

# CS157A: Introduction to Database Management Systems

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Chapter 1: Introduction

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Chapter 2: The Relational Model of Data

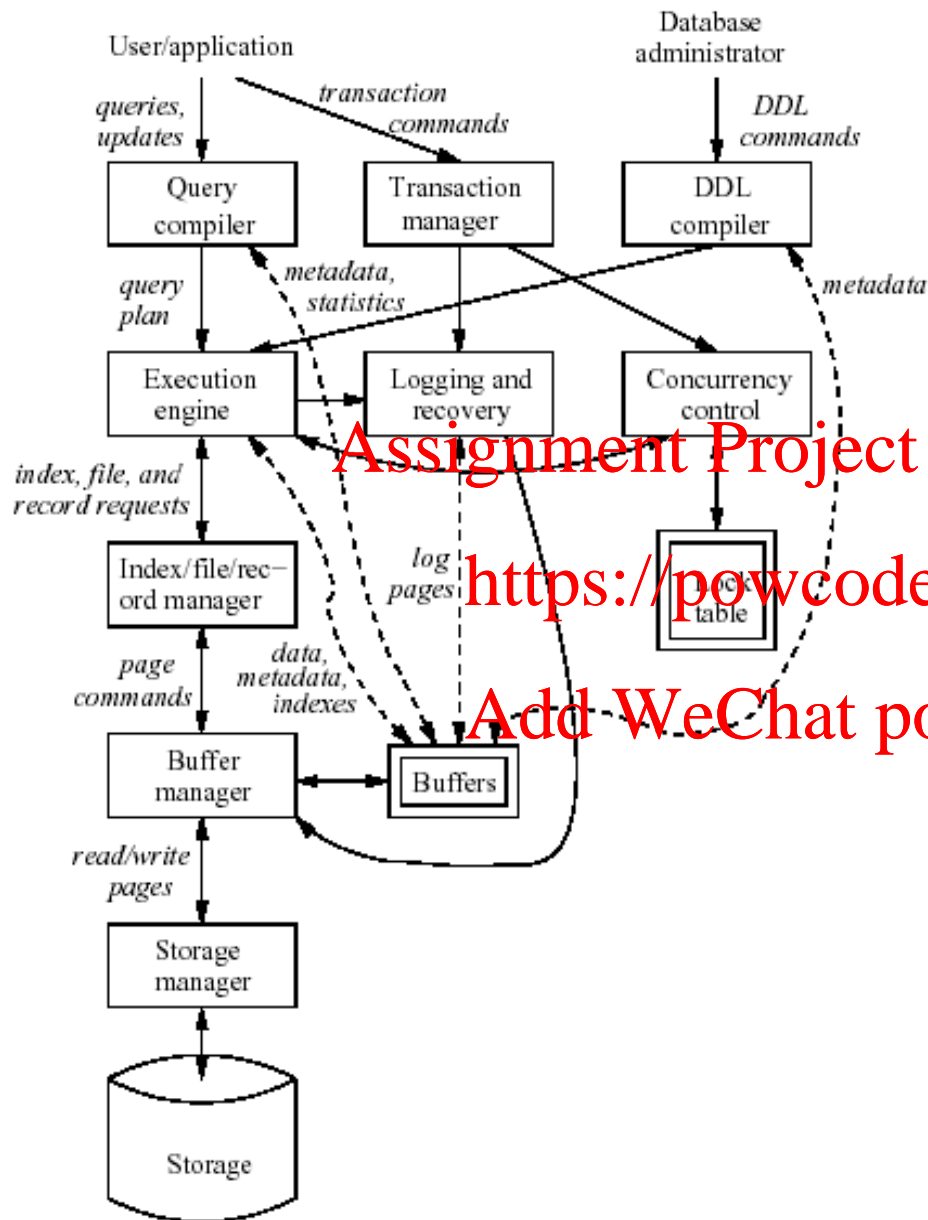
Suneuy Kim

# I. Database Management System (DBMS)

- Database is a collection of data that is managed by a DBMS.
- DBMS is specially designed software applications that interact with the user, other applications, and the database itself to capture and analyze data.
- Features of DBMS
  - Data definition - defining schema for the database, removing schema from the database, and altering an existing schema
  - Data modification – inserting, deleting, and updating data
  - Data retrieval – obtaining information from the database for user queries
  - Administration – Registering and monitoring users, enforcing data security, monitoring performance, maintaining data integrity, dealing with concurrency control, and recovering information in case of failures

# Terminology

- A **database schema** of a database system is its structure described in a formal language supported by the DBMS and refers to the organization of data as a blueprint of how a database is constructed - Wikipedia
- SQL (Structured Query Language) - RDBMS
  - Data Definition Language (DDL) for declaring database schemas  
e.g.) CREATE, DROP, ALTER
  - Data Manipulation Language (DML) for querying and for modifying databases  
e.g.) SELECT, INSERT, DELETE, UPDATE
  - Data Control Language (DCL) for controlling access to data stored in a database  
e.g.) GRANT, REVOKE



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DBMS components

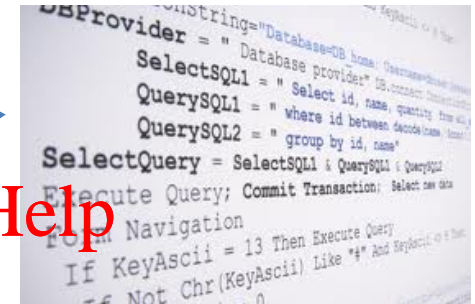
# Database People

Database Designer



defines schema

Database Application Programmer



queries/modifies data

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Database Administrator



- executes DDL
- loads data,
- monitors and maintains databases

builds system

DBMS  
Implementer

## II. Data Model

- Data model consists of
  - Structure of the data
  - Operations on the data
  - Constraints on the data
- Representative data models
  - Relational data model
  - Semi-structured data model
  - NoSQL data model

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# Relational Data Model

- Structure: tables (relations)
- Operations – relational algebra, table-oriented  
e.g.) select, project, join, etc.  
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- Constraints  
e.g.) referential integrity constraints,  
key constraints

# Example: Table Movies

title	year	length	genre
Gone with the Wind	1939	231	drama
Star Wars	1977	124	sciFi
Wayne's World	1992	95	comedy

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# Semi-structured Data Model

- Structure: trees or graphs  
e.g.) XML data
- Operations involve following paths in the implied tree  
e.g.) /Movies/Movie/Version
- Constraints involve the data type of values associated with a tag  
e.g.) `<xs:element name = "Movie" type = "movieType" minOccurs = "0" maxOccurs = "unbounded" />`

# Example: XML data

```
<?xml version="1.0" encoding="UTF-8"?>
```

```
<Movies>
```

```
  <Movie title = "King Kong">
```

```
    <Version year ="1933">
```

```
      <Star>Far Wray</Star>
```

```
    </Version>
```

```
    <Version year = "1976">
```

```
      <Star>Carrie Fisher</Star>
```

```
      <Star>Jessica Lange</Star>
```

```
    </Version>
```

```
  </Movie>
```

```
  <Movie title = "Footloose">
```

```
    <Version year = "1984">
```

```
      <Star> Kevin Bacon</Star>
```

```
      <Star>John Lithgow</Star>
```

```
      <Star>Sarah Jessica Parker</Star>
```

```
    </Version>
```

```
  </Movie>
```

```
</Movies>
```

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# Relational vs. Semi-structured data models

- Semi-structured models: flexible
- Relational models:
  - Used by major commercial database systems
  - Efficient access and modification of data
  - Easy of use
  - SQL allows us to program at high level

























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## DB-engines Ranking

<http://db-engines.com/en/ranking>

Rank			DBMS	Database Model
Aug 2020	Jul 2020	Aug 2019		
1.	1.	1.	Oracle 	Relational, Multi-model 
2.	2.	2.	MySQL 	Relational, Multi-model 
3.	3.	3.	Microsoft SQL Server 	Relational, Multi-model 
4.	4.	4.	PostgreSQL 	Relational, Multi-model 
5.	5.	5.	MongoDB 	Document, Multi-model 
6.	6.	6.	IBM Db2 	Relational, Multi-model 
7.	 8.	 8.	Redis 	Key-value, Multi-model 
8.	 7.	 7.	Elasticsearch 	Search engine, Multi-model 
9.	9.	 11.	SQLite 	Relational
10.	 11.	 9.	Microsoft Access	Relational

# III. Relation Model

- Relation: two dimensional table to represent data
- Attributes: columns of relation
- Tuples: rows of a relation
- Domains: data type for each attribute
- Relation Schema: name of a relation and the set of attributes (attribute names and associated domains) for a relation
- Database schema - a set of schemas for the relations of a database.

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# Relational Model

- Instances: actual contents at given point in time

title	year	length	genre
Gone with the wind	1939	231	drama
Star Wars	1977	124	sciFi
Wayne's World	1992	95	comedy

- Key: attribute whose value is unique in each tuple (Or set of attributes whose combined values are unique)  
e.g.) Movies(title, year, length, genre)
- Note:
  - The attributes in a relation schema are a set, not a list
  - Relations are sets of tuples, not lists of tuples

# Example: Schema

## Database Schema about Library

```
BOOK (  
    title: string,  
    author:string,  
    copies:integer  
)  
  
LOAN (  
    uID:integer,  
    title:string,  
    loanDate:date,  
    overdue: boolean  
)  
  
USER (  
    uID:integer,  
    uNAME:string,  
    age:integer,  
    loaned:integer,  
)
```

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## IV. Relational Algebra

- An algebra whose operands are relations or variables that represent relations.

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# Core relational operations

- Union, intersection, and difference.
  - *both operands have the same number of attributes and the domains of the corresponding attributes are the same.*
- Selection: selecting certain rows.
- Projection: projecting certain columns.
- Products and joins: combining two relations.
- Renaming of relations and attributes

# Running Example

Book(title, author, copies)

User (uID, uName, age, loaned)

Loan (uID, title, loanDate, overdue)

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Notes:

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- copies means the number of copies left
- loaned means the number of books the user loaned.

# Set operations

- $R \cup S$

Relation with tuples from R and S with duplicates removed.

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- $R \cap S$

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Relation with tuples that appear in both R and S.

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- $R - S$

Relation with tuples from R but not from S

Difference operation is NOT commutative. That is,  $R - S$  is not equal  $S - R$ .

# Example: Set operations

## Book1

title	author	copies
Faraway Child	Amy Maida Wadsworth	3
Evening in the Ashes	Dorothy Love	20
The Sage and the Lace	James Dove	4

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## Book2

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title	author	copies
Faraway Child	Amy Maida Wadsworth	3
Silent Wife	A.S.A. Harrison	10
Cloud of Unknown	Carl McColman	17

# Books1 U Books2

title	author	copies
Evening in the Ashes	Dorothy Love	20
Faraway Child	Amy Maida Wadsworth	3
The Sage and the Lace	James Dove	4
Cloud of Unknown	Carl McColman	17
Silent Wife	A. C. A. Harrison	10

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# Book1 $\cap$ Book2

title	author	copies
Faraway Child	Amy Mayda Wadsworth	3

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Book1 — Book2

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title	author	copies
Evening in the Ashes	Dorothy Love	20
The Sage and the Lace	James Dove	4

# Select

- $R1 := \sigma_C(R2)$ 
  - $C$  is a condition that involves attributes of  $R2$ .
  - $R1$  is all those tuples of  $R2$  that satisfy  $C$ .

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# Example: Select

- Users who loaned more than 20 books.

$\sigma_{\text{loaned} > 20}(\text{User})$

- Users who loaned more than 20 books with age > 10.

$\sigma_{\text{loaned} > 20 \wedge \text{age} > 10}(\text{User})$

- Loans of book 'Bambi' being overdue

$\sigma_{\text{title}='Bambi' \wedge \text{overdue}=\text{true}}(\text{Loan})$

Book

title	author	copies

User

uID	uName	age	loaned

Loan

uID	title	loanDate	overdue



# Projection

$R1 := \pi_L(R2)$

- $L$  is a list of attributes from the schema of  $R2$ .
- $R1$  is constructed by looking at each tuple of  $R2$ , extracting the attributes on list  $L$ , in the order specified, and creating from those components a tuple for  $R1$ .
- Eliminate duplicate tuples, if any

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# Example: Projection

- Ids and #of loaned books of all users

$\pi_{uID, loaned}(User)$

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- Ids and names of users who loaned more than 20 books

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$\pi_{uID, uName}(\sigma_{loaned > 20}(User))$

Book

title	author	copies

User

uID	uName	age	loaned

Loan

uID	title	loanDate	overdue

# Different ways of handling duplicates

Titles and overdue information of all loans

$\pi_{\text{title,overdue}}(\text{Loan})$

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Relational Algebra Sets <https://powcoder.com> SQL: Bags

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title	overdue	title	overdue
Bambi	TRUE	Bambi	TRUE
Lion King	FALSE	Bambi	TRUE
Eye of Sierras	FALSE	Lion King	FALSE
		Eye of Sierras	FALSE

# Quiz

Are the following relational algebra expressions useful ?

- $\sigma_{\text{loaned} > 20}(\sigma_{\text{age} > 10}(\text{User}))$
  - $\pi_{\text{title}}(\pi_{\text{title}, \text{author}}(\text{Book}))$
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Book

title	author	copies

User

uID	uName	age	loaned

Loan

uID	title	loanDate	overdue

# Extended Projection

- Using the same  $\Pi_L$  operator, where the projection list  $L$  can have:
  - an expression  $x \rightarrow y$  where  $x$  and  $y$  are attributes.  $x$  is renamed to  $y$ .
  - an expression  $E \rightarrow z$ , where  $E$  involves operations and  $z$  is the name of the results of the expression  
e.g.)  $a+b \rightarrow x$  represents sum of the attributes  $a$  and  $b$ , renamed  $x$
  - duplicate occurrences of the same attribute

# Example: Extended Projection

R =

A	B
10	20
30	40

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$\pi_{A+B \rightarrow C, A, A}(R) =$

C	A1	A2
30	10	10
70	30	30

# Cartesian Product (= Cross Join)

$R3 := R1 \times R2$

- Pair each tuple  $t1$  of  $R1$  with each tuple  $t2$  of  $R2$ .
- Concatenation  $t1t2$  is a tuple of  $R3$ .
- Schema of  $R3$  is the attributes of  $R1$  and then  $R2$ , in order.
- But beware attribute  $A$  of the same name in  $R1$  and  $R2$ : use  $R1.A$  and  $R2.A$ .

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# Example: Cartesian Product

R1		R2			R3				
A	B				A	R1.B	R2.B	C	D
1	2	2	5	6	1	2	2	5	6
3	4	4	7	8	1	2	4	7	8
		9	10	11	1	2	9	10	11
					3	4	2	5	6
					3	4	4	7	8
					3	4	9	10	11



# Example: Cartesian Product

Ids and #of loaned books of users who loaned "Bambi" being overdue.

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$\pi_{\text{User.uID}, \text{loaned}}(\sigma_{\text{User.uID} = \text{Loan.uID} \wedge \text{title} = \text{"Bambi"} \wedge \text{overdue} = \text{true}}(\text{User} \times \text{Loan}))$

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Book

title	author	copies

User

uID	uName	age	loaned

Loan

uID	title	loanDate	overdue

# Theta-Join

- $R3 := R1 \bowtie_C R2$ 
  - Take the product  $R1 \times R2$ .
  - Then apply  $\sigma_C$  to the result, where  $C$  can be any boolean-valued condition.
- User names that happen to be the same as one of the book titles.

$\pi_{uName}(User \bowtie_{uName = title} Book)$

Book

title	author	copies

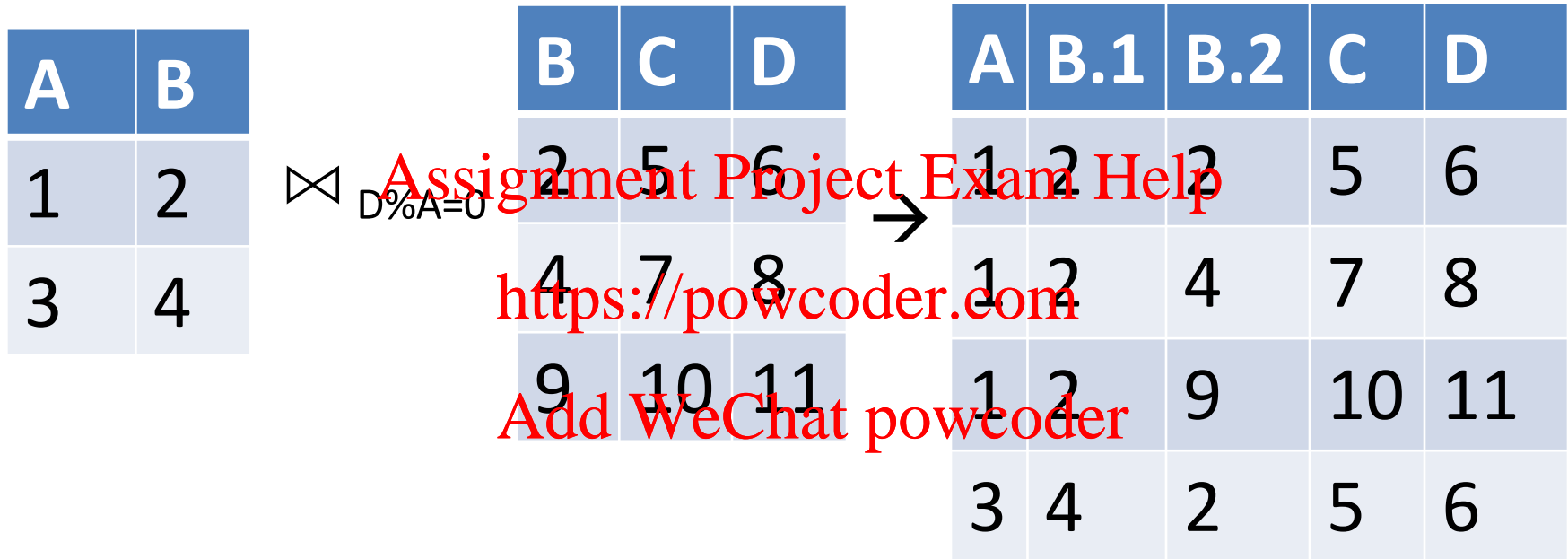
User

uID	uName	age	loaned

Loan

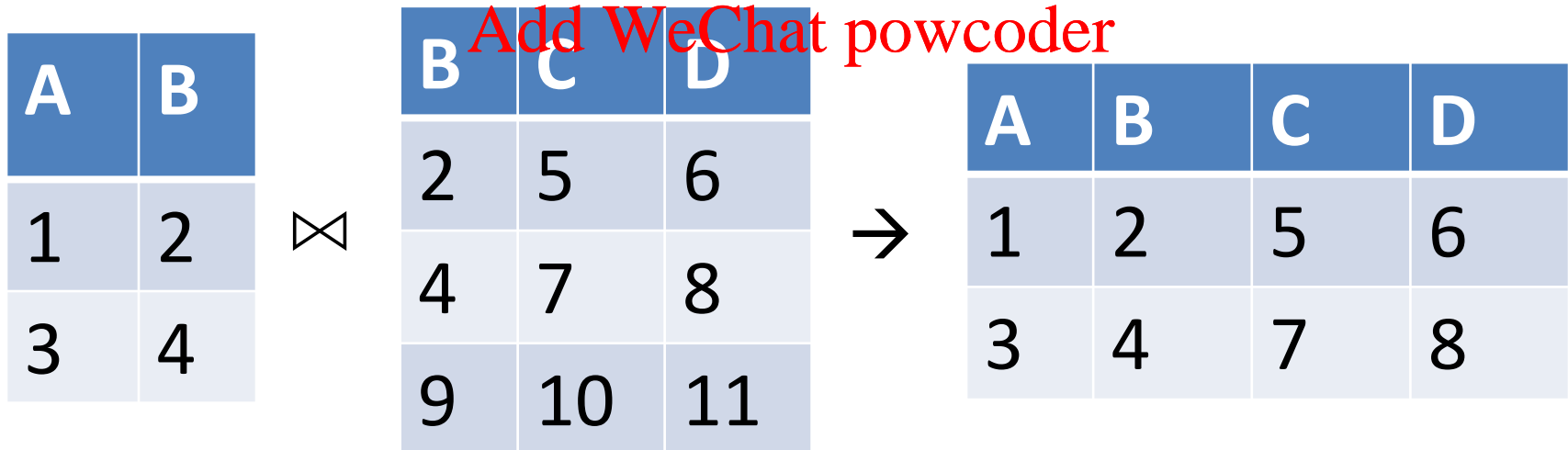
uID	title	loanDate	overdue

# Example: Theta Join



# Natural Joins

- $R3 := R1 \bowtie R2$ .
  - Equating attributes of the same name, and
  - Projecting out one copy of each pair of equated attributes.



# Example: Natural Join

Ids and #of loaned books of users who loaned "Bambi" being overdue.

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$\pi_{uID, loaned}(\sigma_{title="Bambi", overdue=true}(User \bowtie Loan))$

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Book

title	author	copies

User

uID	uName	age	loaned

Loan

uID	title	loanDate	overdue

# Joins

- A *theta join* allows for arbitrary comparison relationships (such as  $\geq$ ).
- An *equijoin* is a theta join using the equality operator. <https://powcoder.com>
- A *natural join* is an equijoin on attributes that have the same name in each relations . The resulting relation will contain only one column for each pair of the same named columns.

# Renaming

- The  $\rho$  operator gives a new schema to a relation.
- $\rho_{S(A_1, \dots, A_n)}(R)$  makes  $S$  be a relation with attributes  $A_1, \dots, A_n$  and the same tuples as  $R$ .

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# Example: Renaming

$R(A, B)$

$S(B, C, D)$

(1)  $R \times \rho_{S(X, C, D)}(S)$

(2)  $\rho_{RS(A, B, X, C, D)}(R \times S)$

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(1) and (2) are the same except for that resulting relation of (1) doesn't have any name while that of (2) has a name **RS**.



# Division ( $R \div S$ )

The DIVISION operation is useful for a special kind of query involving **all**. For example,

- Retrieve the names of employees who work on **all** the projects that 'Jonh Smith' works on.
- Find all pizzerias that serve **every** pizza eaten by people over 30.

$$\text{Division } T(Y) = R(Z) \div S(X)$$

$T(Y) = R(Z) \div S(X)$ , where

- the  $Z$  and  $X$  are schemas of  $R$  and  $S$ , respectively,
- the attributes of  $S$  are a subset of the attributes of  $R$ ; that is  $X \in Z$  and
- $Y = Z - X$  ( $Y$  is the set of attributes of  $R$  that are not attributes of  $S$ ; that is,  $Y = Z - X$  (and hence  $Z = X \cup Y$ ))

$$T(Y) = R(Z) \div S(X)$$

- For a tuple  $t$  to appear in the result  $T$  of the Division, the values in  $t$  must appear in  $R$  in combination with every tuple in  $S$ .
- Example:  $b1$  and  $b4$  appear in  $R$  in combination with all three tuples in  $S$ .

R			S		T
A	B		A		B
a1	b1	÷	a1	=	b1
a2	b1		a2		b4
a3	b1		a3		
a4	b1				
a1	b2				
a3	b2				
a2	b3				
a3	b3				
a4	b3				
a1	b4				
a2	b4				
a3	b4				

# Division using a sequence of $\pi$ , $\times$ , and $-$ operators

- $T1 := \pi_Y (R)$
- $T2 := \pi_Y((S \times T1) - R)$
- $T := T1 - T2$

R		S	T
A	B	A	B
a1	b1	a1	b1
a2	b1	a2	
a1	b2		

$\div$  =

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T1	$S \times T1$		$(S \times T1) - R$		T2	T
B	A	B	A	B	B	B
b1	a1	b1	a2	b2	b2	b1
b2	a1	b2				
	a2	b1				
	a2	b2				

# Relationships among Operations

## Independent operators

- $\cup$
- $-$
- $\sigma$  (select)
- $\pi$  (project)
- $\times$  (product)
- $\rho$  (renaming)

Operators that can be expressed in terms of other R.A operators

- $R \cap S = R - (R - S)$

- $R \bowtie_C S = \sigma_C (R \times S)$

- $R \bowtie_L S = \pi_L (\sigma_C (R \times S))$

–  $C$  is  $R.A1=S.A1 \wedge R.A2=S.A2 \dots$   
where  $A1, A2, \dots$  are shared attributes by  $R$  and  $S$ .

–  $L$  is list of attributes of  $R$  followed by attributes of  $S$  that are not also in  $R$ .

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# Expressing Complex Queries

- Relational algebra expressions
- Expression trees
- Linear Notations

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# R.A.

Movies(title, year, length, genre, studioName, producerC#)

"What is the title and year of movies made by Fox that are at least 100 minutes long ?"

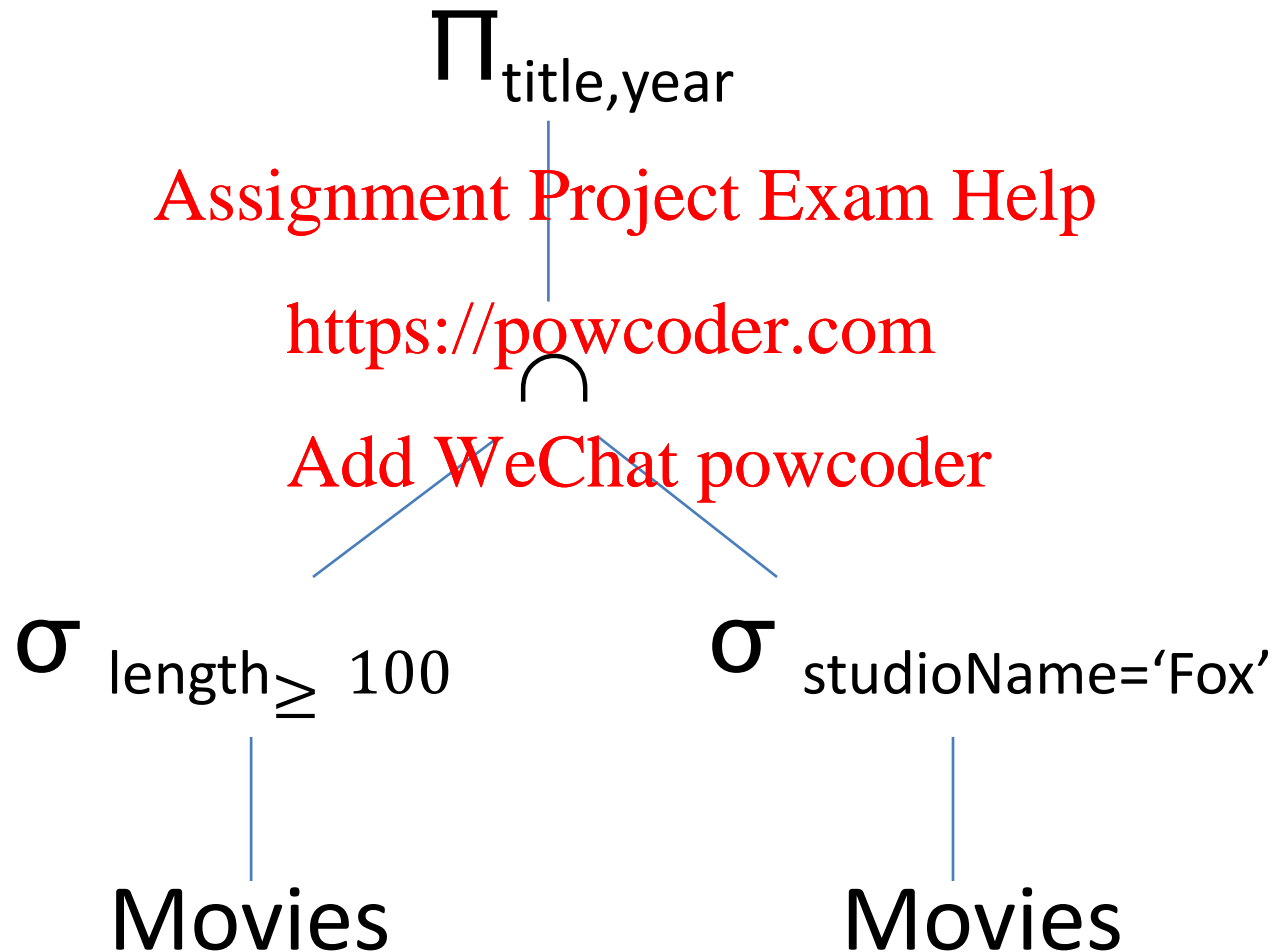
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R.A. Expression:

$$\Pi_{\text{title, year}}(\sigma_{\text{length} \geq 100}(\text{Movies}) \cap \sigma_{\text{studioName} = \text{'Fox'}}(\text{Movies}))$$
$$\Pi_{\text{title, year}}(\sigma_{\text{length} \geq 100 \text{ AND studioName} = \text{'Fox'}}(\text{Movies}))$$

# Expression Trees





# Linear Notations

- $R(t,y,l,g,s,p) := \sigma_{\text{length} \geq 100}(\text{Movies})$
  - $S(t,y,l,g,s,p) := \sigma_{\text{studioName} = \text{'Fox'}}(\text{Movies})$
  - $T(t,y,l,g,s,p) := R \cap S$
  - $\text{Answer}(\text{title}, \text{year}) := \Pi_{t,y}(T)$
- or
- $\text{Answer}(\text{title}, \text{year}) := \Pi_{t,y}(R \cap S)$

# Constraints on Relations

A referential integrity constraint asserts that a value appearing in one context will also appear in another related context.

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Example

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Movies (title, year, length, genre,  
studioName, producerC#)

MovieExec (name, address, cert#, netWorth)

$\Pi_{\text{producerC\#}}(\text{Movies}) \in \Pi_{\text{cert\#}}(\text{MovieExec})$

# Constraints on Relations

## Key constraints

A key uniquely identifies each tuple in a relation.

Any two tuples in a relation must not have the same key.

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# Relational Algebra Exercise

## 2.4.1

Product (maker, model, type)

PC(model, speed, ram, hd, price)

Laptop(model, speed, ram, hd, screen, price)

Printer(model, color, type, price)

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- (a) What PC models have a speed of at least 3.00 ?
- (b) Which manufacturers make laptops with a hard disk of at least 100GB ?
- (c) Find the model number and price of all products (of any type) made by manufacturer B.
- (d) Find the model numbers of all color laser printers.
- (e) Find those manufacturers that sell Laptops, but not PCs.

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(f) Find those hard disk sizes that occur in two or more PC's

(g) Find those pairs of PC models that have both the same speed and RAM. **A pair should be listed only once**; e.g., list(i,j) but not (j,i)

(h) Find the manufacturers of **at least two** different computers (PC's or laptops) with speeds of at least 2.80.

(i) Find the manufacturer(s) of the computer (PC or laptop) with **the highest available** speed.

(j) Find the manufacturers of PC's with **at least three** different speeds.

(k) Find the manufacturers who sell **exactly three** different models of PC.

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(a) What PC models have a speed of at least 3.00 ?

$\pi_{\text{model}}(\sigma_{\text{speed} \geq 3.0} \text{PC})$

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---

PC.model

---

1005

---

1006

---

1013



(b) Which manufacturers make laptops with a hard disk of at least 100GB ?

$\pi_{\text{maker}} (\sigma_{\text{hd} \geq 100} (\text{Product} \bowtie \text{Laptop}))$

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Product.maker

'A'

'B'

'E'

'F'

'G'

(c) Find the model number and price of all products (of any type) made by manufacturer B.

$\pi_{\text{model,price}}$

(

$\sigma_{\text{maker} = 'B'}$

(Product  $\bowtie$

$(\pi_{\text{model,price}}(\text{PC}) \cup \pi_{\text{model,price}}(\text{Laptop}) \cup \pi_{\text{model,price}}(\text{Printer}))$

)

)

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Product.model	PC.price
1004	649
1005	630
1006	1049
2007	1429

(d) Find the model numbers of all color laser printers

$\pi_{\text{model}}(\sigma_{\text{color} = \text{true and type} = \text{'laser'}} \text{Printer})$

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Printer.model
3003
3007

(e) Find those manufacturers that sell Laptops, but not PCs.

$$\pi_{\text{maker}}(\sigma_{\text{type}='laptop'} \text{Product}) - \pi_{\text{maker}}(\sigma_{\text{type}='pc'} \text{Product})$$

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(f) Find those hard disk sizes that occur  
in two or more PC's

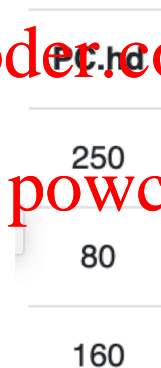
$\pi_{PC.hd}$

$(PC \bowtie_{PC.model \neq PC2.model \text{ and } PC.hd = PC2.hd} PC2) \rho_{PC2} PC$

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(g) Find those pairs of PC models that have both the same speed and RAM. **A pair should be listed only once**; e.g., list(i,j) but not (j,i)

$\pi$  PC.model, PC2.model

(PC  $\bowtie$  PC2.model < PC2.model and PC.speed = PC2.speed and PC.ram = PC2.ram  
 $\rho$  PC2 PC)

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PC.model	PC2.model
1004	1012

(h) Find the manufacturers of **at least two** different computers (PCs or laptops) with speeds of at least 2.80.

$\pi_{\text{maker}}$

$\sigma_{\text{model} \neq \text{model2}}$

(  
 $\pi_{\text{maker,model}} (\text{Product} \bowtie ((\pi_{\text{model}} \sigma_{\text{speed} \geq 2.80} \text{PC}) \cup (\pi_{\text{model}} \sigma_{\text{speed} \geq 2.80} \text{Laptop})))$   
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$\bowtie$

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$\rho_{\text{model2} \leftarrow \text{model}}$

$\pi_{\text{maker,model}} (\text{Product} \bowtie ((\pi_{\text{model}} \sigma_{\text{speed} \geq 2.80} \text{PC}) \cup (\pi_{\text{model}} \sigma_{\text{speed} \geq 2.80} \text{Laptop})))$

)

Product.maker

'B'

'E'

(i) Find the manufacturer(s) of the computer (PC or laptop) with **the highest available** speed.

$\pi$  maker

(

Product  $\bowtie$

(

$\pi$  model

$\sigma$  type = 'pc' or type = 'laptop' (Product)

-

$\pi$  model

(( $\pi$  model,speed PC  $\cup$   $\pi$  model, speed Laptop)

$\bowtie$  speed < speed2

$\rho$  model1<- model, speed2<-speed

( $\pi$  model,speed PC  $\cup$   $\pi$  model, speed Laptop))

)

)

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---

Product.maker

---

'B'



(j) Find the manufacturers of PCs with  
**at least three** different speeds.

$\pi_{\text{maker}} ( \sigma_{s1 \neq s2 \text{ and } s1 \neq s3 \text{ and } s2 \neq s3} ($   
 $( \rho_{s1 \leftarrow \text{speed}} \pi_{\text{maker, speed}} ( \text{Product} \bowtie \text{PC} )$

$\bowtie$

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$\rho_{s2 \leftarrow \text{speed}} \pi_{\text{maker, speed}} ( \text{Product} \bowtie \text{PC} ) )$

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$\bowtie$

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$\rho_{s3 \leftarrow \text{speed}} \pi_{\text{maker, speed}} ( \text{Product} \bowtie \text{PC} ) )$

)

---

Product.maker

'A'

---

'D'

---

'E'

(k) Find the manufacturers who sell **exactly three** different models of PC.

$\pi$  maker

$\sigma_{m1 \neq m2 \text{ and } m2 \neq m3 \text{ and } m1 \neq m3}$

$((\rho_{m1 < -model} \pi_{maker, model} \sigma_{type='pc'} Product) \bowtie$

$(\rho_{m2 < -model} \pi_{maker, model} \sigma_{type='pc'} Product) \bowtie$

$(\rho_{m3 < -model} \pi_{maker, model} \sigma_{type='pc'} Product))$

-

$\pi$  maker

$(\sigma_{m1 \neq m2 \text{ and } m1 \neq m3 \text{ and } m1 \neq m4 \text{ and } m2 \neq m3 \text{ and } m2 \neq m4 \text{ and } m3 \neq m4})$

$((\rho_{m1 < -model} \pi_{maker, model} \sigma_{type='pc'} Product) \bowtie$

$(\rho_{m2 < -model} \pi_{maker, model} \sigma_{type='pc'} Product) \bowtie$

$(\rho_{m3 < -model} \pi_{maker, model} \sigma_{type='pc'} Product) \bowtie$

$(\rho_{m4 < -model} \pi_{maker, model} \sigma_{type='pc'} Product)$

$)$

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Product.maker
'A'
'B'
'D'
'E'