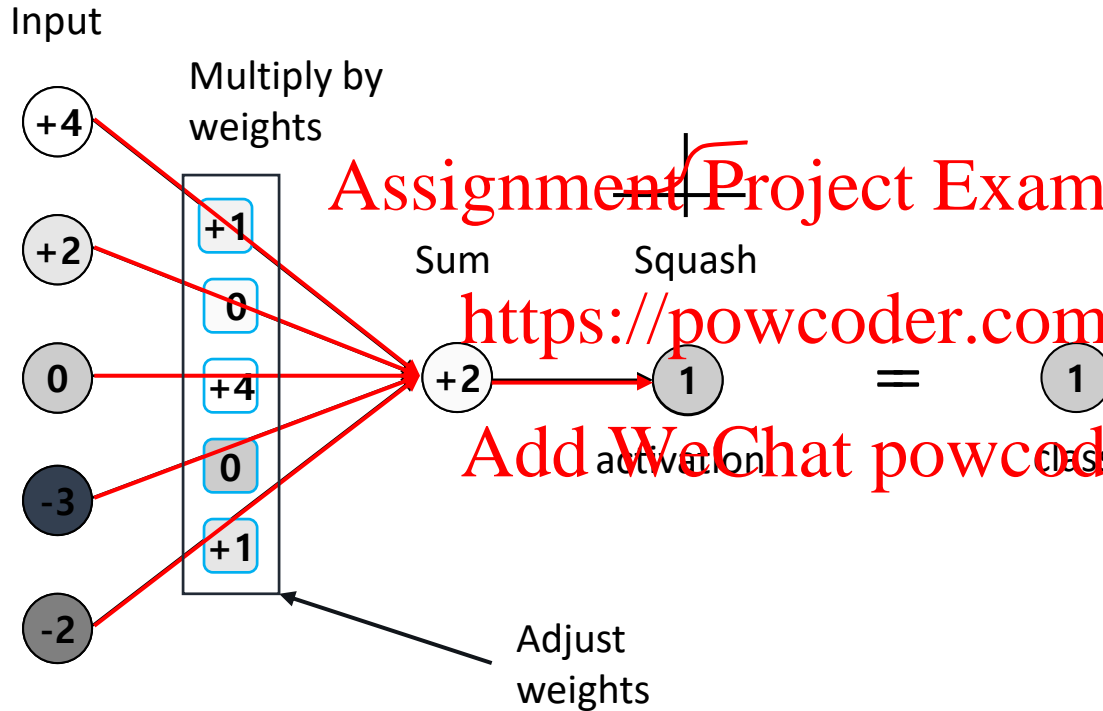
Artificial Neuron: Learning



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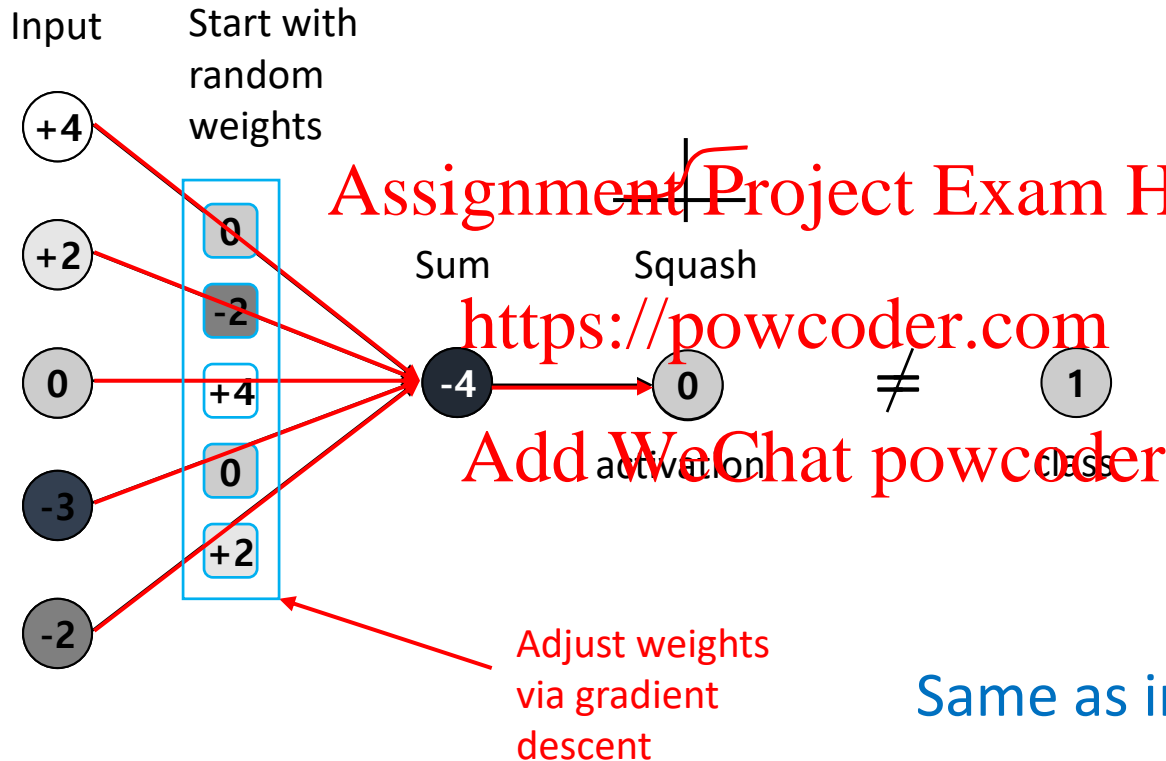
Artificial Neuron: Learning



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Artificial Neuron: Learning



Same as in logistic regression



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Neural Networks: Learning

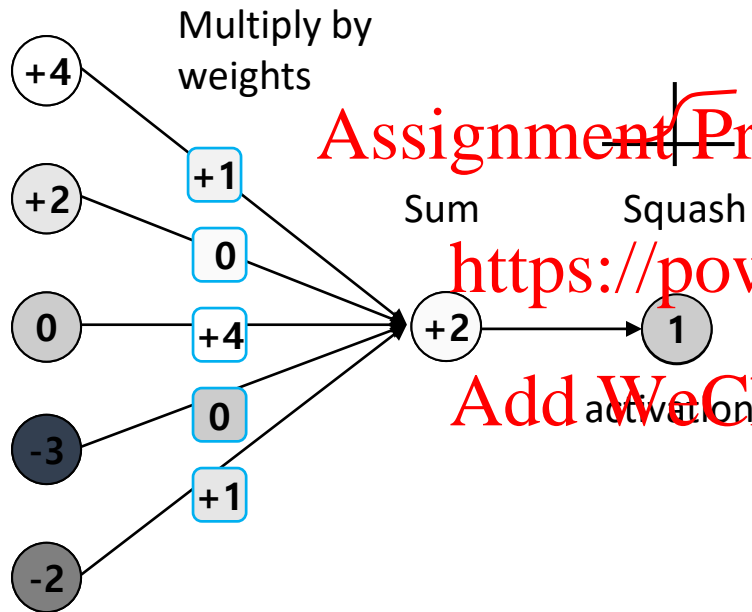
Multi-layer network

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Artificial Neuron: simplify

Input



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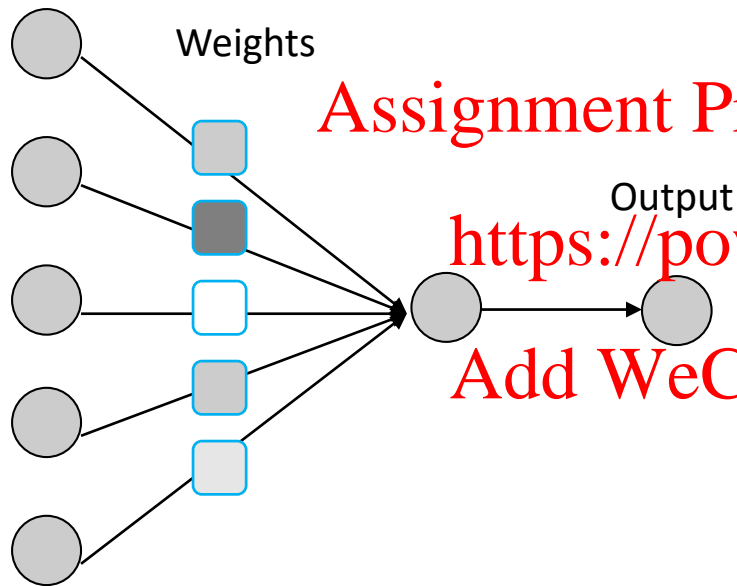
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Artificial Neuron: simplify

Input



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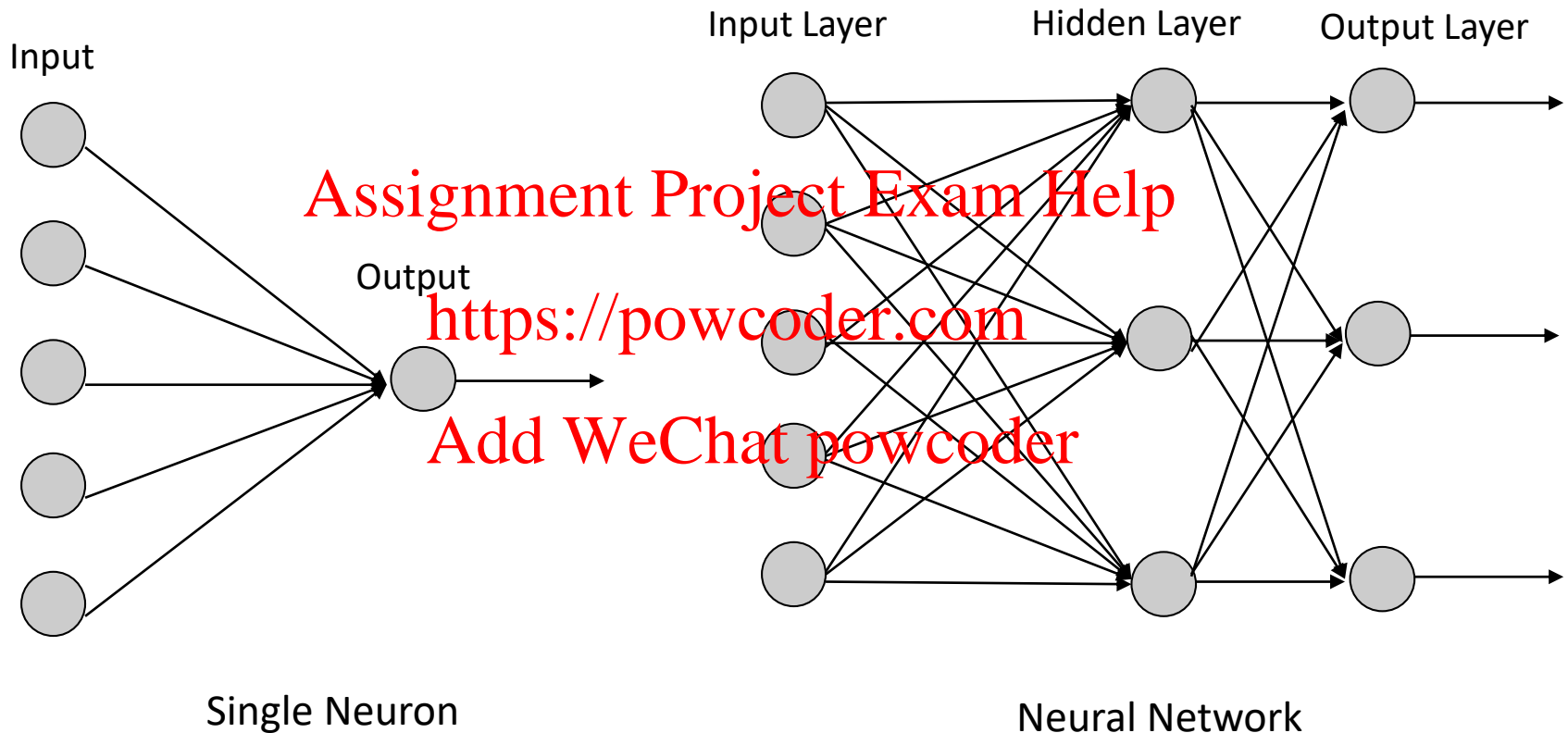
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Artificial Neural Network



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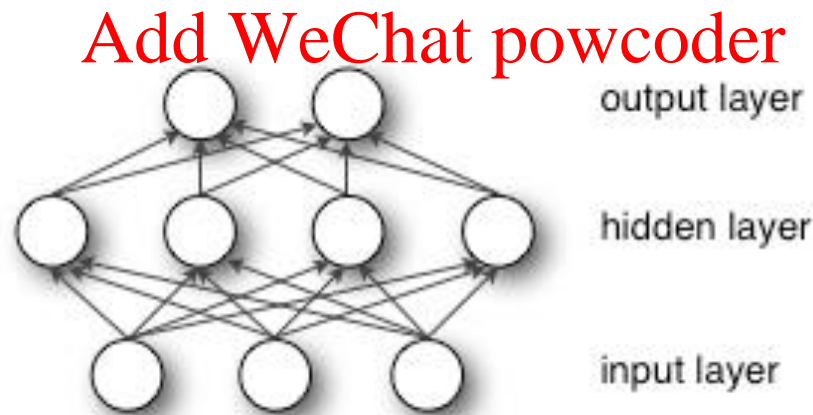
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Deep Network: many hidden layers

Multi-layer perceptron (MLP)

- Just another name for a feed-forward neural network
- Logistic regression is a special case of the MLP with no hidden layer and sigmoid output

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Neural Networks Learn Features

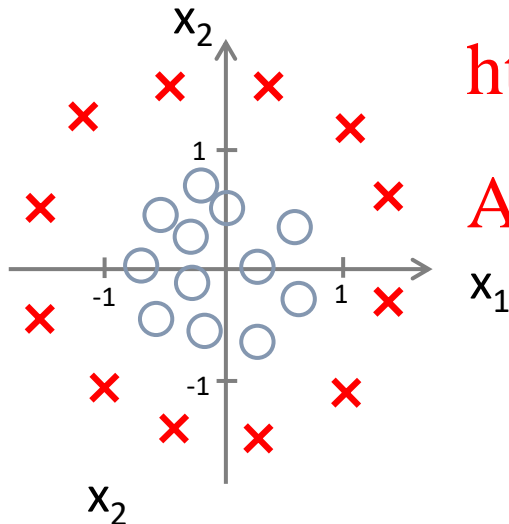
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logistic regression unit == artificial neuron

chain several units together == neural network

“earlier” units learn non-linear feature transformation

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$$h_{\theta}(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2)$$

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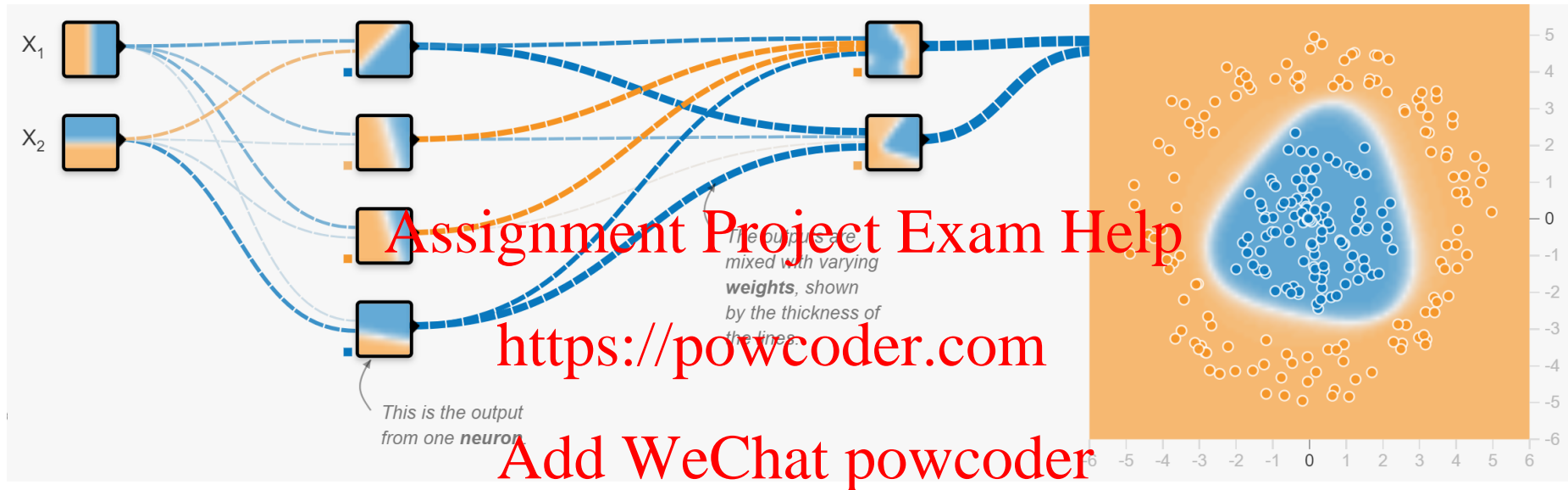
simple neural network

$$h(x) = g(\theta + \theta_1 h^{(1)}(x) + \theta_2 h^{(2)}(x) + \theta_3 h^{(3)}(x))$$

Example

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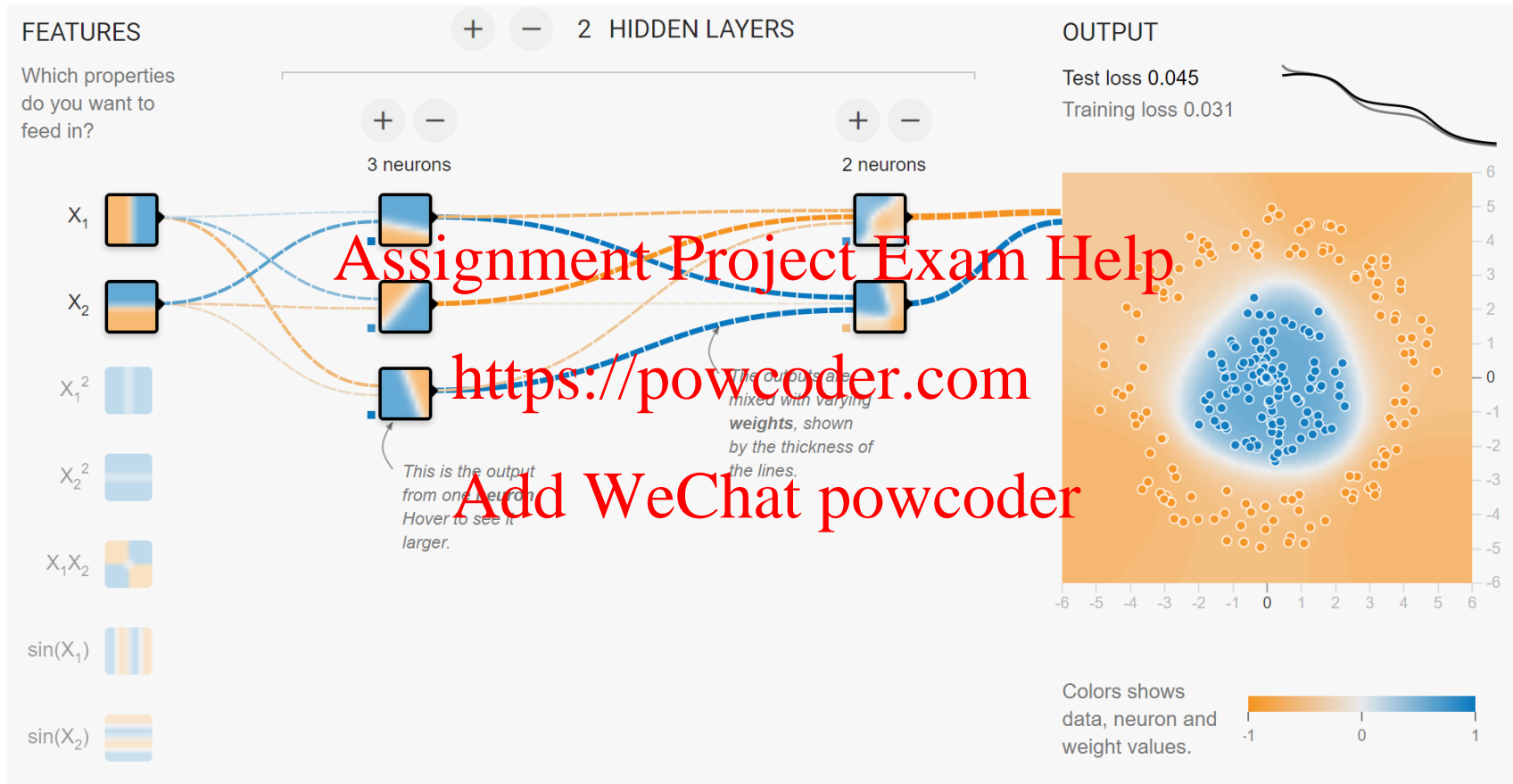
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Training a neural net: Demo

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Tensorflow playground

Artificial Neural Network:

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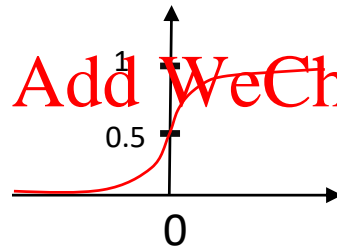
input

$$x = \begin{bmatrix} x_1 \\ \dots \\ x_5 \end{bmatrix}$$

hidden layer activations

$$h^i = g(\Theta^{(i)}x)$$

$$g(z) = \frac{1}{1 + \exp(-z)}$$



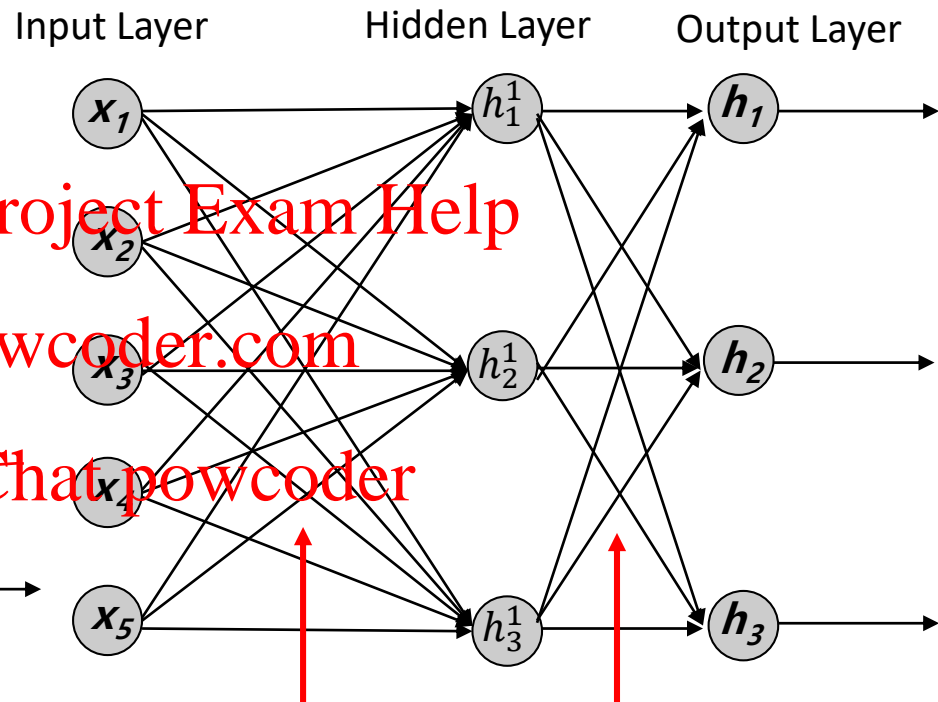
output

$$h_{\Theta}(x) = g(\Theta^{(2)}a)$$

weights

$$\Theta^{(1)} = \begin{pmatrix} \theta_{11} & \dots & \theta_{15} \\ \vdots & \ddots & \vdots \\ \theta_{31} & \dots & \theta_{35} \end{pmatrix}$$

$$\Theta^{(2)} = \begin{pmatrix} \theta_{11} & \dots & \theta_{13} \\ \vdots & \ddots & \vdots \\ \theta_{31} & \dots & \theta_{33} \end{pmatrix}$$



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Cost function

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Neural network: $h_{\Theta}(x) \in \mathbb{R}^K$ $(h_{\Theta}(x))_i = i^{th}$ output

Assignment Project Exam Help training error

$$J(\Theta) = -\frac{1}{m} \left[\sum_{i=1}^m \sum_{k=1}^K y_k^{(i)} \log(h_{\Theta}(x^{(i)}))_k + (1 - y_k^{(i)}) \log(1 - (h_{\Theta}(x^{(i)}))_k) \right]$$

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$$+ \frac{\lambda}{2m} \sum_{l=1}^{L-1} \sum_{i=1}^{s_l} \sum_{j=1}^{s_{l+1}} (\Theta_{ji}^{(l)})^2$$

regularization

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Gradient computation

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$$J(\Theta) = -\frac{1}{m} \left[\sum_{i=1}^m \sum_{k=1}^K y_k^{(i)} \log h_{\theta}(x^{(i)})_k + (1 - y_k^{(i)}) \log(1 - h_{\theta}(x^{(i)})_k) \right]$$

$$+ \frac{\lambda}{2m} \sum_{l=1}^{L-1} \sum_{i=1}^{s_l} \sum_{j=1}^{s_{l+1}} (\Theta_j^{(l)})^2$$

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Cover next time!

$$\min_{\Theta} J(\Theta)$$

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Use “Backpropagation algorithm”

Need code to compute:

- $J(\Theta)$
- $\frac{\partial}{\partial \Theta_{ij}^{(l)}} J(\Theta)$

- Efficient way to compute $\frac{\partial}{\partial \Theta_{ij}^{(l)}} J(\Theta)$
- Computes gradient incrementally by “propagating” backwards through the network

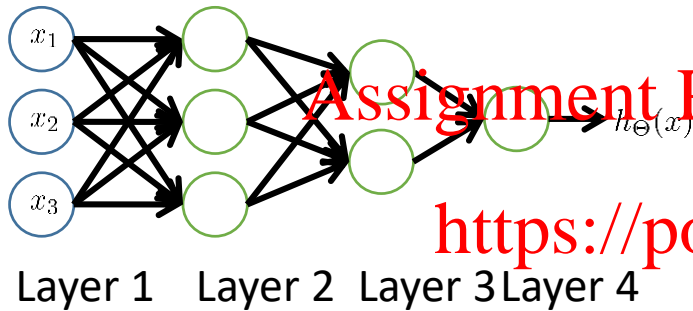
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Network architectures

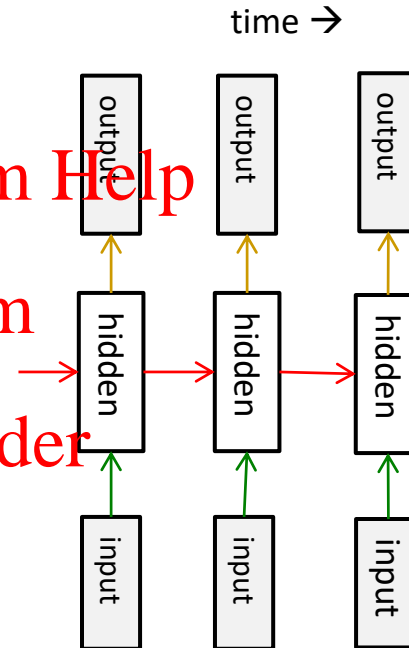
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Feed-forward

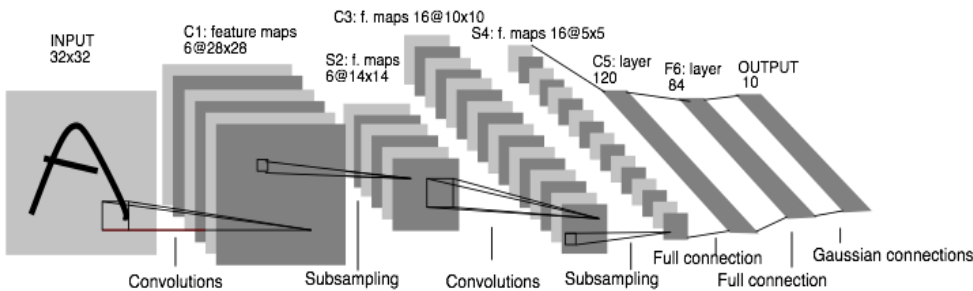
Fully connected



Recurrent



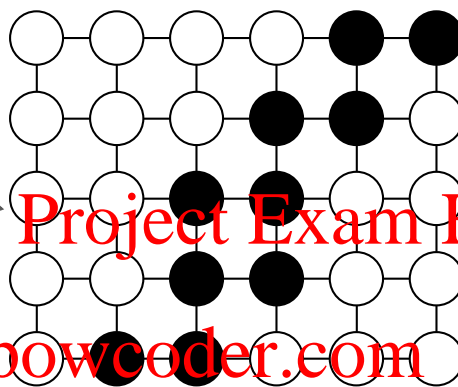
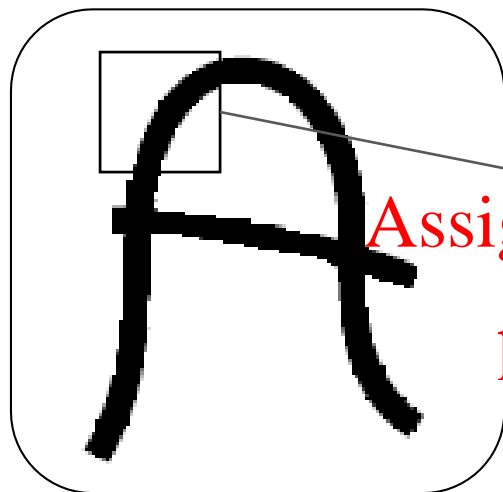
Convolutional



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Representing images

Fully connected



Reshape into a vector

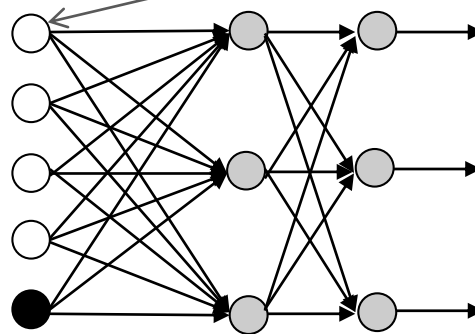


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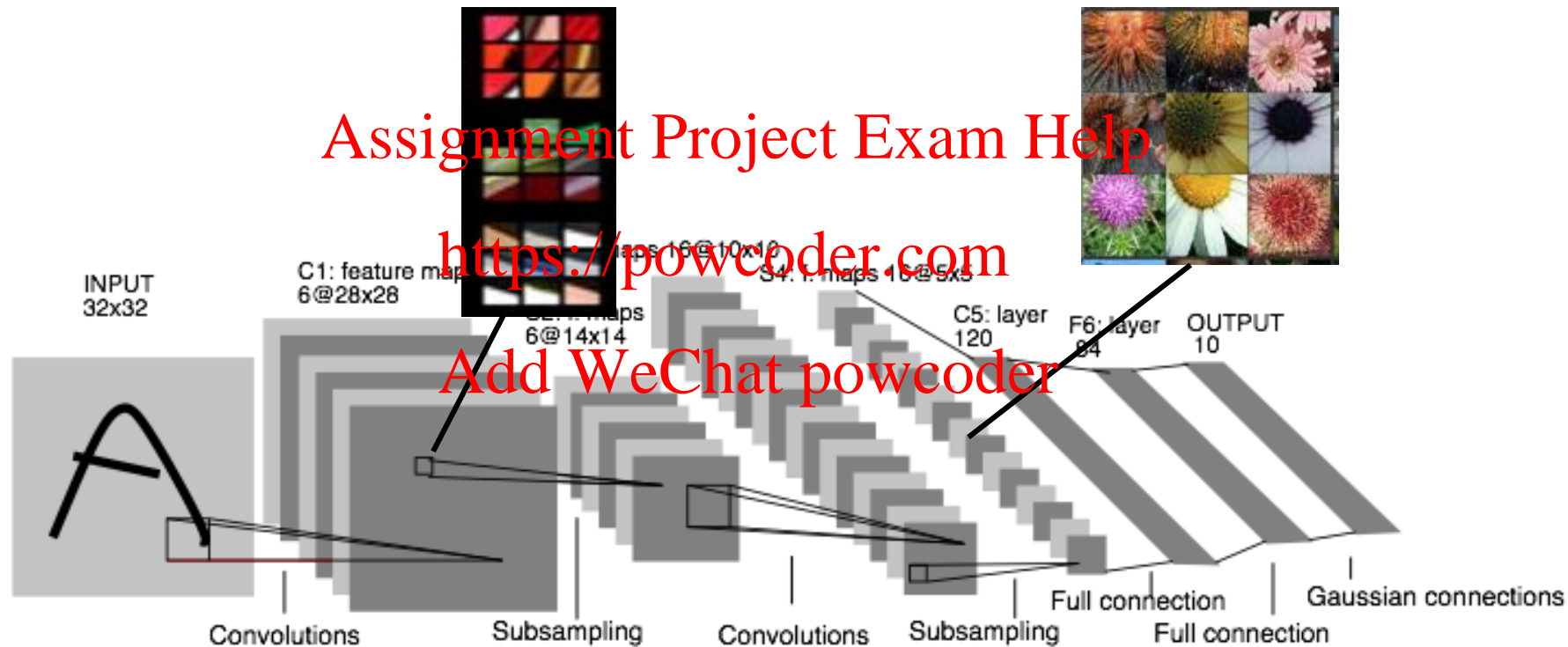
Input Layer



Convolutional Neural Network

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A better architecture for 2d signals



LeNet

Why Deep Learning?

The Unreasonable Effectiveness of Deep Features



Maximal activations of pool_5 units

[R-CNN]

Rich visual structure of features deep in hierarchy.



conv_5 DeConv visualization
[Zeiler-Fergus]

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Summary so far

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- **Neural network** chains together many layers of “neurons” such as logistic units

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- **Hidden neurons** learn more and more abstract non-linear features

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Next Class
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Neural Networks I: Learning:

Learning via gradient descent; computation graphs, backpropagation algorithm.

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Reading: Bishop Ch 5.1-5.3
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