# Assignment Project Exam Help Admeeun Sewagents

Reminder: ps2 due Thursday at midnight (Boston)

- Self-Grading from square riday 9/25 (1 week to turn we Chat powcoder
- Self-Grading form for ps2 out Monday 9/28 (1 week to turn in)
- Lab this week (no more rotations) –
   Linear/Logistic Regression, Anaconda

## Assignment Project Exam Help Add WeChat powcoder

Assignment Project Exam Help
Unsupervised Learning I

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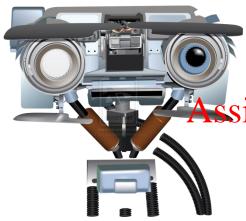
### Assignment Project Exam Help Add WeChar dowcoder

- Unsupervised learning
  - K-Means clustering
     Assignment Project Exam Help
     Gaussian Mixture clustering

https://powcoder.com

Add WeChat powcoder

### Add WeChat powcoder

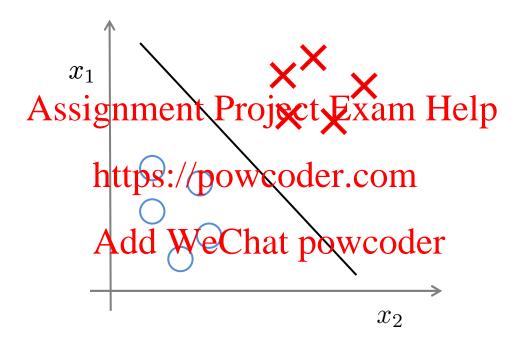


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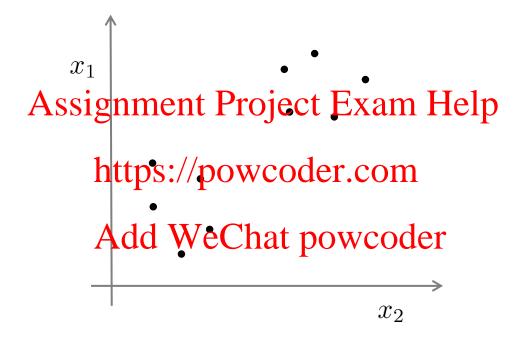
Add WeChat powcoder Clustering

## Add WeChat powcoder Supervised learning



Training set:  $\{(x^{(1)}, y^{(1)}), (x^{(2)}, y^{(2)}), (x^{(3)}, y^{(3)}), \dots, (x^{(m)}, y^{(m)})\}$ 

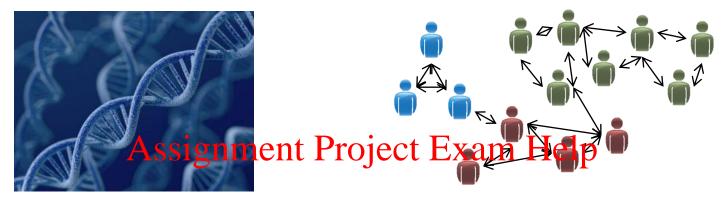
## Add WeChat powcoder Unsupervised learning



Training set:  $\{x^{(1)}, x^{(2)}, x^{(3)}, \dots, x^{(m)}\}$ 

## Clustering Assignment Project Exam Help

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Gene analysihttps://powcoder.sociametwork analysis



Types of voters

Trending news

### Add WeChat powcoder

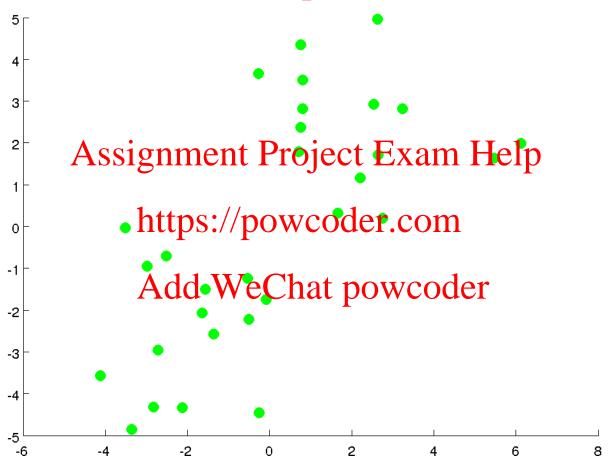


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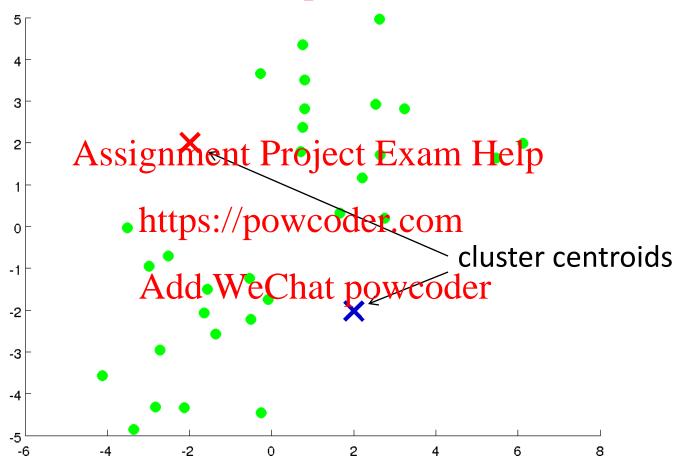
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Add WeChat powcoder K-means Algorithm

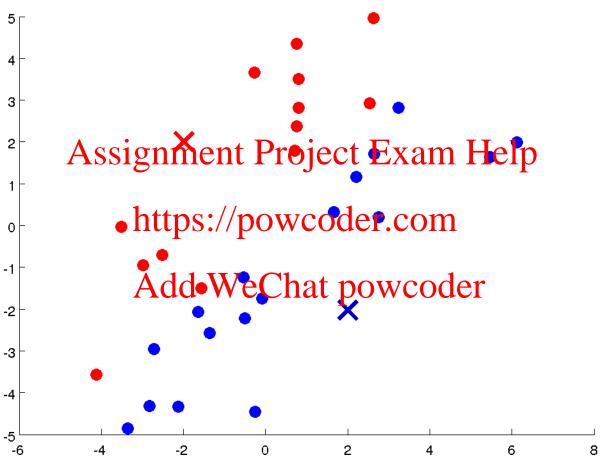
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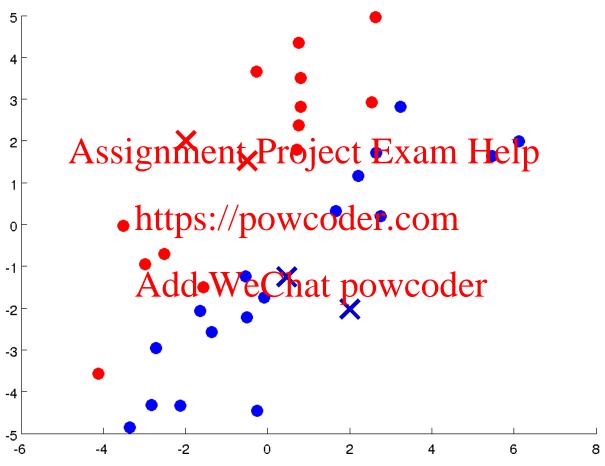
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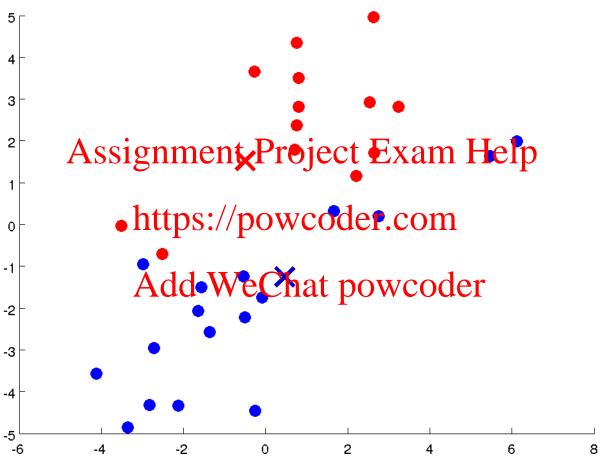




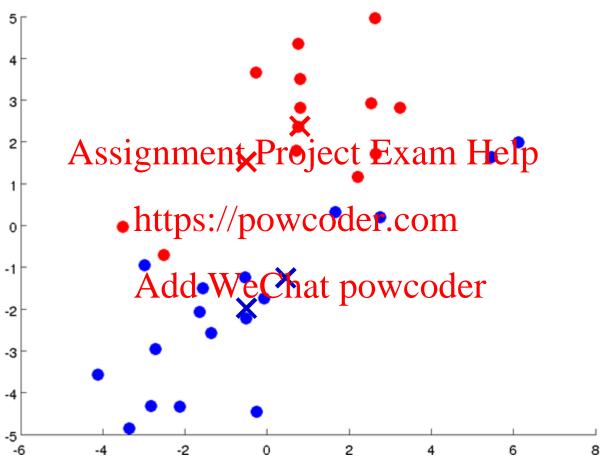




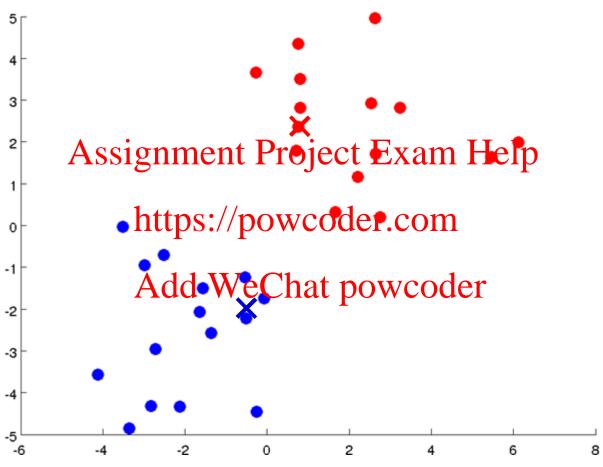




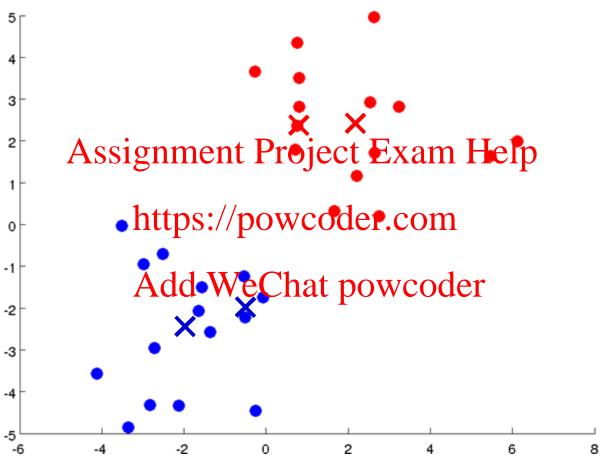




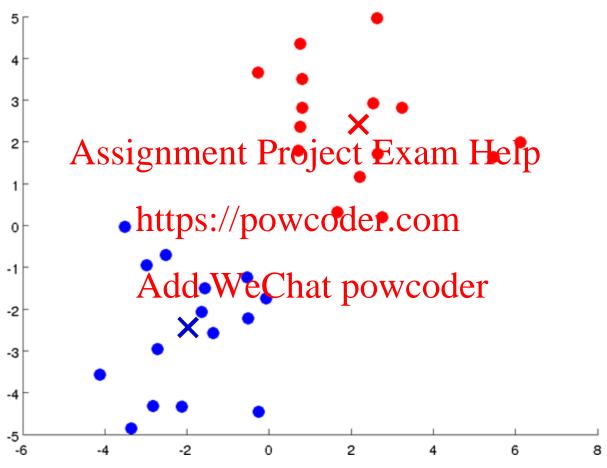




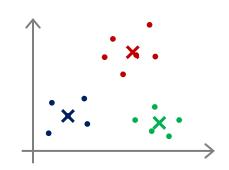








## Add WeChat powcoder K-means algorithm



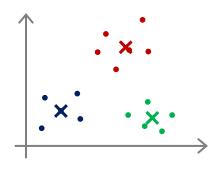
#### Input:

- K (number of clusters) - Assignment Project Exam Help - Training set  $\{x^{(1)}, x^{(2)}, \dots, x^{(m)}\}$
- Training set  $\{x^{(1)}, x^{(2)}, \dots, x^{(m)}\}$ https://powcoder.com

$$x^{(i)} \in \mathbb{R}^n$$
 (drop  $x_0 = 1$  convention)

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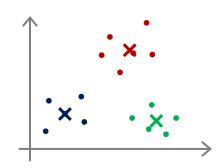
#### K-means algorithm



```
Randomly initialize K cluster centroids \mu_1, \mu_2, \dots, \mu_K \in \mathbb{R}^n

Repeat {
	for i = 1 to m Project Exam Help
	c^{(i)} := index (from 1 to K) of cluster centroid
	closest to x^{(i)}
	for k = 1 to K dd WeChat powcoder
	\mu_k := average (mean) of points assigned to cluster k
}
```

### K-means Cost Author Chat powcoder



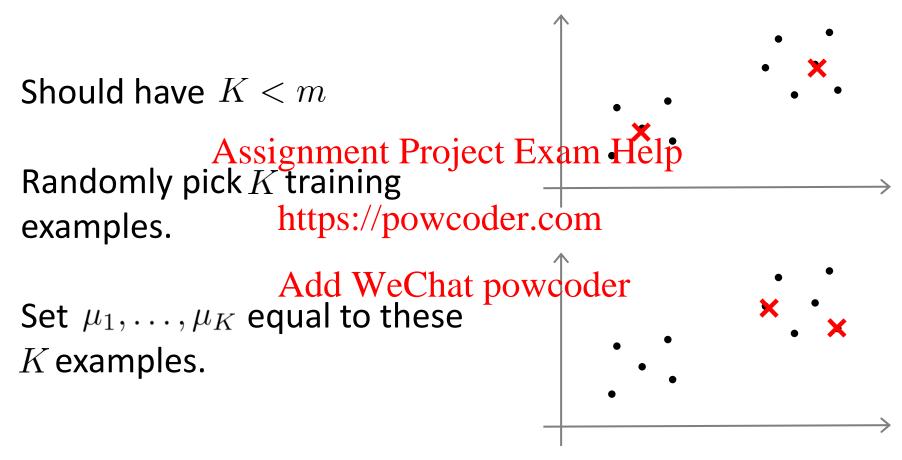
 $c^{(i)}$  = index of cluster (1,2,...,K) to which example  $x^{(i)}$ is currently assigned

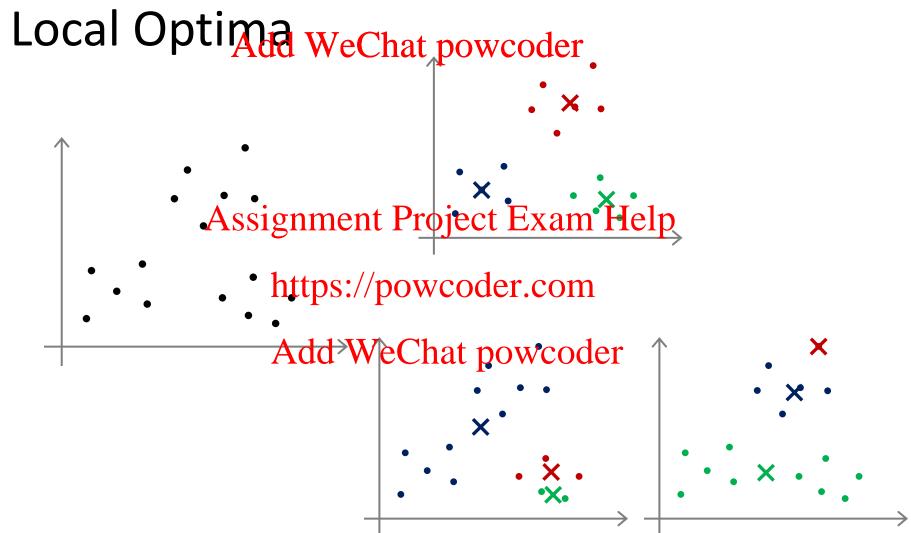
 $\mu_k$  = cluster centroid k ( $\mu_k \in \mathbb{R}^n$ )  $\mu_{c^{(i)}}$  = cluster centroid of cluster to which example xhas been assigned https://powcoder.com

Optimization cost: "distortjon" Add WeChat powcoder 
$$J(c^{(1)}, \dots, c^{(m)}, \mu_1, \dots, \mu_K) = \frac{1}{m} \sum_{i=1}^{m} ||x^{(i)} - \mu_{c^{(i)}}||^2$$

$$\min_{\substack{c^{(1)}, \dots, c^{(m)}, \\ \mu_1, \dots, \mu_K}} J(c^{(1)}, \dots, c^{(m)}, \mu_1, \dots, \mu_K)$$

### Random initialization wcoder





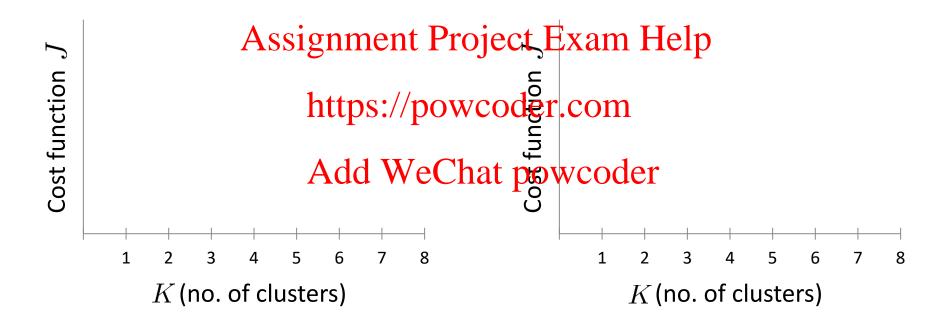
## Assignment Project Exam Help Avoiding Local Optima with Random Initialization Add WeChat powcoder

```
For i = 1 to 100 { Randomly initialize K-means: Exam Help Run K-means: Get c^{(1)},\ldots,c^{(m)},\mu_1,\ldots,\mu_K. Compute costtfpnctipn (distolation) m } J(c^{(1)},\ldots,c^{(m)},\ldots,\mu_K)
```

Pick clustering that gave lowest cost  $J(c^{(1)},\ldots,c^{(m)},\mu_1,\ldots,\mu_K)$ 

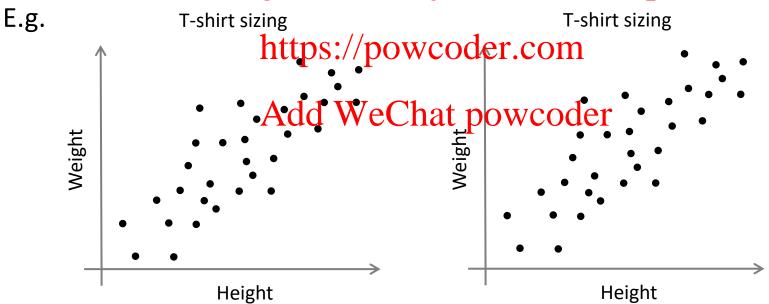
## Assignment Project Exam Help How to chapped Chat powcoder

#### Elbow method:



## How to chaose K? Rechat powcoder

Sometimes, you're running K-means to get clusters to use for some later/downstream purpose. Evaluate K-means based on a metric for how well it performs for that later purpose.



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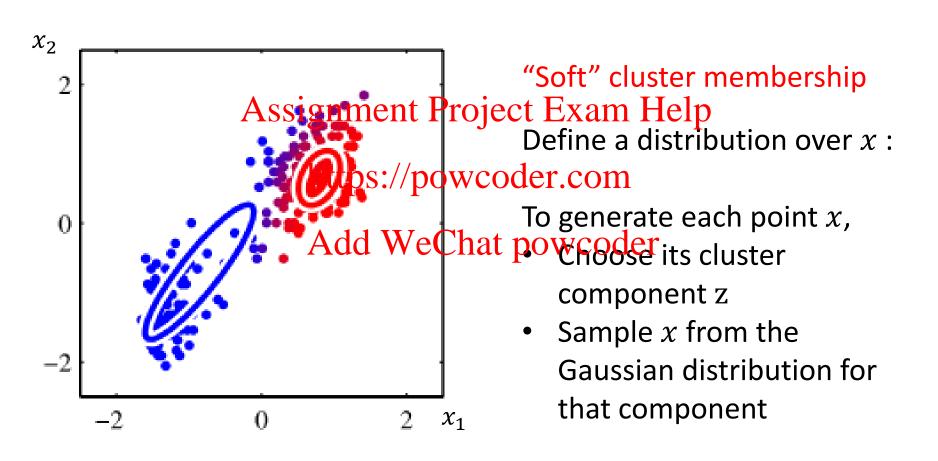
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Add WeChat powcoder Mixtures of Gaussians

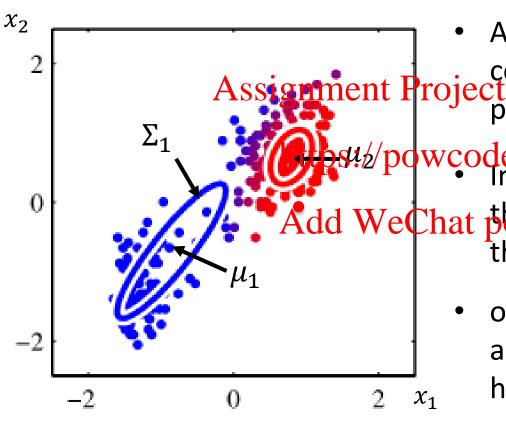
### Assignment Project Grans Helphs:

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### Assignment Project Gaussians:

### compone Manhership variable z



• Assume K components, k-th component is a Gaussian with parameters  $\mu_k$ ,  $\Sigma_k$ 

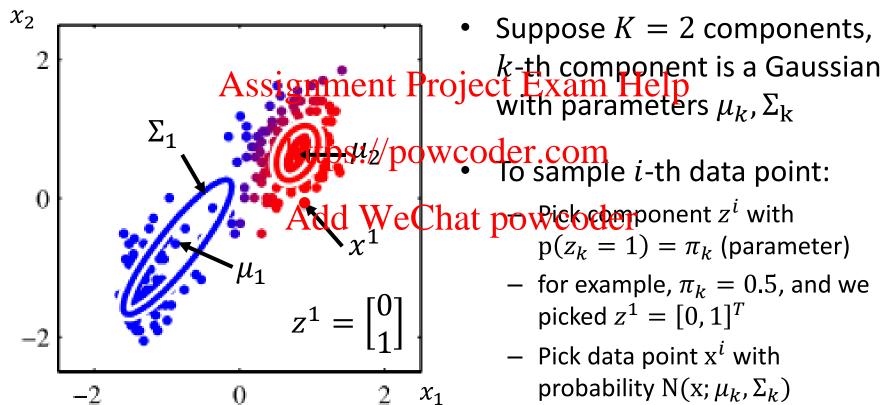
Introduce discrete r.v.  $z \in R^K$  and We Chat plates the component that generates the point

 one element of z is equal to 1 and others are 0, i.e. "onehot":

$$z_k \in \{0,1\}$$
 and  $\sum_k z_k = 1$ 

### Assignment Project Grams Helms:

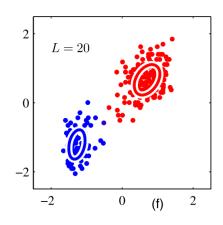
### Dath yenerapion cedample



- Suppose K=2 components,
- wcoder.com
  To sample i-th data point:
- That powick the point z i with  $p(z_k = 1) = \pi_k$  (parameter)
  - for example,  $\pi_k = 0.5$ , and we picked  $z^{1} = [0, 1]^{T}$
  - Pick data point x<sup>i</sup> with probability  $N(x; \mu_k, \Sigma_k)$

### As Minteur Project Granship ns

- $z_k \in \{0,1\}$  and  $\sum_{k=1}^{Add} \frac{\text{WeChat powcoder}}{1}$
- K components, k-th component is a Gaussian with parameters  $\mu_k$ ,  $\Sigma_k$



• define the joint distribution p(x)p in terms of a limit and a conditional distribution p(x|z) and a conditional distribution p(x|z) at the limit of the

$$p(\mathbf{x}) = \sum_{\mathbf{z}} p(\mathbf{z}) p(\mathbf{w}|\mathbf{z}) \lim_{k=1} \sum_{k=1}^{\infty} p(\mathbf{x}|\boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)$$

where

$$p(z_k = 1) = \pi_k \qquad 0 \leqslant \pi_k \leqslant 1 \qquad \sum_{k=1}^K \pi_k = 1$$
$$p(\mathbf{x}|\mathbf{z}) = \prod_{k=1}^K \mathcal{N}(\mathbf{x}|\boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)^{z_k}$$

Substitute and simplify

### Assignment Project Exam Help Maximum Likelihood Solution for AddxWefebetpeyggestans

This distribution is known as a Mixture of Gaussians

Assignment Project Exam, Help
$$k=1$$

https://powcoder.com

• We can estimate parameters using Maximum Likelihood, i.e.

Add WeChat powcoder maximize

$$\ln p(X|\boldsymbol{\pi},\boldsymbol{\mu},\boldsymbol{\Sigma}) =$$

ln 
$$p(x^1, x^2, ..., x^N | \pi_1, ..., \pi_K, \mu_1, ..., \mu_K, \Sigma_1, ..., \Sigma_K)$$

- This algorithm is called Expectation Maximization (EM)
- Very similar to soft version of K-Means!

## Assignment Project Exam Help Expectation Maximization

 We can estimate parameters using Maximum Likelihood, i.e. minimize neg. log likelihood

$$-\ln p(\mathbf{X}|\boldsymbol{\pi},\boldsymbol{\mu},\boldsymbol{\Sigma}) = -\sum_{\mathbf{h}}^{\mathbf{N}} \ln \left\{ \sum_{\mathbf{x} \in \mathbf{V}}^{\mathbf{K}} \mathbf{x}_{\mathbf{k}} \mathbf{H} \mathbf{elp} \atop \mathbf{x}_{\mathbf{k}} \mathcal{N}(\mathbf{x}_{n}|\boldsymbol{\mu}_{\mathbf{k}},\boldsymbol{\Sigma}_{\mathbf{k}}) \right\}$$

#### Add WeChat powcoder

- Problem: don't know values of "hidden" (or "latent") variable
   z, we don't observe it
- Solution: treat  $z^i$  as parameters and use coordinate descent

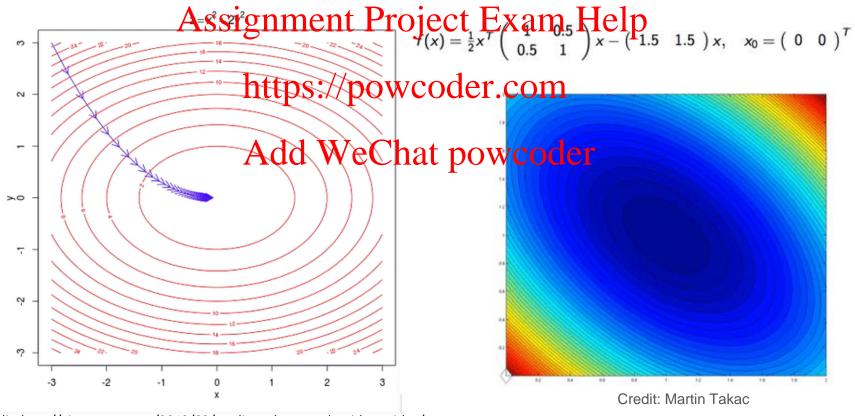
### Assignment Project Exam Help Coordinate Descent Add WeChat powcoder

#### gradient descent:

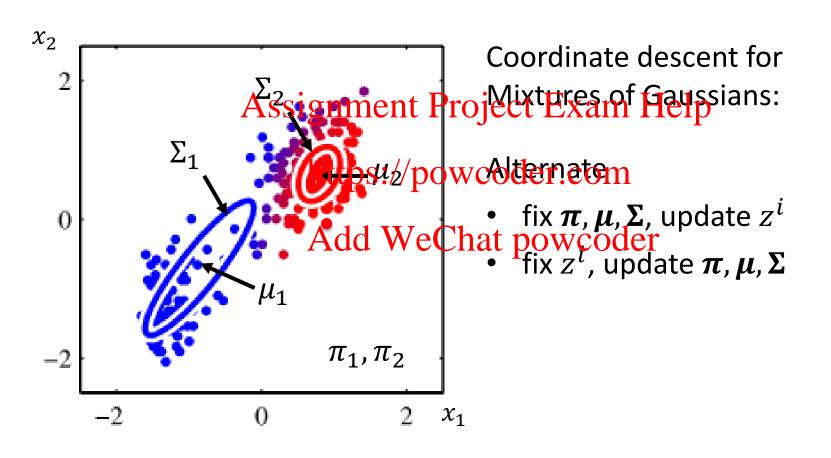
 Minimize w.r.t all parameters at each step

#### coordinate descent:

- fix some coordinates, minimize w.r.t. the rest
- alternate



# Assignment Project Exam Help Expectation Maximization



## Assignment Project Exam Help Expectation Waximization Algorithm

- A general technique for finding maximum likelihood estimators in latent variable models
- Initialize and iteratmuetit Convierge Eseam Help

**E-Step:** estimate posterior probability of the latent variables  $p(z_k|x)$ , holding parameters fixed

**M-Step:** maximize likelihood w.r.t parameters (here  $\mu_k$ ,  $\Sigma_k$ ,  $\pi_k$ ) using latent probabilities from E-step

#### Assignment Project Exam Help From Gaussian Mixtures Example Add WeChat powcoder

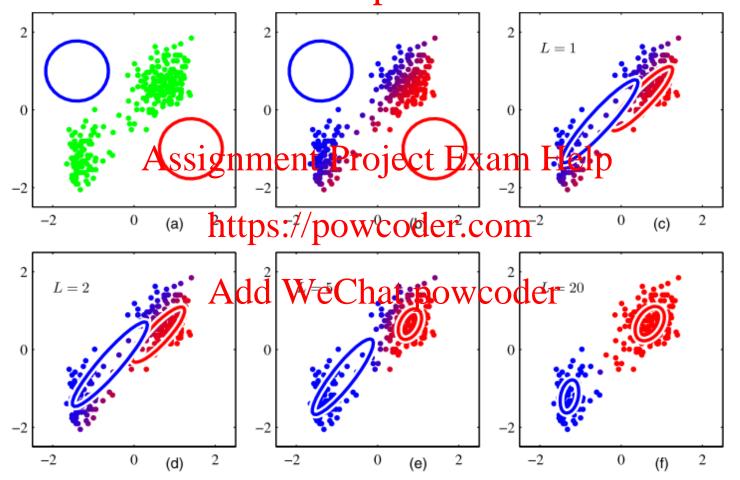


Figure 9.8 Illustration of the EM algorithm using the Old Faithful set as used for the illustration of the K-means algorithm in Figure 9.1. See the text for details.

#### Assignment Project Exam Help EW for Gaussian Wixtures

#### Add WeChat powcoder

- 1. Initialize the means  $\mu_k$ , covariances  $\Sigma_k$  and mixing coefficients  $\pi_k$ , and evaluate the initial value of the log likelihood.
- 2. **E step**. Evaluate the responsibilities using the current parameter values



$$\gamma(z_k) \equiv p \text{Assignment} \frac{P_k^{\pi_k} \mathcal{N}(\mathbf{x}_n | \boldsymbol{\mu}_k, \boldsymbol{\Sigma}_k)}{\text{Froject Exam Help}} \text{Help}$$
(9.23)

3. M step. Re-estimate the parameters using the current responsibilities

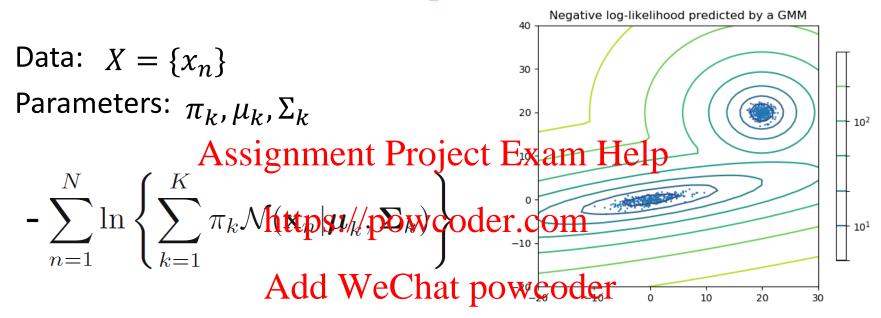
$$\boldsymbol{\mu}_{k}^{\text{new}} = \frac{1}{N_{k}} \sum_{n=1}^{N} \gamma(z_{nk}) \mathbf{x}_{n} \qquad N_{k} = \sum_{n=1}^{N} \gamma(z_{nk}) \qquad (9.24)$$

$$\Sigma_k^{\text{new}} = \frac{1}{N_k} \sum_{n=1}^N \gamma(z_{nk}) \left( \mathbf{x}_n - \boldsymbol{\mu}_k^{\text{new}} \right) \left( \mathbf{x}_n - \boldsymbol{\mu}_k^{\text{new}} \right)^{\text{T}}$$
(9.25)

$$\pi_k^{\text{new}} = \frac{N_k}{N} \tag{9.26}$$

see Bishop Ch. 9.2

## Gaussian Mixtures powcoder



How many possible solutions for K clusters?  $K^N$ 

Is the cost function convex? no

# Assignment Project Exam Help Add weether powers

- Unsupervised learning
- Discrete latent variables:

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  - K-Means clusteting://powcoder.com
  - Gaussian Mixture clustering Add WeChat powcoder
- Next time: Continuous latent variables
  - Principal components analysis

# Assignment Project Exam Help Add Weenat powerser

**Unsupervised Learning I: PCA:** 

dimensionality reduction, PCA Assignment Project Exam Help

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Reading: Bishop 12.1

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