

Problem 1 - Dependencies

Suppose we have the following program (a sequence of instructions), with each instruction labeled as S_{num} :

```

S1:  a := 4;
S2:  b := 2;
S3:  c := 5;
S4:  read(d);
S5:  a := b + 3;
S6:  b := a - 3;
S7:  c := d * b;
S8:  e := a + 6;
S9:  print(c);
S10: print(e);

```

- Give the statement-level dependence graph for the above program. A node in the statement-level dependence graph represents a statement, an edge represents dependence between the statements (i.e. the nodes). Label each edge as a **true** data dependence, an **anti**-data dependence, or an **output** data dependence.
- Assume that each statement takes 1 cycle to execute. What is the execution time of the sequential code? What is the fastest parallel execution time of the program (i.e. the critical path)? You may assume that I/O operations (read and print) can be done in parallel.

Problem 2 - Dependence Analysis

Give the source and sink references, the type (whether a dependence is **true**, **anti**, or **output**), and the distance vectors for all dependences in the following loops.

- ```

do i = 3, 100
 a(i) = a(i - 1) + a(i + 1) - a(i - 2)
enddo

```
- ```

do i = 2, 100
    a(3 * i) = a(3 * i - 3) + a(3 * i + 3)
enddo

```
- ```

do i = 1, 10
 a(i) = a(5) + a(i)
enddo

```

Use  $a_W(i)$  and  $a_R(i)$  to annotate the write access to  $a(i)$  and the read access to  $a(i)$  respectively.

## Problem 3 - Loop Parallelization

Given the following nested loop:

```

do i = 2, 100
 do j = 2, 100
S1: a(i, j) = b(i - 1, j - 1) + 2
S2: b(i, j) = i + j - 1
 enddo
 enddo

```

- (a) Give the statement-level dependence graph. Show the dependence graph for statement instances in a part of the iteration space:  $i = 2 \dots 5, j = 2 \dots 5$ .
- (b) In its current form, can any loop be parallelized? If so, which loop(s)? If not, justify your answer.
- (c) Provide one valid affine schedule for statements  $S_1$  and  $S_2$  such that  $p(S_1) = C_{11} * i + C_{12} * j + d_1$  and  $p(S_2) = C_{21} * i + C_{22} * j + d_2$  in order to achieve synchronization-free parallelism. There could be many possible solutions for  $\{C_{11}, C_{12}, C_{21}, C_{22}, d_1, d_2\}$ . You only need to provide one feasible solution. (Hint: You can let  $d_1 = d_2 = 0$ .)
- (d) Generate two-level loop code for the affine schedule you provided. Please use  $p$  as outermost loop and  $i$  as innermost loop in the transformed loop. Calculate the loop bounds for  $p$  and  $i$  using Fourier-Motzkin elimination. You might need to calculate the overlapping polyhedron for  $S_1$  and  $S_2$  in order to eliminate the  $j$  loop. Please refer to the techniques for code generation in lecture 20 and lecture 21.

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