CS211 Spring 2021 Programming Assignment II

David Menendez

Due: March 12, 2021, 10:00 PM Hand in by March 13, 2021, 4:00 AM

Background: the knapsack problem 1

We have a set of items, each of which has a weight and a value. We want to pack these items into a knapsack, but there is a maximum amount of weight that the knapsack can carry. Our goal is to find the most valuable subset of the items whose total weight does not exceed the knapsack's weight

also assume that the knapsack can carry any combination of items, as long as the weight limit is not exceeded.

For example, we might have five light items with weight 1 and value 10, and one heavy item with weight 4 and value 19 Of Sur/khapsel? Weigh Dhil ts 1, what if He maximum total value of the items we can place in the knapsack?

1.1 Formal definition

An instance of the knapsack problem involves a weight limit L and N items, numbered from 0 to N-1. Each item i has a weight w_i and value v_i .

A solution to the knapsack problem is a set if items S that maximizes the total value

$$\sum_{i \in S} v_i \tag{1}$$

such that

$$\sum_{i \in S} w_i \le L. \tag{2}$$

Non-optimal approaches

A naïve strategy is to test every combination of items and keep the combination with the highest total value of all combinations that do not exceed the weight limit. This strategy requires checking 2^N subsets o items, leaving it impractical for all but the smallest problems.

A greedy approach might sort the items by some metric, such as value or ratio of value to weight, and repeatedly choose the best item that does not exceed the remaining weight limit. Unfortunately, this approach is not guaranteed to find an optimal subset.

Going back to our example, if our weight limit is 5 and we choose the most valuable items first, we will select the heavy item and one light item, for a total value of 49. The optimal subset with total weight 5 is to take five light items, for a total value of 50.

If we choose items to maximize value per weight, we will find the optimal set for weight limit 5. If the weight limit is 6, we will chose five light items again, for a total value of 50. Here, the optimal solution is to choose two light items and the heavy item, for a total value of 59.

1.3 Method: Dynamic programming

We will use a *dynamic programming* approach to find optimal solutions. Dynamic programming finds a solution to a problem by first finding solutions to smaller sub-problems.

For our knapsack problem, we will write V_{ℓ}^n to indicate the maximum total value obtainable with items 0 through n subject to weight limit ℓ . Thus, V_L^{N-1} is the maximum value obtainable using all N items with weight limit L.

We will construct a table containing V_{ℓ}^n for all subproblems from V_1^0 to V_L^{N-1} . To simplify the definition, we define $V_{\ell}^n = 0$ if n < 0 or $\ell < 1$.

To compute V_{ℓ}^n , we must decide whether or not to include item n in the set. The maximum total value if we do not include item n is V_{ℓ}^{n-1} . If we do choose n, then whatever we chose from the preceding items must fit within the limit $\ell - w_n$. Thus, the maximum total value if we do include item n is $v_n + V_{\ell}^{n-1}$. We choose whichever is larger

item
$$n$$
 is $X_n + V_{\ell-m}^{n-1}$. We choose whicher is larger.

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$$V_{n,\ell} = \begin{cases} \max\{V_{\ell}^{n-1}, v_n + V_{\ell-m_n}^{n-1}\} & \text{otherwise} \end{cases}$$
(3)

Note that we can fill this table by columns, from left to right, or by rows, from top to bottom. To compute cell V_{ℓ}^n , velocity S_{ℓ}^{\bullet} to have Ottis reglification of the left and to another value higher in the same column.

Table 1 shows the table we would compute for our running example with one heavy item and five light items. We see that $V_4^4 = 40$. This was computed by comparing V_4^3 and $10 + V_3^3$, since $v_4 = 10$ and $w_4 = 1$. April 1 hrough Griclad La leave to the light items. If the weight limit is 3, the best solution is to take all three light items, thus $V_3^3 = 30$. If the weight limit is 4, the best solution is to take the heavy item, thus $V_4^3 = 39$. A solution for items 0 through 4 will either include item 4 or not. If it does not include item 4, then its maximum value will be the same as the maximum value for items 0 through 3 with the same weight limit. If it does include item 4, then the maximum value will be the value of item 4 plus the maximum value obtainable with the remaining weight. That is, the weight limit minus $w_4 = 1$. Hence the comparison of $V_4^3 = 39$ and $10 + V_3^3 = 40$. The larger is the best possible solution with items 0 through 4 and weight limit 4.

It is worth working through a few examples yourself until you are convinced that this method works.

1.4 Determining the optimum set

The table V_ℓ^n gives the maximum value obtainable with items 0 through n and weight limit ℓ , but does not directly indicate which items were selected. This information could be kept in a separate table indicating whether the optimum solution for a particular subproblem includes that item, based on which choice was made when computing V_ℓ^n .

Table 1: Maximum total value within a weight limit

i	0	1	2	3	4	5
v_i	39	10	10	10	10	10
w_i	4	1	1	1	1	1
$\overline{\ell}$	V_{ℓ}^{0}	V_{ℓ}^1	V_{ℓ}^2	V_{ℓ}^3	V_{ℓ}^4	V_{ℓ}^{5}
1	0	10	10	10	10	10
2	0	10	20	20	20	20
3	0	10	20	30	30	30
4	39	39	39	39	40	40
5	39	49	49	49	49	50
6	39	49	59	59	59	59

Alternatively, the set of items can be found by examining the table. In general, if $V_{\ell}^{n} = V_{\ell}^{n-1}$, we can assume that item n was not included in the solution. We consider the items in reverse order, from N-1 to 0, with an initial weight limit of L. For each item n, we compare V_{ℓ}^{n} and V_{ℓ}^{n-1} . If they are the same, then item n is not included and we continue. If they are not the same, we reduce the remaining weight by w_{n} and continue.

Applying this method to table 1, we conclude that the optimum subset of items 0 through 5 with weight in the project Exam Help

Ambiguous cases If $V_{\ell}^{n-1} = v_n + V_{\ell-w_n}^{n-1}$, this means there are (at least) two subsets that have the maximum total value. In our running example, when $\ell = 1$, any of the five light items can be chosen to obtain the maximum retail only ℓ 0. For the assignment we resolve ambiguity by choosing the solution that does not include the current item. Thus, the set corresponding to V_1^5 would include item 1.

2 ProgramAdd WeChat powcoder

You will write a program knapsack which chooses items from a manifest. knapsack takes two arguments: the weight limit and a manifest file. It chooses a selection of items from the manifest that maximizes the total value without exceeding the weight limit. Once the selection is made, knapsack will print the selected items, one per line, in the same order they appear in the manifest file. After the list, knapsack will print the total value and total weight of the selected items.

The weight limit is a positive integer written in decimal. (You may use atoi or some other function to covert the string to an integer.)

The manifest file is specified using a path that should be passed to open without interpretation. Your implementation SHOULD check for the correct number of arguments and report an error if first argument is not a positive integer or if the file specified by the second argument cannot be opened. You will not be tested for these cases.

Usage

\$ cat manifest.01.txt

```
Heavy 4 39
Light1 1 10
Light2 1 10
Light3 1 10
Light4 1 10
Light5 1 10
$ ./knapsack 5 manifest.01.txt
Light1
Light2
Light3
Light4
Light5
50 / 5
~/D/R/2/2/p/src $
$ ./knapsack 6 manifest.01.txt
Heavy
Light1
Light2
59 / 6
```

2.1 Assignment Project Exam Help

The manifest file begins with an integer indicating the number of items in the manifest. This is followed by the item definitions. Each item is specified by giving a *name*, a *weight*, and a *value*. The name is a string timest 3/ provided the string transfer and value are positive integers.

All integers will be given in decimal notation.

The format specifies only that names and numbers are separated by whitespace. It is not advised to assume that items vill positive where the line at powcoder. Your program will only be given manniests with unquery named items. It is not necessary to

Your program will only be given manifests with uniquely hamed items. It is not necessary to check the uniqueness of item names. Your program SHOULD confirm that all specified weights and values are positive.

There is no specified maximum number of items, but you may assume that the number of items will fit in a regular int, signed or unsigned.

Note that the %s format specifier does not allocate space, and may only be safely used when an upper limit is given: %31s.

2.2 Output format

knapsack prints the names of the selected items, one per line, in the same order they are given in the manifest file. Item names must be given exactly as in the file.

Immediately after the list of items, knapsack must print the total value and total weight of the selected items, separated by a slash (/). The numbers must be printed in decimal, without leading zeros, and must be separated from the slash by a single space character.

3 Grading

Your submission will be awarded up to 100 points, based on how many test cases your program completes successfully.

The auto-grader provided for students includes half of the test cases that will be used during grading. Thus, it will award up to 50 points.

Make sure that your program meets the specifications given, even if no test case explicitly checks it. It is advisable to perform additional tests of your own devising.

3.1Academic integrity

You must submit your own work. You should not copy or even see code for this project written by anyone else, nor should you look at code written for other classes. We will be using state of the art plagiarism detectors. Projects which the detectors deem similar will be reported to the Office of Student Conduct.

Do not post your code on-line or anywhere publically readable. If another student copies your code and submits it, both of you will be reported.

Do not look for solutions to the knapsack problem on-line. Do not look at sample code. You must submit your own original work.

SAssignment Project Exam Help

Your solution to the assignment will be submitted through Sakai. You will submit a Tar archive file containing the sturge code and makefiles for your project. Your archive should not include any compiled code or objectile S.// DOW COUCH.COIII

The remainder of this section describes the directory structure (section 4.1), the requirements for your makefiles (section 4.2), how to create the archive (section 4.3), and how to use the provided auto-grader (section A4).dd WeChat powcoder

4.1 Directory structure

Your project should be stored in a directory named src, which will contain three sub-directories. Each subdirectory will have the name of a particular program, and contain (1) a makefile, and (2) any source files needed to compile your program. Typically, you will provide a single C file named for the program. That is, the source code for the program factor would be a file factor.c, located in the directory src/factor.

This diagram shows the layout of a typical project:

src

- +- Makefile
- +- knapsack.c

If you are providing your own tests, as described in section 4.5, they will be in a directory named tests inside the program directory. For example,

src

+- Makefile

```
+- factor.c
+- tests
+- manifest.01.txt
+- test.01.20.txt
```

4.2 Makefiles

We will use make to manage compilation. Each program directory will contain a file named Makefile that describes at least two targets. The first target must compile the program. An additional target, clean, must delete any files created when compiling the program (typically just the compiled program).

The auto-grader script is distributed with an example makefile, which looks like this (note that an actual makefile must use tabs rather than spaces for indentation):

```
TARGET = knapsack

CC = gcc

CFLAGS = -g -std=c99 -Wall -Wvla -Werror -fsanitize=address,undefined

$(TARGET): $(TARGET).c

ASSIGNMENT Project Exam Help
```

clean:

```
rm -rf $(TARGET) *.o *.a *.dylib *.dSYM
```

It is simplest to the the into power decory and remain in this will ensure that you programs will be compiled with the recommended options.

It is further recommended that you use make to compile your programs, rather than invoking the compiler directly. This will easile that your personal testing is performed with the same compiler settings as the auto-grader. The makefus created but he build wre tow by the auto-grader refer to the makefus you create in the source directory and therefore pick up any changes made.

You may add additional compiler options as you see fit, but you are advised to leave the compiler warnings, sanitizers, and debugger information (-g). The makefile shown here specifies the C99 standard, in order to allow C++-style // comments; you may change that to C90, if you prefer.

Compiler options The sample makefile uses the following compiler options, listed in the CFLAGS make variable:

- -g Include debugger information, used by GDB and AddressSanitizer.
- -std=c99 Require conformance with the 1999 C Standard. (Disable GCC extensions.)
- -Wall Display most common warning messages.
- -Wvla Warn when using variable-length arrays.
- **-Werror** Promote all warnings to errors.

-fsanitize=address,undefined Include run-time checks provided by AddressSanitizer and UBSan. This will add code that detects many memory errors and guards against undefined behavior. (Note that these checks discover problems with your code. Disabling them will not make your code correct, even if it seems to execute correctly.)

4.3 Creating the archive

We will use tar to create the archive file. To create the archive, first ensure that your src directory contains only the source code and makefiles needed to compile your project. Any compiled programs, object files, or other additional files should be moved or removed.

Next, move to the directory containing src and execute this command:

pa2\$ tar -vzcf pa2.tar src

tar will create a file pa2.tar that contains all files in the directory src. This file can now be submitted through Sakai.

To verify that the archive contains the necessary files, you can print a list of the files contained in the archive with this command:

pa2\$ tar -tf pa2.tar

You should also use the auto-grader to confirm that your archive is correctly structured. Pa2\$./grader.py grant Project Exam Help

4.4 Using the auto-grader

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Setup The auto-grace distributed an nearly fiper-yater of Counpack the archive, move the archive to a directory and use this command:

\$ tar -xf pa2-grader.tar

This will create a directory pa2 containing the auto-grader itself, grader.py, a library autograde.py, and a directory of test cases data.

Do not modify any of the files provided by the auto-grader. Doing so may prevent the auto-grader from correctly assessing your program.

You may create your src directory inside pa2. If you prefer to create src outside the pa2 directory, you will need to provide a path to grader.py when invoking the auto-grader (see below).

Usage While in the same directory as grader.py and src, use this command:

pa2\$./grader.py

The auto-grader will compile and execute the programs in the directory src, assuming src has the structure described in section 4.1.

To stop the auto-grader after the first failed test case, use the --stop or -1 option.

To obtain usage information, use the -h option.

Program output By default, the auto-grader will not print the output from your program, except for lines that are incorrect. To see all program output for unsuccessful tests, use the --verbose or -v option:

To see program output for all tests, use -vv. To see no program output, use --quiet or -q.

Checking your archive We recommend that you use the auto-grader to check an archive before submitting. To do this, use the **--archive** or **-a** option with the archive file name. For example,

```
pa2$ ./grader.py -a pa2.tar
```

This will unpack the archive into a temporary directory, grade the programs, and then delete the temporary directory.

Specifying source directory If your src directory is not located in the same directory as grader.py, you may specify it using the --src or -s option. For example,

Assignment Project Exam Help
Refreshing the build directory In the unlikely event that your build directory has become

Refreshing the build directory In the unlikely event that your build directory has become corrupt or otherwise unusable, you can simply delete it using rm -r build. Alternatively, the --fresh or -f option will delete and recreate the build directory before testing.

https://powcoder.com 4.5 Providing your own tests

The tests provided with the auto-grader may not check every possible input scenario. If you wish to be certain that your program is direct, you should design and test additional test cases. This may be done by entering the cases manually and running the program yourself, of by using the user test capability of the auto-grader.

To provide additional tests for the auto-grader, create a directory named tests inside the directory containing your source code and make file (see section 4.1).

First, create one or more manifest files, with names following the pattern $\mathtt{manifest}.X.\mathtt{txt}$, where X is a unique identifier not containing a period.

Next, create one or more reference files. The reference file will contain the expected output of knapsack for a particular weight limit and manifest file, which is indicated by the reference file name. A reference file for weight limit L and manifest X should be named $\mathtt{ref}.X.L.\mathtt{txt}$.

For example, ref.abc.13.txt contains the expected output for knapsack given width 13 and manifest file manifest.abc.txt.

User tests are not required. The capacity for user tests is provided to assist you in development, but it will not directly affect your grade.