Assignment Project Exam Help Announcements Add WeChat powcoder

Reminder: pset5 out, due midnight today

- pset5 self-graiging for Project/Forday, toble 11/16 (1 week)

 https://powcoder.com
- pset 6 out next week 11/12 Add WeChat powcoder



Reinforcement Learning

Deep Mind's bot playing Atari Breakout

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https://powcoder.com

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https://www.youtube.com/watch?v=TmPfTpjtdgg



Reinforcement dearning roject Exam Help

- Plays Atari video games
 https://powcoder.com
 Beats human champions at Poker and Go
- Robot learns to prekly stadio coder
- Simulated quadruped learns to run



What is reinforcement learning?

Reinforcement Learning

Types of Ada Weichgt powcoder



Supervised

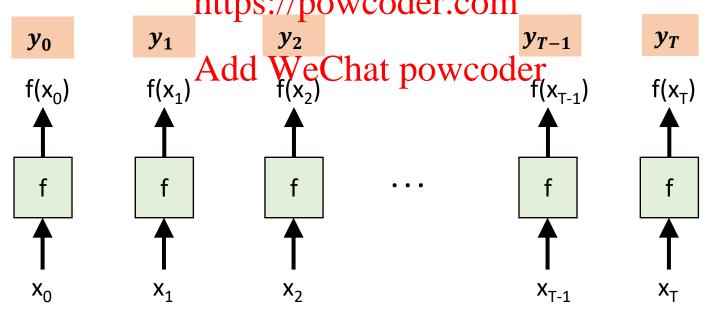
Add WeChat powcoder Unsupervised

Reinforcement

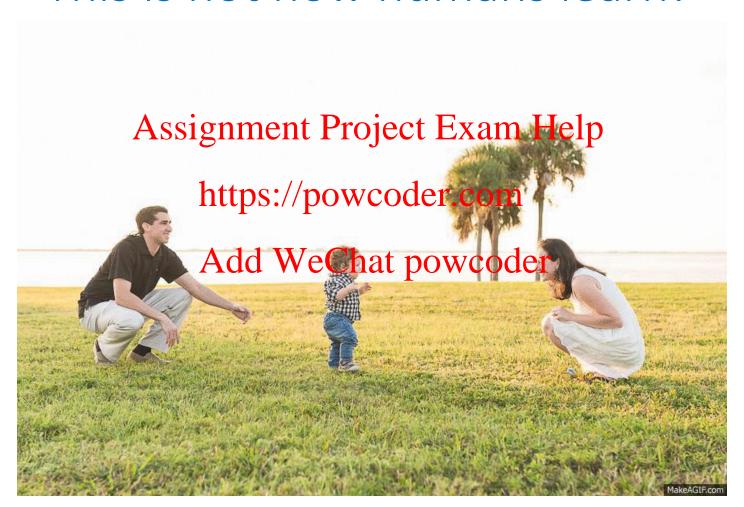
Assignment Project Exam Help Supervised Learning Add WeChat powcoder

- model f receives input x
- also gets correct output y
- predictions do not change future inputs Assignment Project Exam Help

Supervised learning: (in arbitrary order of examples) https://powcoder.com_____



Add WeChat powcoder This is not how humans learn!



Assignment Project Exam Help Reinforcement learning Add WeChat powcoder

- agent receives input x, chooses action
- gets R (reward) after T time steps
- actions affect the next input (state) Assignment Project Exam Help

Reinforcement learning:

https://powcoder.com $f(x_0) \qquad f(x_1) \qquad f(x_2) \qquad f(x_{T-1}) \qquad f(x_{T-1}) \qquad f(x_T) \qquad$

Assignment Project Exam Help Input is the "world's" state Add WeChat powcoder

- Current game board layout
- Picture of table with blocks
- Quadriped poisition and red of the Earth Help



Assignment Project Exam Help Output is an action Add WeChat powcoder

- Which game piece to move where (discrete)
- Orientation and position of robot arm (continuous)
- Joint angles signmentubed detgE (contitulpus)



Actions affect state!

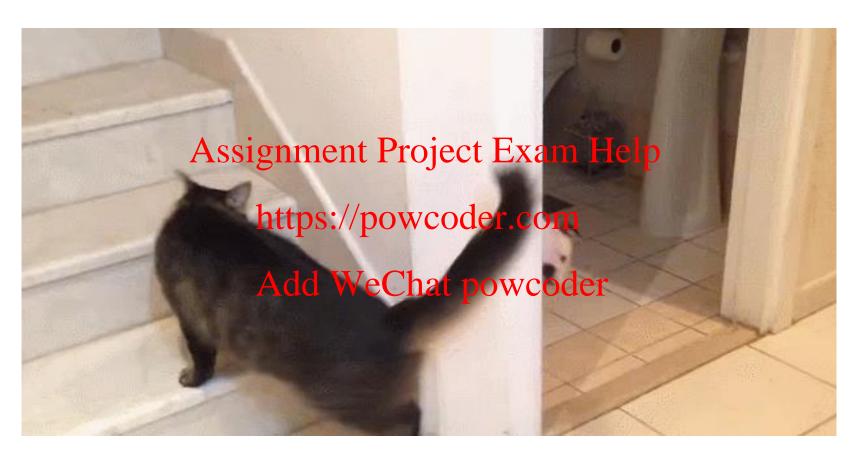
Assignment Project Exam Help action Feward



Only some actions lead to rewards



Assignment Project Exam Help Somadrave Canadrave Canadr



Assignment Project Exam Help Reward examples Add Wechat powcoder

- Wining the game (positive)
- Successfully picking up block (positive)
- Falling (negativement Project Exam Help



Assignment Project Exam Help Goal of reinforcement learning Add WeChat powcoder

- Learn to predict actions that maximize future rewards
- Need a new mathematical framework Assignment Project Exam Help

Reinforcement learning:

https://powcoder.com $f(x_0) \qquad f(x_1) \qquad f(x_2) \qquad f(x_2) \qquad f(x_{T-1}) \qquad f(x_T)$ $f \qquad f \qquad f \qquad f \qquad f \qquad f$ $x_0 \qquad x_1 \qquad x_2 \qquad x_{T-1} \qquad x_T$



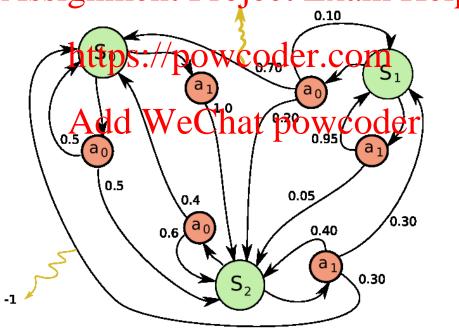
Markov Decision Process

Reinforcement Learning

Assignment Project Exam Help Markov Decision Process (MPD) Add WeChat powcoder

Definition: a mathematical framework for modeling <u>decision</u> making in situations where outcomes are partly <u>random</u> and partly under the control of a decision maker.

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https://en.wikipedia.org/wiki/Markov decision process

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Output

- $R: S \to \mathbb{R}$ (Reward)
- Psa transition probabilities ($p(s, a, s) \in \mathbb{R}$)
- γ discount factord WeChat powcoder

MDP = (S, A, R, Psa,
$$\gamma$$
)

Assignment Project Exam Help Discount factor y Add WeChat powcoder

 discount factor prevents the total reward from going to infinity $(0 \le \gamma \le 1)$

 Assignment Project Exam Help
 makes the agent prefer immediate rewards to rewards that are potentially received far away in the future

• E.g., two paths to the goal state: 1) longer path but gives higher reward 2) shorter path with smaller reward; the γ value controls which the path the agent should prefer

Assignment Project Exam Help (Simple example) Add WeChat powcoder



Assignment Project Exam Help MDP (Simple example) Add WeChat powcoder

	1	2	3	4
1		nt Project //powcode	Exam Hel r.com	#
2	Add	WeChat po	wcoder	7
3				

MDP (Simple Weethat power better

States S = loc

States S = locations		1	2	3	4	
• Actions $A = \{ \uparrow, \rightarrow, \leftarrow, \downarrow \}$ Assignment Project I	I Exan	ı He	ln		† 5	
https://powcoder	2		P		7	•
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MDP (Simple Weethat provided r

States S = locations

3

• Actions $A = \{ \uparrow, \rightarrow, \leftarrow, \downarrow \}$ • Reward $R: S \rightarrow \mathbb{R}$ 1 0 0
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https://powcoder.com 0

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MDP (Simple Weethat power better

States S = locations		1	2	3	4
• Actions $A = \{ \uparrow, \rightarrow, \leftarrow, \downarrow \}$ • Reward $R: S \rightarrow \mathbb{R}$	1 Exan	- <u>.02</u> 1 He	02	02	+1
• Reward $R: S \to \mathbb{R}$ https://powcode			4Ρ	02	-1
	3	02	02		02
Add WeChat po	WCO	aer			

MDP (Simple We Charpowe beer

- States S = locations
- Actions $A = \{ \uparrow, \rightarrow, \leftarrow, \downarrow \}$ Reward $R: S \rightarrow \mathbb{R}$
- Transition Psahttps://powcodes

	1	2	3	4
_ <u>1</u> Exan	02 1 He	02	02	+1
2 r.con	02	*P	02	-1
3	02	02		02

$$P_{(3,3),\uparrow}((2,3)) \triangleq 0.8$$
 We Chat powcoder $P_{(3,3),\uparrow}((3,4)) = 0.1$ $P_{(3,3),\uparrow}((3,2)) = 0.1$ $P_{(3,3),\uparrow}((1,3)) = 0$ \vdots

MDP - Dynamics Add WeChat powcoder 1

- Start from state S_0
- Choose action A_0
- Transit to Assignment Project Example lo
- coder
 1
 2
 3
 4

 1
 -.02
 -.02
 -.02
 +1

 2
 -.02
 -.02
 -1

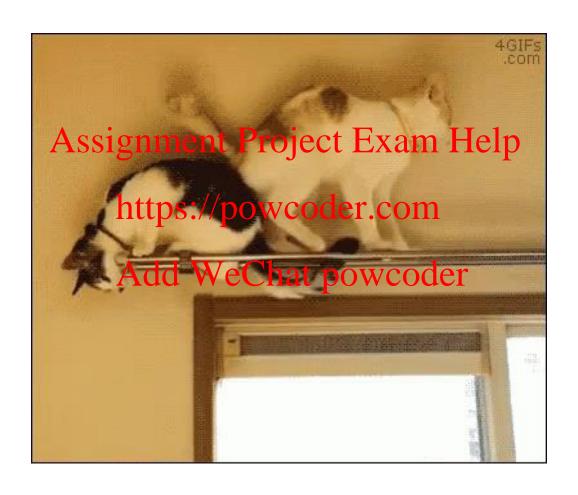
 E3amble 10
 -.02
 -.02
- Continue... https://powcoder.com

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Total payoff:

$$R(s_0) + \gamma R(s_1) + \gamma^2 R(s_2) + \cdots$$

Assignment Project Exam Help How dad/wethatps@coderd actions?



Choosing actions in MDP Add WeChat powcoder

States S = locations			1	2	3	4
Actions A = $\{\uparrow, \rightarrow, \leftarrow, \downarrow\}$						
Reward $R: S \to \mathbb{R}$		1	02	02	02	+1
Transition Psassignment Project		Exa	mo bl e	elp	02	-1
https:	//powcode	er 3 0	m 02	02		02

• Goal - Choose actions as to maximize expected total payoff:

$$E\left[R(s_0) + \gamma R(s_1) + \gamma^2 R(s_2) + \cdots\right]$$

- In our example:
 - R get to charge station, avoid stairs
 - γ discourage long paths, how much to delay reward

MDP Assignment Project Exam Help Add We Chat revised ar

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States S = locations			1	2	ω	4
Actions A = $\{\uparrow, \rightarrow, \leftarrow, \downarrow\}$		_			_	<u> </u>
Reward $R: S \to \mathbb{R}$		1	→	\rightarrow	\uparrow	+1
Transition Psassignment Project		Exa	m (H)	elp	1	-1
https://	//powcode	er 3 0	m >		1	1

• Goal - Choose actions as to hat in the control of the control of

$$E\left[R(s_0) + \gamma R(s_1) + \gamma^2 R(s_2) + \cdots\right]$$

• Policy is a function $\pi: S \to A$



Policy Value and Q functions

Reinforcement Learning

MDP Assignment Project Exam Help Policy Value Tunction

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States S = locations			1	2	ω	4
Actions A = $\{\uparrow, \rightarrow, \leftarrow, \downarrow\}$			_			•
Reward $R: S \to \mathbb{R}$		1	\	\rightarrow	\rightarrow	+1
Transition Psassignme	nt Project	Exa	m KH	elp	→	-1
Policy $\pi: S \to A$ https:	//powcode	er 3 0	m >	—	1	1

Value function for polity a Chatspower

$$V^{\pi}(s) = \mathbb{E}\left[R(s_0) + \gamma R(s_1) + \gamma^2 R(s_2) + \cdots \mid s_0 = s, \pi\right]$$

Expected sum of discounted rewards

Assignment Project Exam Help MDP – Policy value function Add WeChat powcoder

$$V^{\pi}(s) = \mathbb{E}\left[R(s_0) + \gamma R(s_1) + \gamma^2 R(s_2) + \cdots \middle| s_0 = s, \pi\right]$$

$$\Rightarrow V^{\pi}(s) = E[R(s_0)] + E[\gamma R(s_1) + \gamma^2 R(s_2) + \cdots]$$
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Bellman's equation: https://powcoder.com

$$V^{\pi}(s) = R(s) + \gamma E_{s'} [V(s')]$$

exp

expectation over values of next state

$$V^{\pi}(s) = R(s) + \gamma \sum_{s' \in S} P_{s\pi(s)}(s') V^{\pi}(s')$$

Assignment Project Exam Help MDP – Policy value function Add WeChat powcoder

$$V^{\pi}(s) = R(s) + \gamma \sum_{s' \in S} P_{s\pi(s)}(s') V^{\pi}(s')$$

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Policy π

3

Assignment Project Exam Help Optimal value function Add WeChat powcoder

If the agent uses a given policy π to select actions, the corresponding value function is given by:

$$V^{\pi}$$
Assign (n) entry Project s Exam (slep)

https://powcoder.com
There exists an optimal value function that has higher value than other function that has higher value than other function that has higher value.

$$V^*(s) = \max_{\pi} V^{\pi}(s) \quad \forall s \in \mathbb{S}$$

The optimal policy π^* is the policy that corresponds to the optimal value function

$$\pi^* = \arg\max_{\pi} V^{\pi}(s) \quad \forall s \in \mathbb{S}$$

Assignment Project Exam Help Value function vs. Q-function Add WeChat powcoder

For convenience, RL algorithms introduce the Q-function, which takes a state-action pair and returns a real value

The optimal Q-function: Q_p^* for Q_p^* to the highest expected total reward received by an agent starting in s and choosing action a which maximize value by a which maximize a which a which

$$V^*(s) = \max_{a} Q^*(s, a) \quad \forall s \in \mathbb{S}$$

 $Q^*(s,a)$ is an indication for how good it is for an agent to pick action a while being in state s

Assignment Project Exam Help Optimal Q-function Add WeChat powcoder

If we know the optimal Q-function $Q^*(s,a)$, the optimal policy π^* can be easily extracted by choosing the action a that gives maximum $Q^*(s, a)$ for state s:
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$$\pi^*(s) = \underset{\text{https://powcoder.com}}{\operatorname{arg.max}} Q^*(s, a) \quad \forall s \in \mathbb{S}$$

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RL Approaches

Reinforcement Learning

Assignment Project Exam Help Reinforcement learning approaches Add WeChat powcoder

Value-based RL

- Estimate the optimal value function
- *i.e.*, the maximum value achievable under any policy
- Guarantestig ponvente Projetin Emam Help

Policy-based RL https://powcoder.com • Search directly for the optimal policy

- · re-define the policy we ech step one compute the value according to this new policy until the policy converges
- Guaranteed to converge, often faster than value

Q-learning

- Search for the optimal Q-function
- No prior knowledge of MDP required

Assignment Project Exam Help Value Iteration Algorithm Add WeChat powcoder

Given $P_{s,a}(s') = p(s'|s,a)$, iteratively compute the Q and value functions using Bellman's equation.

```
Initialize V(s) to arbitrary values

Repeat https://powcoder.com

For all s \in S

For all a \notin A

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Q(s,a) \leftarrow E[r|s,a] + \gamma \sum_{s' \in S} P(s'|s,a)V(s')

V(s) \leftarrow \max_a Q(s,a)

Until V(s) converge
```

Assignment Project Exam Help Policy Iteration Algorithm Add WeChat powcoder

Given $P_{s,a}(s') = p(s'|s,a)$, π , iteratively compute the policy's value function and improve the policy to maximize it

Assignment Project Exam Help Reinforcement learning approaches Add WeChat powcoder

Optimal value function

need Psa

$$V^*(s) = \max_{\pi} V^{\pi}(s)$$

$$\text{Bellman:} \underline{\mathsf{AVSS}} \text{ ign} \underline{\overline{\mathsf{m}}} ents \text{ Project } \underline{\mathtt{Exan}} P_{\underline{\mathsf{Help}}} V^*(s')$$

Optimal policy

https://powcoder.com

need π , Psa

$$\pi^*(s) = \arg\max_{a \in A} \underbrace{\sum_{s' \in S} P_{sa}(s)}_{e} pewsoder$$

Optimal state-action value function Q

easier!

Define
$$Q: S \times A \to \mathbb{R}$$

Bellman:
$$Q^*(s, a) = R(s) + \gamma \max_{a \in A} Q^*(s', a)$$



Q-Learning (discrete)

Reinforcement Learning

Assignment Project Exam Help Q-value function Add WeChat powcoder

- A value function is a prediction of future reward
 - "How much reward will I get from action a in state s?"
- Q-value function gives expected total reward Assignment Project Exam Help
 from state s and action a

 - under polityttps://powcoder.com
 - with discount factor γ

$$Q^{\pi}(s, A) dd \mathbb{W}_{e} Chat powcod r_{t+3} + ... \mid s, a]$$

Value functions decompose into a Bellman equation

$$Q^{\pi}(s,a) = \mathbb{E}_{s',a'}\left[r + \gamma Q^{\pi}(s',a') \mid s,a\right]$$

Assignment Project Exam Help Optimal Q-value function Add WeChat powcoder

An optimal value function is the maximum achievable value

$$Q^*(s,a) = \max_{\pi} Q^{\pi}(s,a) = Q^{\pi^*}(s,a)$$

► Once we haves@igmanonacProtiocativExam Help

► Optimal value maximise weer all decisions old formally:

$$Q^*(s, a) = r_{t+1} + \gamma \max_{a_{t+1}} r_{t+2} + \gamma^2 \max_{a_{t+2}} r_{t+3} + \dots$$

= $r_{t+1} + \gamma \max_{a_{t+1}} Q^*(s_{t+1}, a_{t+1})$

► Formally, optimal values decompose into a Bellman equation

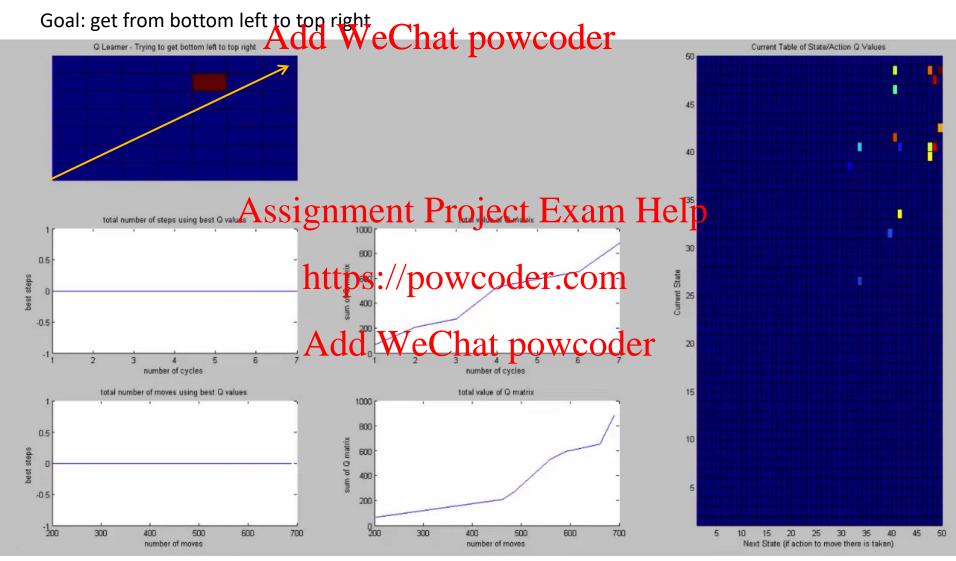
$$Q^*(s,a) = \mathbb{E}_{s'}\left[r + \gamma \max_{a'} Q^*(s',a') \mid s,a
ight]$$

Assignment Project Exam Help Q-learning algorithm Add WeChat powcoder

The agent interacts with the environment, updates Q recursively

```
initialize Assignment, Projecti Exame Helprily
observe initial state s
                 https://pbwcoder.com
repeat
      select and carry out an action a
      observe reward wechan poweoder
      Q[s,a] = Q[s,a] + \alpha(r + \gamma \max_{a'} Q[s',a'] - Q[s,a])
      s = s'
until terminated
                             discount
                                        largest increase over all
             current value
                                        possible actions in new state
                     learning rate
```

Q-learniassignment Project Exam Help



https://www.youtube.com/watch?v=R88CiN7dTZc

Assignment Project Exam Help Exploration Add WeChat powcoder

- How does the agent select actions during learning? Should it trust the learned values of Q(s, a) to select actions based on it? or try other actions hoping this may give it a better reward? Assignment Project Exam Help
- This is known as the exploration dilemma
- Simple ε -greedy approach: at each step with small probability ϵ , the agent will pickla and off action (explore) or with probability (1- ϵ) the agent will select an action according to the current estimate of Q-values
- The ϵ value can be decreased overtime as the agent becomes more confident with its estimate of Q-values



Continuous state

Reinforcement Learning

Assignment Project Exam Help Continuous state - Pong Add WeChat powcoder



https://www.youtube.com/watch?v=YOW8m2YGtRg

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MDP for Pong Add WeChat powcoder

In this case, what are these?

- S set of States
- A set of Actionsnment Project Exam Help
- $R: S \to \mathbb{R}$ (Reward)
- Psa transition probabilities $(p(s, a, s) \in \mathbb{R})$

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Can we learn Q-value?

- Can discretize state space, but it may be too large
- Can simplify state by adding domain knowledge (e.g. paddle, ball), but it may not be available
- Instead, use a neural net to learn good features of the state!



Deep RL

Reinforcement Learning

Assignment Project Exam Help Deep RL playing DOTA Add WeChat powcoder



https://www.youtube.com/watch?v=eHipy j29Xw

Assignment Project Exam Help Deep Rl Add WeChat powcoder

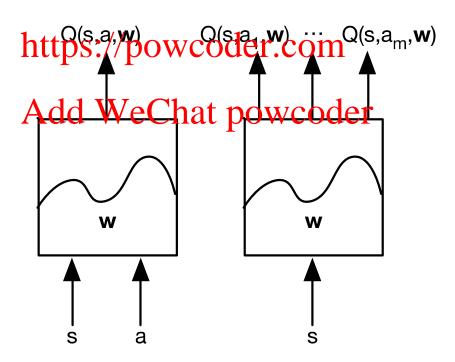
- V, Q or π can be approximated with deep network
- Deep Q-Learning
 - Input: state, action Assignment Project Exam Help
 Output: Q-value Cover today
- Alternative: leatpsa/plicy/cledwo.dom
 - Input: state
 - Output: distribution worker hattons wooder

Assignment Project Exam Help Q-value network Add WeChat powcoder

Represent value function by Q-network with weights w

$$Q(s, a, \mathbf{w}) \approx Q^*(s, a)$$

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Assignment Project Exam Help Q-value network Add WeChat powcoder

Optimal Q-values should obey Bellman equation

$$Q^*(s,a) = \mathbb{E}_{s'} \left[r + \gamma \max_{s,a} Q(s',a')^* \mid s,a \right]$$

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- ► Treat right-hand side rs://pmax coder.com as a target
- Minimise MSE loss by stochastic gradient descent Add WeChat powcoder

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$$I = \left(r + \gamma \max_{a} Q(s', a', \mathbf{w}) - Q(s, a, \mathbf{w})\right)^{2}$$

- ightharpoonup Converges to Q^* using table lookup representation
- ▶ But diverges using neural networks due to:
 - Correlations between samples
 - Non-stationary targets

Assignment Project Exam Help Deep Q-network (DQN) Add WeChat powcoder

To remove correlations, build data-set from agent's own experience

Assignment Project Exame, Help'
$$s_{3}, a_{3}, r_{4}, s_{4}$$

$$https://powcoder.com$$

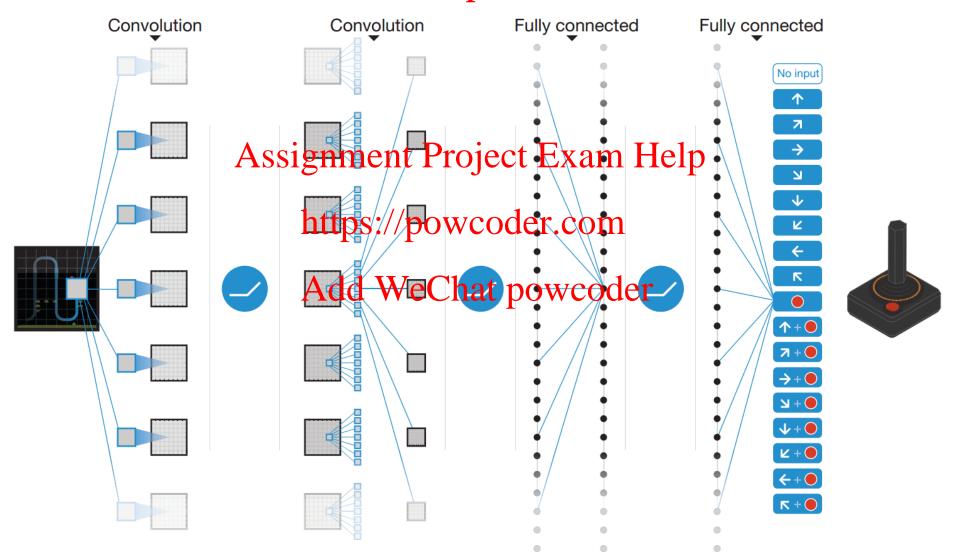
$$s_{t}, a_{t}, r_{t+1}, s_{t+1} \rightarrow s_{t}, a_{t}, r_{t+1}, s_{t+1}$$
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Sample experiences from data-set and apply update

$$I = \left(r + \gamma \max_{a'} Q(s', a', \mathbf{w}^-) - Q(s, a, \mathbf{w})\right)^2$$

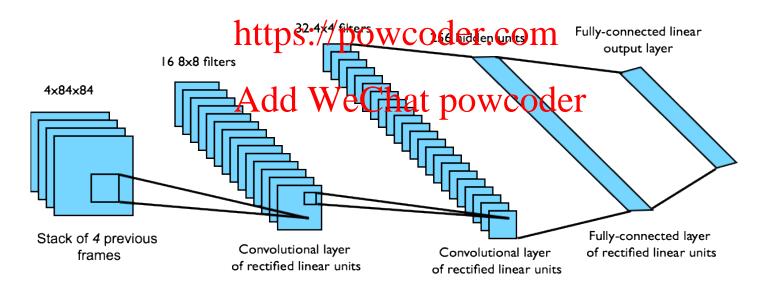
To deal with non-stationarity, target parameters \mathbf{w}^- are held fixed

Assignment Project Exam Help DQN - Playing Atari Add WeChat powcoder



Assignment Project Exam Help DQN - Playing Atari Add WeChat powcoder

- End-to-end learning of values Q(s, a) from pixels s
- Input state s is stack of raw pixels from last 4 frames
- Output is Q(s, a) for 18 joystick/button positions
- Reward is Assaigenmeente Porojacts Epxam Help

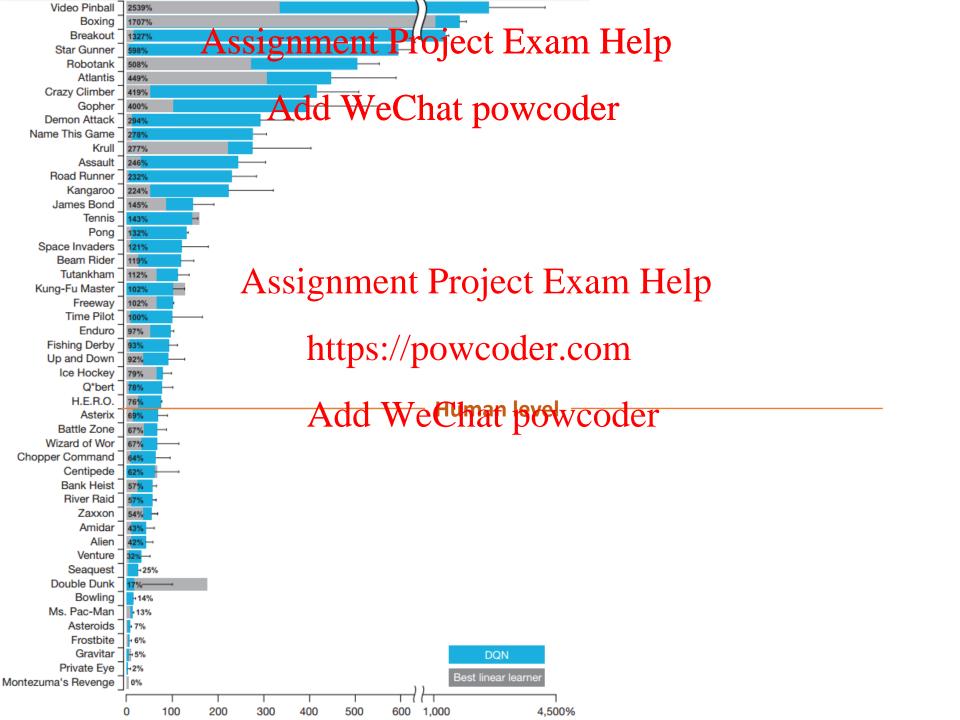


Network architecture and hyperparameters fixed across all games

Assignment Project Exam Help DQN - Playing Atari Add WeChat powcoder

Algorithm 1 Deep Q-learning with Experience Replay

```
Initialize replay memory \mathcal{D} to capacity N
Initialize action-value function Q with random weights
for episode = 1, M dossignment Project Exam Help
     Initialise sequence s_1 = \{x_1\} and preprocessed sequenced \phi_1 = \phi(s_1)
     for t = 1, T do
          t = 1, T do https://powcoder.com With probability \epsilon select a random action a_t
          otherwise select a_t = \max_{t} Q^*(\phi(s_t), a; \theta)
Execute action a_t in emulator and observe reward r_t and image x_{t+1}
          Set s_{t+1} = s_t, a_t, x_{t+1} and preprocess \phi_{t+1} = \phi(s_{t+1})
          Store transition (\phi_t, a_t, r_t, \phi_{t+1}) in \mathcal{D}
          Sample random minibatch of transitions (\phi_j, a_j, r_j, \phi_{j+1}) from \mathcal{D}
         Set y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}
          Perform a gradient descent step on (y_j - Q(\phi_j, a_j; \theta))^2 according to equation 3
     end for
end for
```



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DQN for Atari Add WeChat powcoder

DQN paper:

www.nature.com/articles/nature142 36

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DQN demo:

https://www.youtubetpon//potvier.com qXKQf2BOSE

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DQN source code:

www.sites.google.com/a/deepmind.c om/dgn/



Assignment Project Exam Help Downsides of RL Add WeChat powcoder

- RL is less sampling efficient than supervised learning because it involves bootstrapping, which uses an estimate of the Q-value to update the Q-value predictor.
- Rewards are usually sparse described raining requires to reach the goal by chance Add WeChat powcoder
- Therefore, RL might not find a solution at all if the state space is large or if the task is difficult

Assignment Project Exam Help Summary Add WeChat powcoder

- The goal of Reinforcement learning:
 - learn to predict actions that maximize future rewards
- Markov Dassignment Project Exam Help
 - Formalizes theths frameworker.com
- MDP = (S, A, R, Psa, γ)
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 Approaches to reinforcement learning:
- - Learn value function (offline)
 - Learn optimal policy (offline)
 - Learn Q-function (online)

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Referenced WeChat powcoder

Andrew Ng's Reinforcement Learning course, lecture 16

https://www.youtube.com/watch?v=RtxI449ZjSc

Assignment Project Exam Help Andrej Karpathy's blog post on policy gradient

http://karpathy.github.jo/2016/05/31/rl/https://powcoder.com

Mnih et. al, Playing Atari with Deep Reinforcement Learning (DeepMind) https://www.cs.toronta.add~WieChat/apowcoder

Intuitive explanation of deep Q-learning

https://www.nervanasys.com/demystifying-deep-reinforcement-learning/

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Reinforcement Learning II

Q-learning cont'd; deep Q-learning (DQN)
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https://powcoder.com

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