PURDUE CS47100 SEPT 11, 2019 PROF. JENNIFER NEVILLE Assignment Project Exam Help

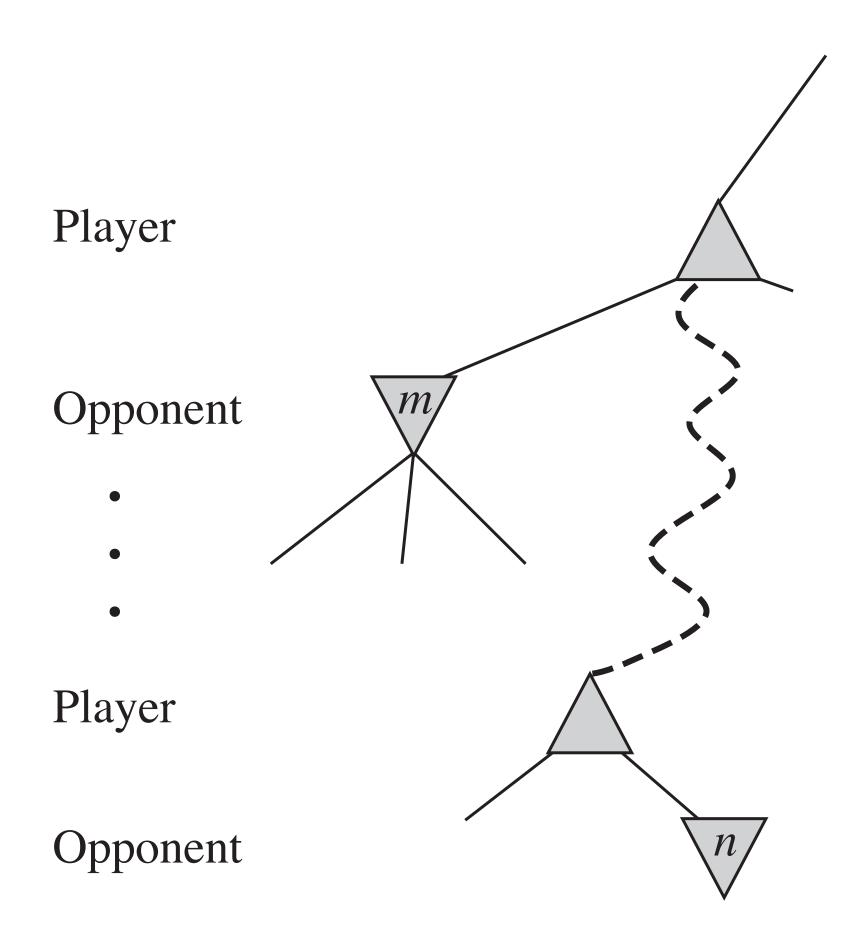
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INTRODUCTION TO AI

RECAP: ADVERSARIAL SEARCH

- Minimax search is a way of finding an optimal move in a zero-sum two player game
- Alpha-beta pruning is a way of finding the optimal minimax solution while avoiding searching subtrees of moves which won't be selected https://powcoder.com
 - Some branches will never be played by rational welcomes they include sub-optimal decisions (for either player)
 - Pruning produces results that are exactly equivalent to complete (unpruned) search
 - Node *ordering* can improve effectiveness; Perfect ordering gives time complexity $O(b^{m/2})$, thus, can search twice as far as ordinary minimax in equal time



RESOURCE LIMITS

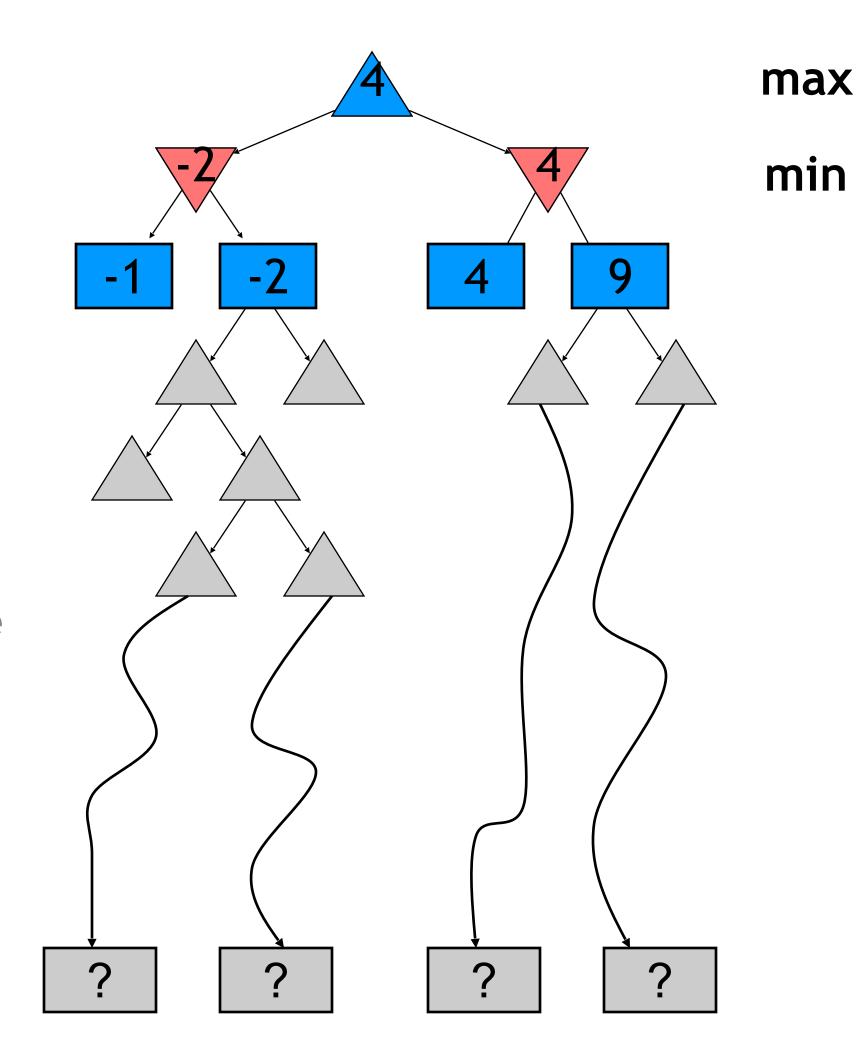


RESOURCE LIMITS

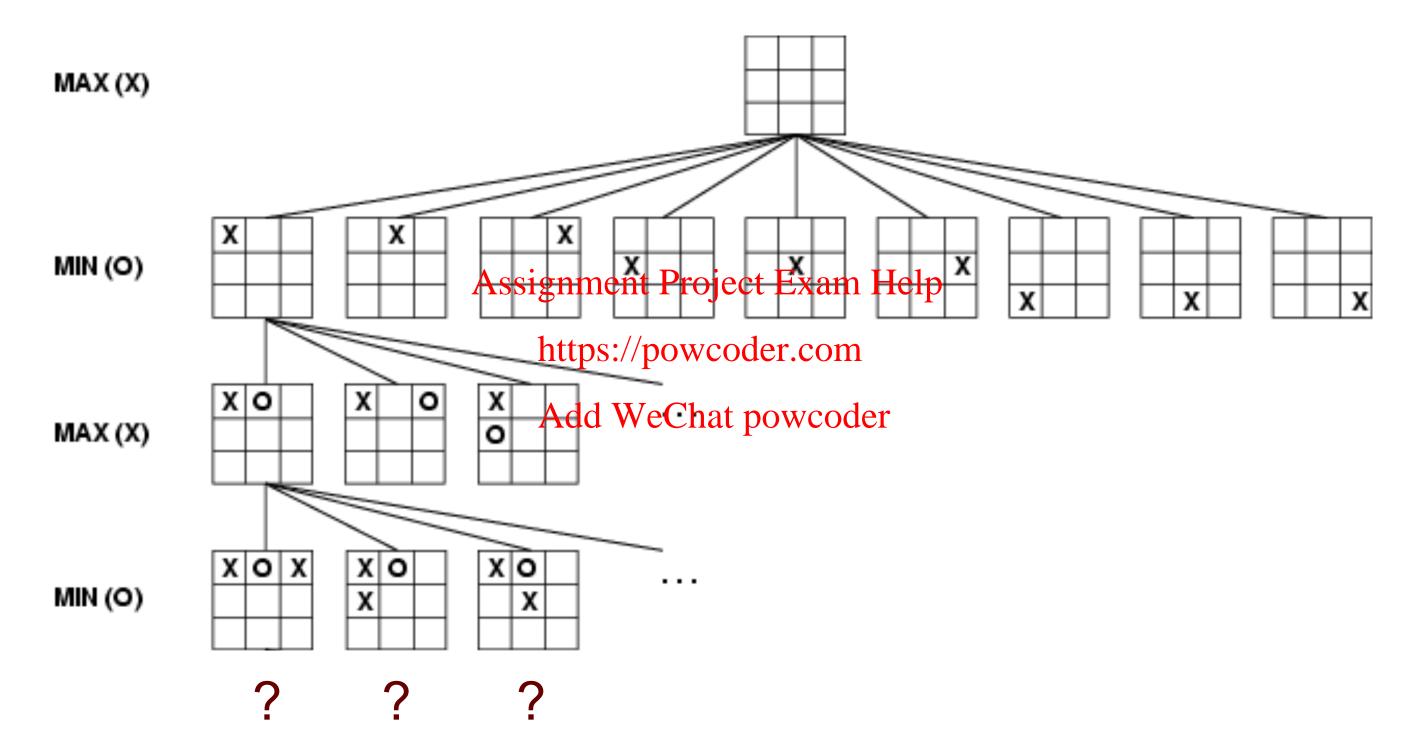
- Problem: In realistic games, cannot search to leaves
- Example:
 - Suppose we have 100 seconds, can explore 10K nodes / seconds
 - So can check 1M nodes per move

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- \blacktriangleright $\alpha\text{-}\beta$ reaches about depth 8 decent chess program
- Guarantee of optimal play is gone; More plies makes a BIG difference
- > Solution: Depth-limited search
 - Instead, search only to a limited depth in the tree
 - Replace terminal utilities with an evaluation function for nonterminal positions

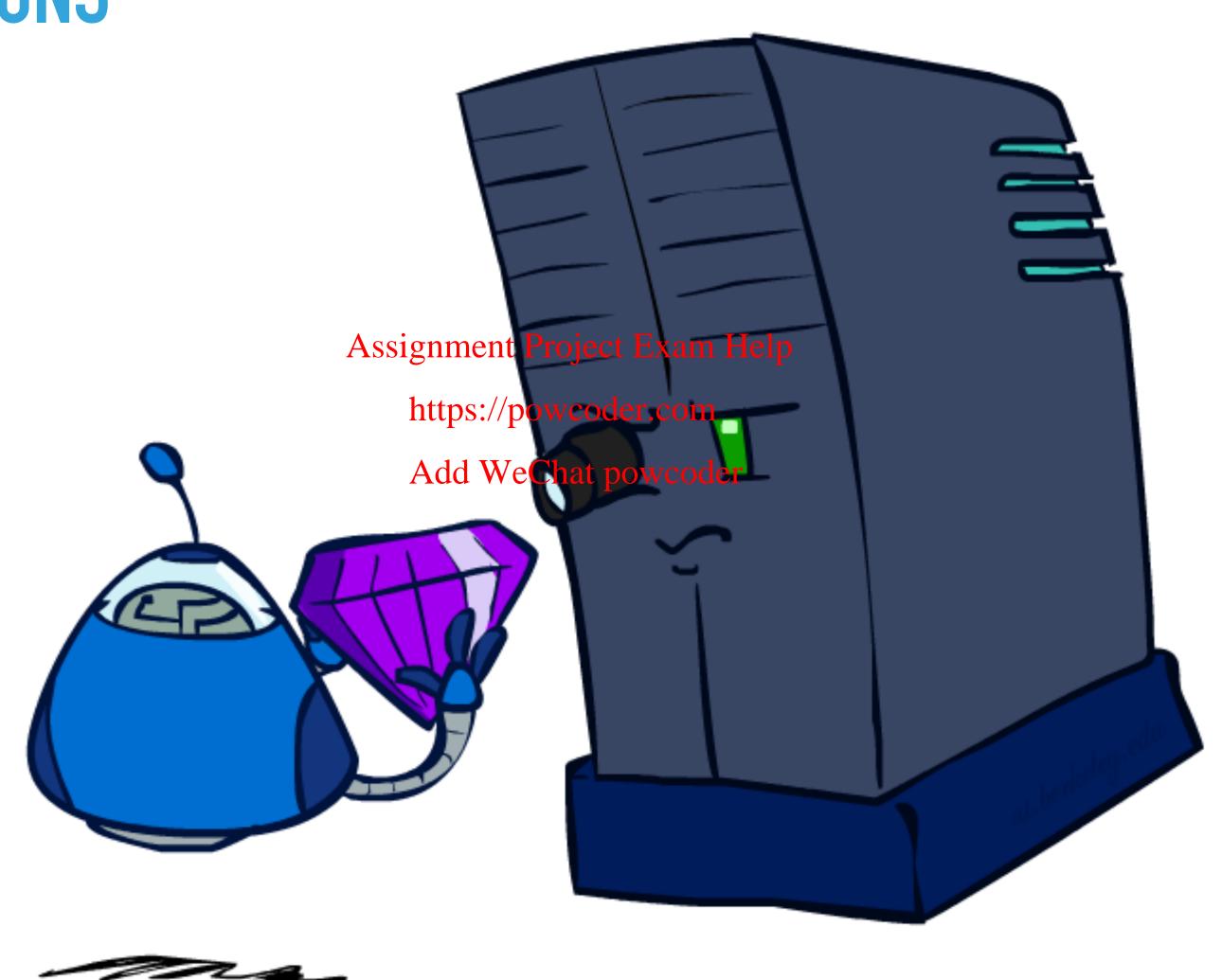


WHAT TO DO WHEN SEARCH IS INTRACTABLE



- Stop the search before you reach terminal states (using depth cutoff)
- Evaluate nodes using an evaluation function What properties should the evaluation function have?

EVALUATION FUNCTIONS



EVALUATION FUNCTIONS

- Desirable properties
 - Order terminal states in same way as true utility function

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Strongly correlated with the actual minimax value of the states

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- Efficient to calculate
- ▶ Typically use **features** simple characteristics of the game state that are correlated with the *probability of winning*
- The evaluation function combines feature values to produce a score:

$$Eval(x) = w_1 f_1(s) + w_2 f_2(s) + \dots + w_n f_n(s) = \sum_{i=1}^n w_i f_i(s)$$

EXAMPLE FEATURES

- What would be some useful features for chess?
 - Relative number of Bishops; Knights; Rooks; Pawns
 - Total number of pieces
 - Has queen?
 - Castled?
 - In check?
 - Distance of furthest pawn from start
 - Relative freedom (relative total number of possible moves)
 - etc.

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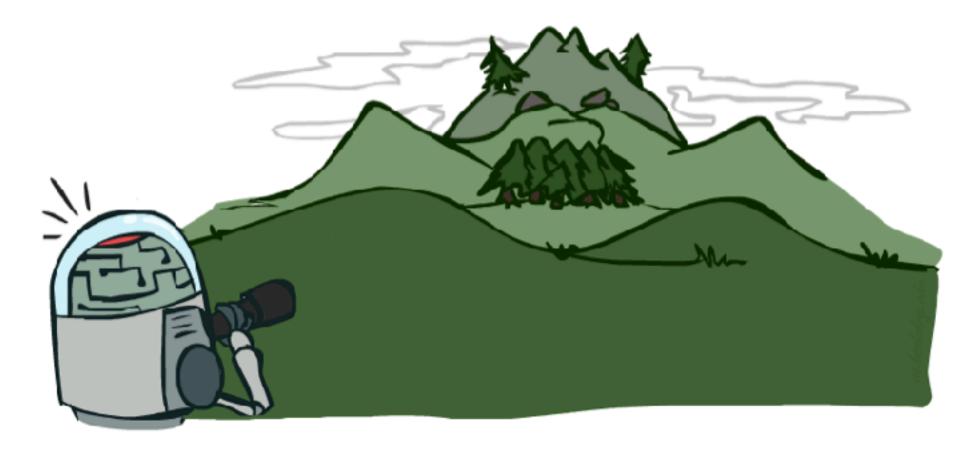
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DEPTH MATTERS

- Evaluation functions are always imperfect
- The deeper in the tree the evaluation function is buried, the less the quality of the evaluation function matters
- An important example of the tradeoff between complexity of features and complexity of computation

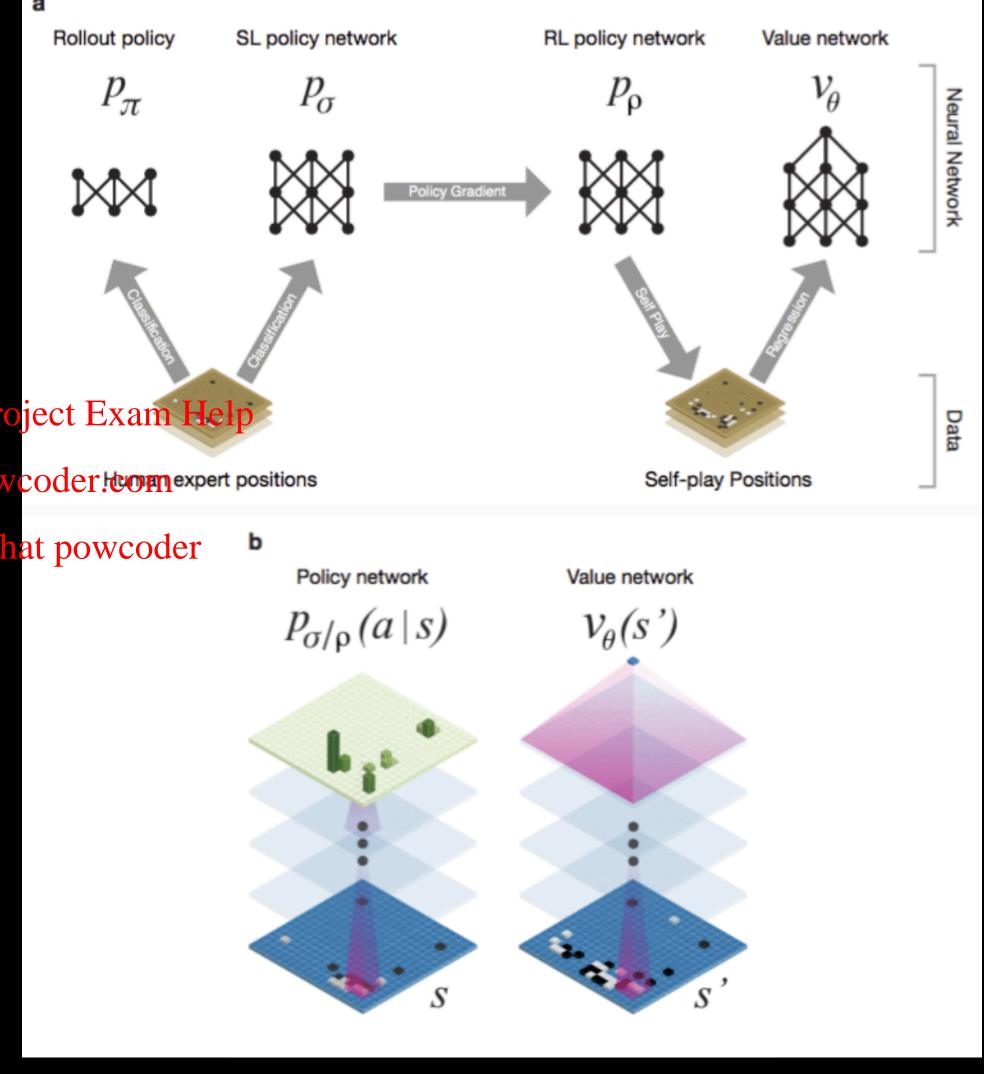




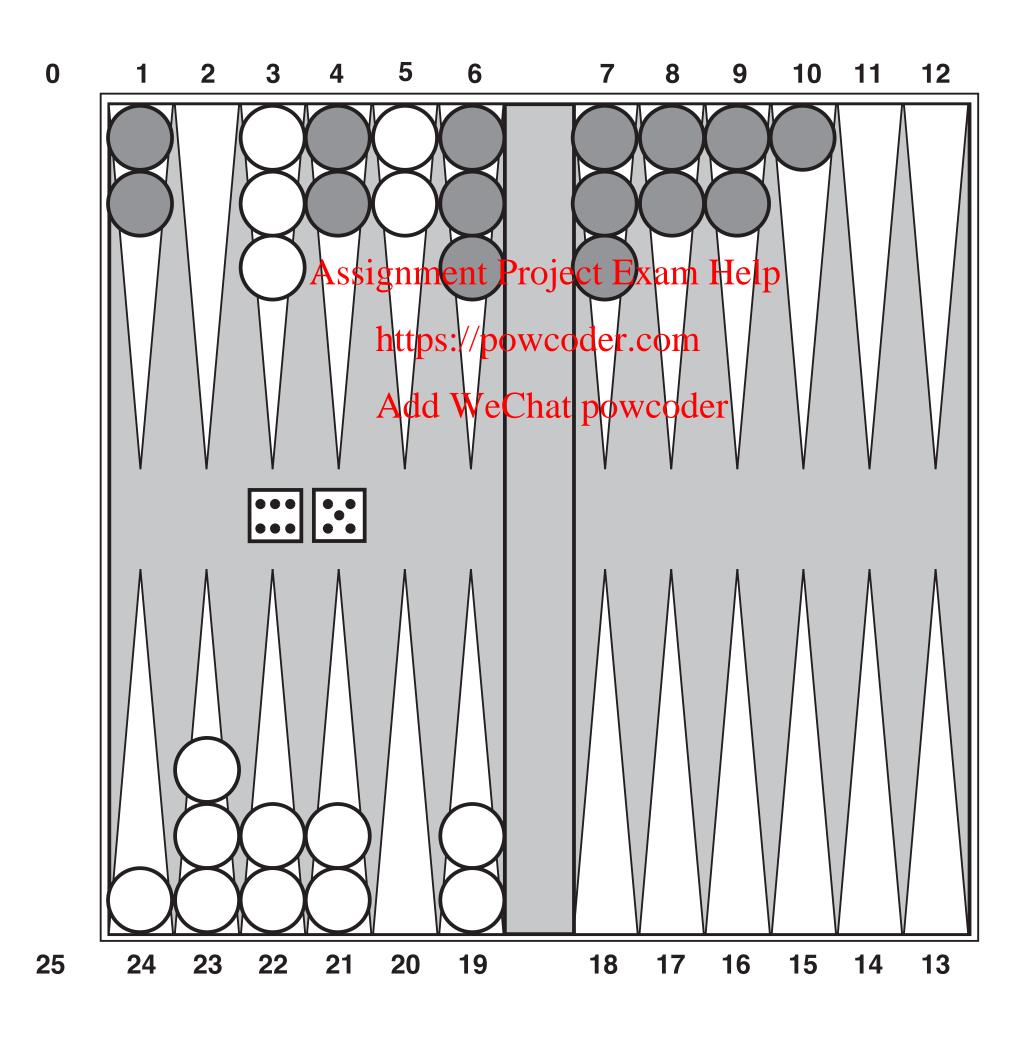
HOW COULD YOU LEARN A Assignment Project Exam Help GOOD EVALUATION FUNCTION https://powcoder.com/Add WeChat powcoder

ALPHAGO SYSTEM

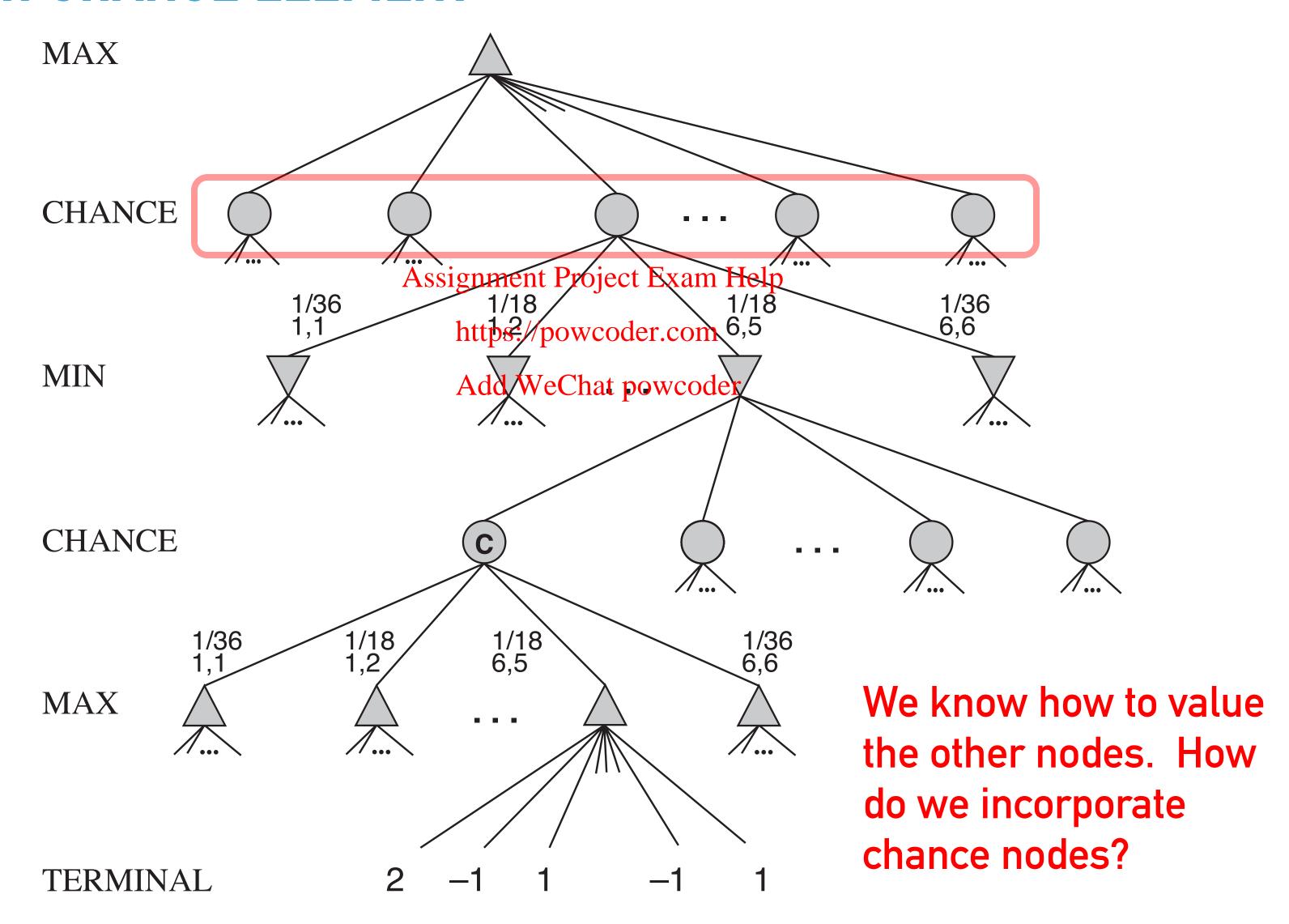
- Deep learning +
 Reinforcement learning
- One model predicts next move ssignment Project Exam Help given current state of board, trainedps://powcoder.toomexpert positions on 30 million positions from humand WeChat powcoder games
- Another model predicts likelihood of winning given current state, trained on 30 million positions from selfplay
- **System** combines two models using Monte Carlo search



WHAT IF A GAME HAS A "CHANCE ELEMENT"?

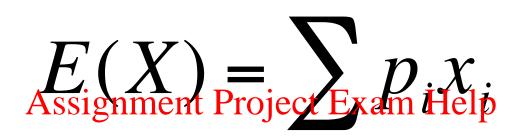


GAME TREE WITH CHANCE ELEMENT



EXPECTED VALUE

The sum of the probability of each possible outcome multiplied by its value:



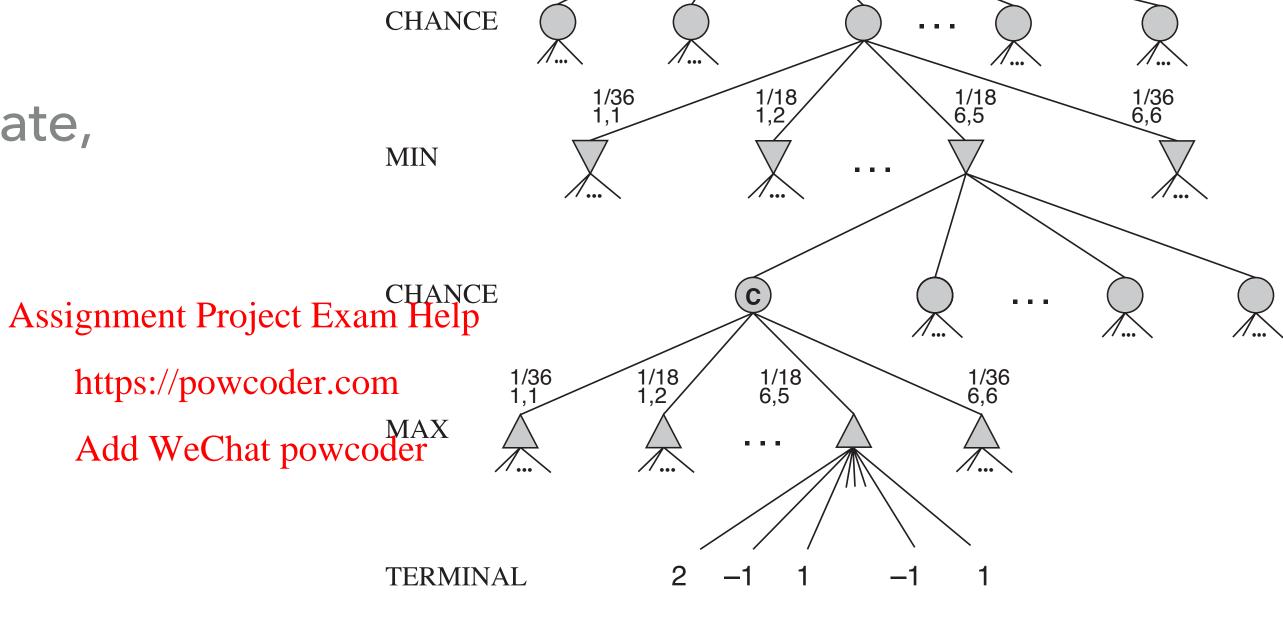
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- Are there pathological cases where this statistic could do something strange
 - Extreme values ("outliers")
 - Functions that are a non-linear transformation of the probability of winning

EXPECTED MINIMAX VALUE

- Now three different cases to evaluate, rather than just two.
 - MAX, MIN, CHANCE



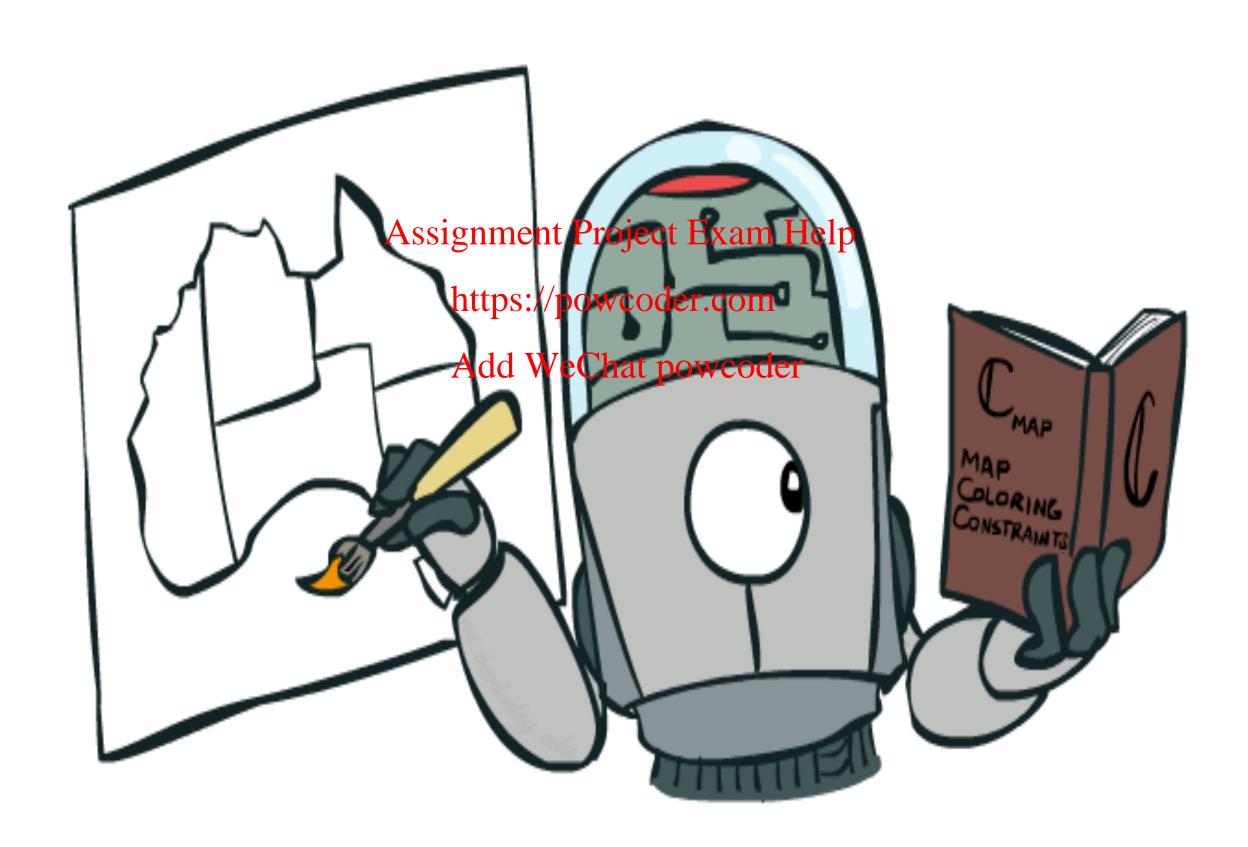
MAX

EXPECTED-MINIMAX-VALUE(n) = UTILITY(n)

 $max_{s \in successors(n)}$ MINIMAX-VALUE(s) $min_s \in successors(n)$ MINIMAX-VALUE(s) $\sum_{s \,\in\, successors(n)} P(s) \times EXPECTEDMINIMAX(s) \quad if \ CHANCE \ node$

if terminal node if MAX node if MIN node

CONSTRAINT SATISFACTION PROBLEMS



WHAT IS SEARCH FOR?

- Planning: sequences of actions
 - The path to the goal is the important thing
 - Paths have various costs, depths

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- ▶ Heuristics give problem-specific guidan ad WeChat powcoder
- ▶ Identification: assignments to variables
 - The goal itself is important, not the path
 - All paths at the same depth (for some formulations)



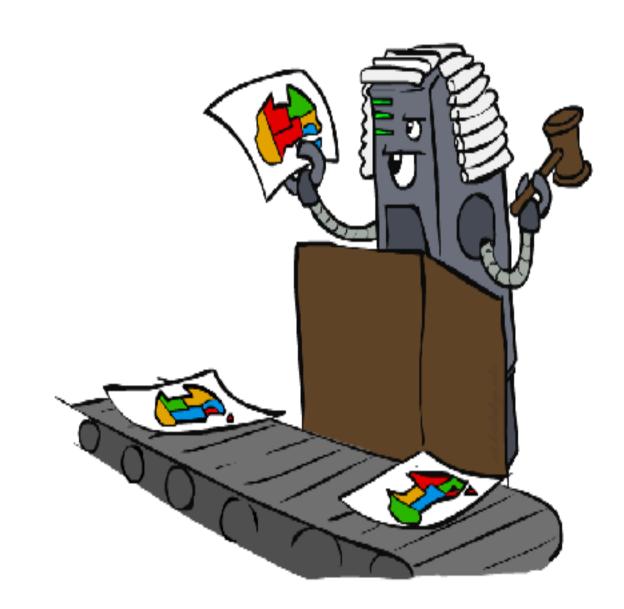


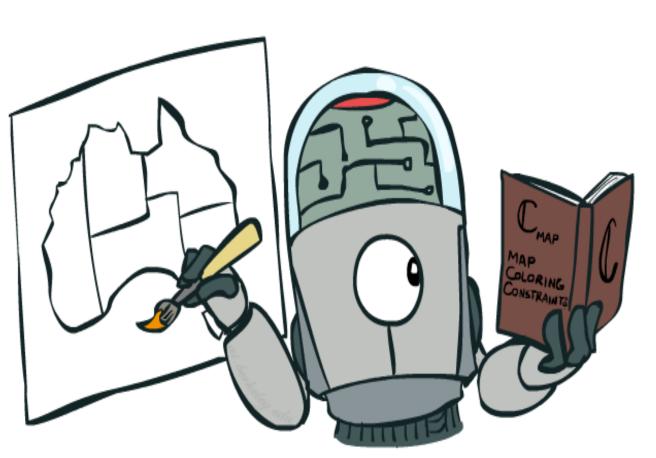
CONSTRAINT SATISFACTION PROBLEMS

- Standard search problems:
 - State is a "black box": arbitrary data structure
 - ▶ Goal test can be any function over states Assignment Project Exam Help

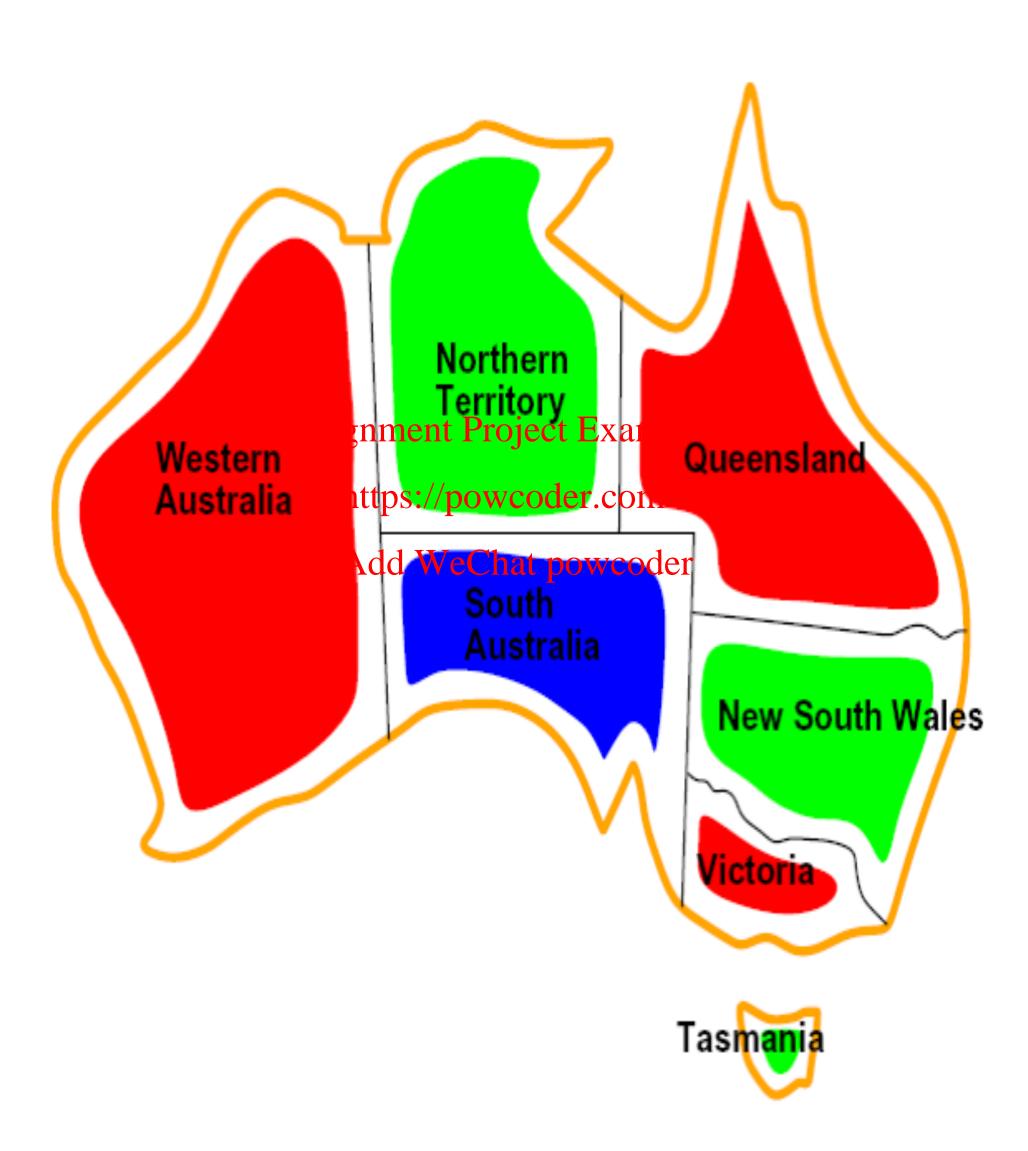
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- Constraint satisfaction problems (CSPs) a special subset of search problems
 - State is defined by variables X_i with values from a domain D
 - Goal test is a set of constraints specifying allowable combinations of values for subsets of variables
- Simple example of a formal representation language
- > Allows useful general-purpose algorithms with more power than standard search algorithms





CSP EXAMPLES



EXAMPLE: MAP COLORING

- Variables: WA, NT, Q, NSW, V, SA, T
- \triangleright Domains: D = {red, green, blue}
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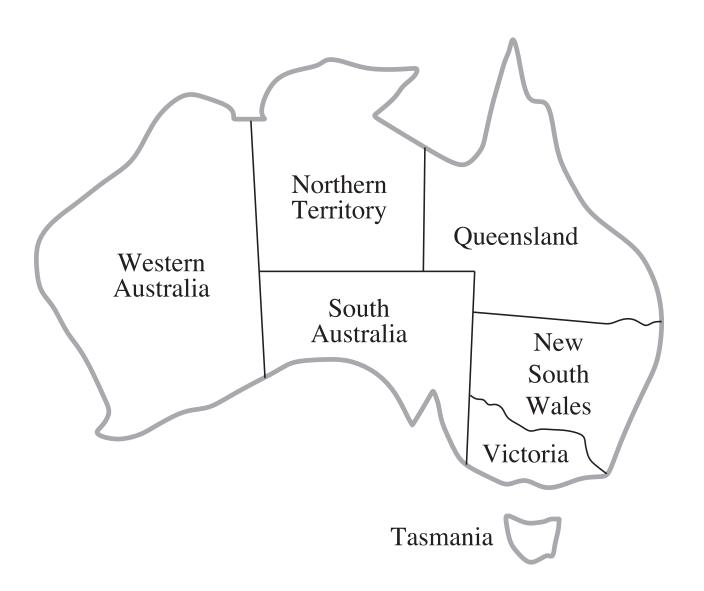
 Constraints: adjacent regions must have different colors

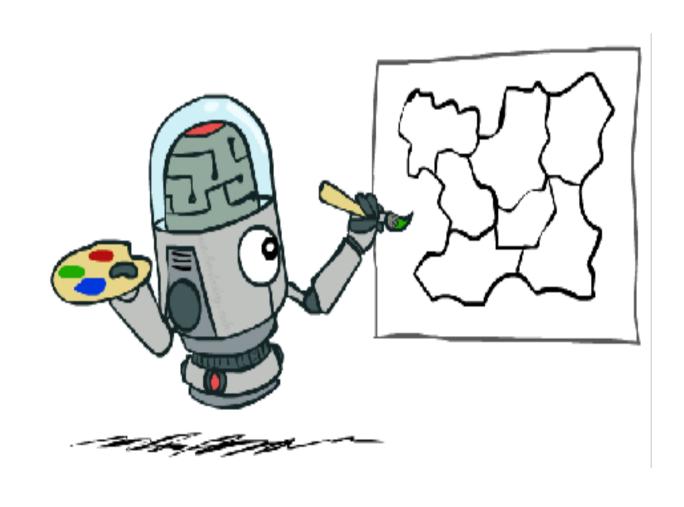
Implicit: WA ≠ NT

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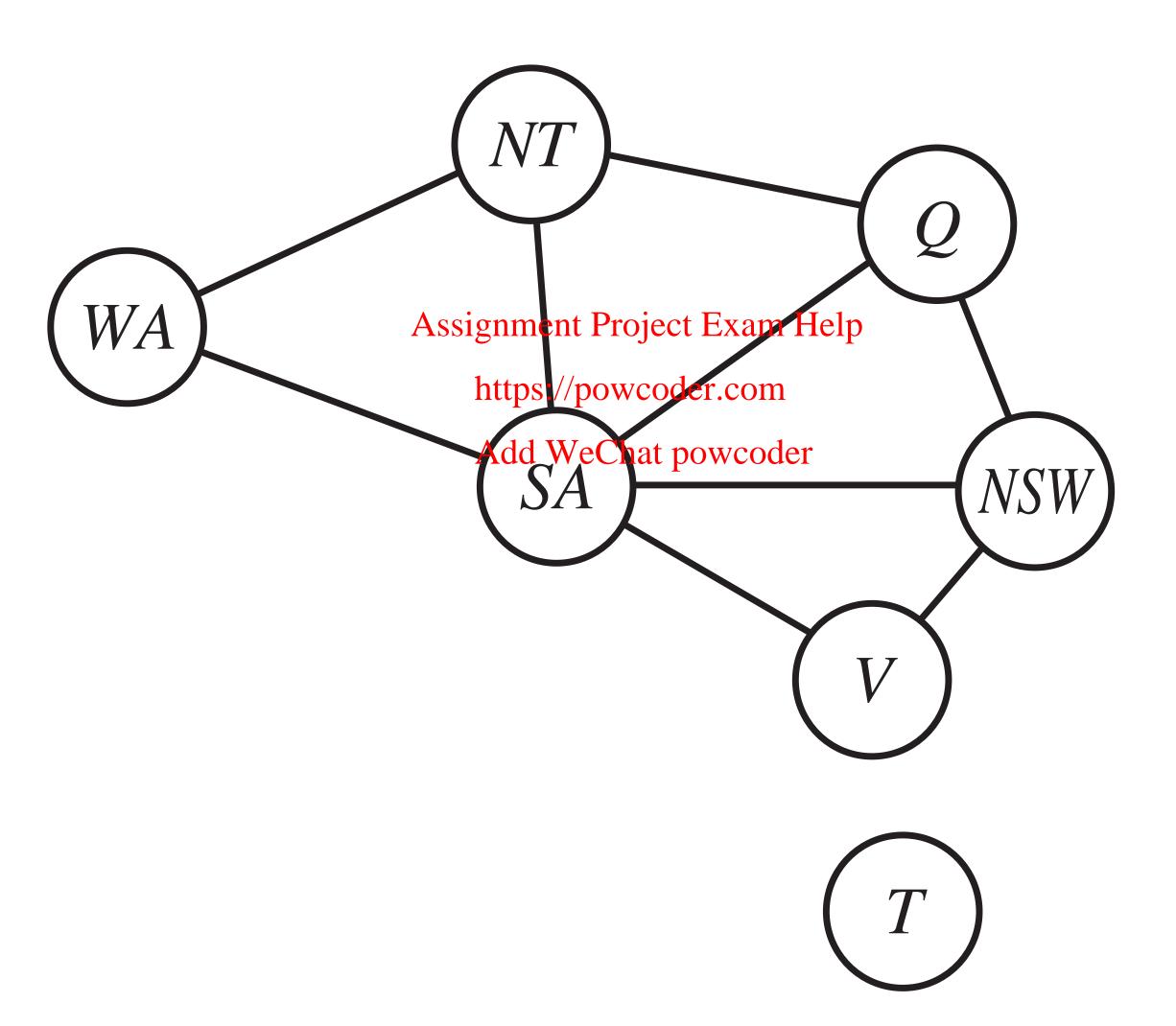
Explicit: $(WA, NT) \in \{(red, green), (red, blue), ...\}$

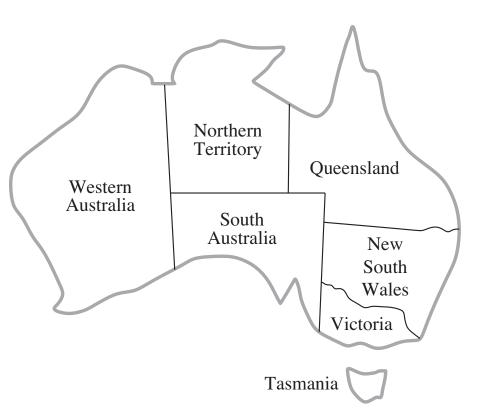
Solutions are assignments satisfying all constraints, e.g.:





CONSTRAINT GRAPHS



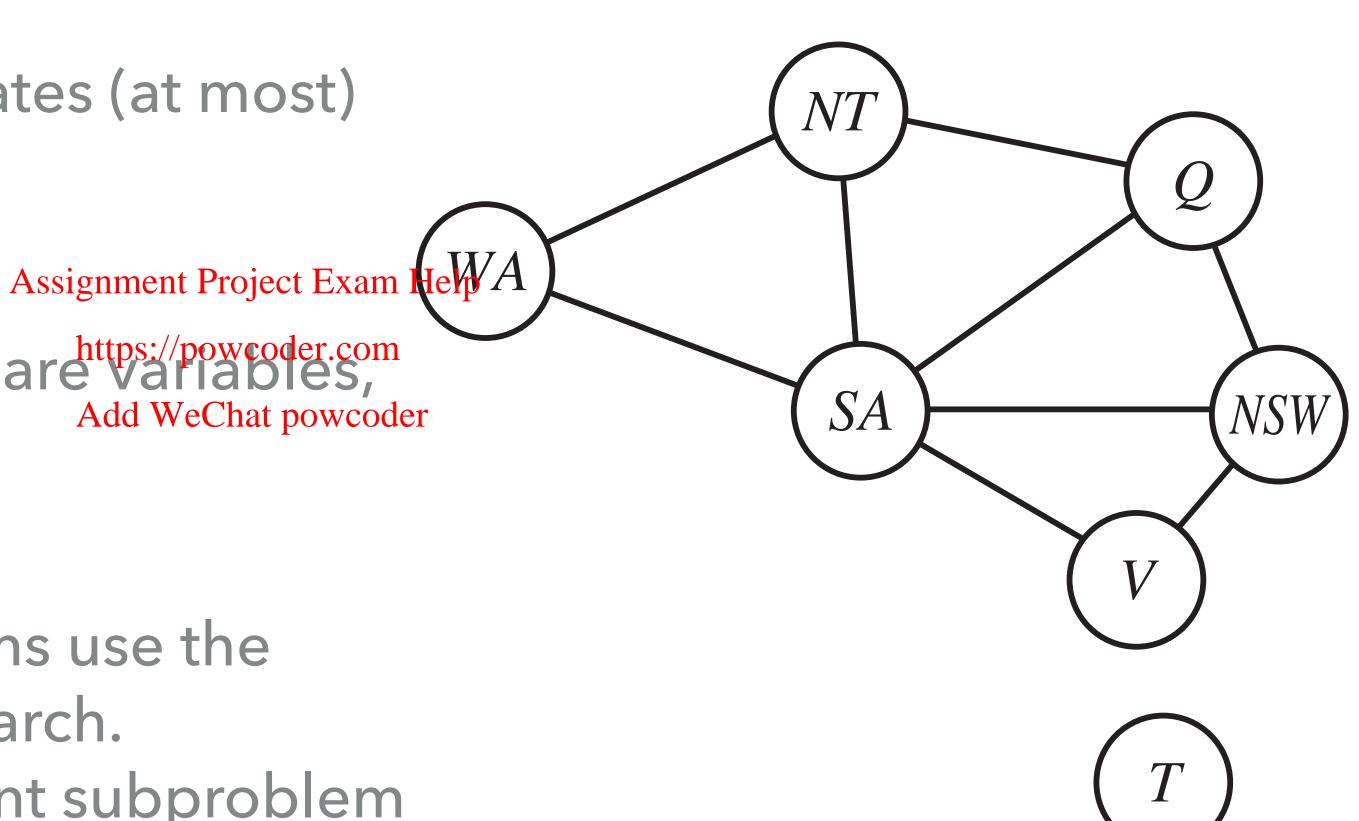


CONSTRAINT GRAPHS

 Binary CSP: each constraint relates (at most) two variables

Binary constraint graph: nodes are variables, Add WeChat powcoder arcs show constraints

 General-purpose CSP algorithms use the graph structure to speed up search.
 E.g., Tasmania is an independent subproblem



EXAMPLE: N-QUEENS

ightharpoonup Variables: Q_k

▶ Domains: {1,2,3,...*N*}

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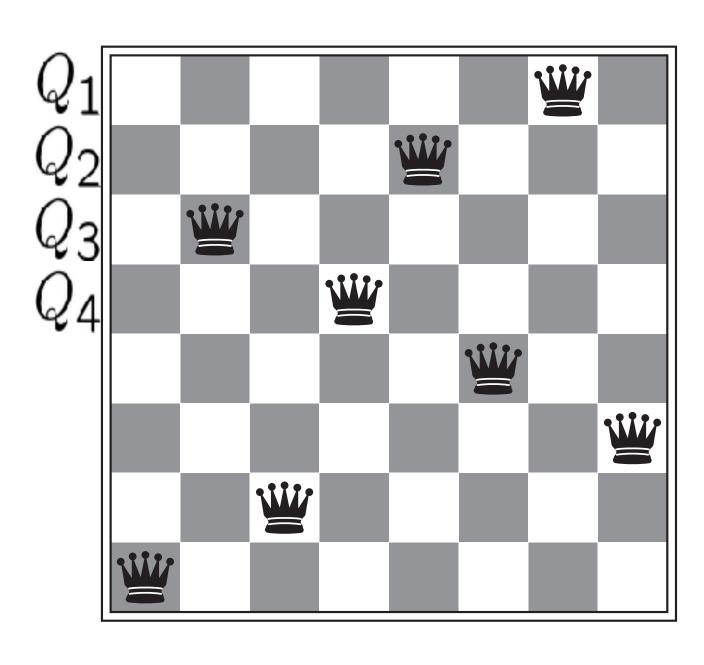
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Constraints:

Implicit: $\forall i, j$ non-threatening (Q_i, Q_j)

Explicit: $(Q_1, Q_2) \in \{(1, 3), (1, 4), \ldots\}$

. . .



EXAMPLE: SUDOKU

- Objective
 - Fill the empty cells with numbers between 1 and 9

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Rules

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- Numbers can appear only once on each row
- Numbers can appear only once on each column
- Numbers can appear only once on each region
- Variables? Domain?
- Constraints?

8			4		6			7
						4		
	1					6	5	
5		9		3		7	8	
				7				
	4	8		2		1		3
	5	2					9	
		1						
3			9		2			5

SOLVING CSPS



STANDARD SEARCH FORMULATION

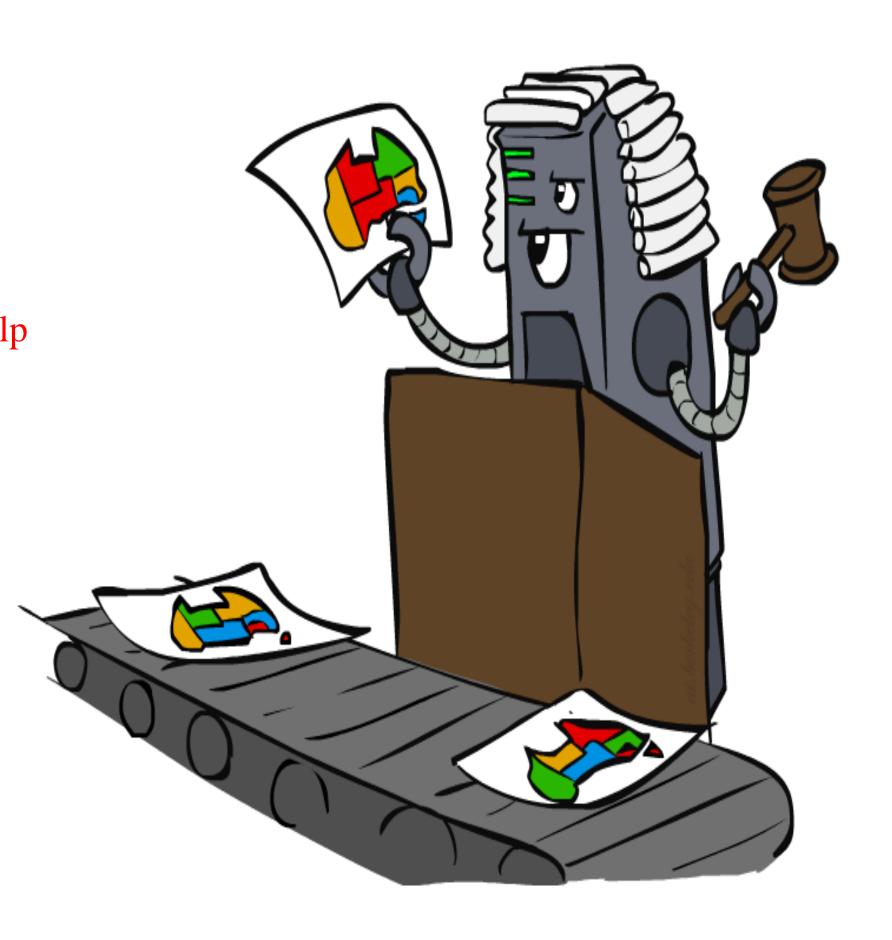
- Standard search formulation of CSPs
- States defined by the values assigned so far

 (ie. partial assignments)

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 - Initial state: the empty assignment, https://powcoder.com

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- Successor function: assign a value to an unassigned variable
- Goal test: the current assignment is complete and satisfies all constraints



SEARCH METHODS

What would BFS do?

What would DFS do?

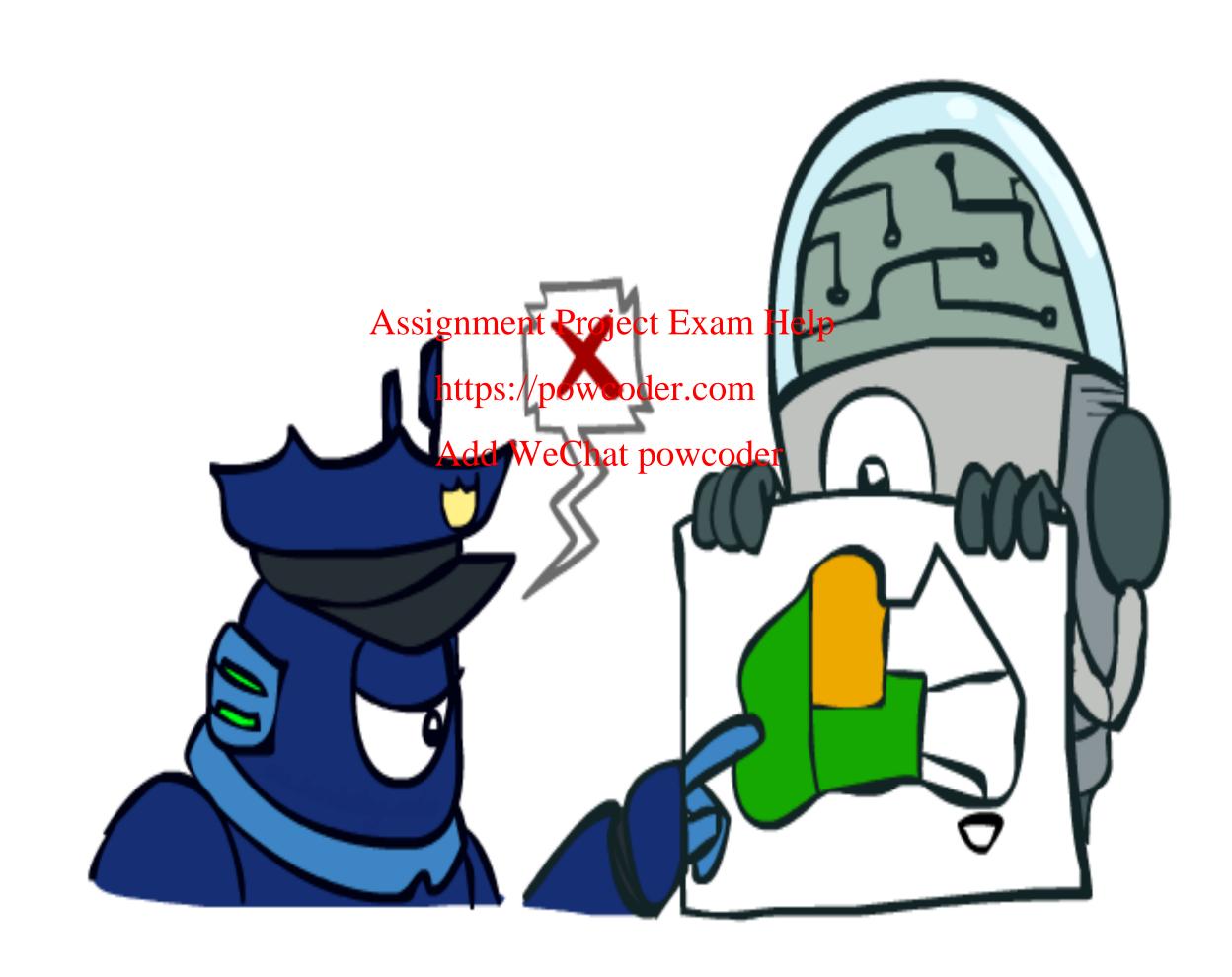
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e space search have

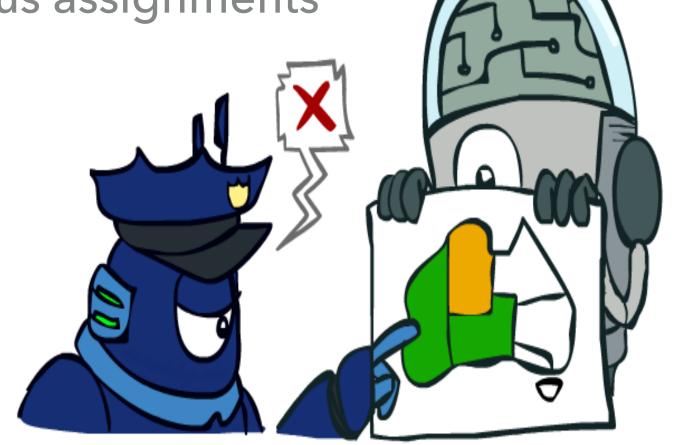
What problems does naive state space search have in this setting?

BACKTRACKING SEARCH



BACKTRACKING SEARCH

- ▶ Backtracking search is the basic uninformed algorithm for solving CSPs
- Idea 1: One variable at a time
 - Variable assignments are commutative, so fix ordering and only consider assignments to a single variable at each step
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 - I.e., [WA = red then NT = green] same as [NT_d were pother WA = red]
- Idea 2: Check constraints as you go
 - Incremental goal test" i.e. consider only values which do not conflict previous assignments
 - Might have to do some computation to check the constraints
- Depth-first search with these two improvements is called backtracking search (not the best name)
- Can solve n-queens for n ≈ 25



BACKTRACKING EXAMPLE

