

# CS 314 Principles of Programming Languages

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## Lecture 5: Syntax Analysis (Parsing)

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*Rutgers University*

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# Class Information

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- Homework 1 is being graded now.  
The sample solution will be posted soon.
- Homework 2 will be posted tomorrow.

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# Review: Context Free Grammars (CFGs)

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- A formalism to for describing languages
- A CFG  $G = \langle T, N, P, S \rangle$ :
  1. A set  $T$  of terminal symbols (tokens).
  2. A set  $N$  of nonterminal symbols.
  3. A set  $P$  production (rewrite) rules.
  4. A special start symbol  $S$ .
- The language  $L(G)$  is the set of sentences of terminal symbols in  $T^*$  that can be derived from the start symbol  $S$ :

$$L(G) = \{w \in T^* \mid S \Rightarrow^* w\}$$

# Elements of BNF Syntax

Terminal Symbol:

**Symbol-in-Boldface**

Non-Terminal Symbol: *Symbol-in-Angle-Brackets*

Production Rule:

Non-Terminal ::= Sequence of Symbols

or

Non-Terminal ::= Sequence | Sequence |

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Example:

...

**<if-stmt> ::= if <expr> then <stmt>**

**<expr> ::= id <= id**

**<stmt> ::= id := num**

terminal

terminal non-terminal

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# Review: Context Free Grammar

...

$\langle \text{if-stmt} \rangle ::= \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stmt} \rangle$

$\langle \text{expr} \rangle ::= \text{id} \leq \text{id}$

$\langle \text{stmt} \rangle ::= \text{id} := \text{num}$

...

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Context free grammar

Rule 1  $\$1 \Rightarrow 1\&$

Rule 2  $\$0 \Rightarrow 0\$$

Rule 3  $\&1 \Rightarrow 1\$$

Rule 4  $\&0 \Rightarrow 0\&$

Rule 5  $\$ \# \Rightarrow \rightarrow A$

Rule 6  $\& \# \Rightarrow \rightarrow B$

Not a context free grammar

CFGs are rewrite systems with restrictions on the form of rewrite (production) rules that can be used. The left hand side of a production rule can only be **one non-terminal symbol**.

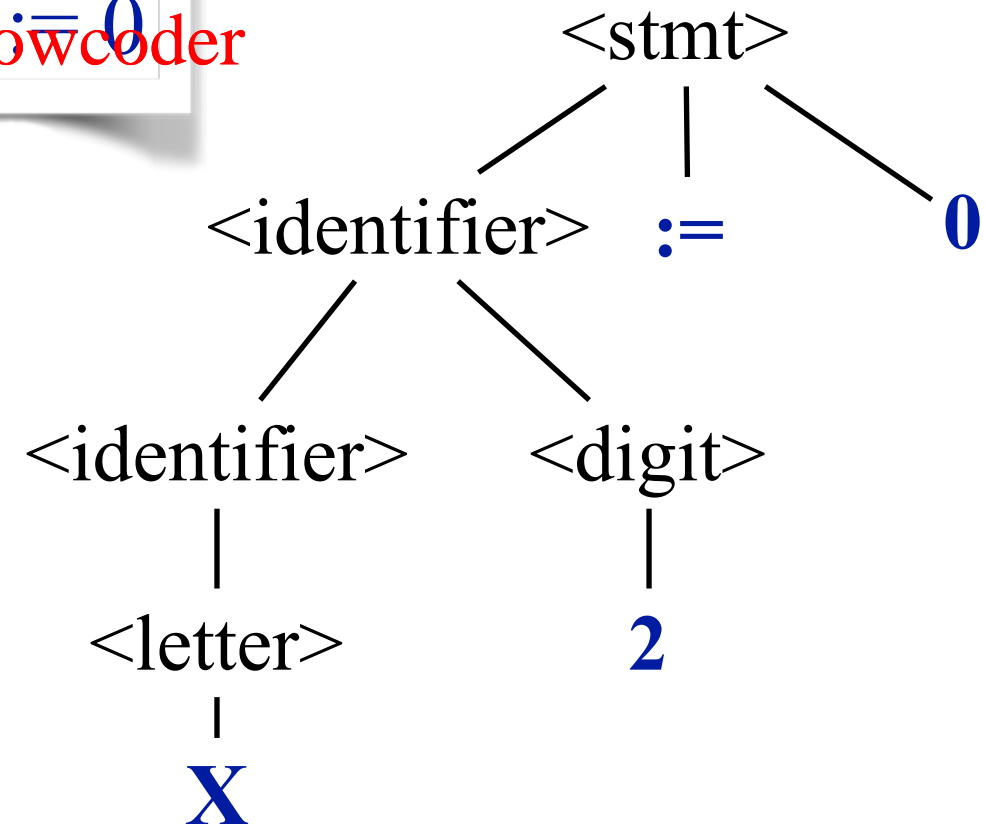
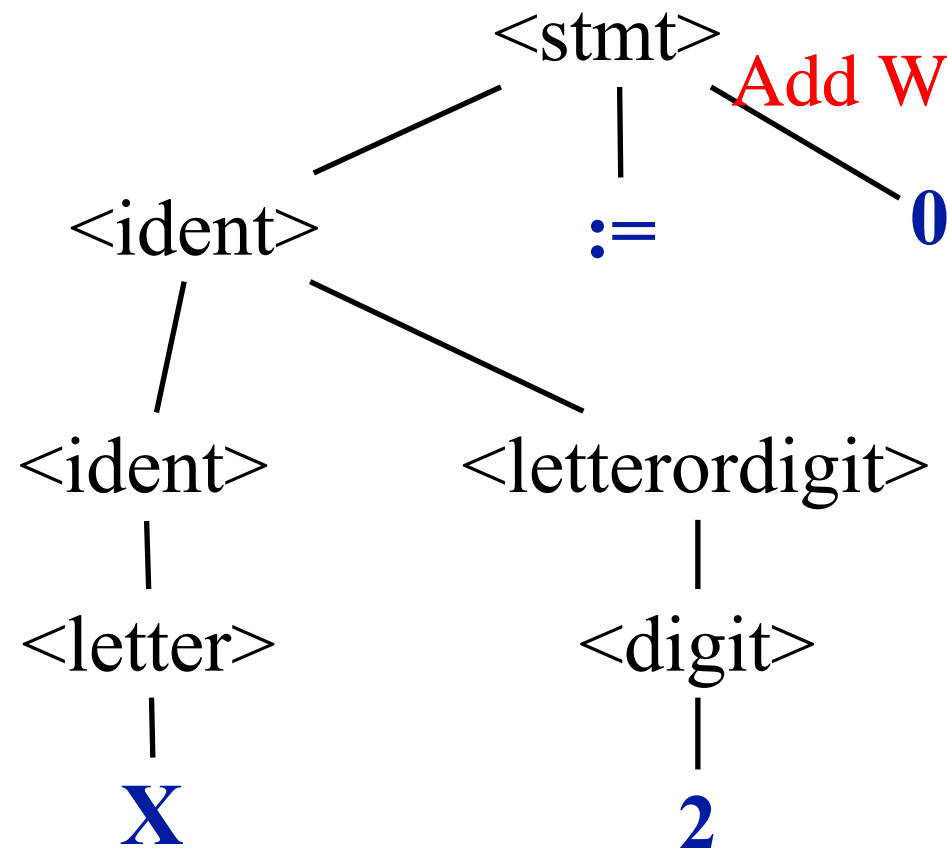
# A Language May Have Many Grammars

Consider  $G'$ :

1.  $\langle \text{letter} \rangle ::= \mathbf{A} \mid \mathbf{B} \mid \mathbf{C} \mid \dots \mid \mathbf{Z}$
2.  $\langle \text{digit} \rangle ::= \mathbf{0} \mid \mathbf{1} \mid \mathbf{2} \mid \dots \mid \mathbf{9}$
3.  $\langle \text{ident} \rangle ::= \langle \text{letter} \rangle \mid$
4.  $\quad \quad \quad \langle \text{ident} \rangle \langle \text{letterordigit} \rangle$
5.  $\langle \text{stmt} \rangle ::= \langle \text{ident} \rangle \mathbf{:=} \mathbf{0}$
6.  $\langle \text{letterordigit} \rangle ::= \langle \text{letter} \rangle \mid \langle \text{digit} \rangle$

The Original Grammar  $G$ :

1.  $\langle \text{letter} \rangle ::= \mathbf{A} \mid \mathbf{B} \mid \mathbf{C} \mid \dots \mid \mathbf{Z}$
2.  $\langle \text{digit} \rangle ::= \mathbf{0} \mid \mathbf{1} \mid \mathbf{2} \mid \dots \mid \mathbf{9}$
3.  $\langle \text{identifier} \rangle ::= \langle \text{letter} \rangle \mid$
4.  $\quad \quad \quad \langle \text{identifier} \rangle \langle \text{letter} \rangle \mid$
5.  $\quad \quad \quad \langle \text{identifier} \rangle \langle \text{digit} \rangle$
6.  $\langle \text{stmt} \rangle ::= \langle \text{identifier} \rangle \mathbf{:=} \mathbf{0}$



# Review: Grammars and Programming Languages

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**Many grammars may correspond to one programming language.**

Good grammars:

- Captures the logic structure of the language  
⇒ structure carries some semantic information  
(example: expression grammar)
- Use meaningful names
- Are easy to read
- Are unambiguous
- ...

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# Review: Ambiguous Grammars

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*“Time flies like an arrow; fruit flies like a banana.”*

**A grammar  $G$  is ambiguous iff there exists a  $w \in L(G)$  such that there are:**

- two distinct parse trees for  $w$ , or
- two distinct leftmost derivations for  $w$ , or
- two distinct rightmost derivations for  $w$ .

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*We want a unique semantics of our programs, which typically requires a unique syntactic structure.*

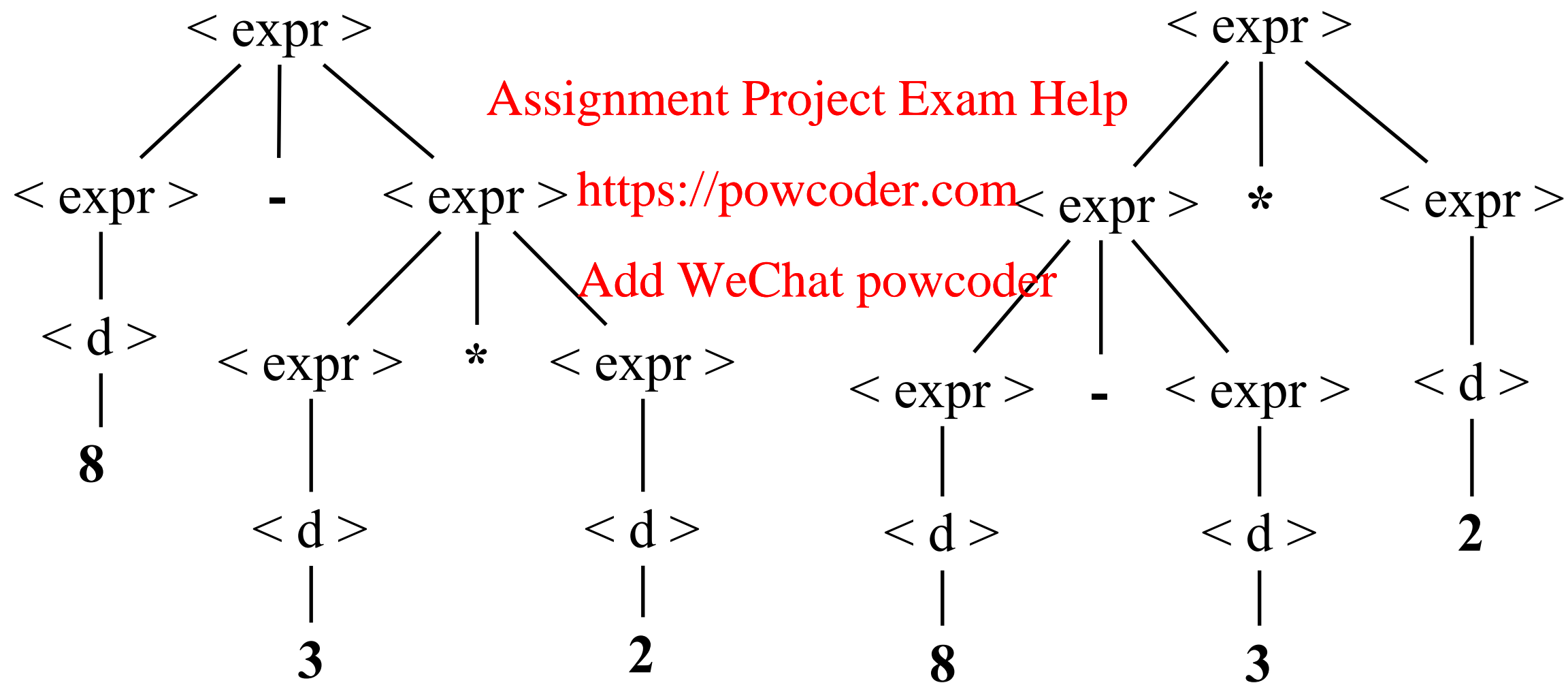


# Review: Arithmetic Expression Grammar

Parse “8 - 3 \* 2”:

$\langle \text{start} \rangle ::= \langle \text{expr} \rangle$   
 $\langle \text{expr} \rangle ::= \langle \text{expr} \rangle - \langle \text{expr} \rangle \mid$   
 $\quad \langle \text{expr} \rangle * \langle \text{expr} \rangle \mid$   
 $\quad \langle d \rangle \mid \langle l \rangle$   
 $\langle d \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid 9$   
 $\langle l \rangle ::= a \mid b \mid c \mid \dots \mid z$

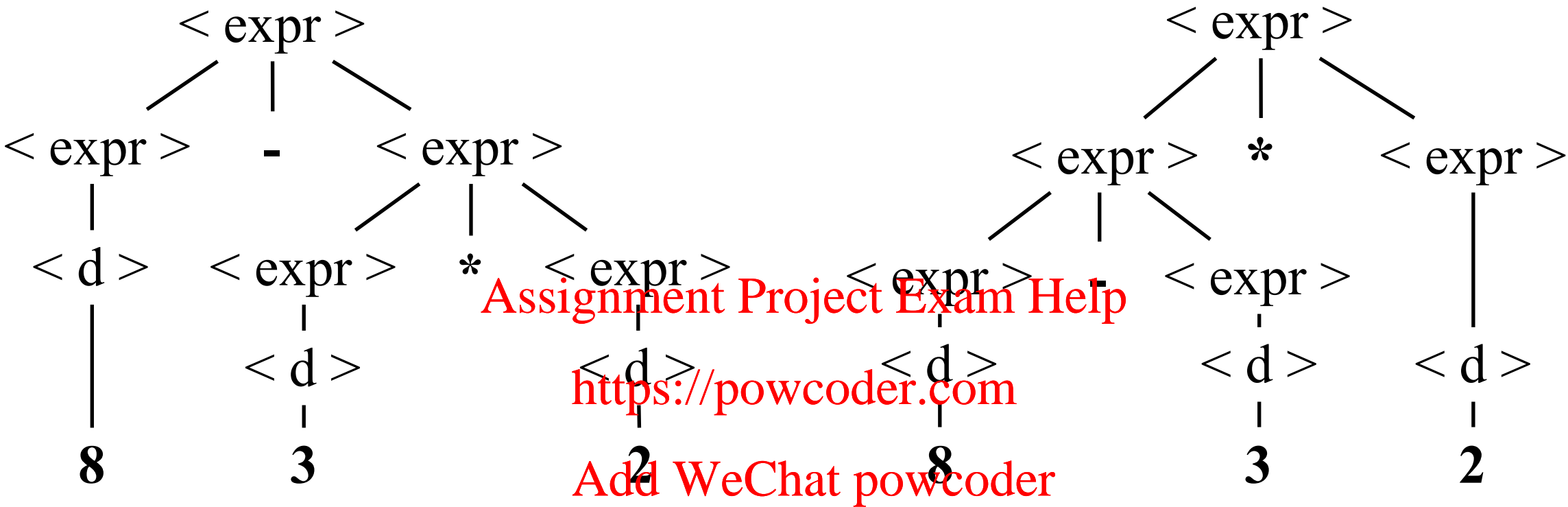
Two parse trees!



# Review: Arithmetic Expression Grammar

Parse “8 - 3 \* 2”:

Two Parse Trees → Two leftmost derivations!



leftmost derivation	
<expr>	⇒ <sub>L</sub>
<expr> - <expr>	⇒ <sub>L</sub>
<d> - <expr>	⇒ <sub>L</sub>
<d> - <expr> * <expr>	⇒ <sub>L</sub>
<d> - <d> * <expr>	⇒ <sub>L</sub>
<d> - <d> * <d>	

leftmost derivation	
<expr>	⇒ <sub>L</sub>
<expr> * <expr>	⇒ <sub>L</sub>
<expr> - <expr> * <expr>	⇒ <sub>L</sub>
<d> - <expr> * <expr>	⇒ <sub>L</sub>
<d> - <d> * <expr>	⇒ <sub>L</sub>
<d> - <d> * <d>	

# Review: Ambiguity

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How to deal with ambiguity?

- Change the language

Example: Adding new terminal symbols as delimiters.

Fix the *dangling else, expression* grammars.

- Change the grammar

Example: Impose **associativity** and **precedence** in an *arithmetic expression* grammar.

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# Changing the Grammar to Impose Precedence

```
< start > ::= < expr >
< expr > ::= < expr > + < expr > |
               < expr > - < expr > |
               < expr > * < expr > |
               < expr > / < expr > |
               < d > | < l >
< d >      ::= 0 | 1 | 2 | 3 | ... | 9
< l >      ::= a | b | c | ... | z
```



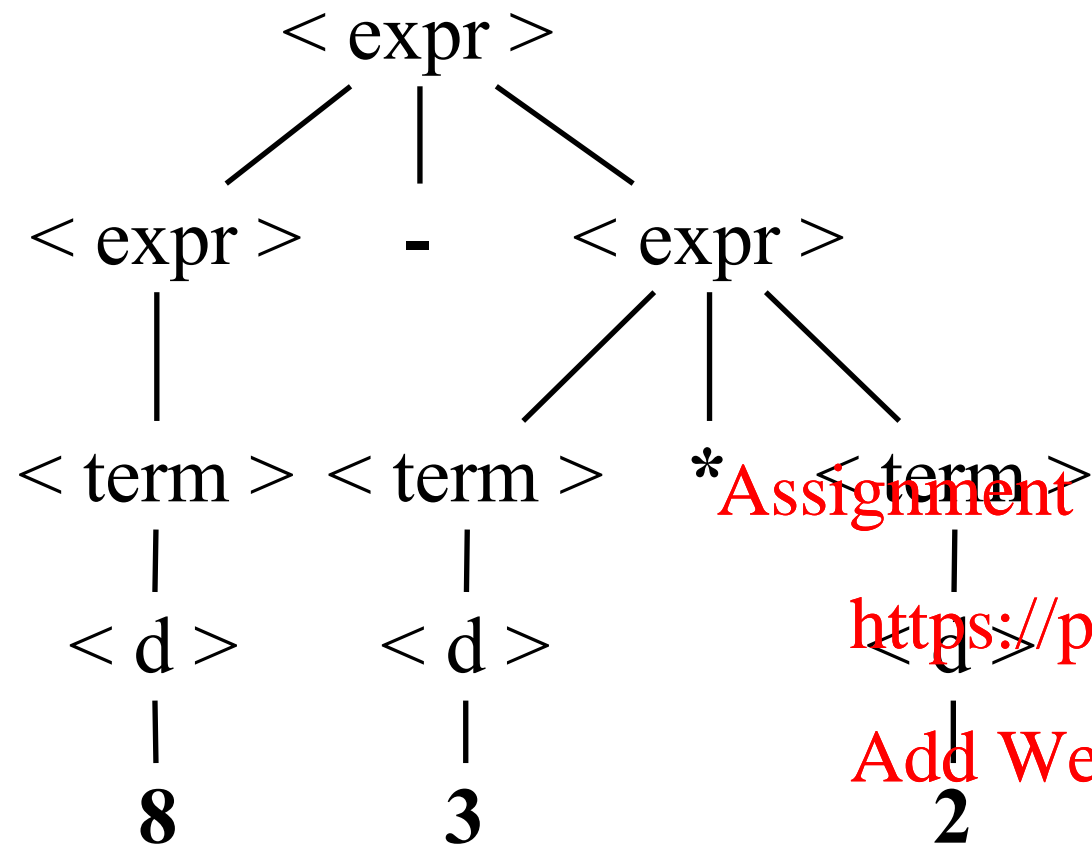
```
< start > ::= < expr >
< expr > ::= < expr > + < expr > |
               < expr > - < expr > |
               < term >
< term > ::= < term > * < term > |
               < term > / < term > |
               < d > | < l >
< d >      ::= 0 | 1 | 2 | 3 | ... | 9
< l >      ::= a | b | c | ... | z
```

Original Grammar  $G$

Modified Grammar  $G'$

# Grouping in Parse Tree Now Reflects Precedence

Parse “8 - 3 \* 2”:



$\langle \text{start} \rangle ::= \langle \text{expr} \rangle$

$\langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid$

$\langle \text{expr} \rangle - \langle \text{expr} \rangle \mid$

$\langle \text{term} \rangle$

$\langle \text{term} \rangle ::= \langle \text{term} \rangle * \langle \text{term} \rangle \mid$

$\langle \text{term} \rangle / \langle \text{term} \rangle \mid$

$\langle \text{d} \rangle \mid \langle 1 \rangle$

$\langle \text{d} \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid 9$

$\langle 1 \rangle ::= a \mid b \mid c \mid \dots \mid z$

Modified Grammar  $G'$

Only One Possible Parse Tree

# Precedence

- *Low Precedence:*  
Addition + and Subtraction -
- *Medium Precedence:*  
Multiplication \* and Division /
- *Highest Precedence:*  
Exponentiation ^

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$\langle \text{start} \rangle ::= \langle \text{expr} \rangle$

$\langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid$

$\langle \text{expr} \rangle - \langle \text{expr} \rangle \mid$

$\langle \text{term} \rangle$

$\langle \text{term} \rangle ::= \langle \text{term} \rangle * \langle \text{term} \rangle \mid$

$\langle \text{term} \rangle / \langle \text{term} \rangle \mid$

$\langle \text{d} \rangle \mid \langle \text{l} \rangle$

$\langle \text{d} \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid 9$

$\langle \text{l} \rangle ::= \mathbf{a} \mid \mathbf{b} \mid \mathbf{c} \mid \dots \mid \mathbf{z}$

# Still Have Ambiguity...

How about  $3 - 2 - 1$  ?

$(3 - 2) - 1$

OR?

$3 - (2 - 1)$

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$\langle \text{start} \rangle ::= \langle \text{expr} \rangle$

$\langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid \underline{\langle \text{expr} \rangle - \langle \text{expr} \rangle} \mid \langle \text{term} \rangle$

$\langle \text{term} \rangle ::= \langle \text{term} \rangle * \langle \text{term} \rangle \mid \langle \text{term} \rangle / \langle \text{term} \rangle \mid \langle d \rangle \mid \langle l \rangle$

$\langle d \rangle ::= \mathbf{0} \mid \mathbf{1} \mid \mathbf{2} \mid \mathbf{3} \mid \dots \mid \mathbf{9}$

$\langle l \rangle ::= \mathbf{a} \mid \mathbf{b} \mid \mathbf{c} \mid \dots \mid \mathbf{z}$

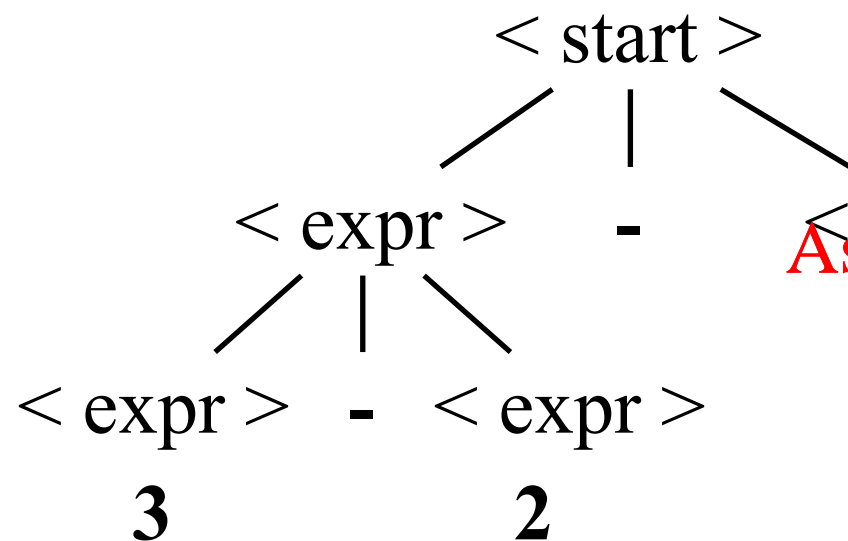
# Still Have Ambiguity...

How about  $3 - 2 - 1$  ?

$3 - 2 - 1$

OR?

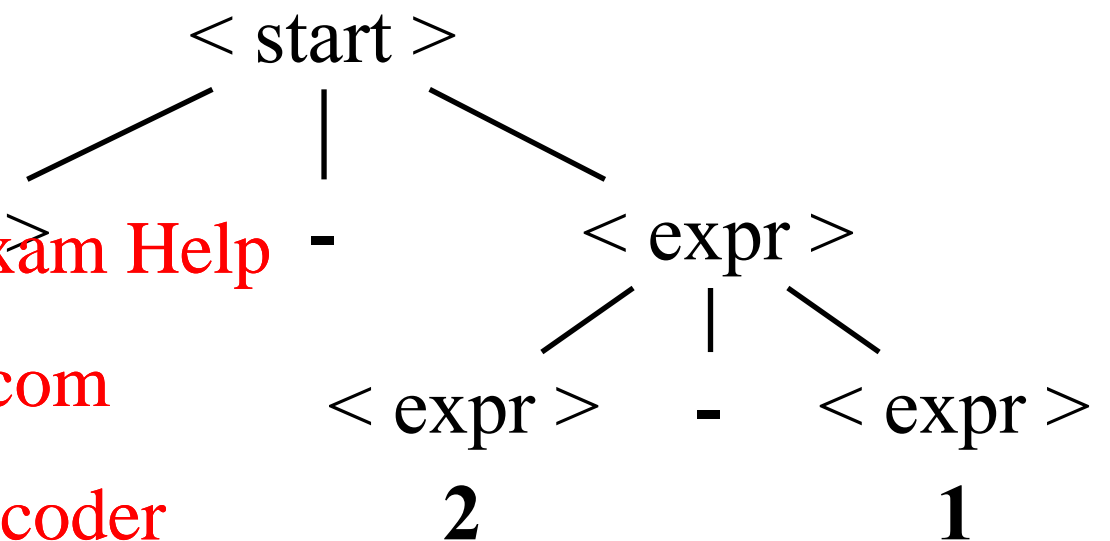
$3 - 2 - 1$



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$\langle \text{start} \rangle ::= \langle \text{expr} \rangle$

$\langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid \underline{\langle \text{expr} \rangle - \langle \text{expr} \rangle} \mid \langle \text{term} \rangle$

$\langle \text{term} \rangle ::= \langle \text{term} \rangle * \langle \text{term} \rangle \mid \langle \text{term} \rangle / \langle \text{term} \rangle \mid \langle \text{d} \rangle \mid \langle \text{l} \rangle$

$\langle \text{d} \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid 9$

$\langle \text{l} \rangle ::= a \mid b \mid c \mid \dots \mid z$



# Still Have Ambiguity...

- Grouping of operators of same precedence not disambiguated.
- Non-commutative operators: only one parse tree correct.

$\langle \text{start} \rangle ::= \langle \text{expr} \rangle$

$\langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid \langle \text{expr} \rangle - \langle \text{expr} \rangle \mid \langle \text{term} \rangle$

$\langle \text{term} \rangle ::= \langle \text{term} \rangle * \langle \text{term} \rangle \mid \langle \text{term} \rangle / \langle \text{term} \rangle \mid \langle d \rangle \mid \langle 1 \rangle$

$\langle d \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid 9$

$\langle 1 \rangle ::= a \mid b \mid c \mid \dots \mid z$

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# Imposing Associativity

Same grammar with left / right recursion for - :

Our choices:

$$\begin{aligned} \langle \text{expr} \rangle &::= \langle d \rangle - \langle \text{expr} \rangle \mid \\ &\quad \langle d \rangle \\ \langle d \rangle &::= 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid 9 \end{aligned}$$
$$\begin{aligned} \langle \text{expr} \rangle &\Rightarrow \\ \langle d \rangle - \langle \text{expr} \rangle &\Rightarrow \\ \langle d \rangle - \langle d \rangle - \langle \text{expr} \rangle &\Rightarrow \\ \langle d \rangle - \langle d \rangle - \langle d \rangle - \langle \text{expr} \rangle &\Rightarrow \\ &\vdots \end{aligned}$$

Or:

$$\begin{aligned} \langle \text{expr} \rangle &::= \langle \text{expr} \rangle - \langle d \rangle \mid \\ &\quad \langle d \rangle \\ \langle d \rangle &::= 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid 9 \end{aligned}$$
$$\begin{aligned} \langle \text{expr} \rangle &\Rightarrow \\ \langle \text{expr} \rangle - \langle d \rangle &\Rightarrow \\ \langle \text{expr} \rangle - \langle d \rangle - \langle d \rangle &\Rightarrow \\ \langle \text{expr} \rangle - \langle d \rangle - \langle d \rangle - \langle d \rangle &\Rightarrow \\ &\dots \end{aligned}$$

Which one do we want for - in the calculator language?

# Associativity

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- Deals with operators of same precedence
- Implicit grouping or parenthesizing
- Left to right:  $*$ ,  $/$ ,  $+$ ,  $-$
- Right to left:  $^$

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# Complete, Unambiguous Arithmetic Expression Grammar

$\langle \text{start} \rangle ::= \langle \text{expr} \rangle$   
 $\langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid$   
 $\quad \langle \text{expr} \rangle - \langle \text{expr} \rangle \mid$   
 $\quad \langle \text{expr} \rangle * \langle \text{expr} \rangle \mid$   
 $\quad \langle \text{expr} \rangle / \langle \text{expr} \rangle \mid$   
 $\quad \langle \text{expr} \rangle ^ \langle \text{expr} \rangle \mid$   
 $\quad \langle d \rangle \mid \langle l \rangle$   
 $\langle d \rangle ::= 0 \mid 1 \mid 2 \mid 3 \mid \dots \mid 9$   
 $\langle l \rangle ::= a \mid b \mid c \mid \dots \mid z$

Original Ambiguous Grammar  $G$

$\langle \text{start} \rangle ::= \langle \text{expr} \rangle$   
 $\langle \text{expr} \rangle ::= \langle \text{expr} \rangle + \langle \text{term} \rangle \mid$   
 $\quad \langle \text{expr} \rangle - \langle \text{term} \rangle \mid$   
 $\quad \langle \text{term} \rangle$   
 $\langle \text{term} \rangle ::= \langle \text{term} \rangle * \langle \text{factor} \rangle \mid$   
 $\quad \langle \text{term} \rangle / \langle \text{factor} \rangle \mid$   
 $\quad \langle \text{factor} \rangle$   
 $\langle \text{factor} \rangle ::= \langle g \rangle ^ \langle \text{factor} \rangle \mid$   
 $\quad \langle g \rangle$   
 $\langle g \rangle ::= ( \langle \text{expr} \rangle ) \mid \langle d \rangle \mid \langle l \rangle$   
 $\langle d \rangle ::= 0 \mid 1 \mid 2 \mid \dots \mid 9$   
 $\langle l \rangle ::= a \mid b \mid c \mid \dots \mid z$

Unambiguous Grammar  $G$

# Abstract versus Concrete Syntax

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## Concrete Syntax:

Representation of a construct in a particular language, including placement of keywords and delimiters.

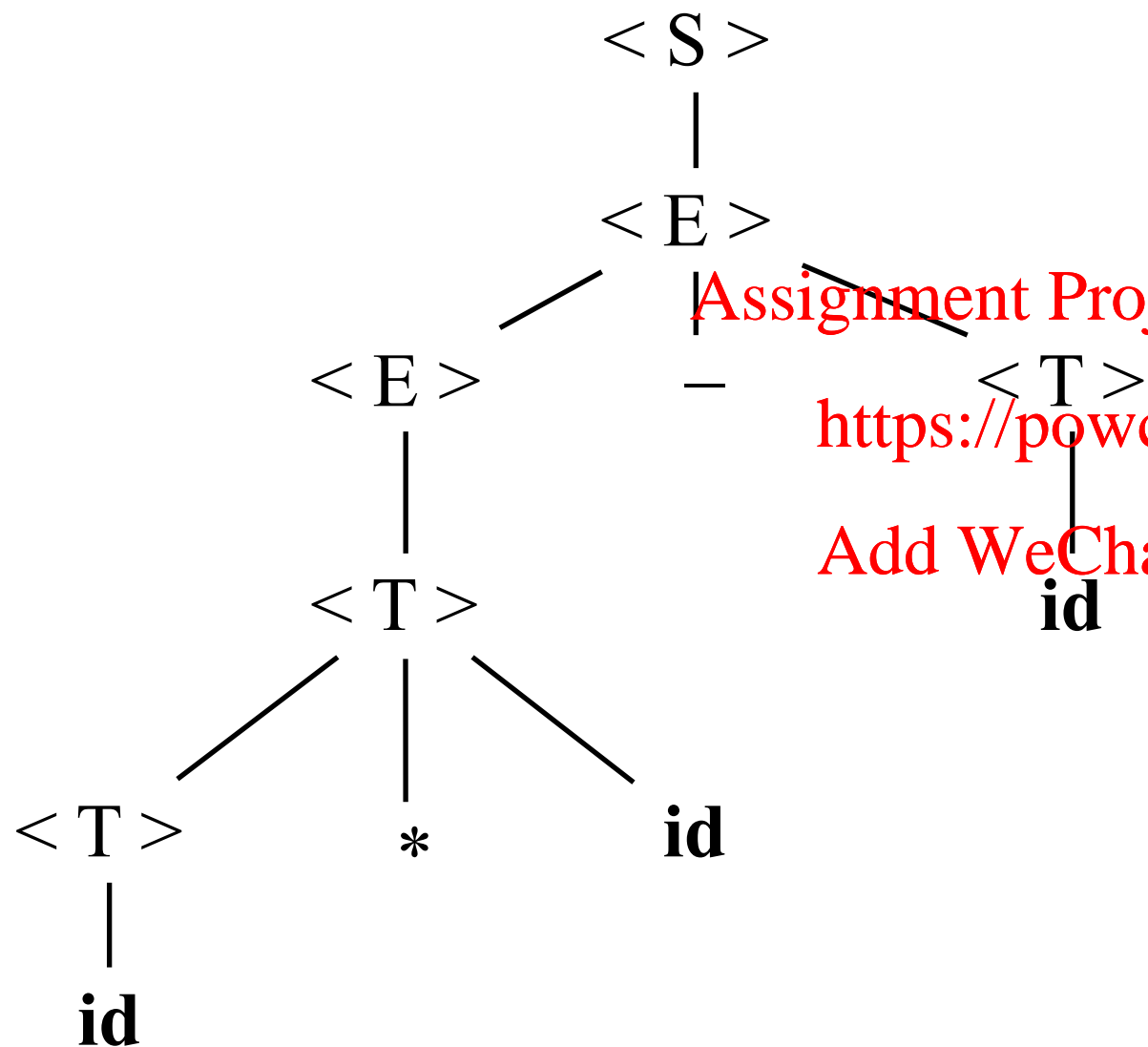
## Abstract Syntax: [Assignment Project Exam Help](https://powcoder.com)

Structure of meaningful components of each language construct.  
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# Example:

Consider  $A * B - C$ :

Concrete Syntax Tree

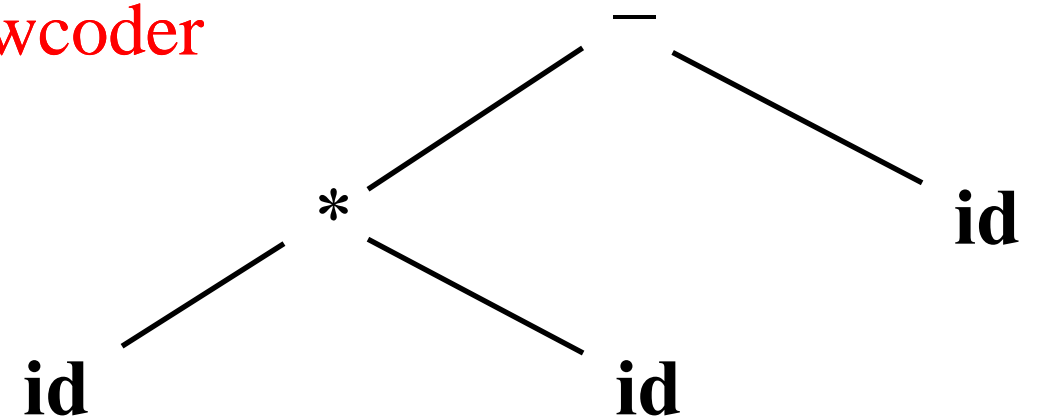


$\langle S \rangle ::= \langle E \rangle$

$\langle E \rangle ::= \langle E \rangle - \langle T \rangle \mid \langle T \rangle$

$\langle T \rangle ::= \langle T \rangle * \text{id} \mid \text{id}$

Abstract Syntax Tree  
(AST)



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# Abstract versus Concrete Syntax

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**Same abstract syntax, different concrete syntax:**

Pascal      **while**  $x \neq A[i]$ , **do**  
               $i := i + 1$   
              **end**

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C            while (  $x \neq A[i]$  )  
               $i = i + 1$ ;

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# Regular vs. Context Free

- All Regular languages are context free languages
- Not all context free languages are regular languages

Example:

$\langle N \rangle ::= \langle X \rangle \mid \langle Y \rangle$

$\langle X \rangle ::= \mathbf{a} \mid \langle X \rangle \mathbf{b}$  is equivalent to:  $\mathbf{a} \mathbf{b}^* \mid \mathbf{c}^+$

$\langle Y \rangle ::= \mathbf{c} \mid \langle Y \rangle \mathbf{c}$

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Question:

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*Is  $\{a^n b^n \mid n \geq 0\}$  a context free language?*



# Regular vs. Context Free

---

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 $\langle Y \rangle ::= \mathbf{a} \langle Y \rangle \mathbf{b} \mid \epsilon$

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# Regular vs. Context Free

- All Regular languages are context free languages
- Not all context free languages are regular languages

Example:

$\langle N \rangle ::= \langle X \rangle \mid \langle Y \rangle$

$\langle X \rangle ::= \mathbf{a} \mid \langle X \rangle \mathbf{b}$  is equivalent to:  $\mathbf{a} \mathbf{b}^* \mid \mathbf{c}^+$

$\langle Y \rangle ::= \mathbf{c} \mid \langle Y \rangle \mathbf{c}$

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Question:

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*Is  $\{a^n b^n \mid n \geq 0\}$  a context free language?*

*Is  $\{a^n b^n \mid n \geq 0\}$  a regular language?*

# Regular Grammars

---

CFGs with restrictions on the shape of production rules.

**Left-linear:**

$$\langle X \rangle ::= \mathbf{a} \mid \langle \underline{X} \rangle \mathbf{b}$$
$$\langle N \rangle ::= \langle \underline{X} \rangle \mathbf{a} \mathbf{b}$$

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**Right-linear:**

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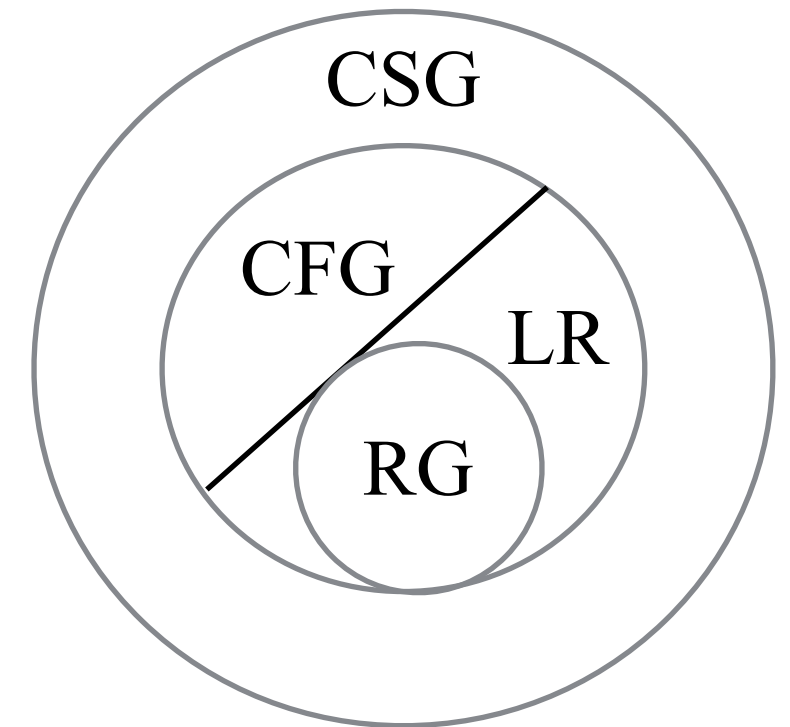
$$\langle Y \rangle ::= \mathbf{a} \mathbf{b} \mid \mathbf{a} \mathbf{b} \langle \underline{Y} \rangle$$
$$\langle N \rangle ::= \mathbf{b} \mid \mathbf{b} \langle \underline{Y} \rangle$$

# Complexity of Parsing

Classification of languages that can be recognized by specific grammars.

Complexity:

Regular grammars	DFA	$O(n)$
LR grammars	Kunth's algorithm	$O(n)$
Arbitrary CFGs	Earley's algorithm	$O(n^3)$
Arbitrary CSGs	LBA	P-SPACE COMPLETE

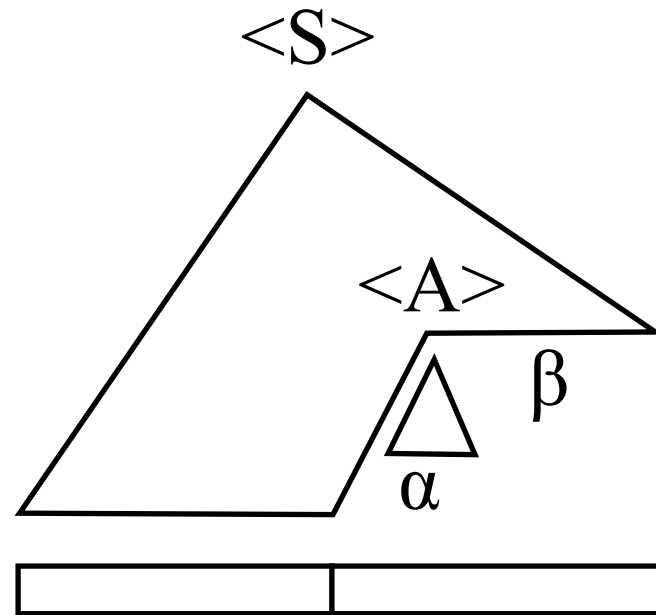


Reading:

Scott Chapter 2.3.4 (for LR parser) and Chapter 2.4.3 for language class.

Earley, Jay (1970), "An efficient context-free parsing algorithm", Communications of the ACM.

# Top - Down Parsing - LL(1)



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Basic Idea:

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- The parse tree is constructed from the root, expanding non-terminal nodes on the tree's frontier following a **leftmost** derivation.
- The input program is read from **left** to right, and input tokens are read (consumed) as the program is parsed.
- The next non-terminal symbol is replaced using one of its rules. The particular choice has to be unique and uses parts of the input (partially parsed program), for instance the first **token** of the remaining input.

# Top - Down Parsing - LL(1) (cont.)

## Example:

$S ::= a S b \mid \epsilon$

How can we parse (automatically construct a leftmost derivation) the input string **a a a b b b** using a PDA (push-down automaton) and only the first symbol of the remaining input?

INPUT: 

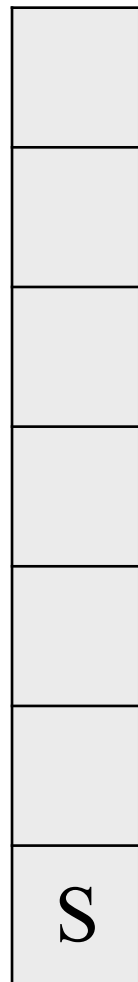
a a a b b b eof
-----------------

# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$

S

Remaining Input:  
a a a b b b



Assignment Project Exam Help Sentential Form:

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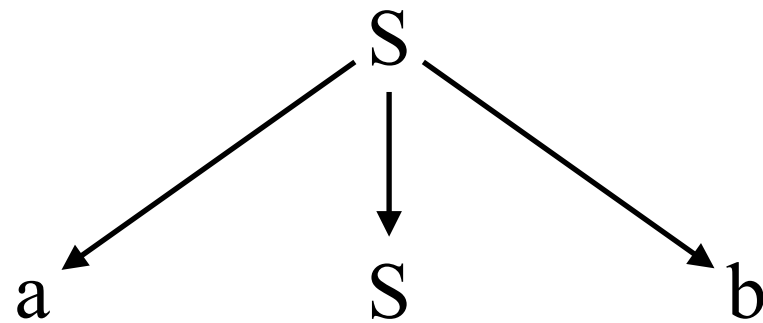
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S

Applied Production:

# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$



Remaining Input:  
a a a b b b

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a S b

Applied Production:

$S ::= a S b$



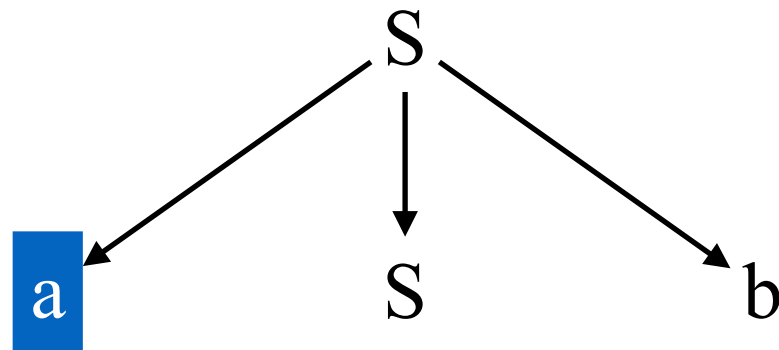


# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$

Remaining Input:

a a a b b b



Match!

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Sentential Form:

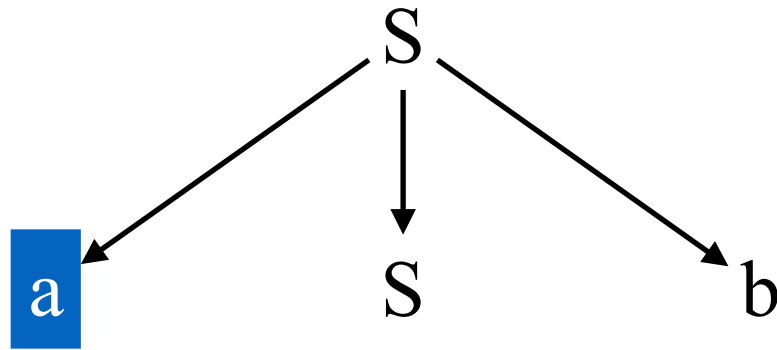
$a S b$

Applied Production:



# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$



Remaining Input:  
a a b b b

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a S b

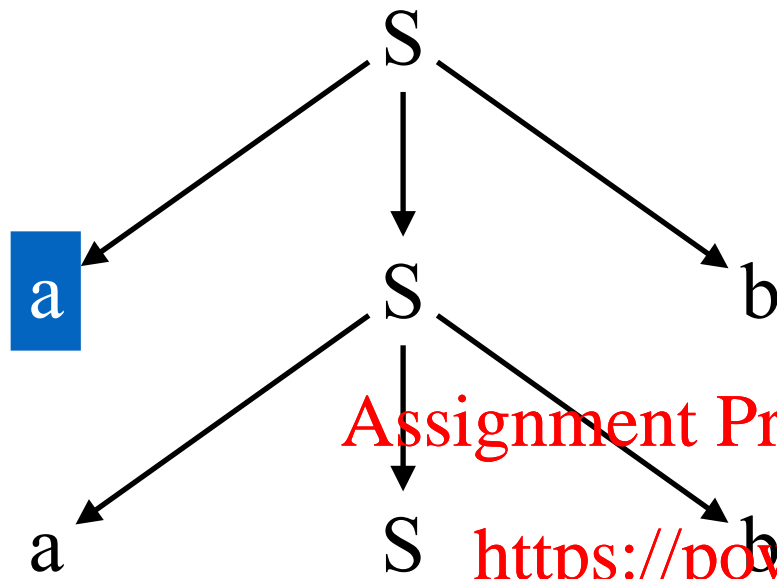
Applied Production:



# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$

Remaining Input:  
a a b b b



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Sentential Form:  
a a S b b

Applied Production:  
 $S ::= a S b$

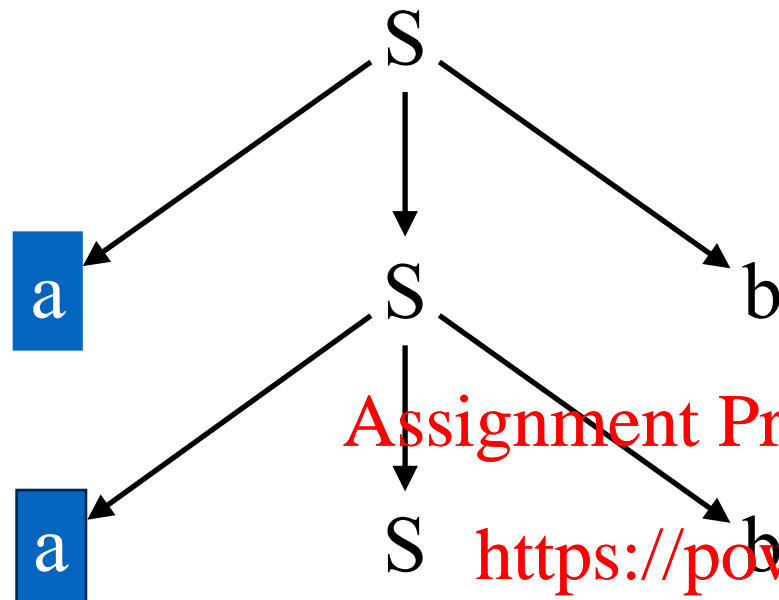
a
S
b
b

# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$

Remaining Input:

a a b b b



Assignment Project Exam Help

Sentential Form:

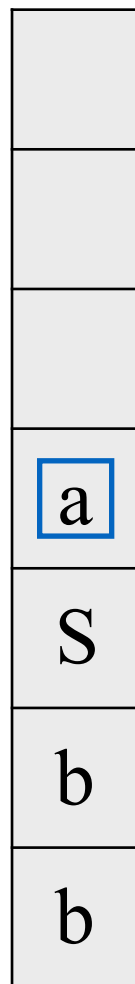
<https://powcoder.com>

a a S b b

Match!

Add WeChat powcoder

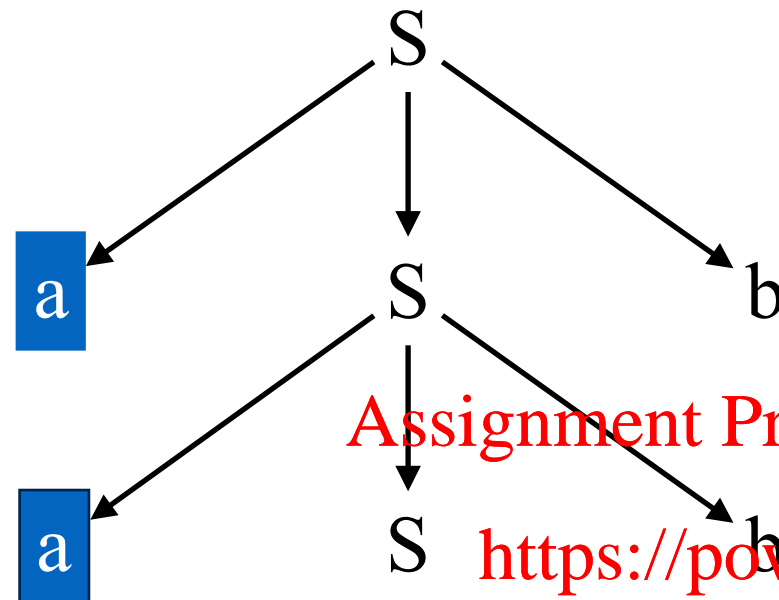
Applied Production:



# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$

Remaining Input:  
a b b b



Assignment Project Exam Help

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Add WeChat powcoder

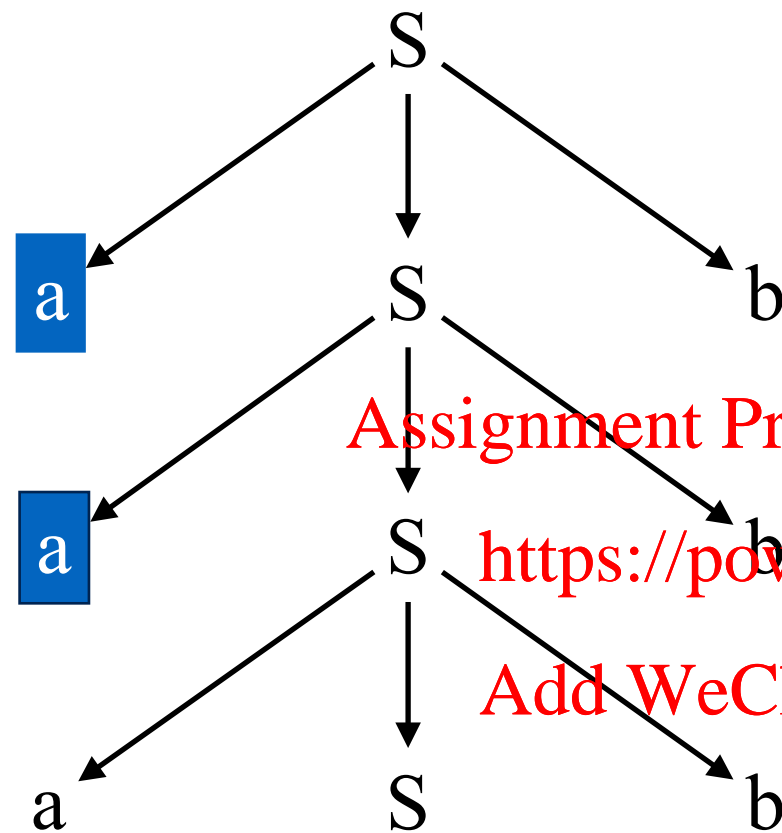
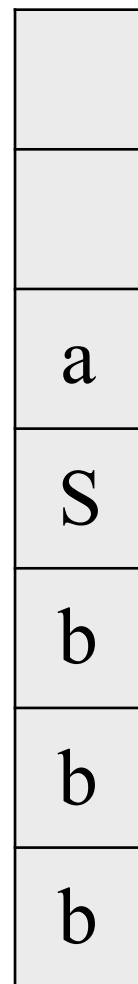
Sentential Form:  
a a S b b

Applied Production:



# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$



Remaining Input:  
a b b b

Assignment Project Exam Help

Sentential Form:

<https://powcoder.com>

a a a S b b b

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Applied Production:

$S ::= a S b$

# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$

Remaining Input:

a b b b

Sentential Form:

a a a S b b b

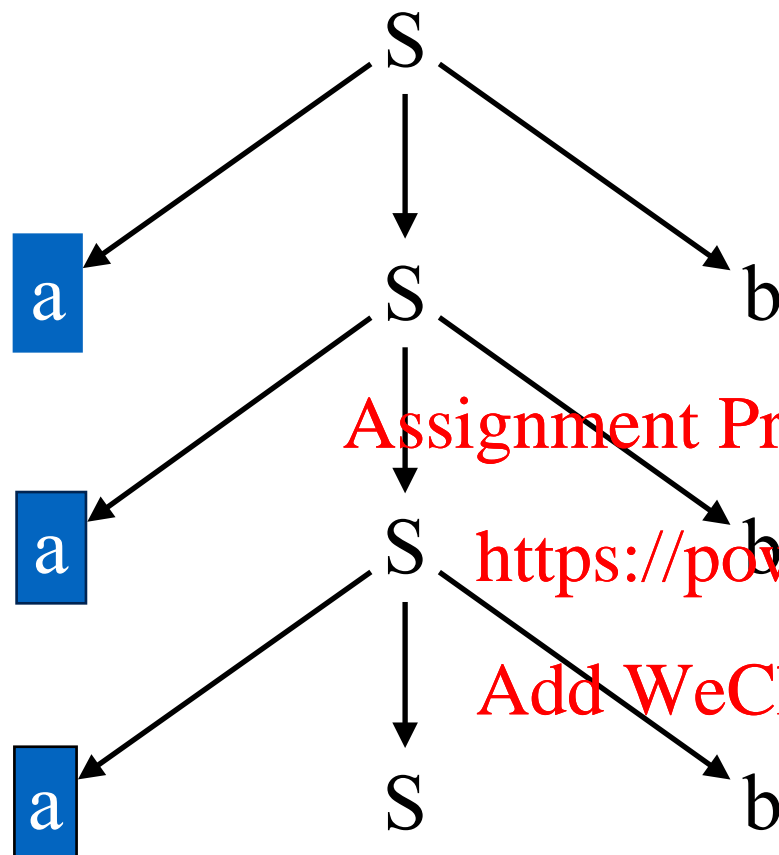
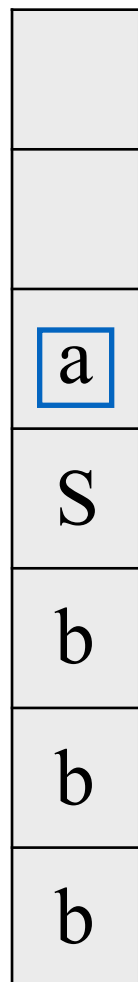
Applied Production:

Match!

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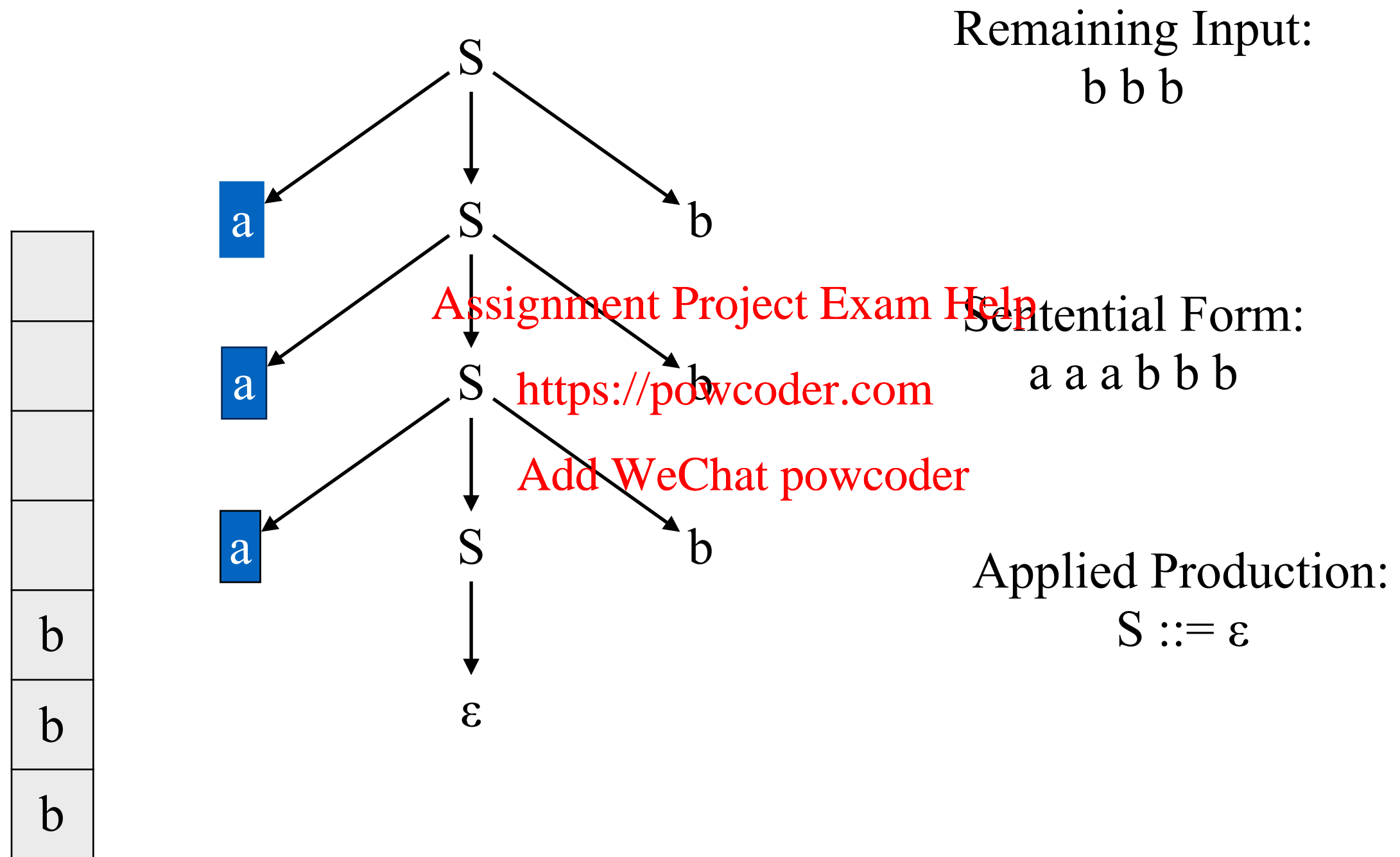


$$S ::= a S b \mid \varepsilon$$



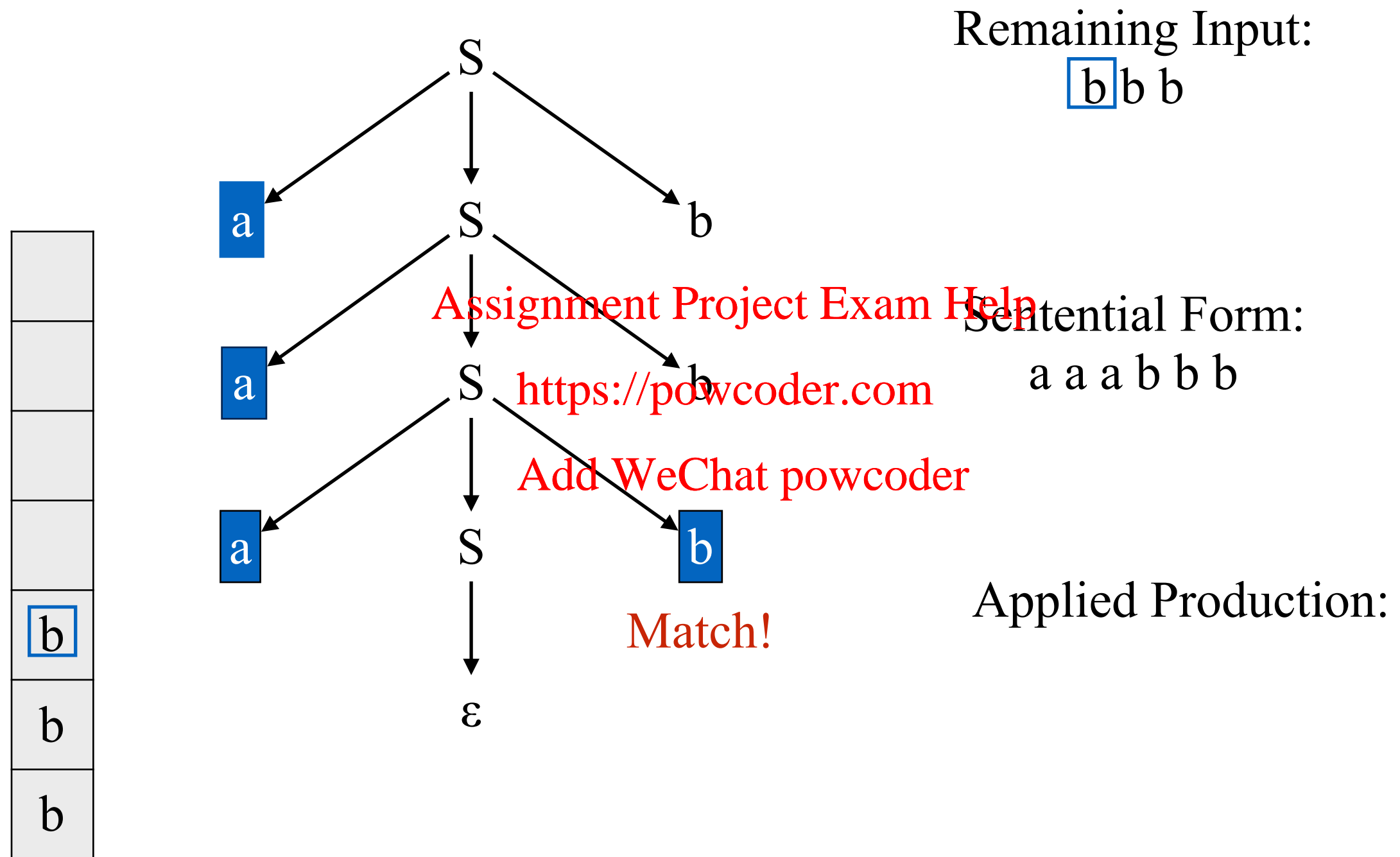

# LL(1) Parsing Example

$S ::= a S b \mid \varepsilon$



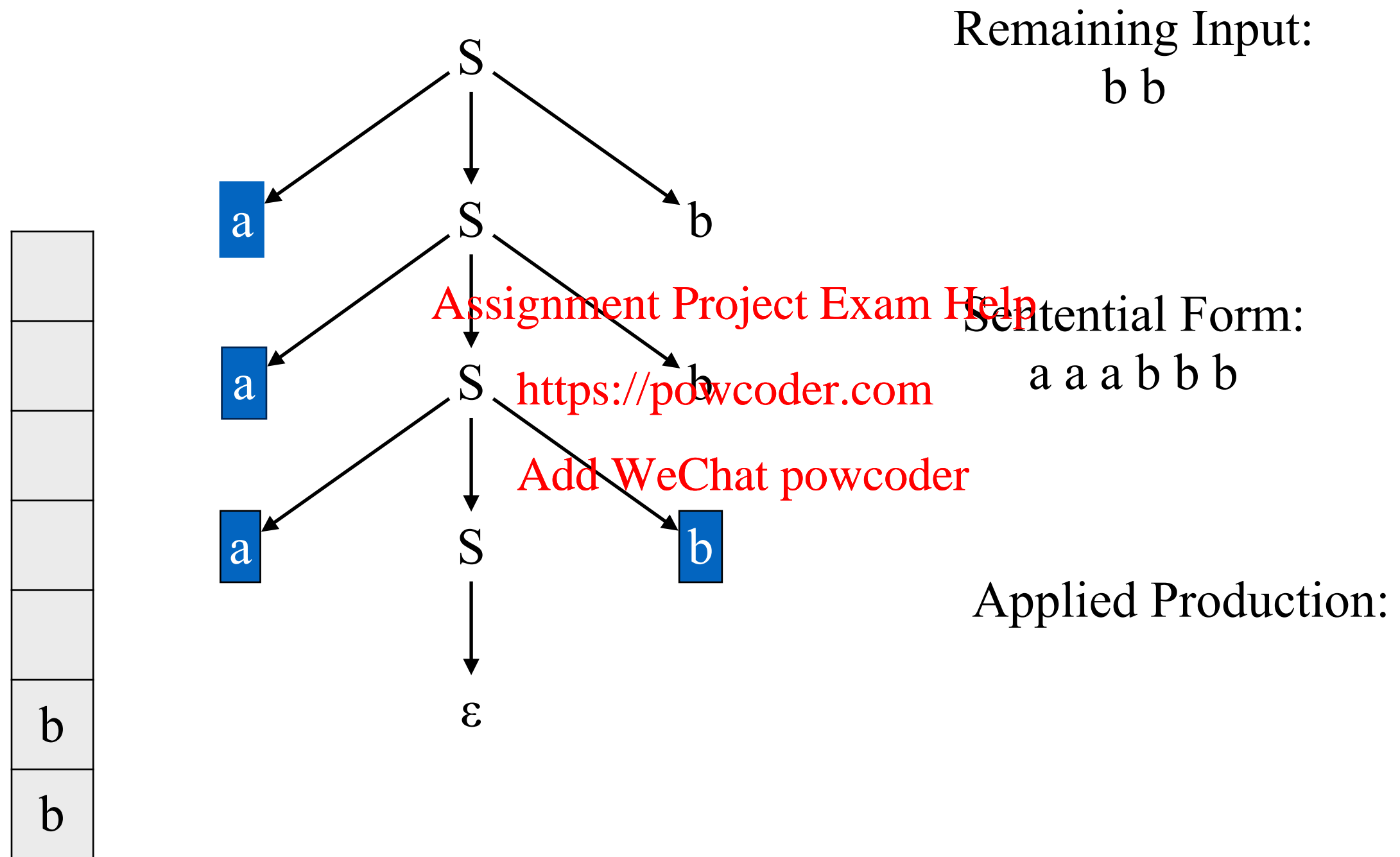
# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$



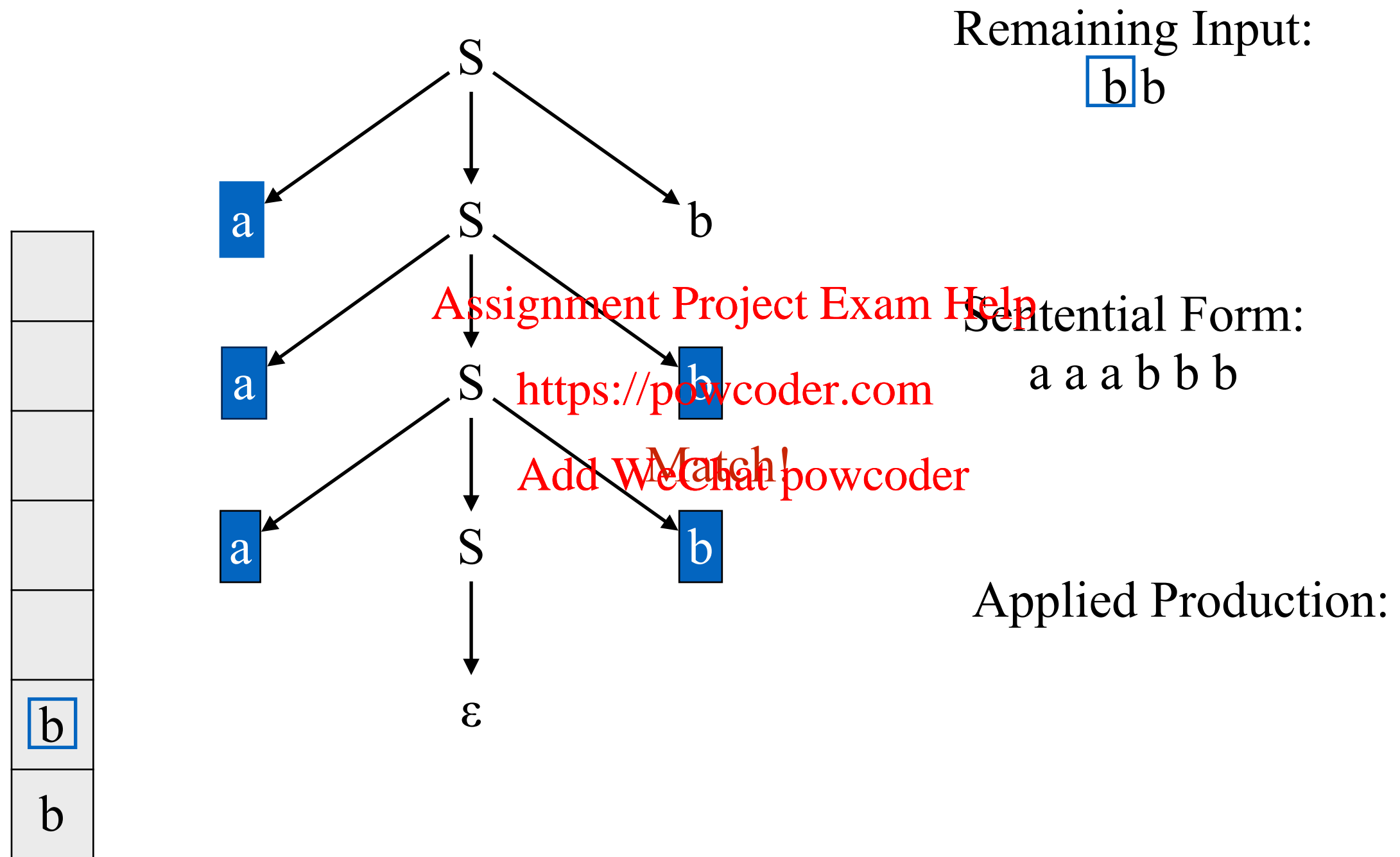
# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$



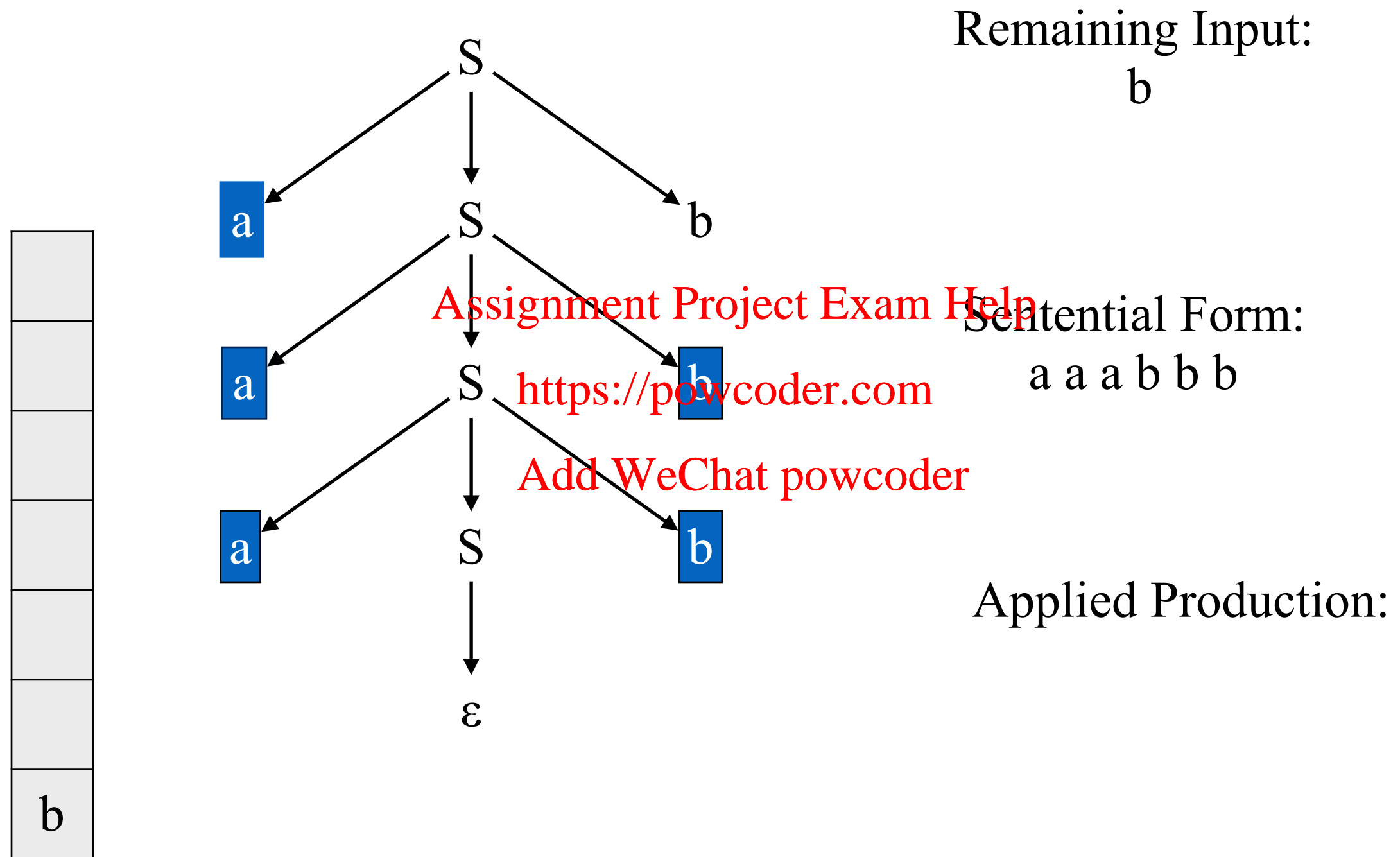
# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$



# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$

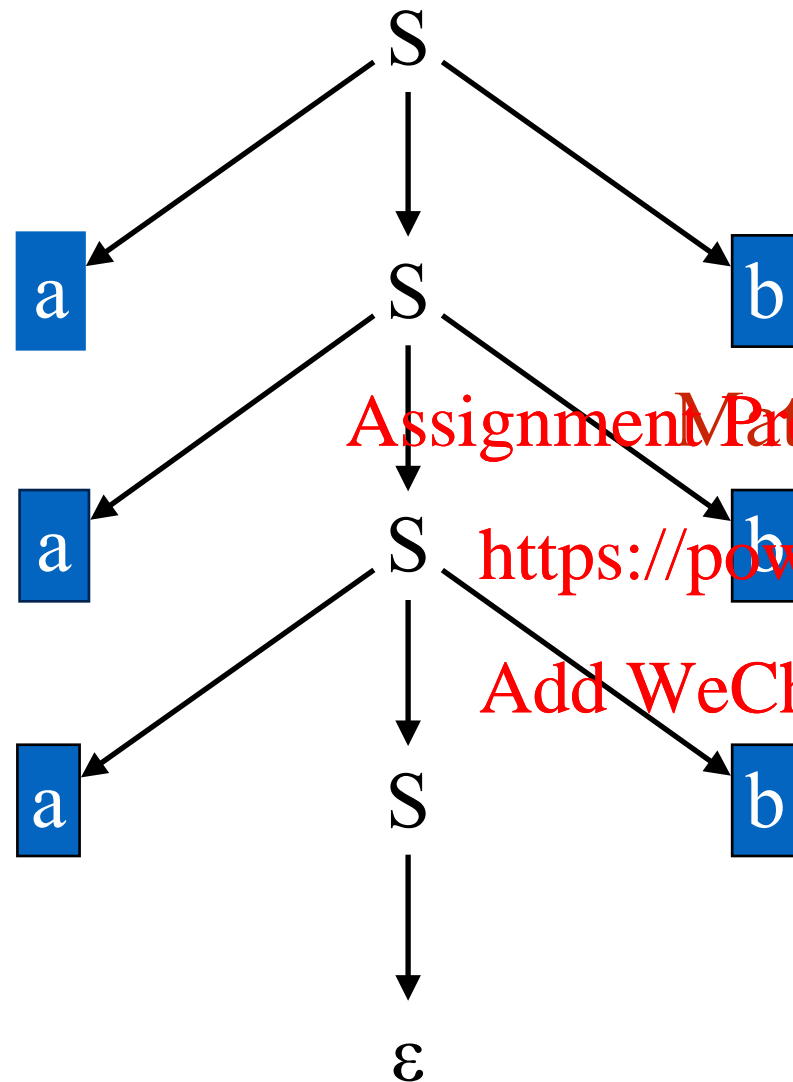


# LL(1) Parsing Example

$S ::= a S b \mid \epsilon$

Remaining Input:

**b**



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Sentential Form:

$a a a b b b$

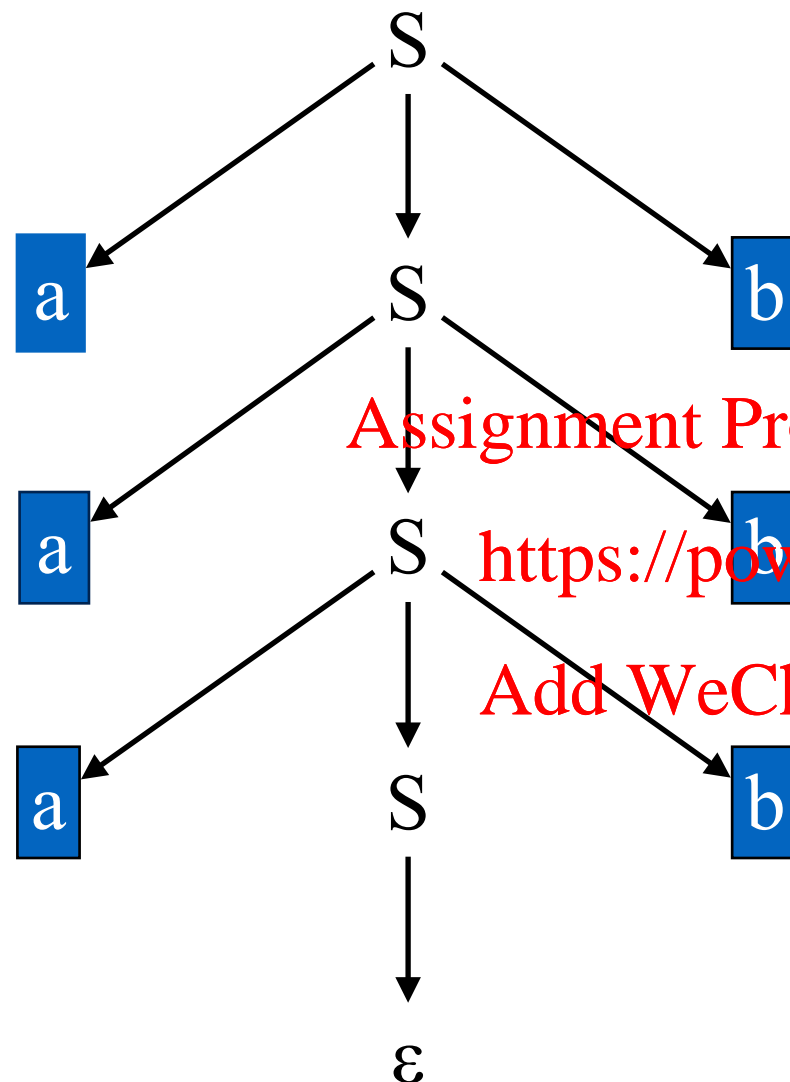
Applied Production:



# LL(1) Parsing Example

$S ::= a S b \mid \varepsilon$

Remaining Input:



Sentential Form:

a a a b b b

Applied Production:

# Next Lecture

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Next Time:

- Read Scott, Chapter 2.3.1 - 2.3.2 (and the materials on companion site)

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