

Add WeChat powcoder Classification, Regularization

Detecting overfitting

Plot model complexity versus objective function on test/train data

As model becomes more complex,
performance on Assirgng Reap Project Exam Help
improving while on test data it increases
https://powcoder.com

Training — Test

SWE 0.5

Tam Help

On 3 M 6 9

Horizontal axis: measure of model complexity. In this example, we use the maximum order of the polynomial basis functions.

Vertical axis: For regression, it would be SSE or mean SE (MSE) For classification, the vertical axis would be classification error rate or cross-entropy error function

Overcoming overfitting

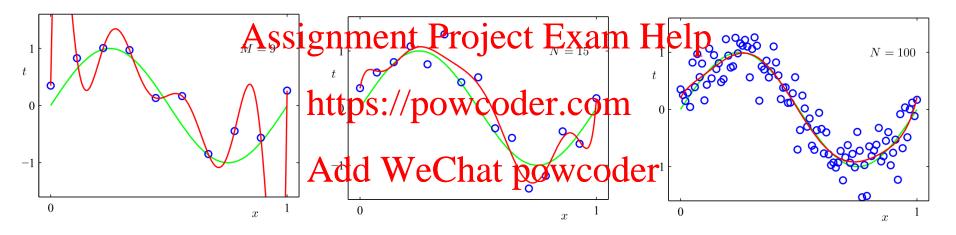
- Basic ideas
 - Use more training data
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 Regularization methods

 - Cross-validation://powcoder.com

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Solution: use more data

M=9, increase N



What if we do not have a lot of data?

Overcoming overfitting

- Basic ideas
 - Use more training data
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 Regularization methods

 - Cross-validation://powcoder.com

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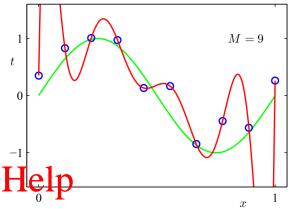
Add WeChat powcoder Regularization

Solution: Regularization

- Use regularization:
 - Add $\lambda \|\theta\|_2^2$ term to SSE cost function
 - "L-2" norm squared, ie sum of sq. elements signment Project Exam Help



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M = 9

0.35

232.37

-5321.83

48568.31

-231639.30

640042.26

-1061800.52

1042400.18

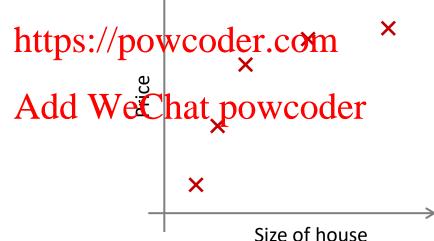
-557682.99

125201.43

Regularized Linear Regression

$$J(\theta) = \frac{1}{2m} \left[\sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \lambda \sum_{j=1}^{n} \theta_j^2 \right]$$

 $\min_{\theta} J(\theta)$ Assignment Project Exam Help



Gradient descent for Linear Regression

```
Repeat {
               \theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_0^{(i)}
              	heta_j := 	heta_j \underbrace{ \underbrace{ \underbrace{ \operatorname{Assign} \underset{m}{\operatorname{m}} \underbrace{ \underset{i=1}{m}} }_{m} \underbrace{ \underbrace{ \operatorname{Project}}_{h_{	heta}} \underbrace{ \operatorname{Exam}}_{i} \underbrace{ \operatorname{Holp}}_{x_j} }_{\operatorname{https://powerder.som}, n)} 
\theta_j := \theta_j (1 - \alpha \frac{\lambda}{m}) - \alpha \frac{1}{m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)} \leftarrow
```

Regularized Normal Equation

Suppose
$$m \leq n$$
, (#examples) (#features)
$$\theta = (X^TX)^{-1}X^Ty \quad \text{Non-invertible/singular}$$

$$\text{Assignment Project Exam Help}$$

If
$$\lambda > 0$$
,
$$\theta = \begin{pmatrix} X^T X \text{Add WeChat powdode} X^T y \\ \vdots \\ 1 \end{pmatrix}$$

Regularized Logistic Regression

Hypothesis:

$$h_{ heta}(x) = g(heta^T x) = rac{1}{1 + e^{- heta^T x}}$$
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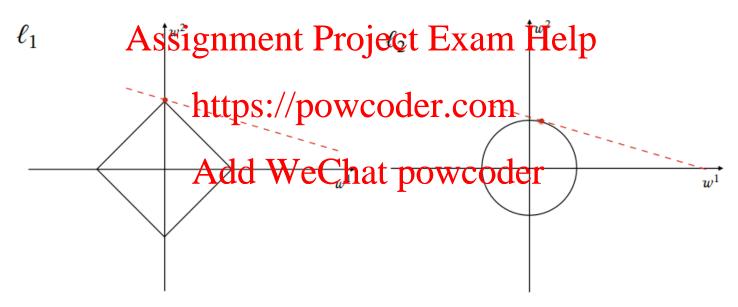
Cost Function:

$$J(\theta) = -\frac{1}{m} \left[\sum_{i=1}^{m} y^{(i)} \log h_{\theta}(x^{(i)}) + (1 - y^{(i)}) \log (1 - h_{\theta}(x^{(i)})) \right]$$

 $\min_{\theta} J(\theta)$ Goal: minimize cost

Many types of Regularization

• Most common are ℓ_1 and ℓ_2



 ℓ_1 often used to create sparsity



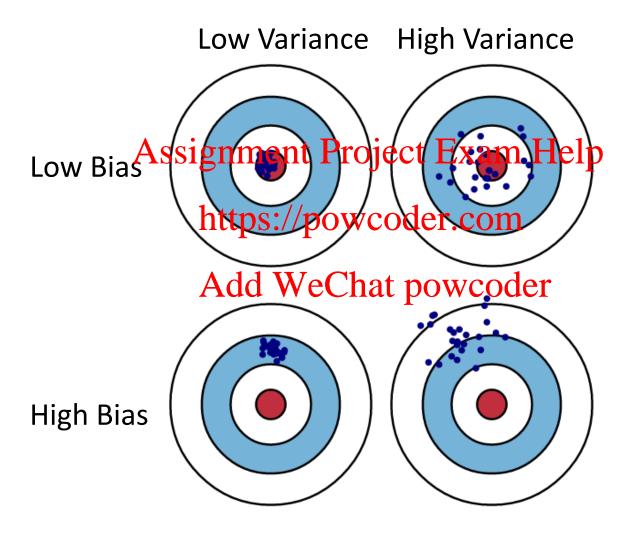
Add WeChat powcoder Blas-Variance

Bias vs Variance

 Understanding how different sources of error lead to bias and variance helps us improve model fitting

- Assignment Project Exam Help
 Error due to Bias: The error due to bias is taken as the difference betweenth processed (prayerage) prediction of our model and the correct value which we are trying to predict (imagine Moldcovie Chaeatohecwhele model fitting process on many datasets)
- Error due to Variance: The variance is how much the predictions for a given point vary between different realizations of the model.

Graphical Illustration



The Bias-Variance Trade-off

There is a trade-off between bias and variance:

- Less complex models (fewer parameters) have high bias and hence low variaing ment Project Exam Help
- More complex models (more parameters) have low bias and hence high variance how coder.com
- Optimal model will have a color

Which is worse?

 A gut feeling many people have is that they should minimize bias even at the expense of variance

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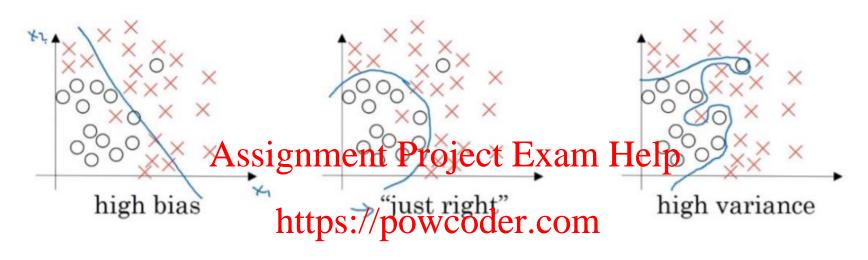
- This is mistaken logic. It is true that a high variance and low bias model can prefer well in some sort of long-run average sense. However, in practice modelers are always dealing with a single realization of the data set
- In these cases, long run averages are irrelevant, bias and variance are equally important, and one should not be improved at an excessive expense to the other.

How to deal with bias/variance

- Can deal with variance by
 - Bagging, e.g. Random Forest
 - Bagging transmighter robbets Examples of the data, averages their prediction https://powcoder.com
- Can deal with high bias by
 - Decreasing regularization/increasing complexity of model
 - Also known as model selection



Add WeChat powcoder Model selection and training/validation/test sets



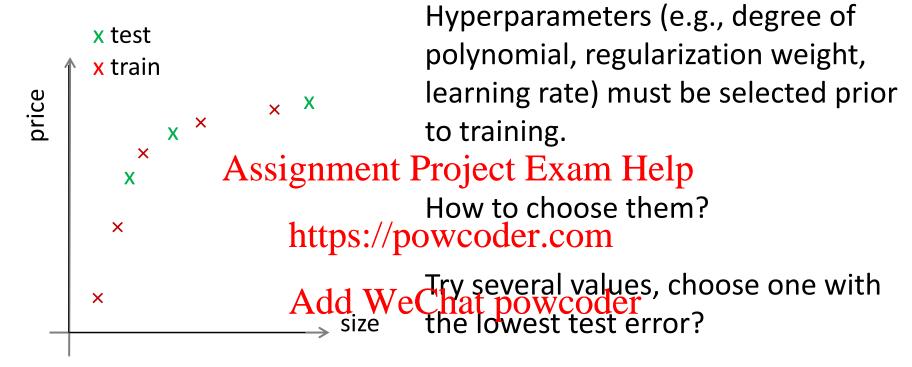
Not performing well on training data

Add WeChat powcoder generalizing well from training to unseen data

(underfit)

(overfit)

Model selection



$$h_{\theta}(x) = \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$

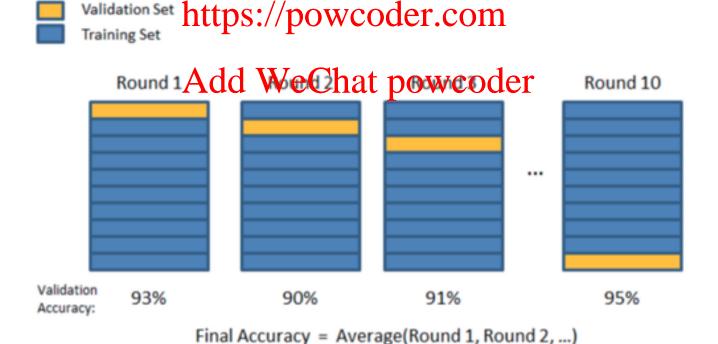
Problem: test error is likely an overly optimistic estimate of generalization error because we "cheat" by fitting the hyperparameter to the actual test examples.

Train/Validation/Test Sets

_	Size	Price	Solution: split data into three sets.
train	2104	400	•
	1600	A330	For each value of a hyperparameter, nment Project Exam Help train on the train set, evaluate
	2400		
	1416	232 <mark>h</mark>	ttps://plearped.parameters on the validation set.
	3000	540 🛕	dd WeChat powcoder
validation	1985	300	Pick the model with the hyper
	1534	315	parameter that achieved the lowest
	1427	199	validation error.
test	1380	212	Report this model's test set error.
	1494	243	

N-Fold Cross Validation

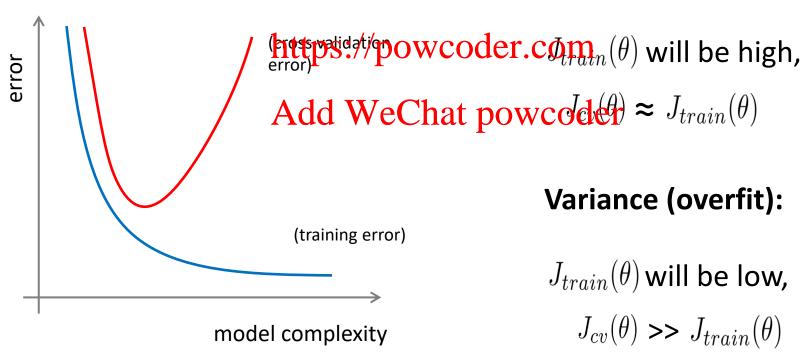
- What is we don't have enough data for train/test/validation sets?
- Solution: use N-fold cross validation.
- Split training set into train/validation sets N times
- Report average spending to the Povoje of Lake 10:



Diagnosing bias vs. variance

Suppose your learning algorithm is performing less well than you were hoping. ($J_{cv}(\theta)$ or $J_{test}(\theta)$ is high.) Is it a bias problem or a variance problem?

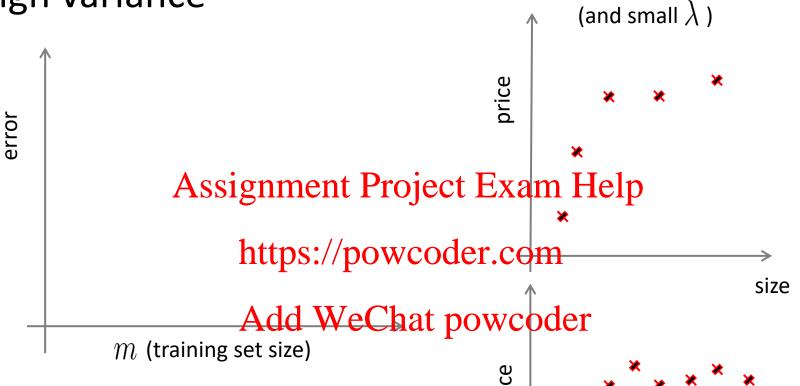
Assignment Project Exhias Hungerfit):



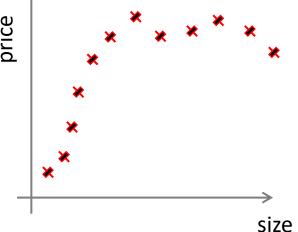
Learning Curves: $h_{\theta}(x) = \theta_0 + \theta_1 x$ High bias price error Assignment Project Exam Help https://powcoder.com size Add WeChat powcoder m (training set size) price If a learning algorithm is suffering from high bias, getting more training data will not (by itself) help much.

size

Learning Curves: High variance



If a learning algorithm is suffering from high variance, getting more training data is likely to help.



 $h_{\theta}(x) = \theta_0 + \theta_1 x + \dots + \theta_{100} x^{100}$

Debugging a learning algorithm

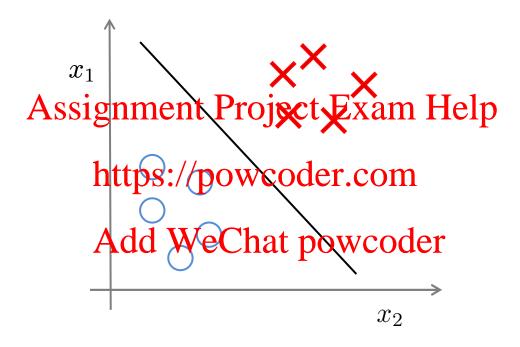
Suppose you have implemented regularized linear regression to predict housing prices. However, when you test your hypothesis in a new set of houses, you find that it makes unacceptably large errors in its prediction. What should you transfect Exam Help

To fix high variance to fix high bias https://powcoder.com

- Get more training examples
- Try getting additional features
- Try smaller sets of Acture eChat powisodeing polynomial features
- Try increasing λ

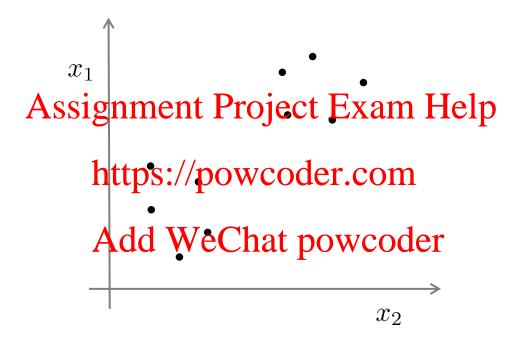
Try decreasing λ

Supervised learning



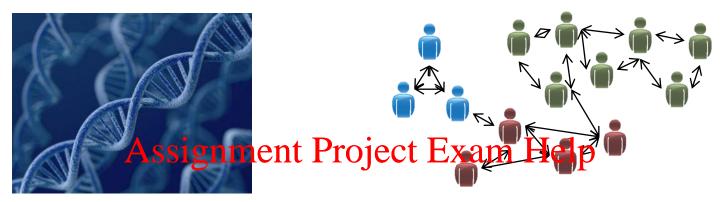
Training set: $\{(x^{(1)},y^{(1)}),(x^{(2)},y^{(2)}),(x^{(3)},y^{(3)}),\dots,(x^{(m)},y^{(m)})\}$

Unsupervised learning

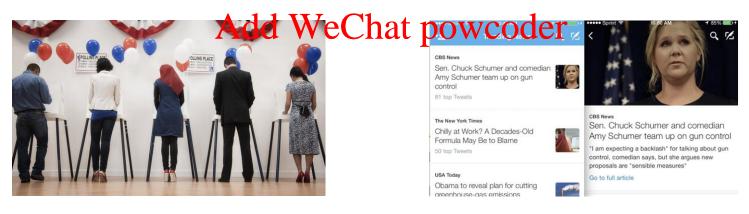


Training set: $\{x^{(1)}, x^{(2)}, x^{(3)}, \dots, x^{(m)}\}$

Clustering

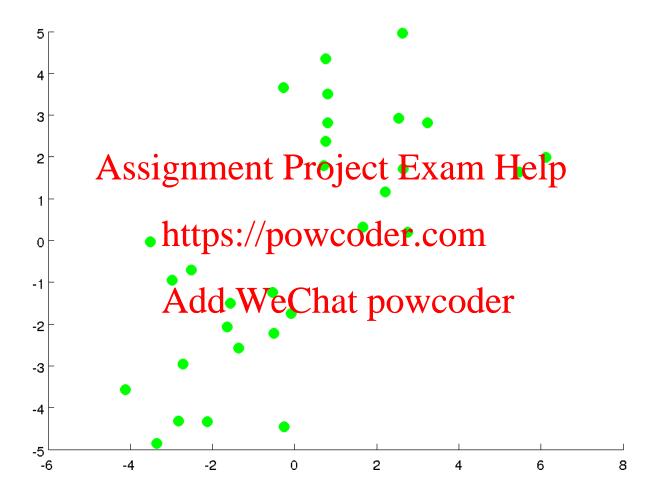


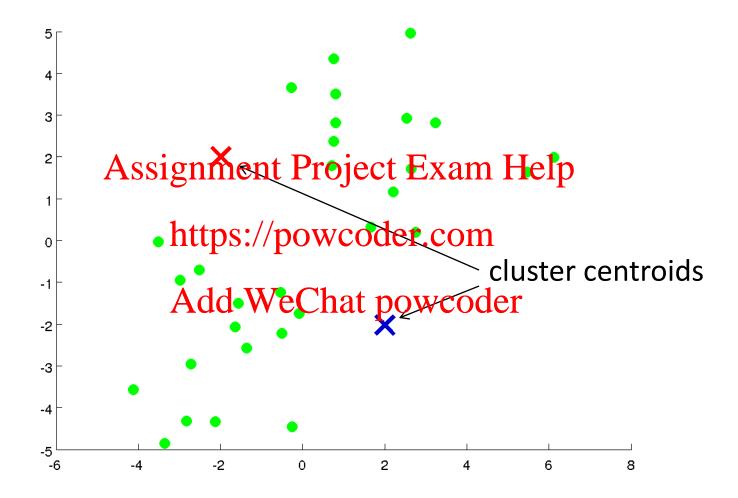
Gene analysihttps://powcoder.sociametwork analysis

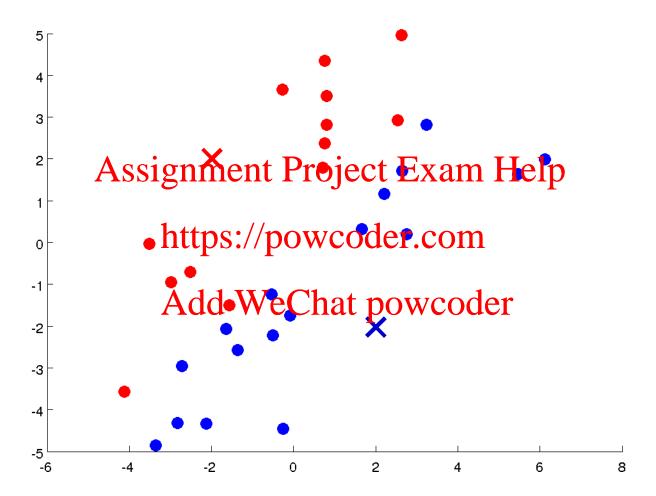


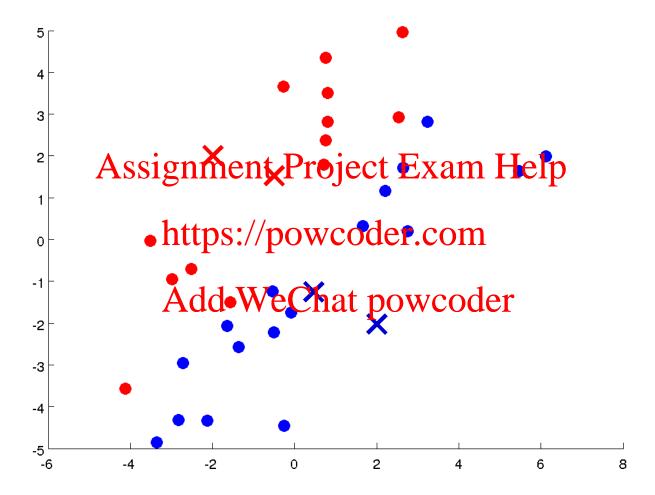
Types of voters

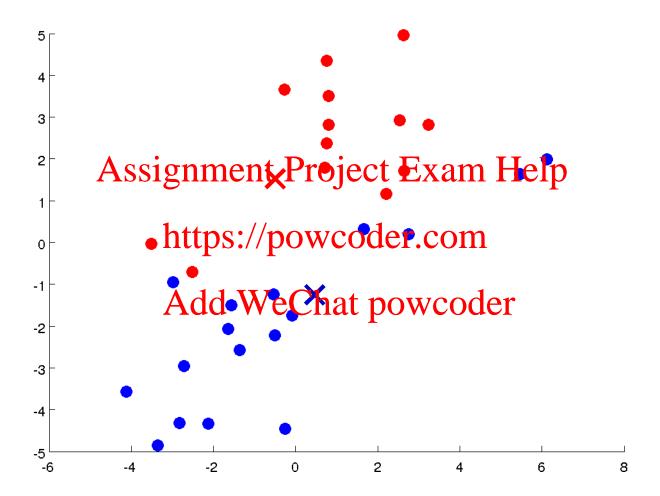
Trending news











Next Class

Unsupervised Learning I: Clustering:

clustering, k-means, Gaussian mixtures.
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Reading: Bishop 9.1-9.2 Add WeChat powcoder

PSet 2 Out

Due in 1 week: 9/24 11:59pm GMT -5 (Boston Time)

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Regression, gradient descent
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